



Wir schaffen Wissen – heute für morgen

Paul Scherrer Institut

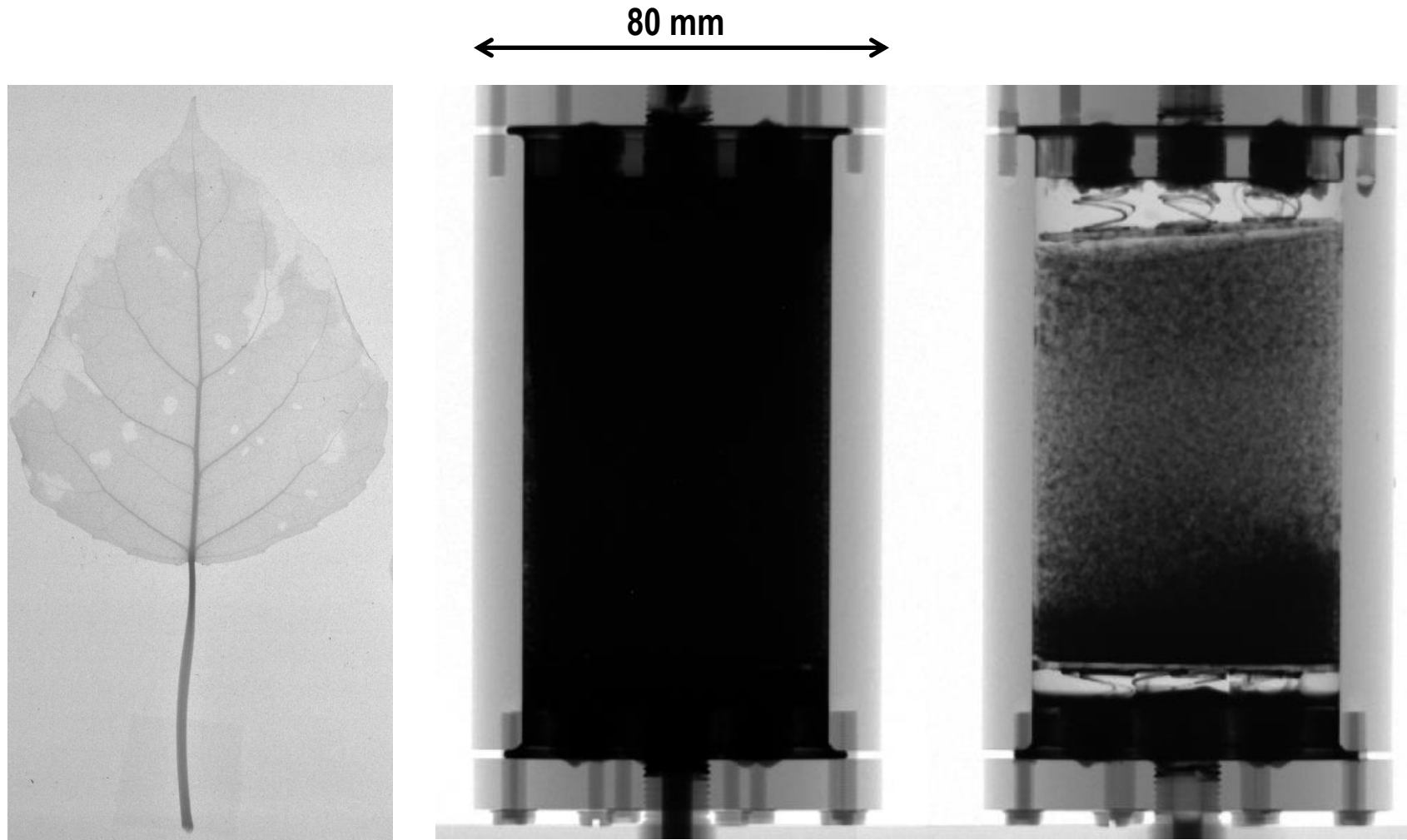
Peter Vontobel

Quantification in Neutron Imaging

1. Introduction
2. Definition of quantification in NI
3. Spatial resolution, sample morphology, defect size, beam divergence, magnification, ...
4. Influence of energy spectrum: white beam - versus mono energetic neutron attenuation
5. Effects due to sample scattering
6. Assessing the importance of disturbing effects
7. QNI software

- **Neutron Imaging:** Neutron intensity measurements with a 2D (area) detector.
- **Quantification:** Any method used to convert raw image data (grey levels, photon stimulated luminescence, ...) into a physical quantity i.e. : length (thickness), area, volume, transmission, attenuation coefficient, phase shift value, dark-field signal, material content, ...
- **Image Correction:** Any method used to remove disturbing effects from the raw images i.e. denoising, offset correction (e.g. dark-current), flat-field correction, intensity normalization, ...
- **Neutron radiation:** Can be described as particles with the Boltzmann neutron transport equation for the phase space distribution function $\Phi(\mathbf{r}, \mathbf{k}, t)$ and/or neutron wave propagation using the Schrödinger equation for neutron wave function ψ .
- **Exponential law of radiation attenuation:** Beer-Lambert law. Can be derived from the Boltzmann neutron transport equation for $\Phi(\mathbf{r}, \mathbf{k}, t)$. It applies only with restrictions discussed in the introductory lecture by M. Morgano.

High and low transmission & contrast



Weak contrast

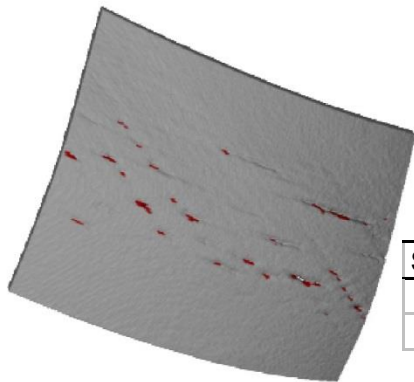
No penetration

3D Volume data set with (arbitrarily scaled) linear attenuation value $\Sigma(x,y,z)$ distribution

Qualitative information: sample morphology as seen by neutrons, material discrimination, defects, **PICTURES**

Quantitative information i.e. **NUMBERS**

- Geometrical information e.g. object size [cm³], wall thickness [cm], ...
- Atom/Molecule densities [cm⁻³], fluid concentrations, ...

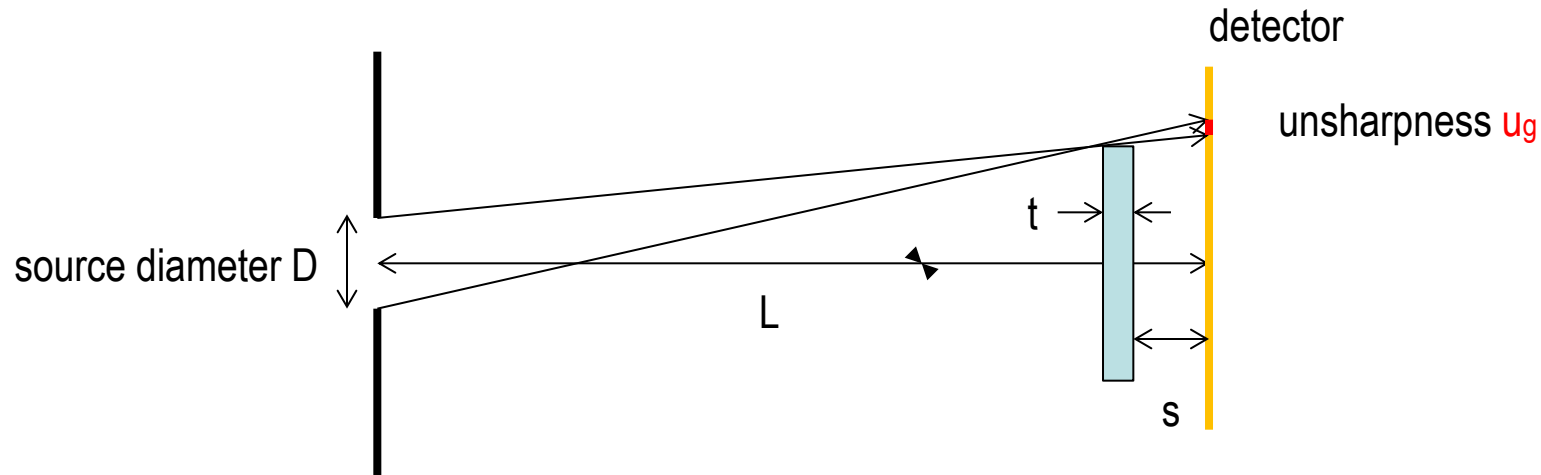


Slice	x [mm]	y [mm]	z [mm]	bot (x)	bot (y)	bot (z)	top (x)	top (y)	top (z)	thickness
67	7.33	2.44	8.91	7	1.85	8.84	7.52	2.38	8.84	0.20 - 0.60
69	7.33	2.71	9.17	7	1.85	9.11	7.66	2.64	9.11	0.20 - 0.60

Geometrical information: Location and size of fissures in rubber bellow with VGStudio Max[®] measurement tool.

Geometrical unsharpness inherent to divergent beam

$$u_g = \frac{s}{L/D}$$



Flux intensity at detector

$$\Phi = S_f \frac{1}{\left(\frac{L}{D}\right)^2}$$

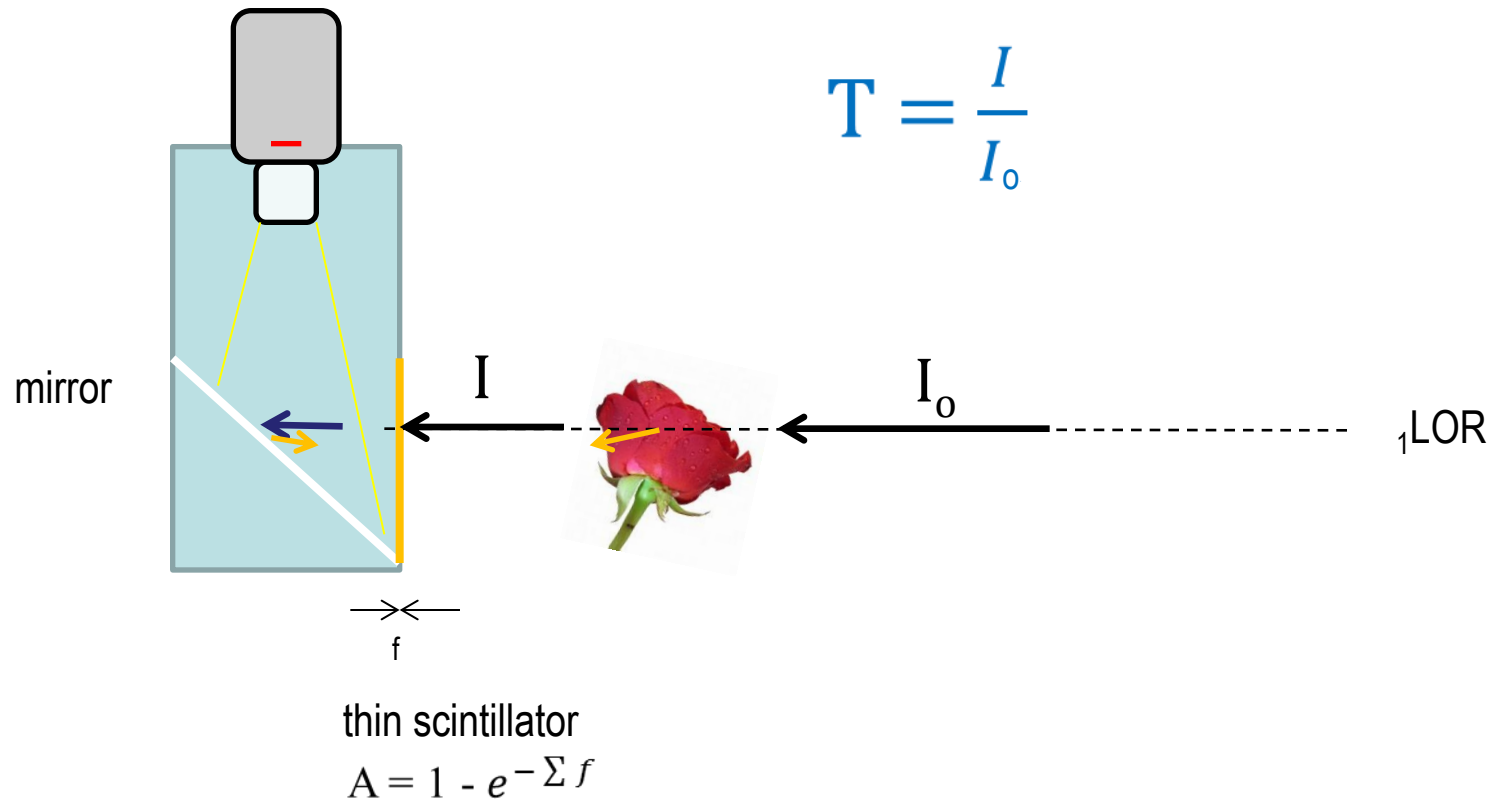
$$s \ll L$$

$$L \gg D$$

In general: $u_g = \text{function}(t)$

Transmission measured with area detector

camera area detector

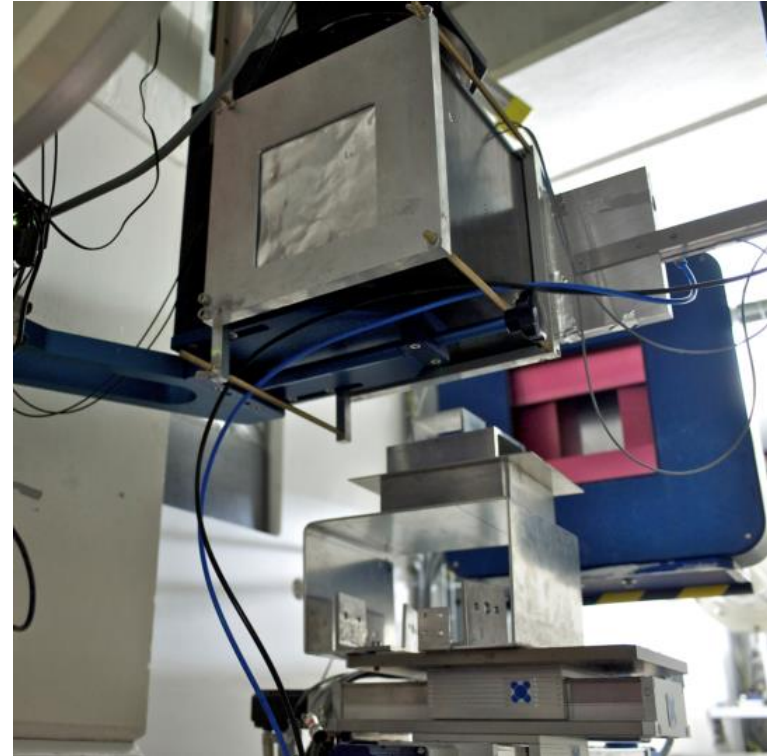
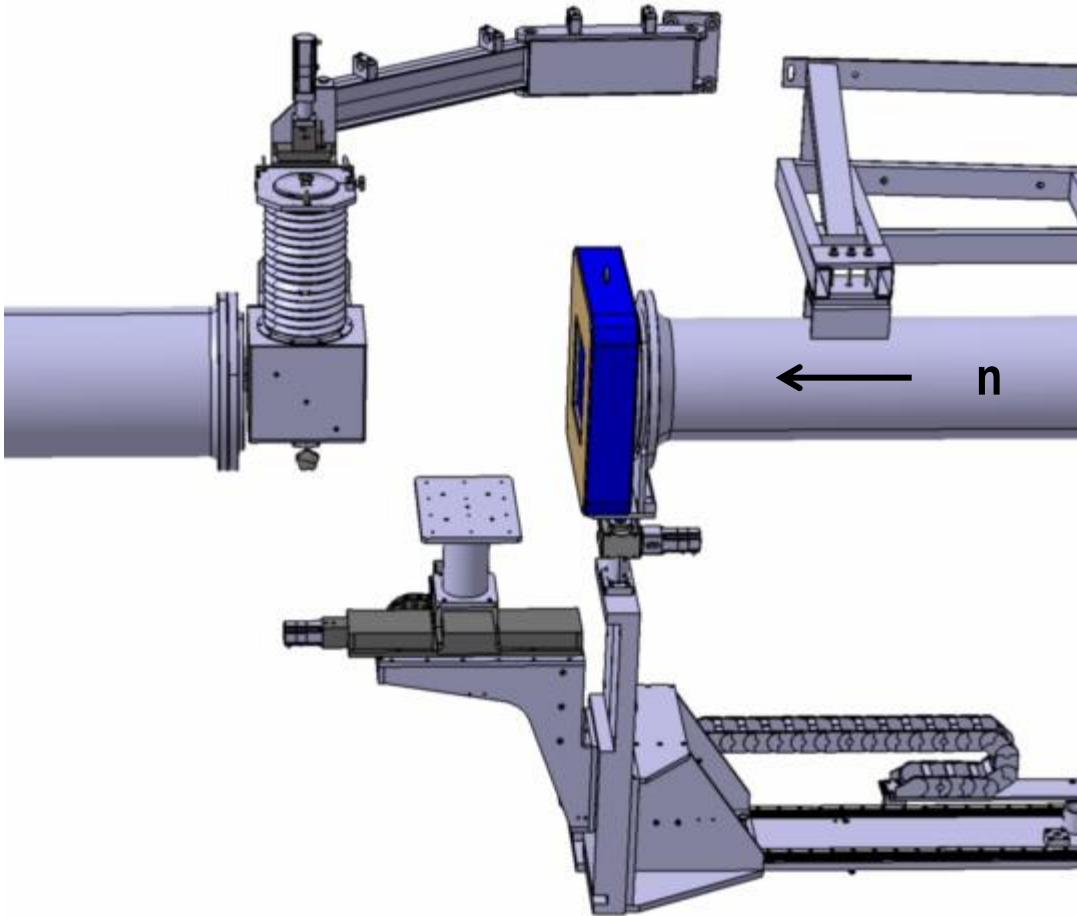


sample scattering

detector back scattering

1 LOR: line of response

Typical camera detector setup: NEUTRA Pos 2

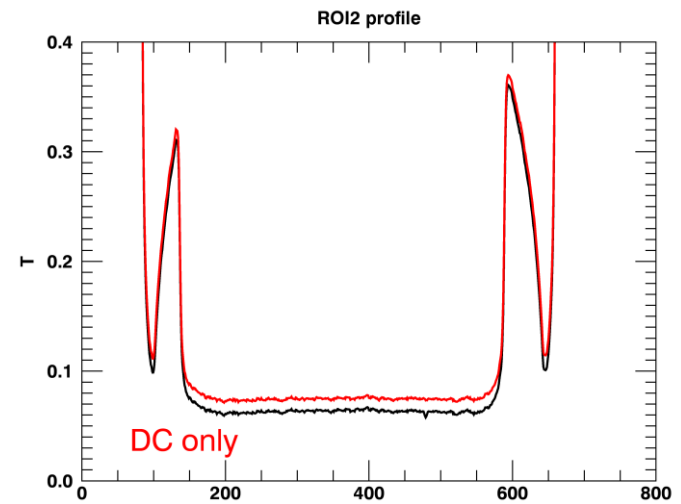
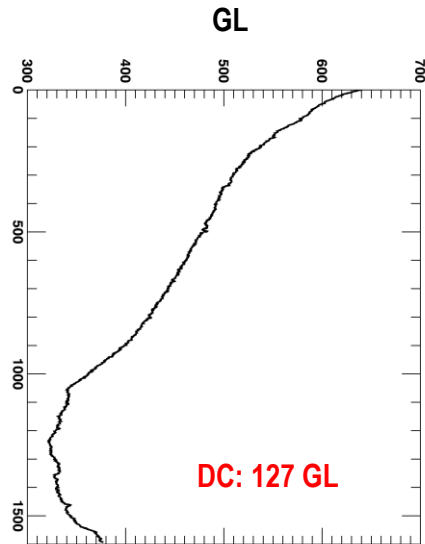
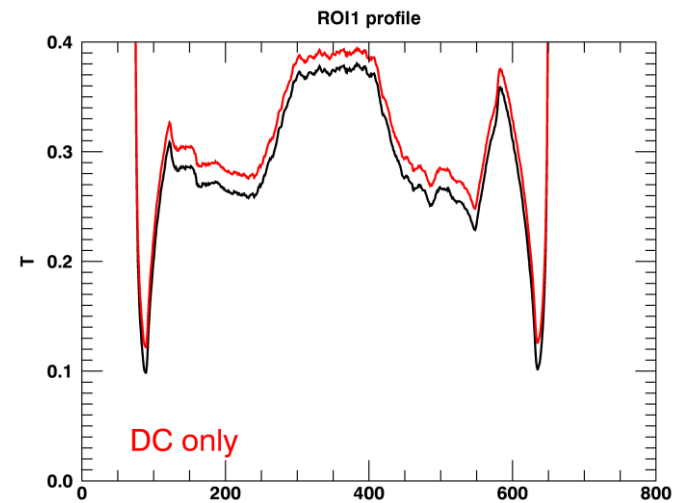


Detector backscattering estimate with black body

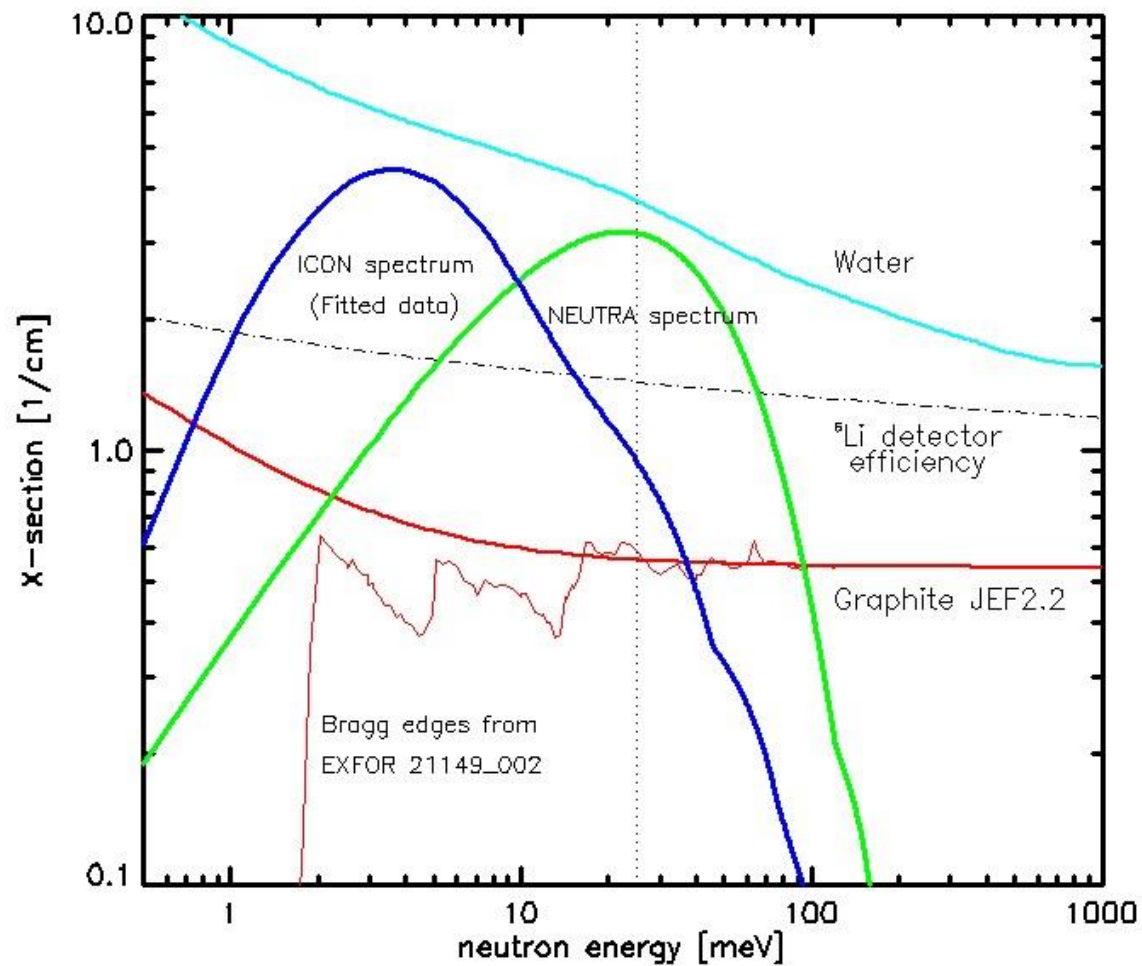


ROI1

ROI2



Cold and thermal neutron energy spectra



In order to be quantitative the exponential law of neutron attenuation should hold for every line of response !

$$I(\rho, \theta) = I_o e^{-\int_{-\infty}^{+\infty} \Sigma(x, y) ds} \quad (1)$$

Main violations are due to (see introductory presentation M Morgano):

1. Scattering of neutrons in the sample and in the detector.
2. Use of a polychromatic neutron beam, effect of „beam hardening“.

Let's redefine the uncollided neutron flux per energy interval as $I(x,E)$. Then it can be shown, that for every small energy interval dE the exponential attenuation law is valid:

$$I(x, E)dE = I_o(E)dE \exp[-\Sigma(E) x] \quad (1)$$

For a known incident energy spectrum $I_o(E)$ we can average over energy

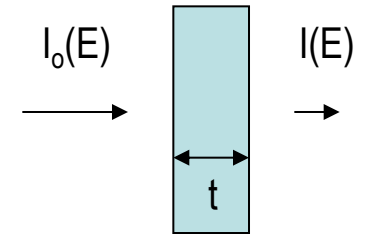
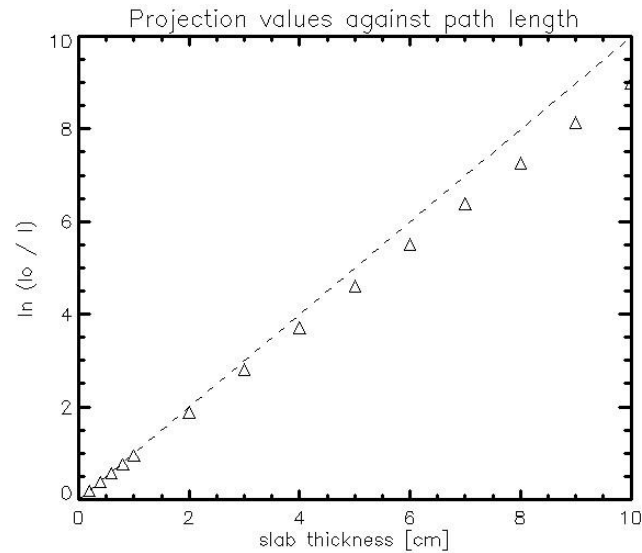
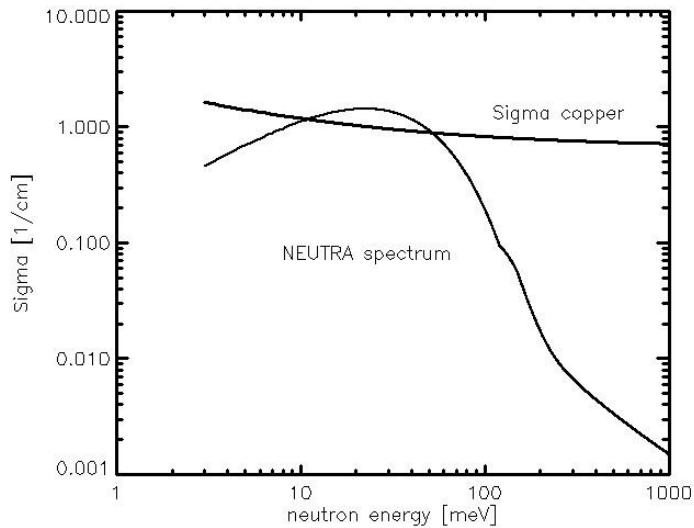
$$\langle I(t) \rangle = \int_{E_{\min}}^{E_{\max}} I(t, E) dE = \int_{E_{\min}}^{E_{\max}} I_o(E) \exp[-\Sigma(E) t] dE \quad (2)$$

We can calculate the total intensity of the uncollided exiting beam after traversing the distance t in a slab, by integrating over the whole energy spectrum e.g. with $E_{\min} = 3 \text{ meV}$, $E_{\max} = 1 \text{ eV}$.

$$\langle I(t) \rangle = \langle I_o \rangle \exp[-\langle \Sigma \rangle t] \quad \therefore \quad \langle \Sigma \rangle = \frac{-\ln \frac{\langle I(t) \rangle}{\langle I_o \rangle}}{t} \quad (3)$$

Using equation (2) and the known energy dependence of the cross section we can calculate an energy averaged cross section $\langle \Sigma \rangle$, that would be measured by an ideal detector registering the uncollided flux component only. This spectrum averaged effective cross section $\langle \Sigma \rangle$ is calculated from equation (3).

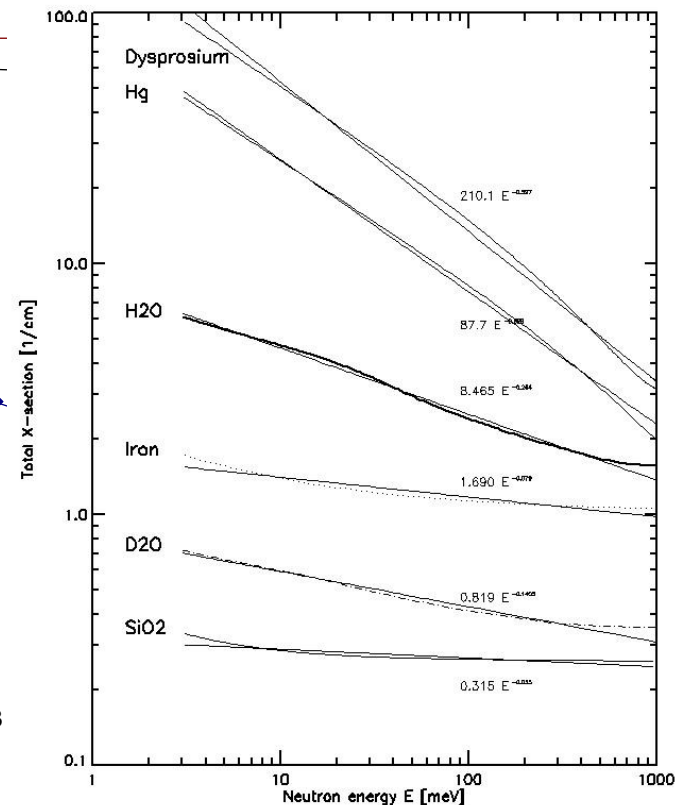
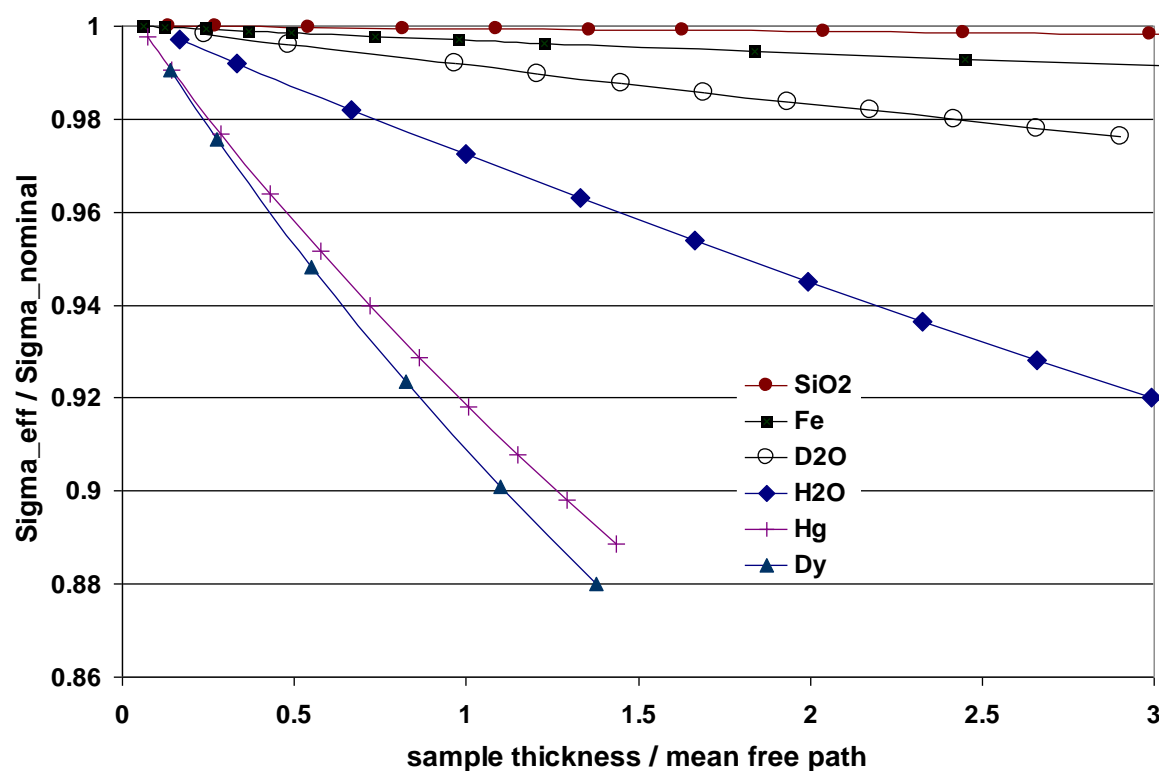
Beam hardening in neutron tomography ?



Effective $\langle \Sigma \rangle$ value
depends on material
penetration length t !

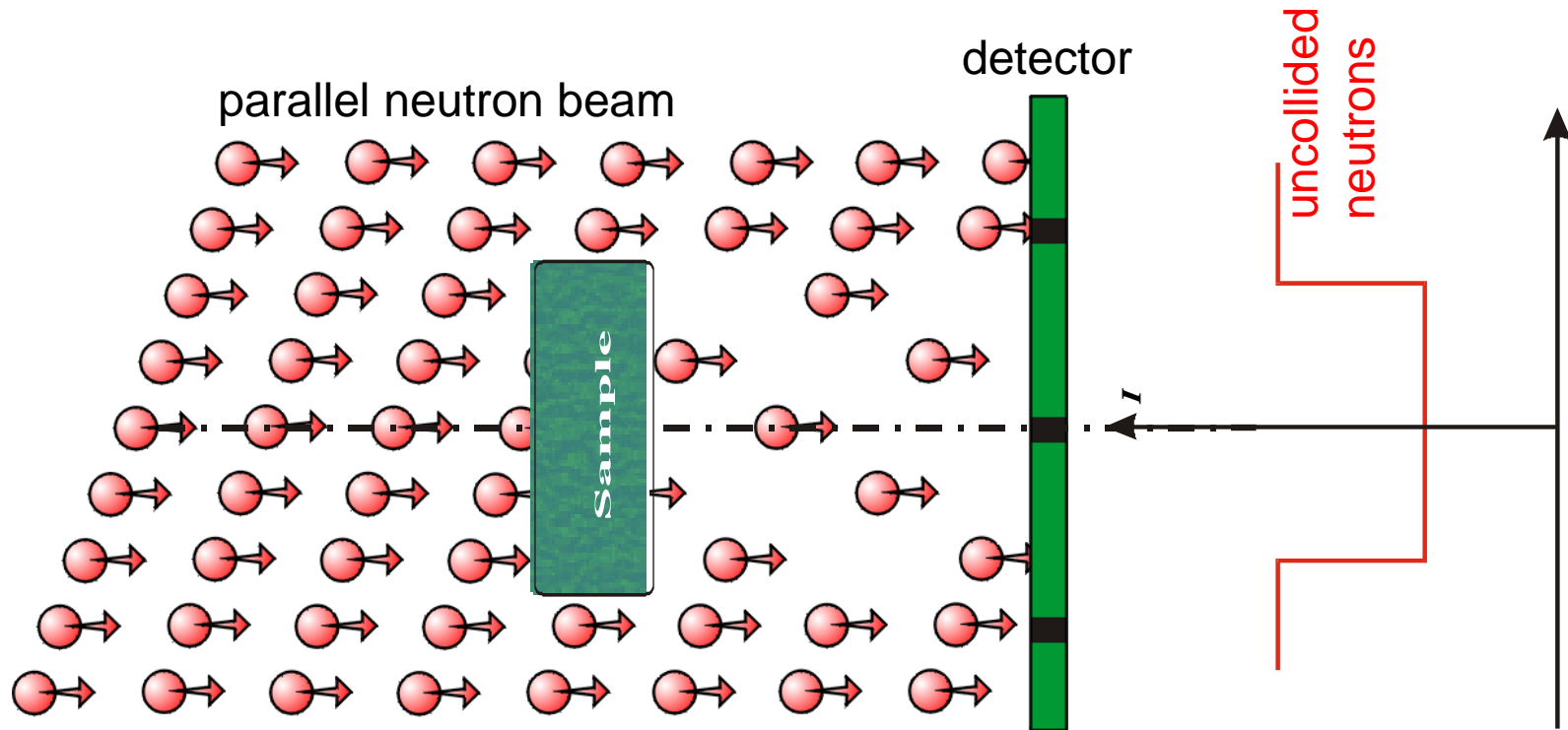
$$\langle \Sigma \rangle = \frac{-\ln \frac{\langle I(t) \rangle}{\langle I_0 \rangle}}{t}$$

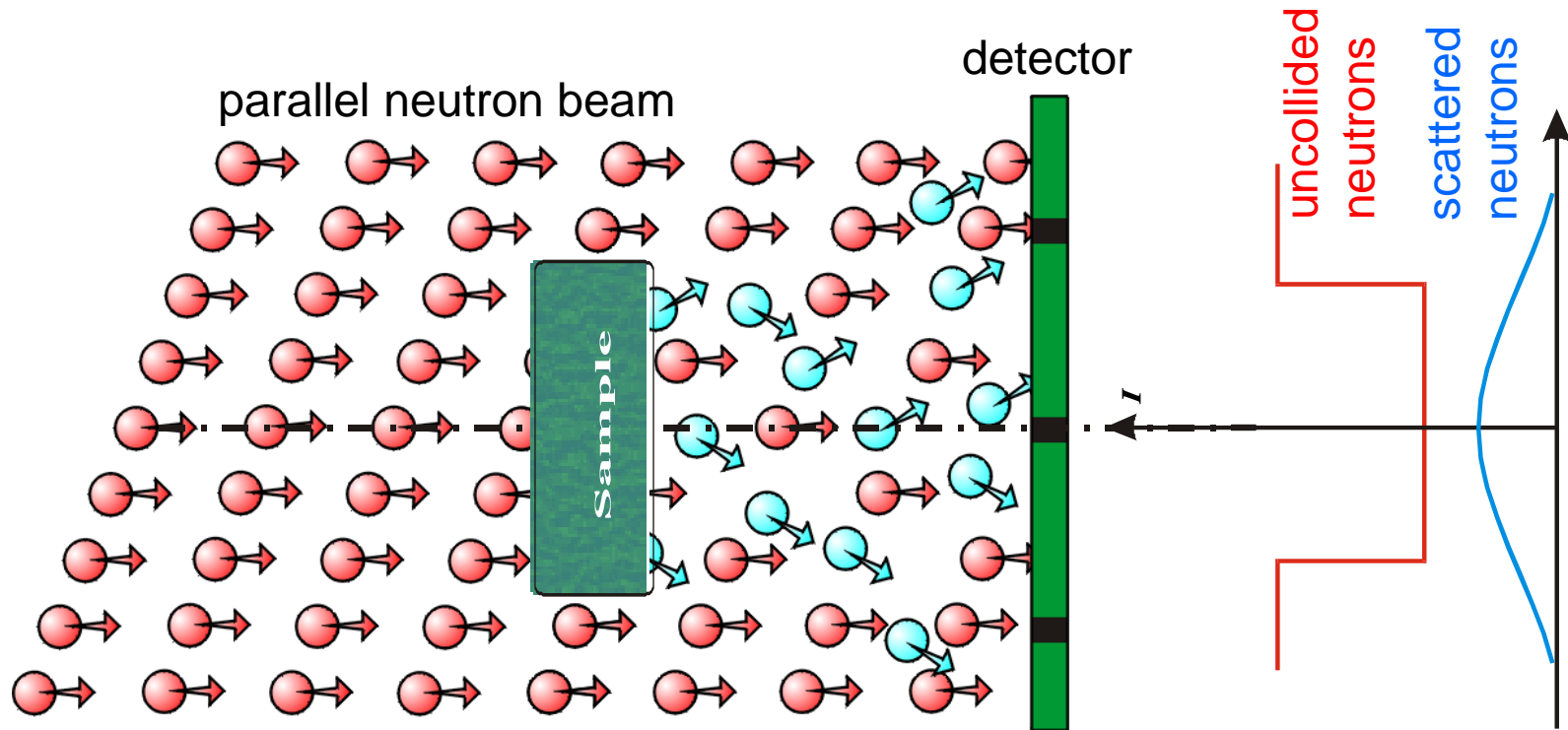
Magnitude of beam hardening in a thermal neutron-spectrum for selected elements and compounds

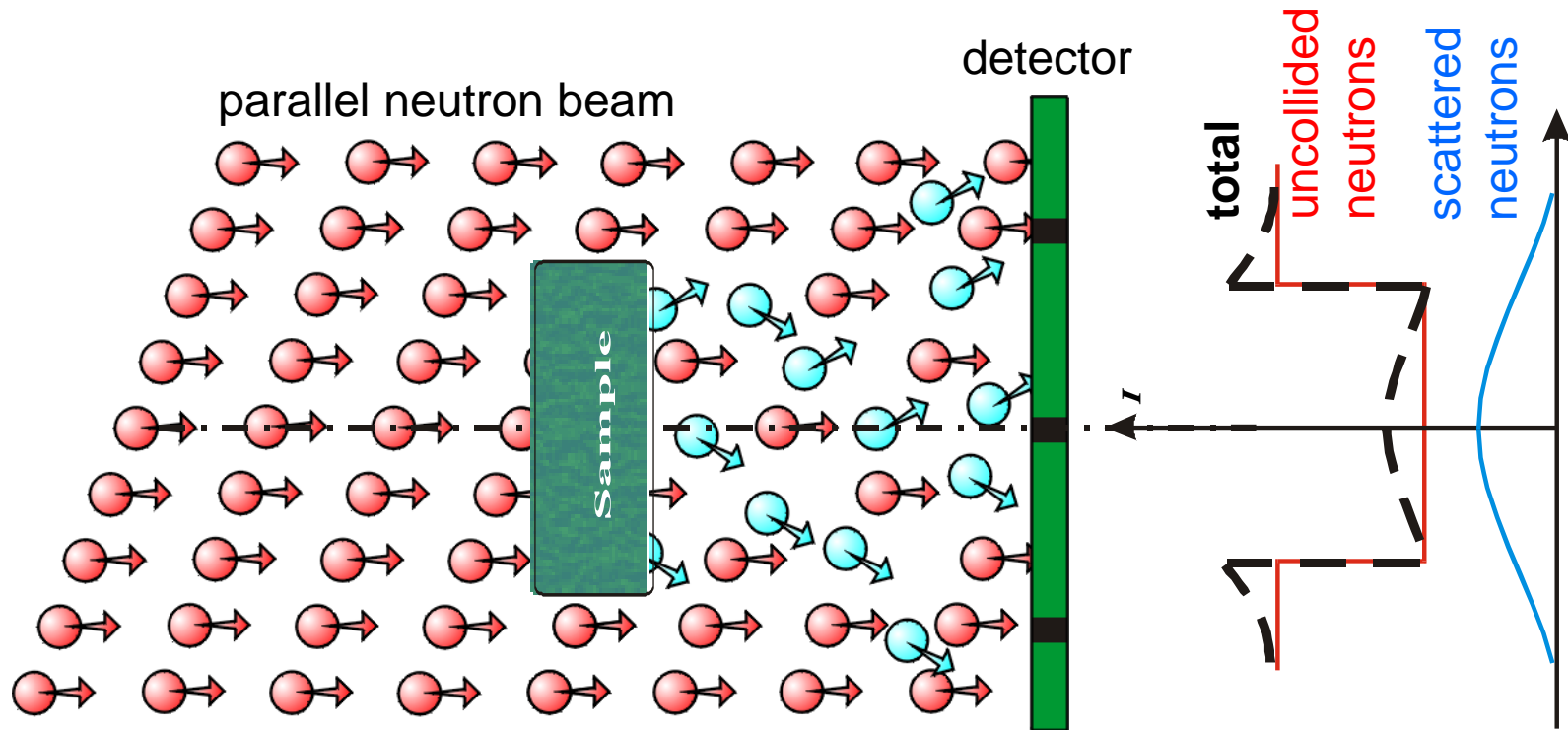


Effect not negligible for neutron absorber materials and H₂O !

Correlation: beam hardening increases with steepness of $\Sigma(E)$







DISS. ETH NO. 16809

CORRECTION METHODS FOR THE
QUANTITATIVE EVALUATION OF
THERMAL NEUTRON TOMOGRAPHY

A dissertation submitted to the
SWISS FEDERAL INSTITUTE OF TECHNOLOGY ZURICH

for the degree of
Doctor of Sciences

presented by
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Dr. Eberhard Lehmann, co-examiner
Prof. Dr. Peter Böni, co-examiner

2006

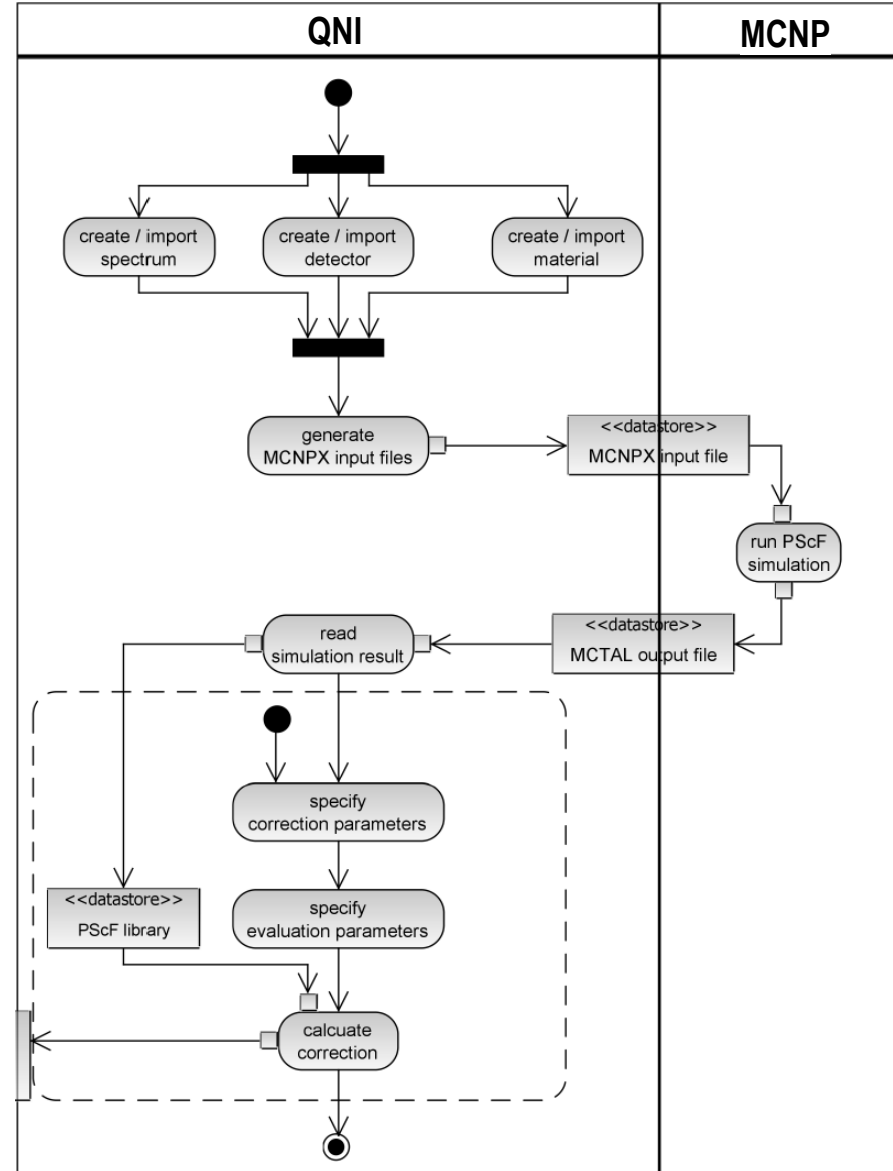
Program implemented in IDL
Executable running with IDL virtual machine.
QNI version 1.0 (2006) available on request from PSI.
No updates, no support, no helpline !

<http://e-collection.ethbib.ethz.ch/cgi-bin/show.pl?type=diss&nr=16809>

Facility, scintillator and sample material properties

Calculate point spread function parameters with MCNP

Iteratively calculate corrections considering detector background & sample scattering



QNI - Quantitative Neutron Imaging

File Spectrum Detector Material Simulation Correction Help

Create material

Name:

Material composition:

Si-28 Fraction:

O-16 Fraction:

☒ Atomic fractions ☐ Mass fractions

Density:

Density type: ☒ Density (g/cm³) ☐ Atomic density (1/cm³)

Ready

QNI - Quantitative Neutron Imaging

File Spectrum Detector Material Simulation Correction Help

Cross sections

Material:

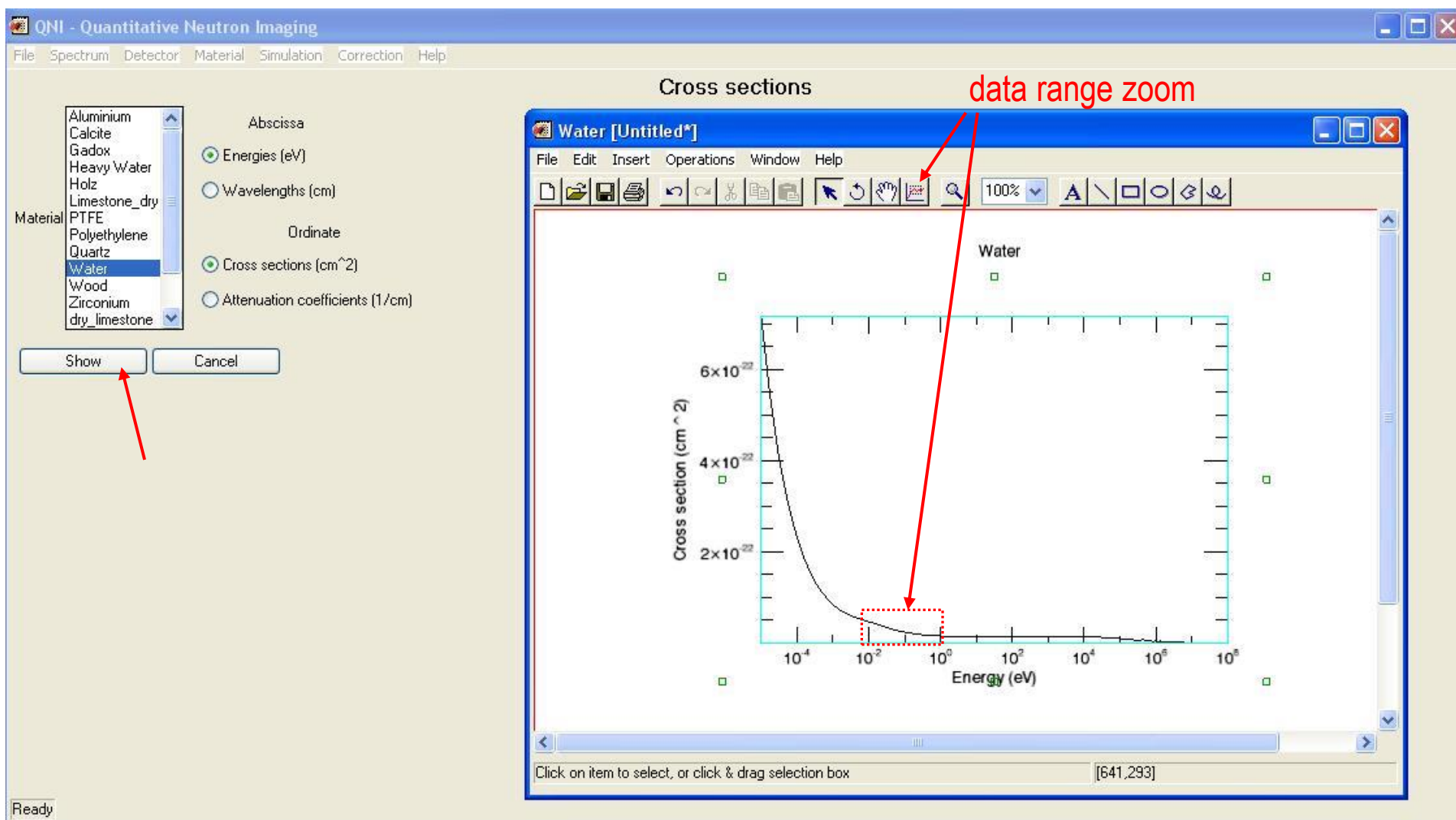
Abscissa

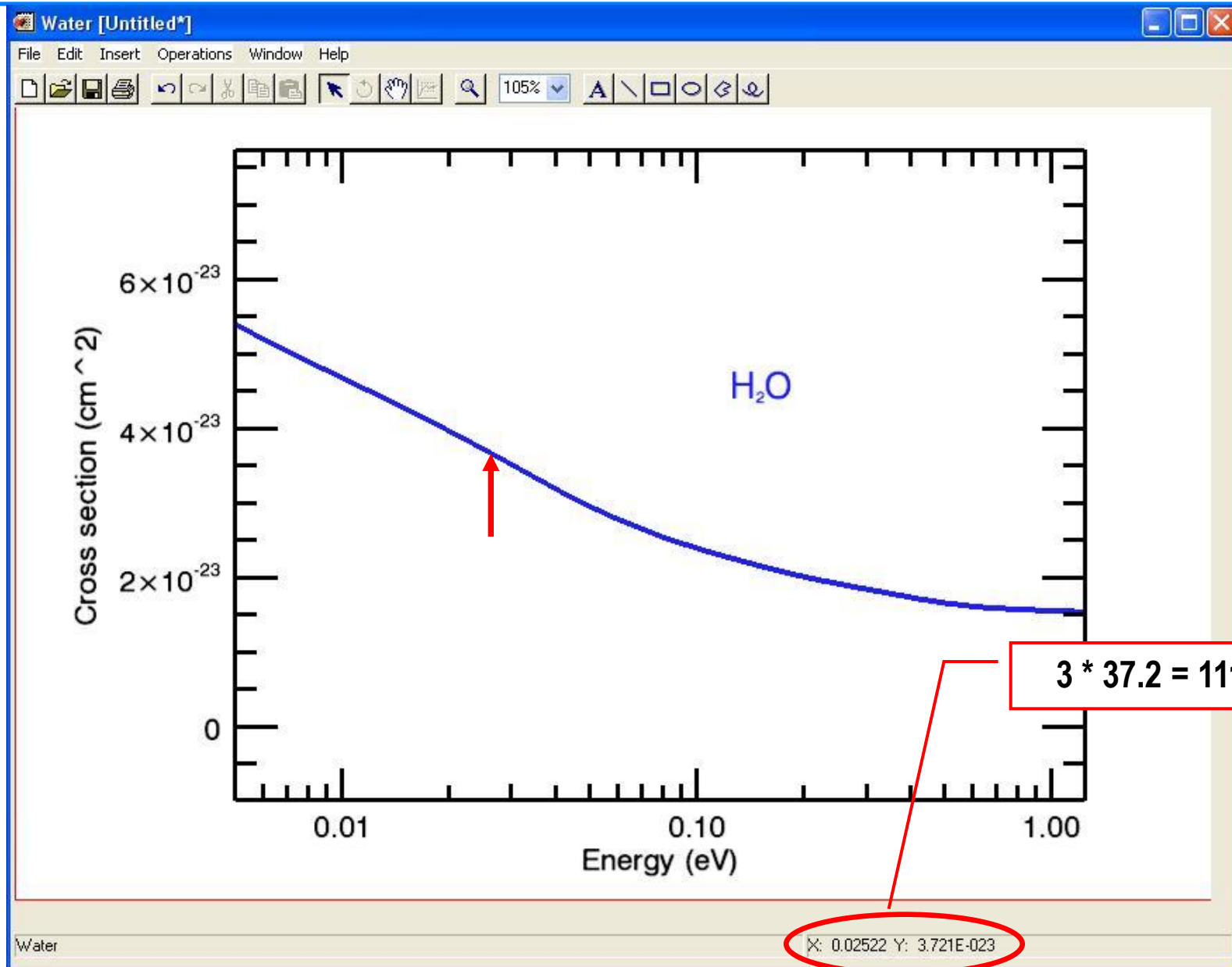
☒ Energies (eV) ☐ Wavelengths (cm)

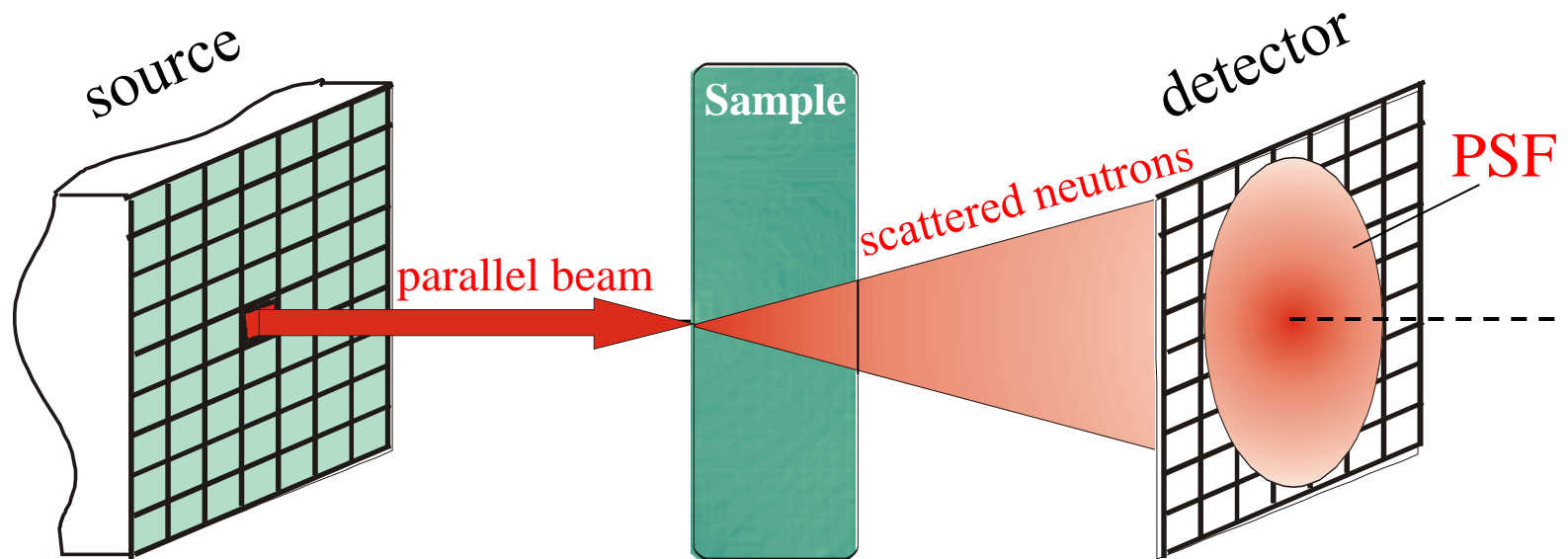
Ordinate

☒ Cross sections (cm²) ☐ Attenuation coefficients (1/cm)

Ready



QNI: H₂O cross section at 25 [meV]



Neutron
spectrum

Beam
divergence

Sample
material

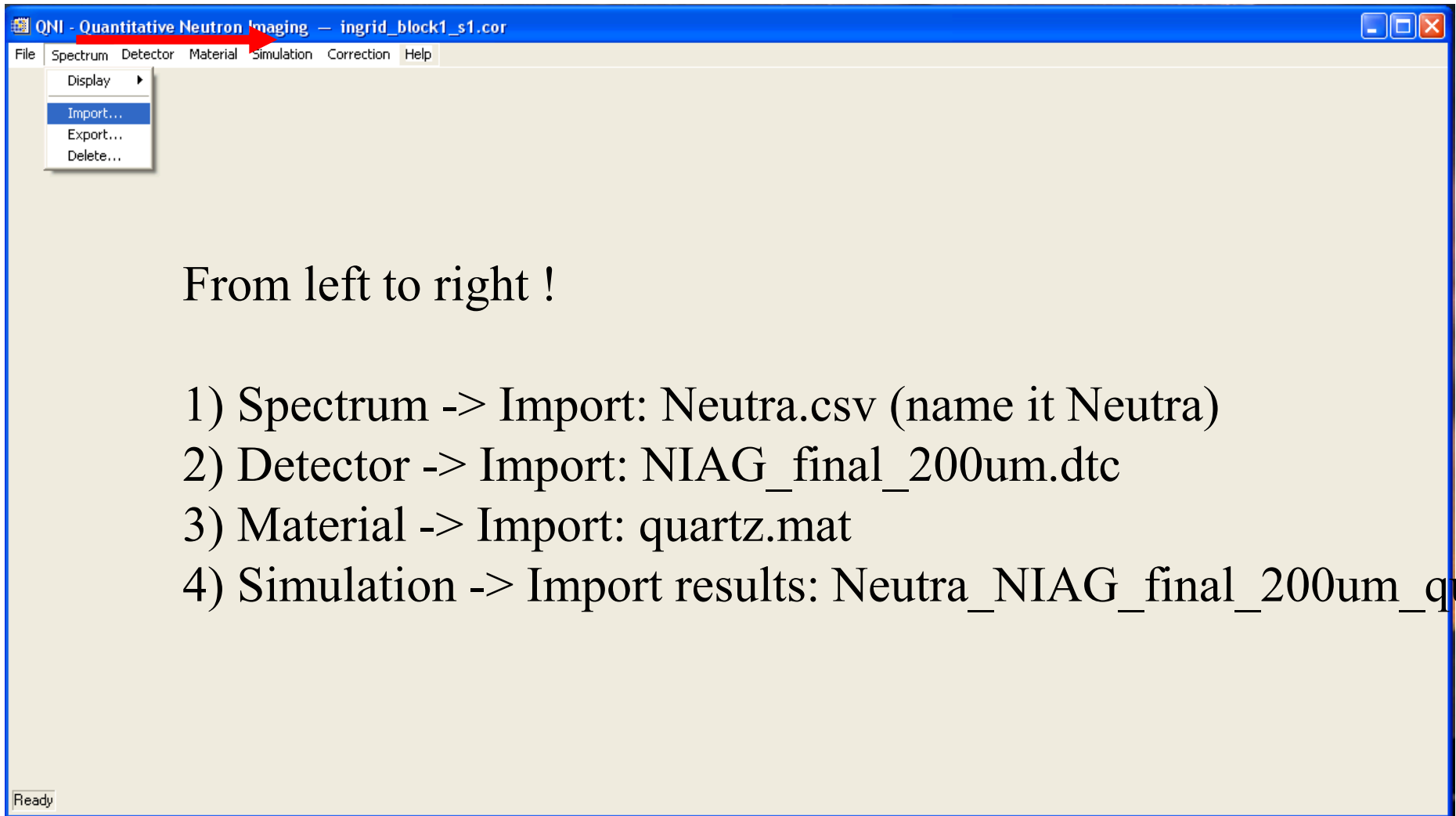
Material
thickness

Sample-detector
distance

→ MCNP →

PSF
or
PScF

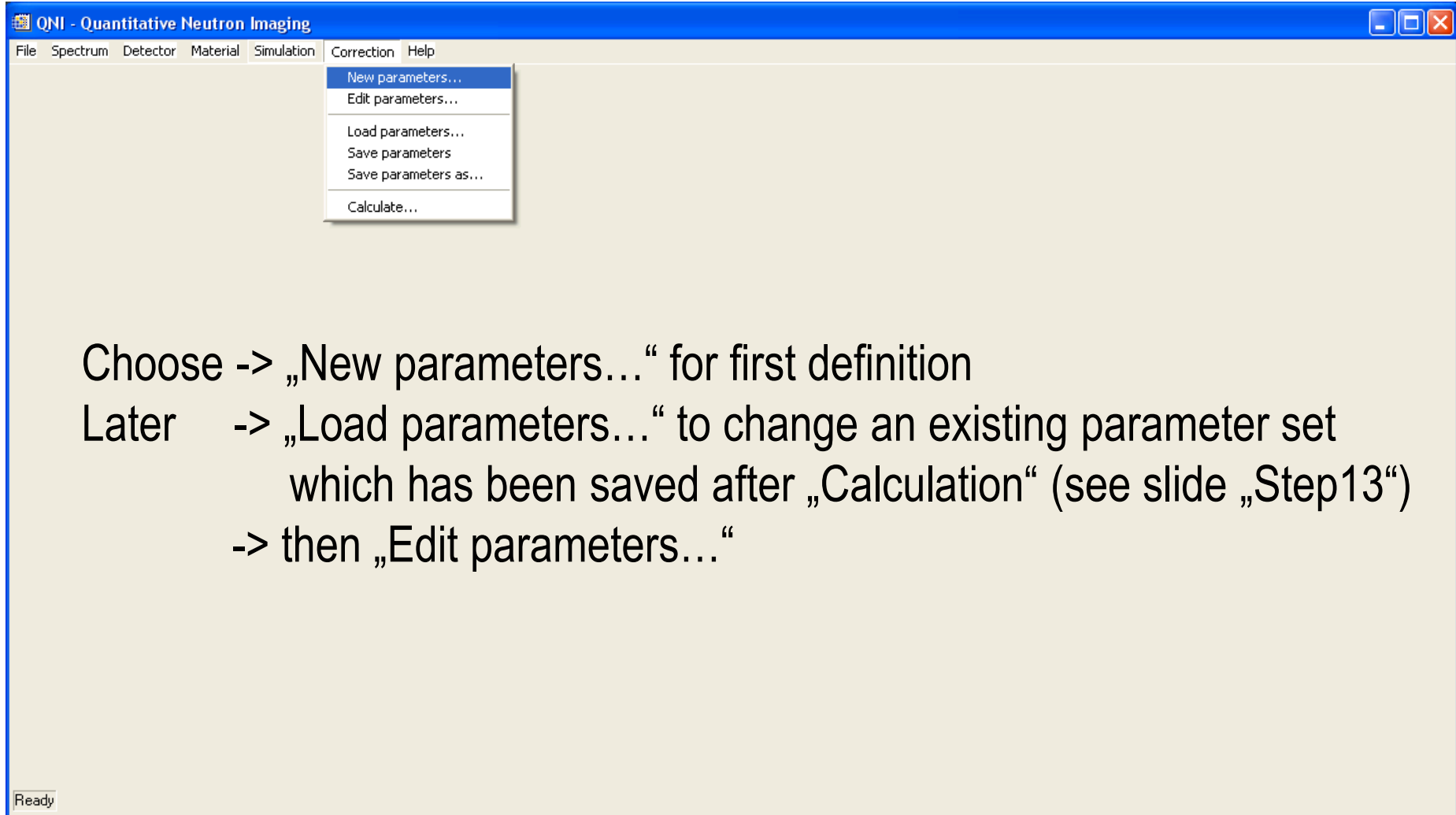
Setting up the problem



From left to right !

- 1) Spectrum -> Import: Neutra.csv (name it Neutra)
- 2) Detector -> Import: NIAG_final_200um.dtc
- 3) Material -> Import: quartz.mat
- 4) Simulation -> Import results: Neutra_NIAG_final_200um_qua

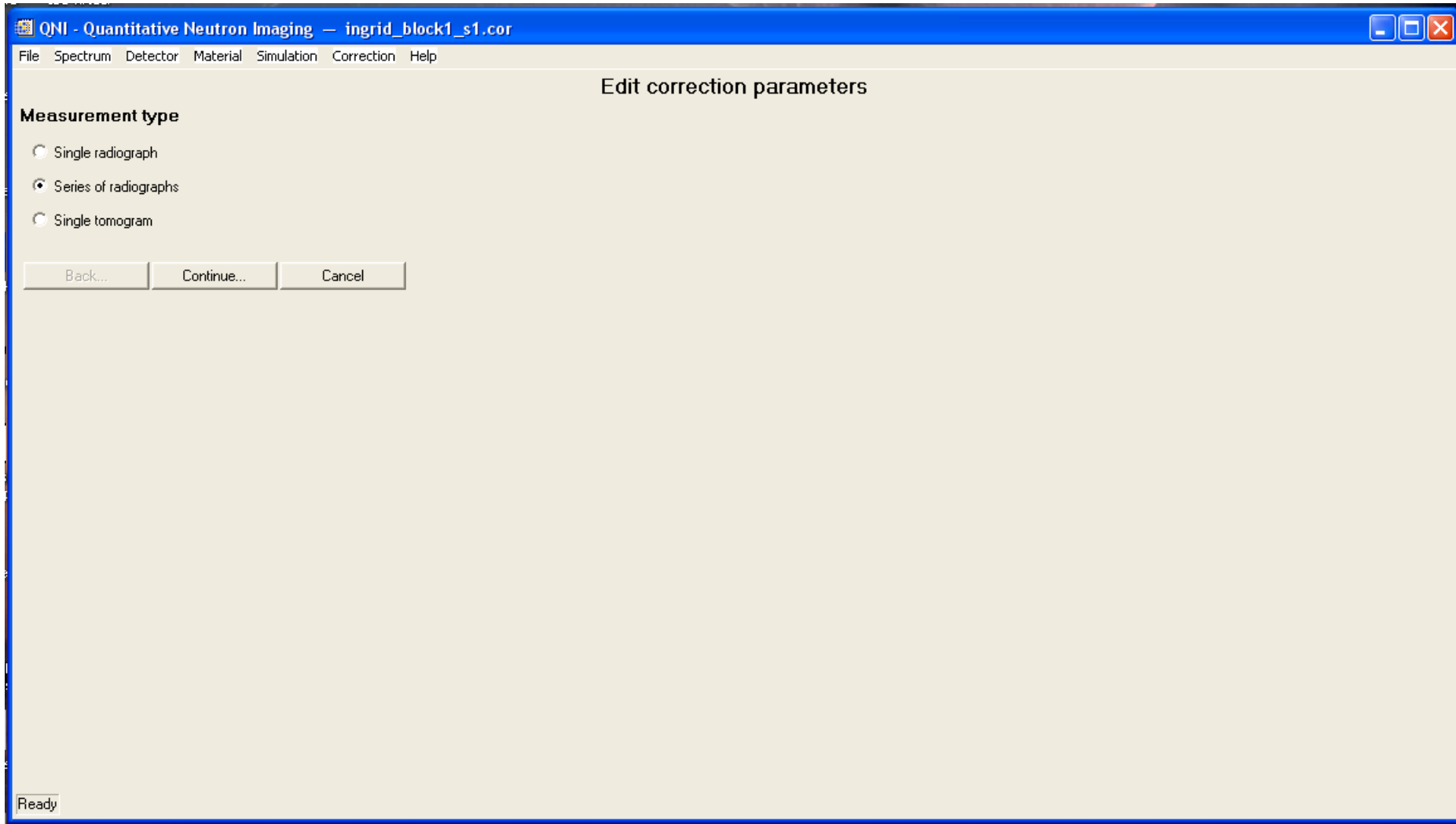
Set up correction parameters



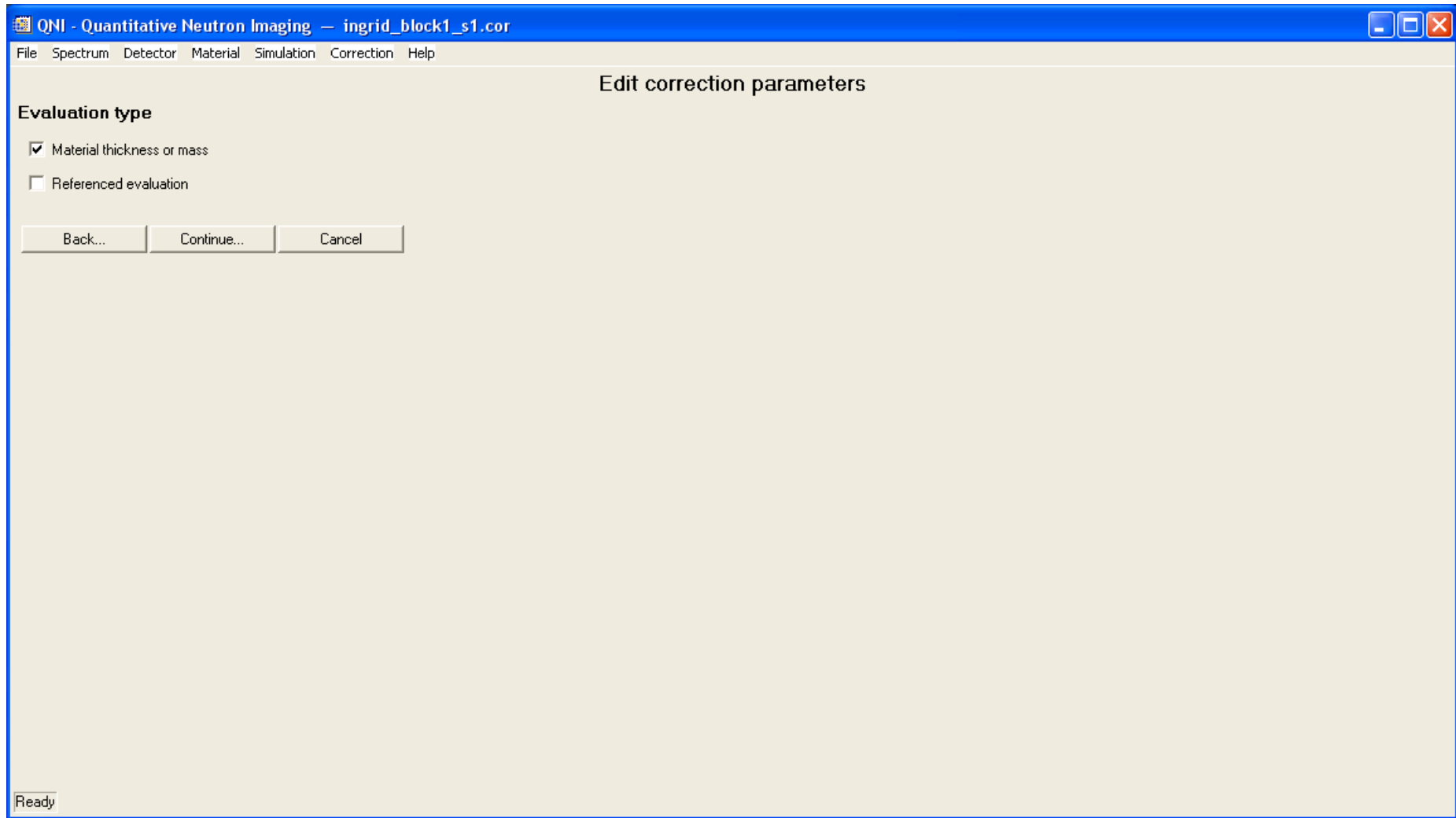
Choose -> „New parameters...” for first definition

Later -> „Load parameters...” to change an existing parameter set
which has been saved after „Calculation“ (see slide „Step13“)
-> then „Edit parameters...”

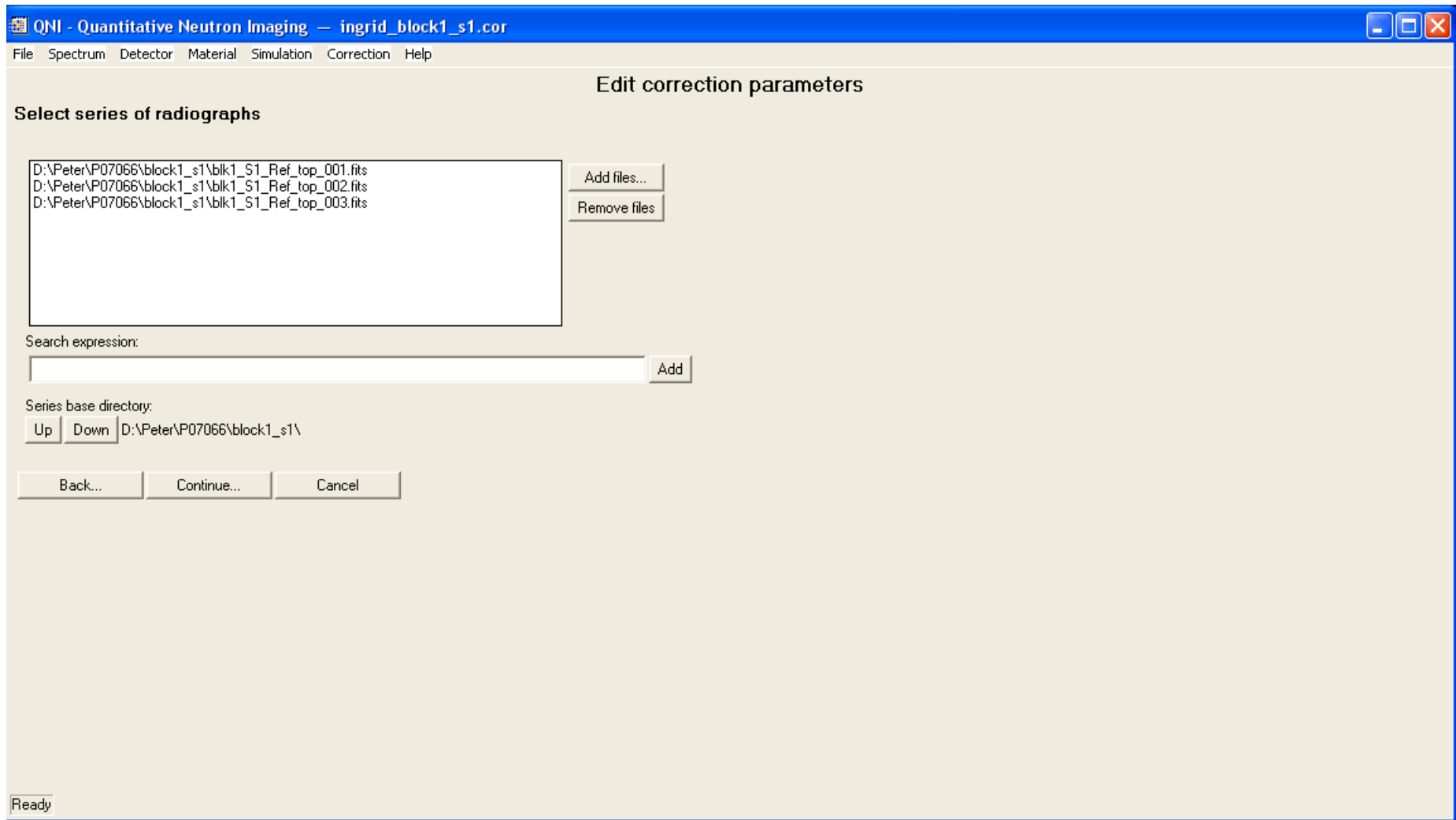
Correction parameters step by step



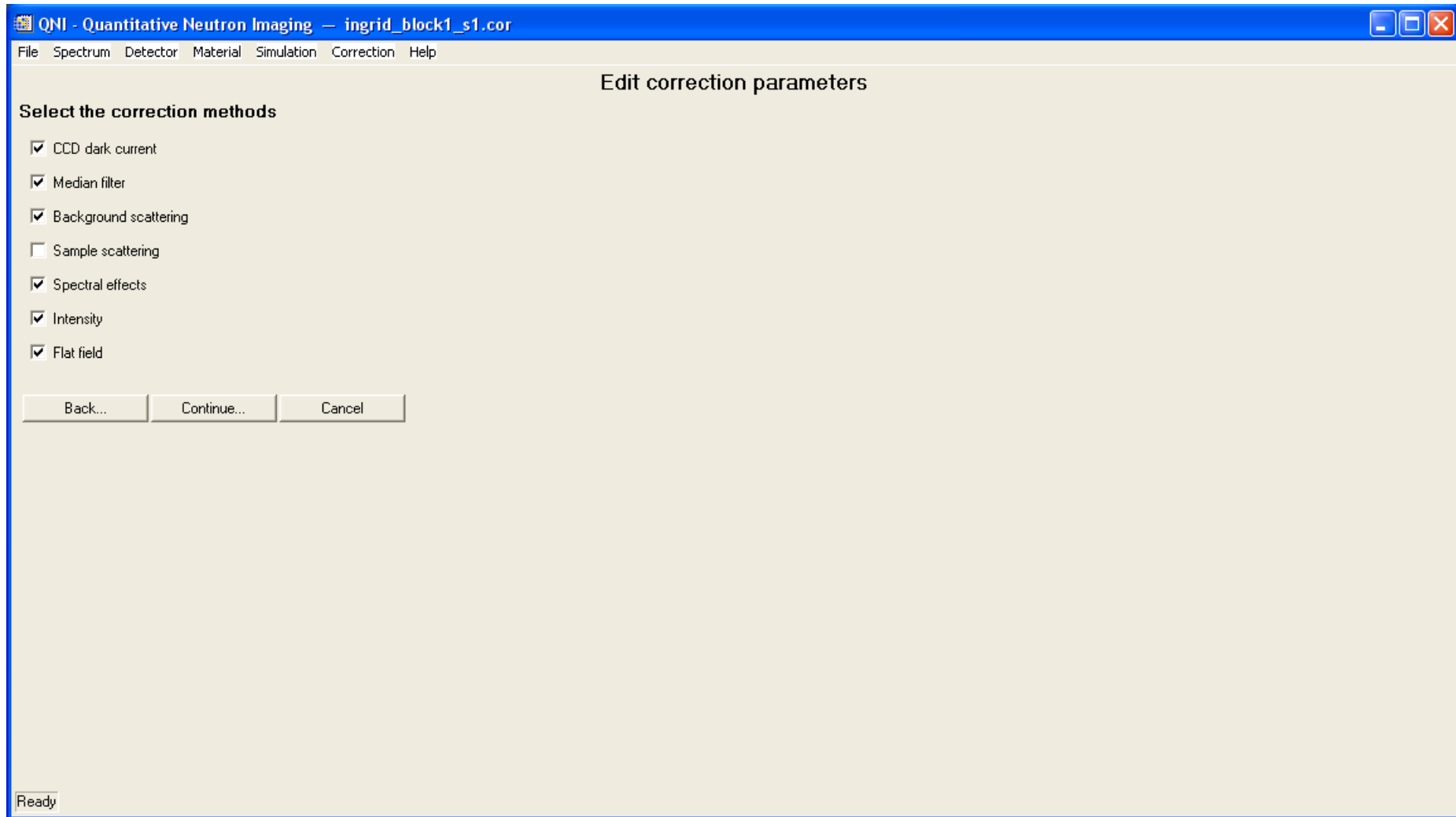
Step 2



Step 3



Step 4



Step 5

QNI - Quantitative Neutron Imaging -- ingrid_block1_s1.cor

File Spectrum Detector Material Simulation Correction Help

Edit correction parameters

Dark current correction

Type: ☒ Image file ☐ Constant value

Method: ☒ Pixelwise ☐ Mean value

Dark current file:

D:\Peter\P07066\dc_background_001.fits
D:\Peter\P07066\dc_background_002.fits
D:\Peter\P07066\dc_background_003.fits

Add files...
Remove files

Search expression:

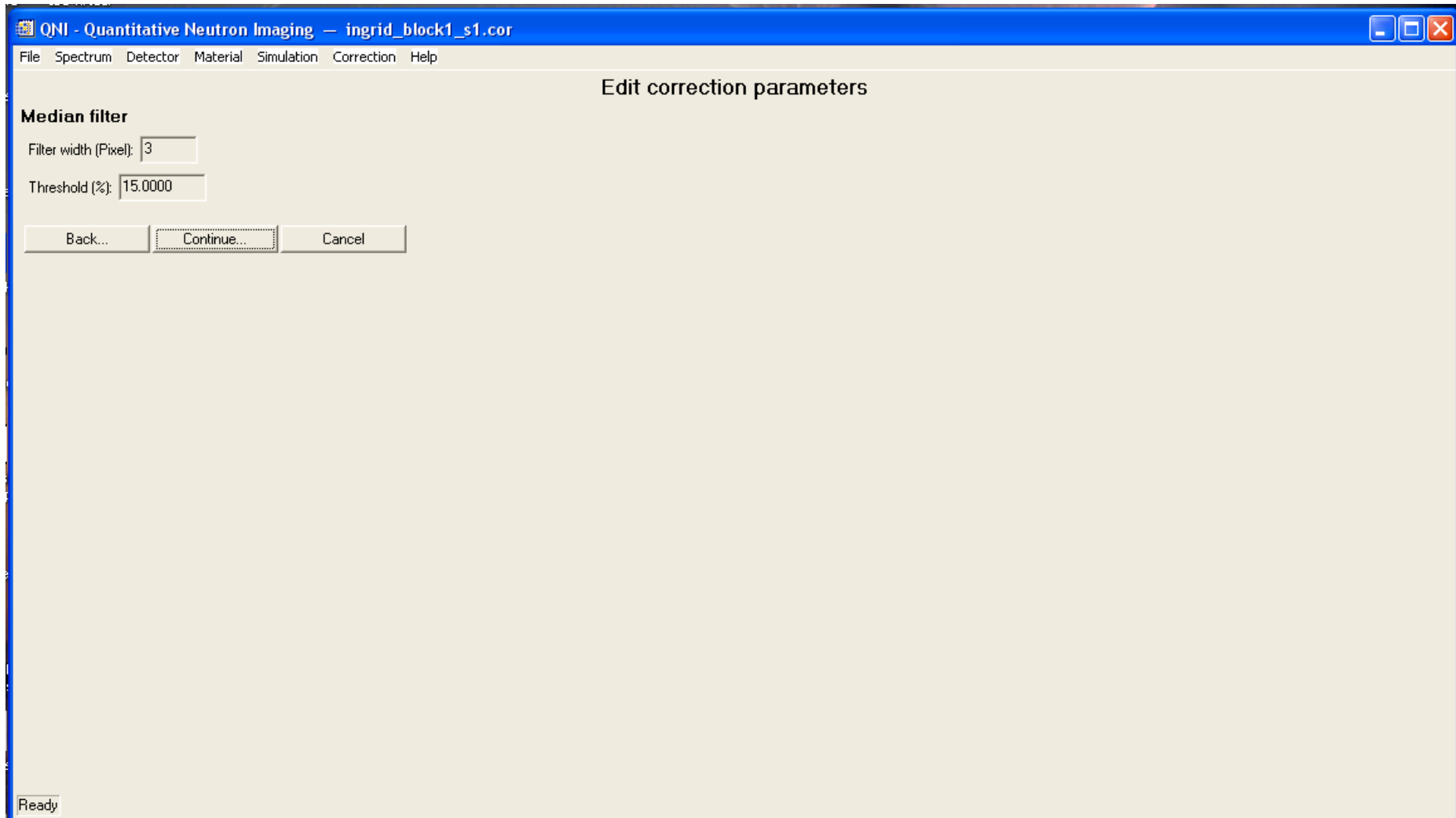
Add

Constant value: 0.000000

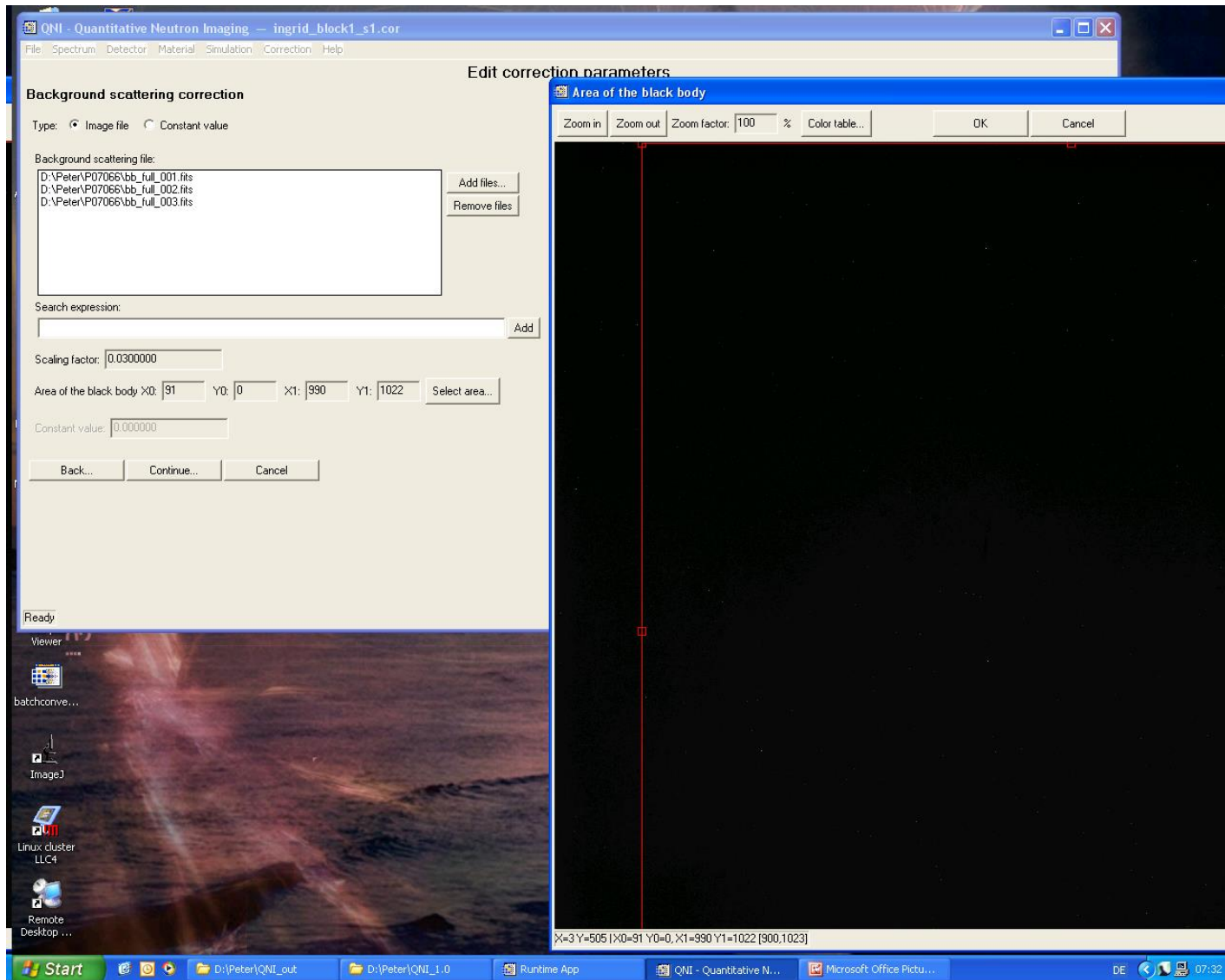
Back... Continue... Cancel

Ready

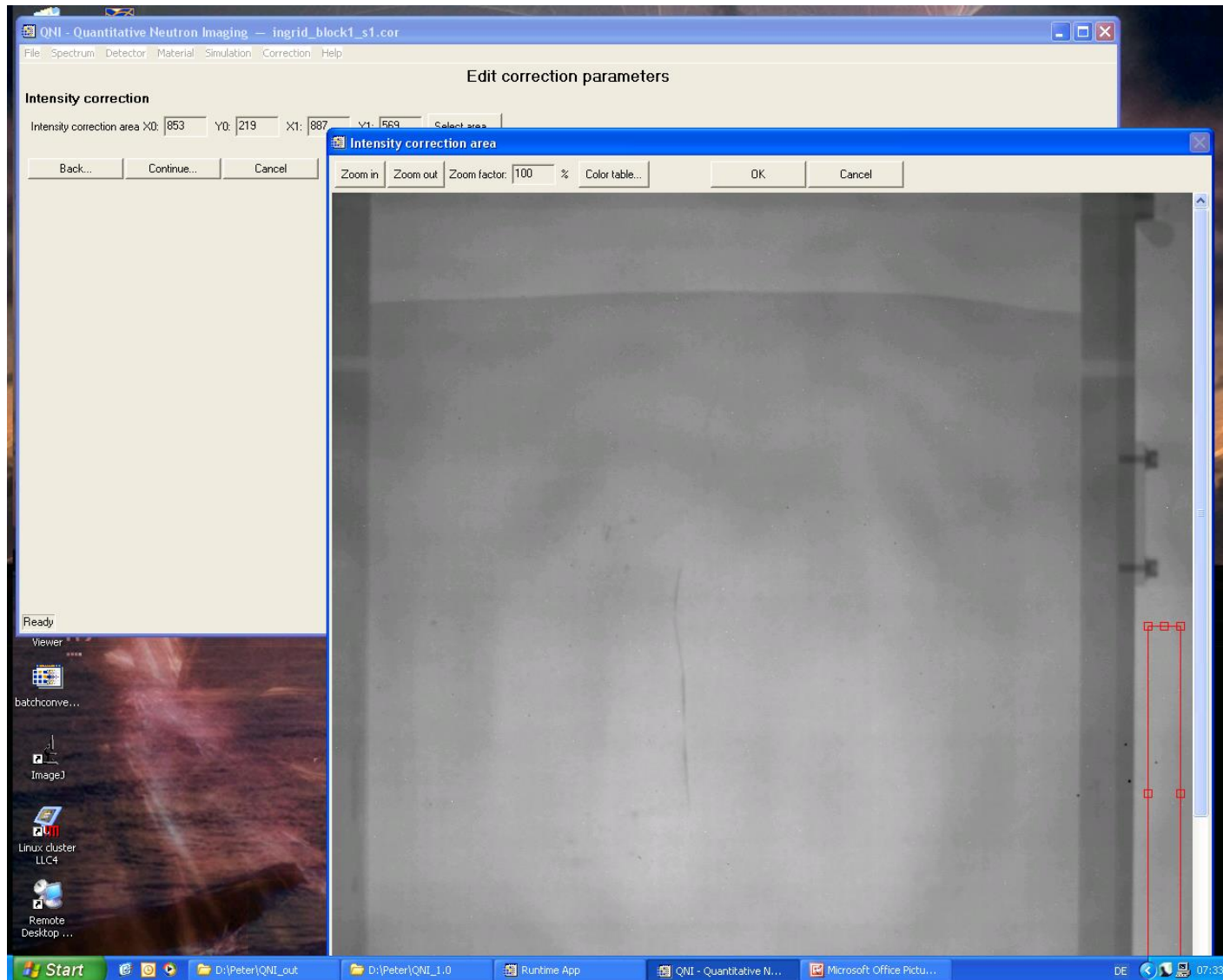
Step 6



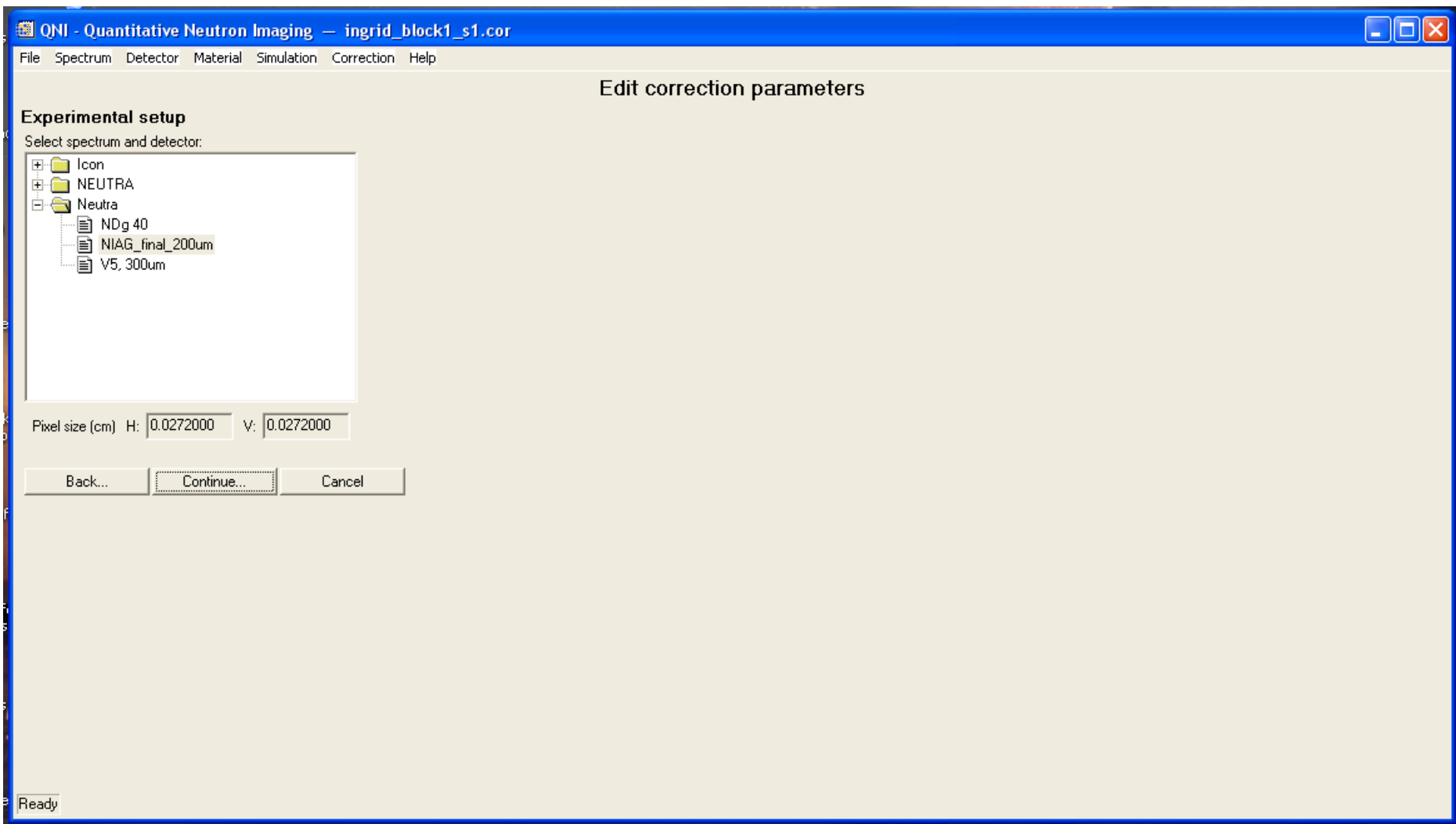
Step 7



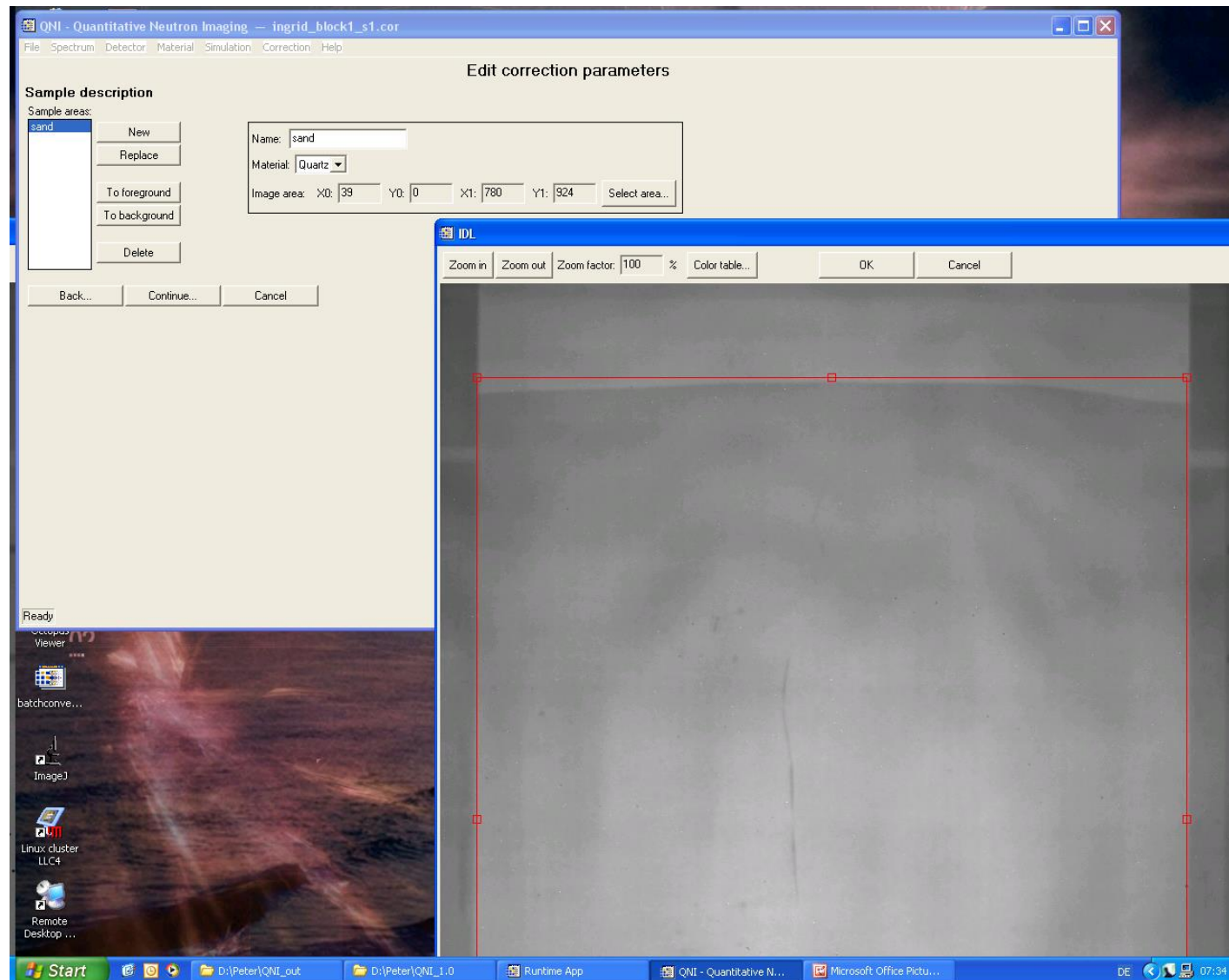
Step 8



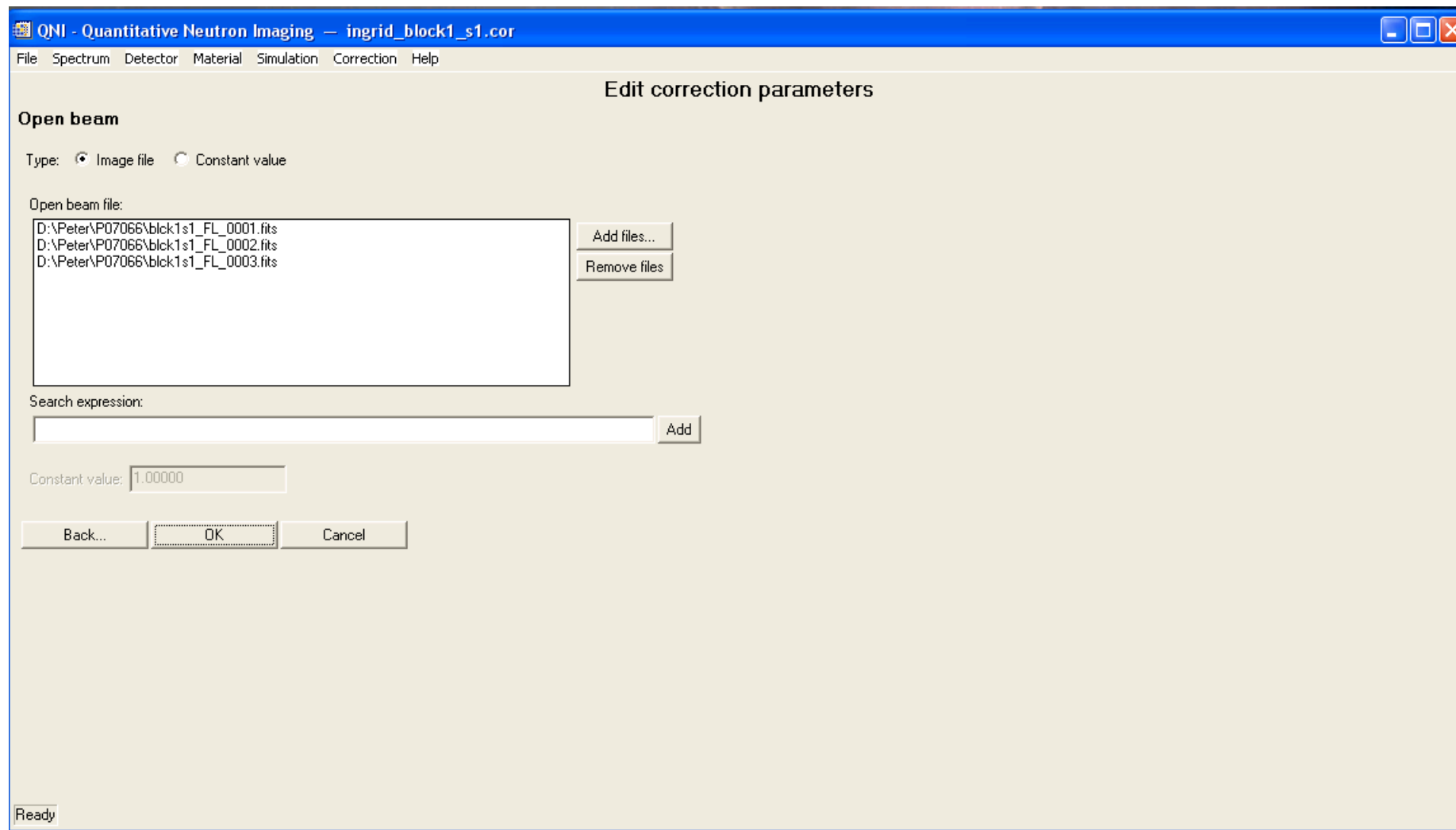
Step 9



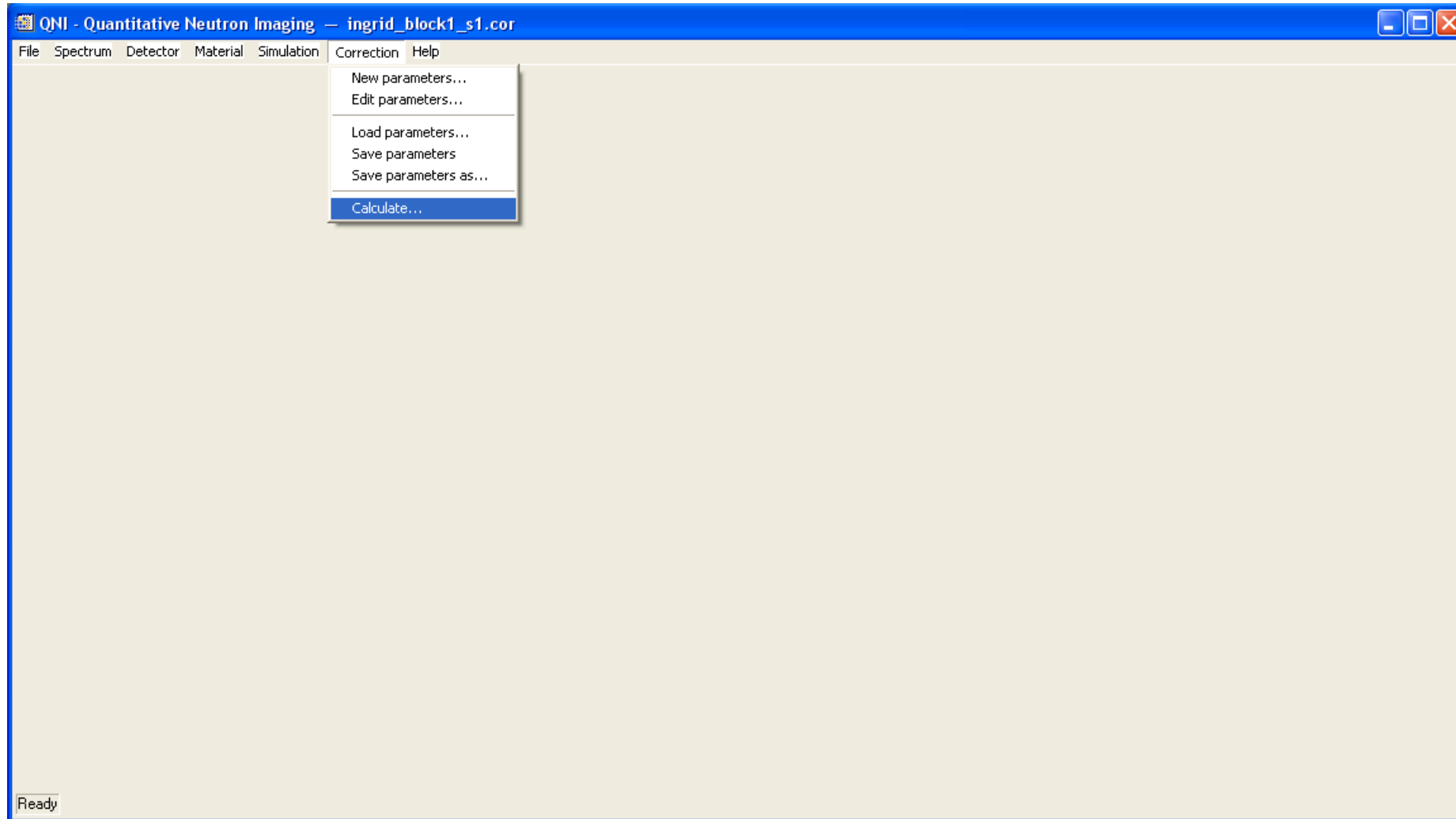
Step 10



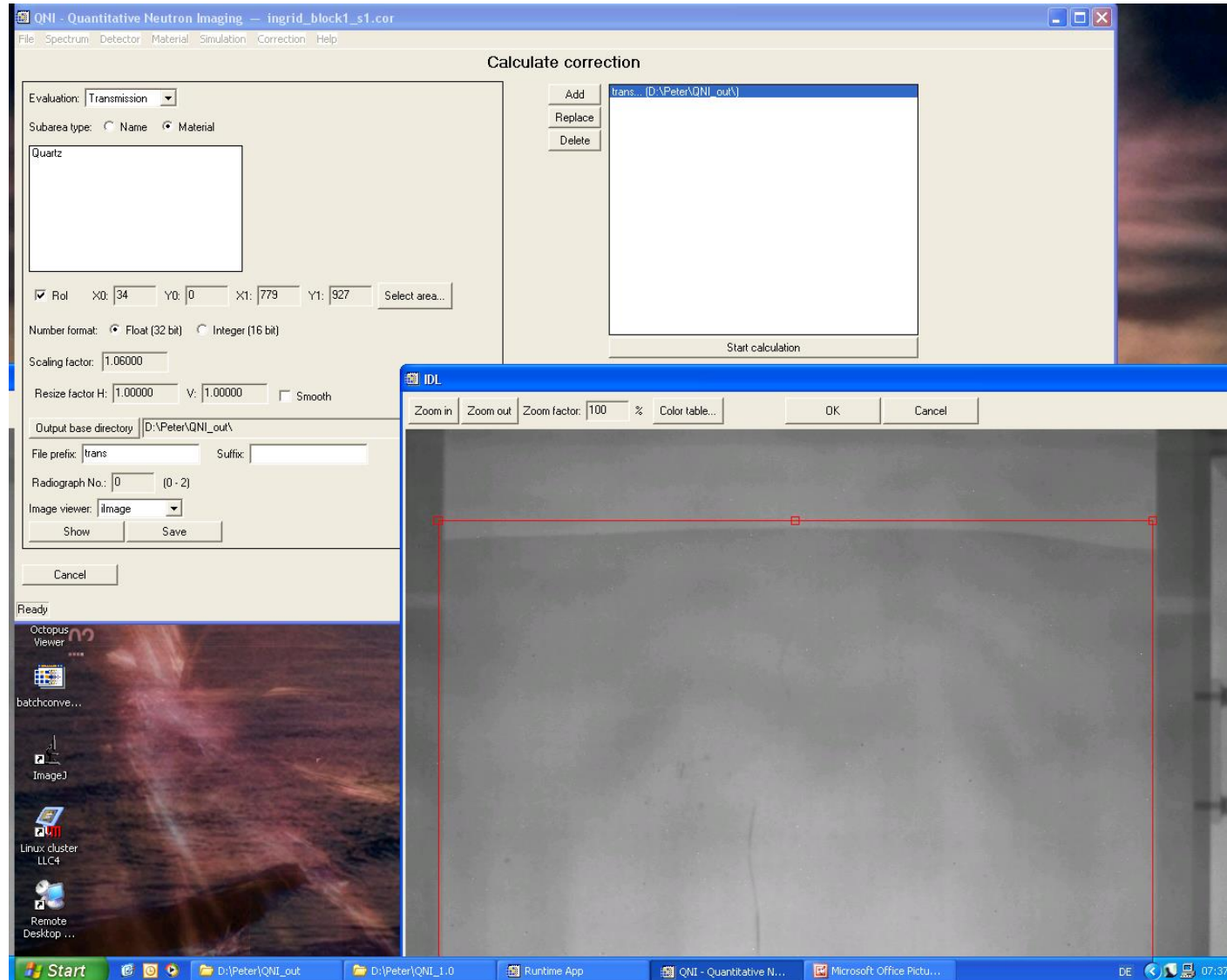
Step 11



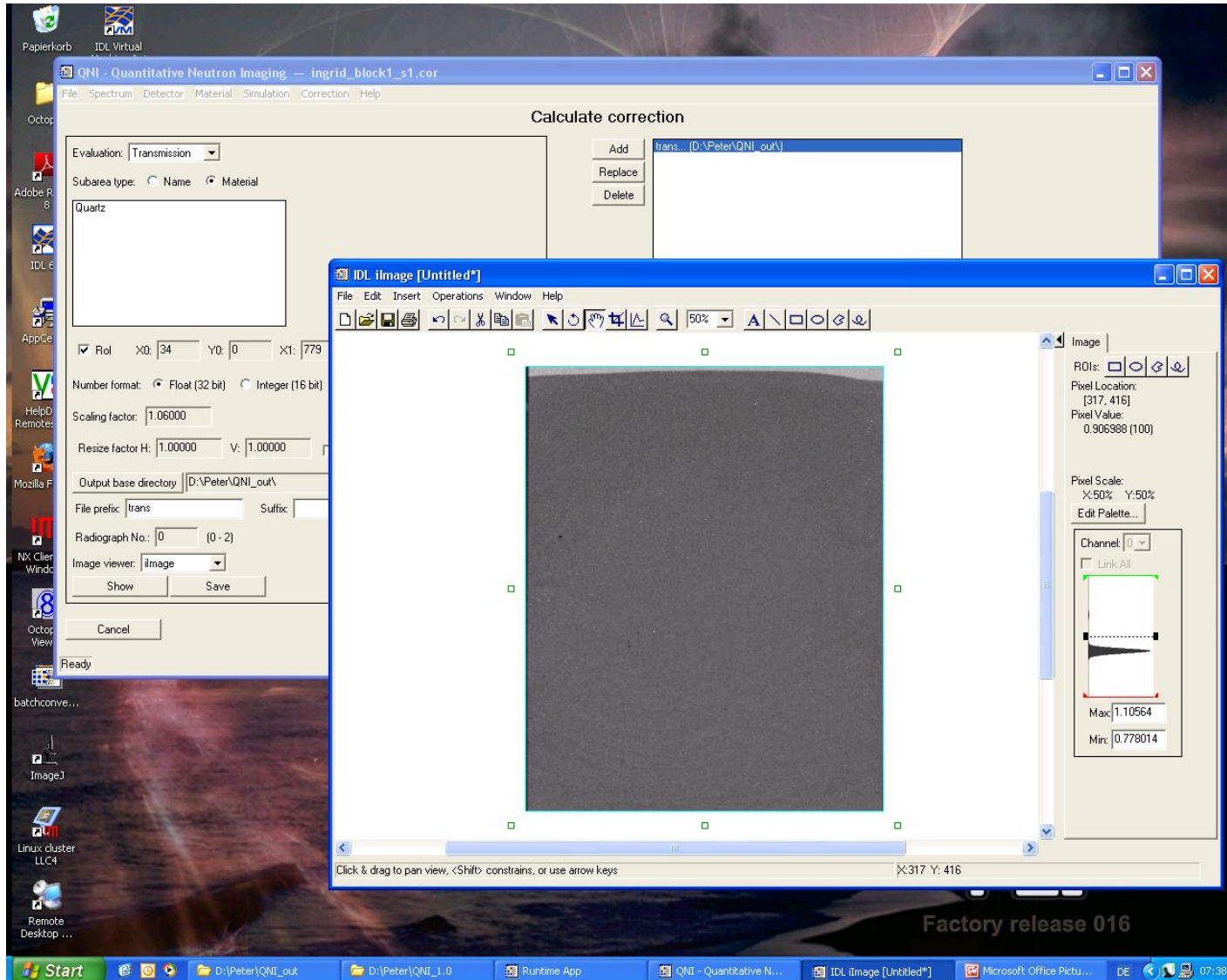
Step 12



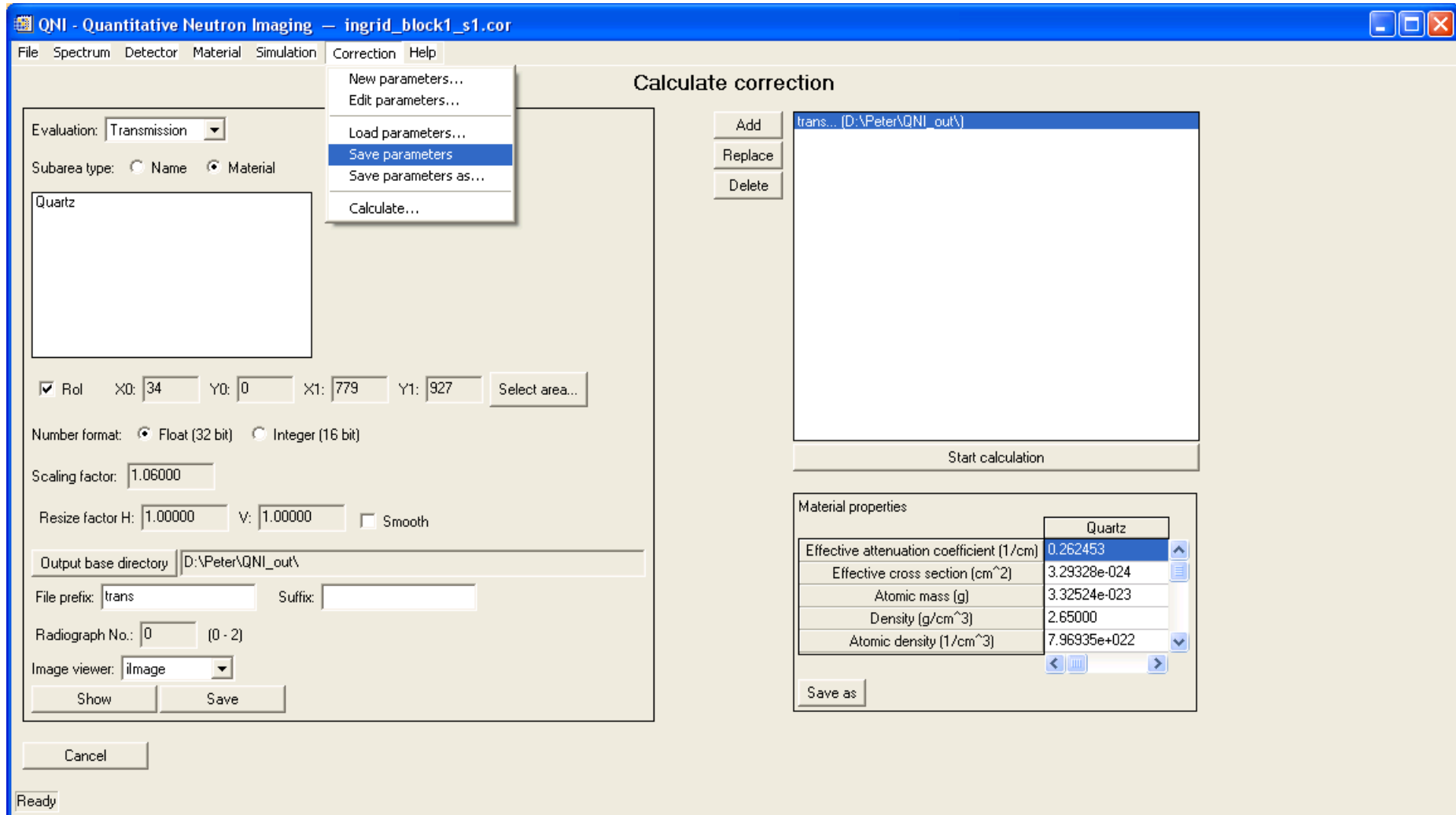
Step 13



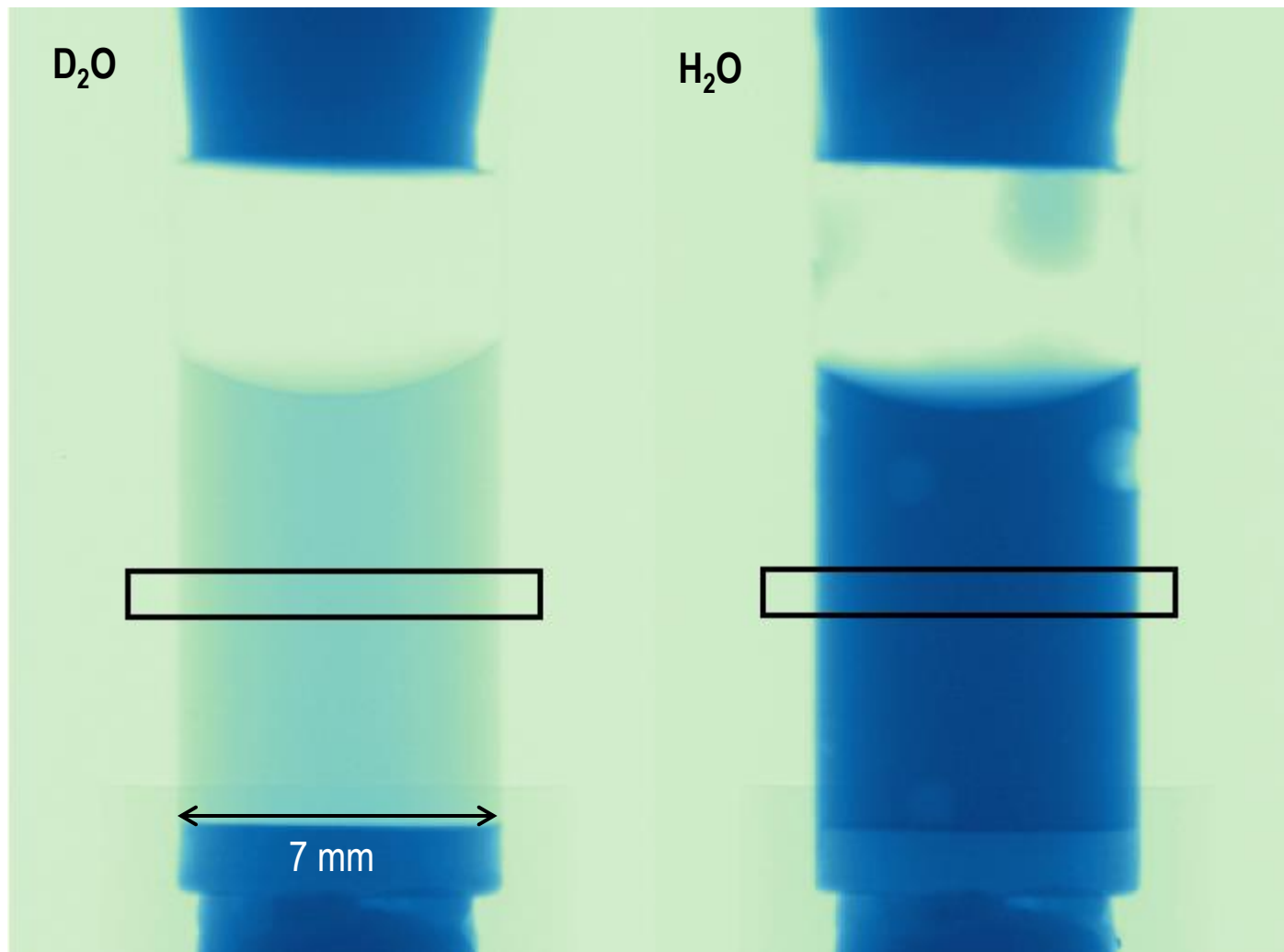
Step 14



Step 15



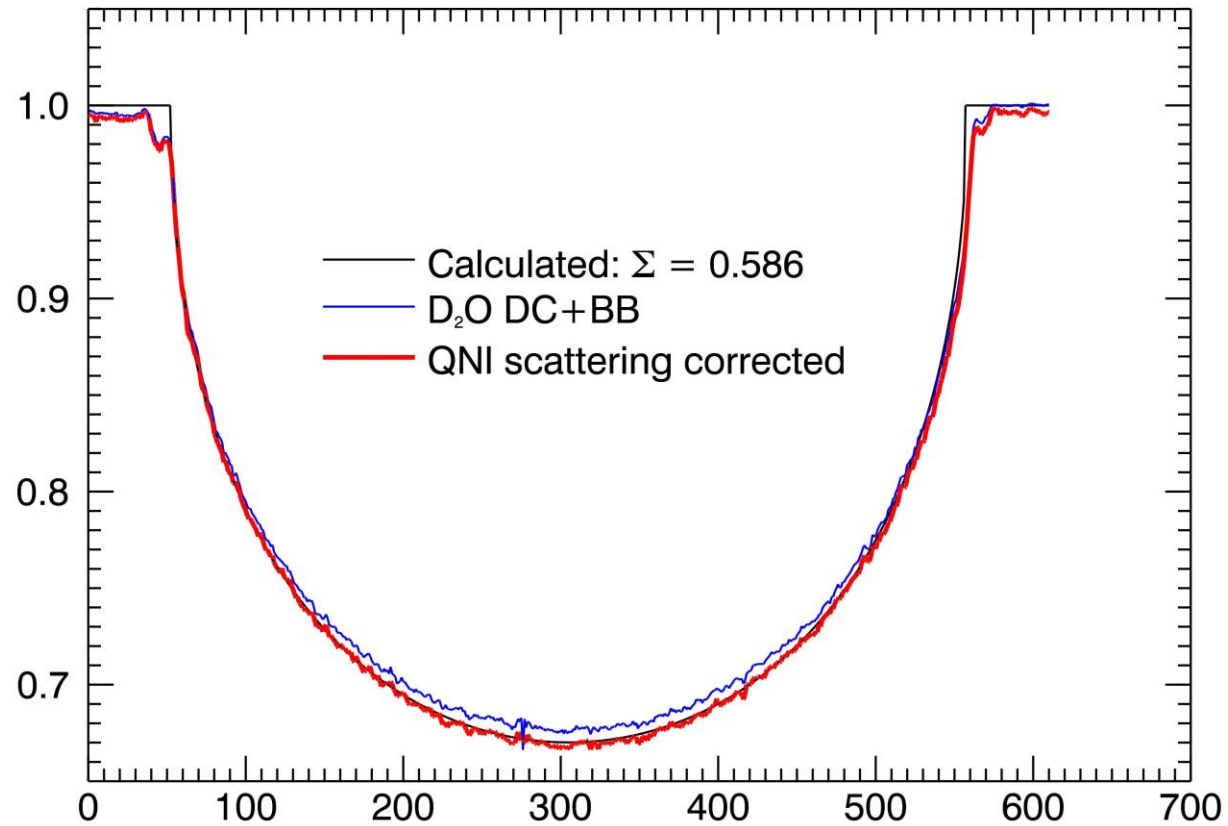
Effect of scattering correction in H₂O & D₂O



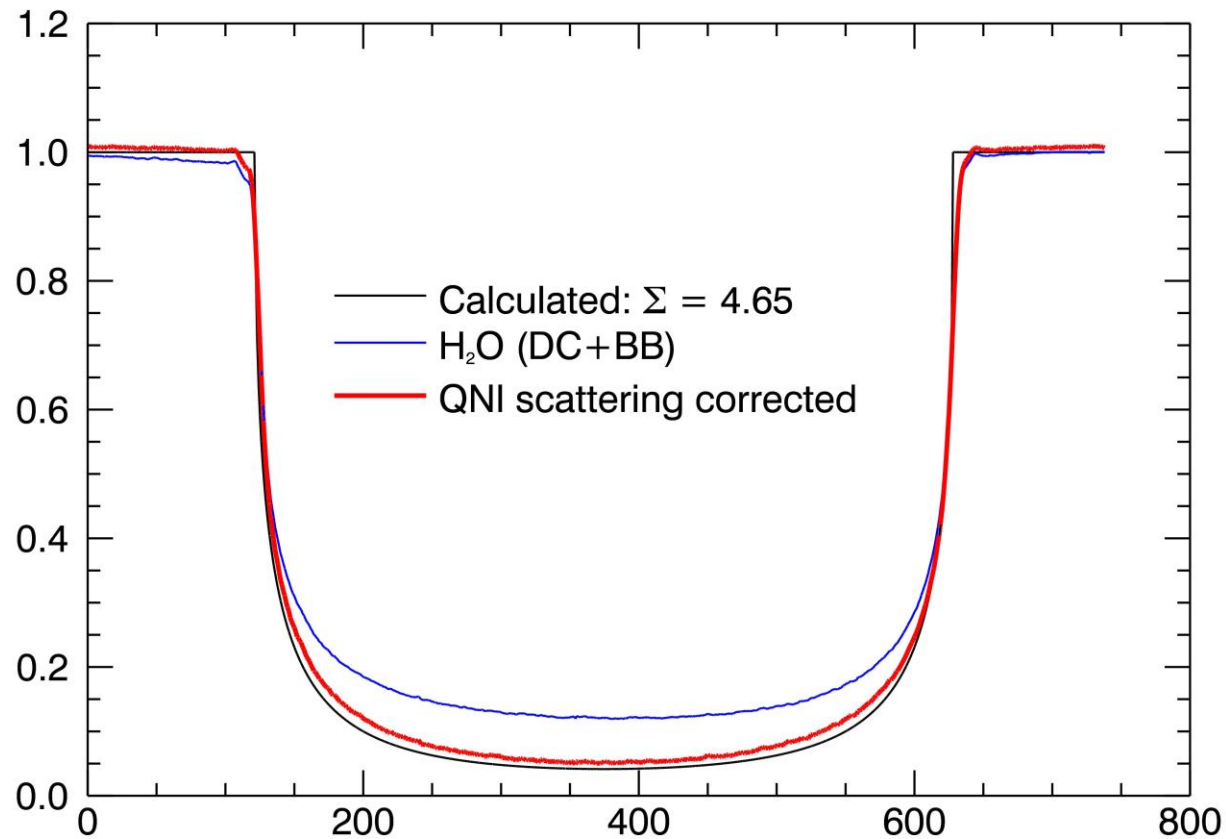
Measurements with μ -setup at ICON

Profile across D₂O cylinder

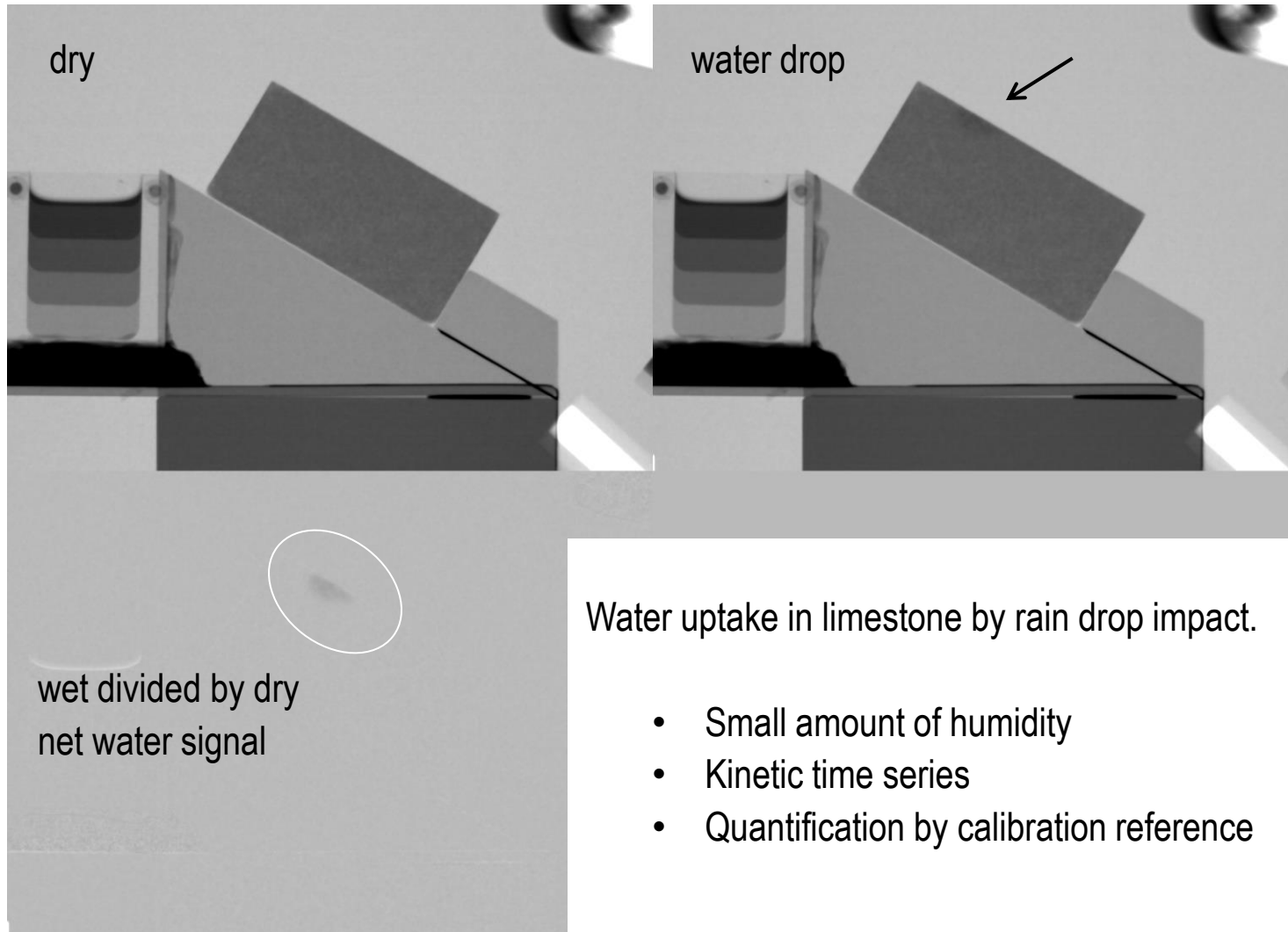
ICON Heavy water cylinder, Gadox 10 μ m



ICON: Water+OPA. Gadox 10 μ m



Referenced evaluation with calibration step wedge



$$T_w = \frac{I_w}{I_{ow}} = e^{-(\Sigma_w t_w + \Sigma_d t_d)}$$

Transmission of wet state T_w

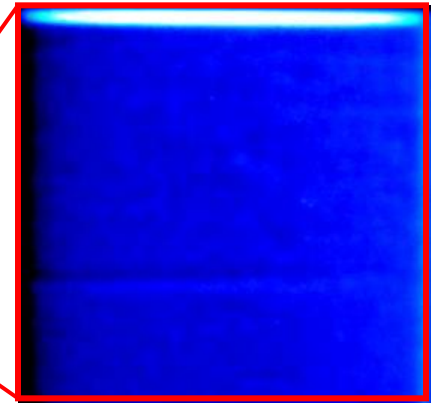
$$T_d = \frac{I_d}{I_{od}} = e^{-\Sigma_d t_d}$$

Transmission of „dry“ state T_d

Referencing wet to „dry“ T

$$\frac{T_w}{T_d} = e^{-\Sigma_w t_w} \quad \therefore -\ln\left(\frac{T_w}{T_d}\right) = \Sigma_w t_w$$

Assuming $\Sigma_w = 3.6$ [1/cm] and summing over results in mass of water lost [g]



Some hints for quantification

- Quantification starts with setting up the experiment correctly: e.g. choosing the appropriate scintillator, field of view and pixel-size, what are the measures to reduce neutron and/or γ -ray background, assess sample transmission before deciding on sample size, is imaging frame rate used in accordance with a sufficient signal-to-noise ratio,...
- If you know what you want to quantify, then think of additional independent measures e.g. measure the sample weight before/after or during the neutron-imaging sequence with a balance in-situ or at least at the start and end of the imaging sequence. Are additional standard references needed ?
- Think about the neutron image evaluation procedure before starting the measurements: e.g. how to assess the backgrounds. If a referenced evaluation is looked for, make sure that sample registration with the reference is guaranteed. If the sample shape changes during the experiment by swelling or shrinking, think of how this will affect a referenced evaluation. Do you need additional markers for sample registration ?
- When using the QNI framework make sure to perform all the required measurements and determine the sample to detector distance.

Thank you for your attention !

PSI neutron imaging links

NIAG: <http://www.psi.ch/niag>

NEUTRA: <http://www.psi.ch/sinq/neutra>

ICON: <http://www.psi.ch/sinq/icon>