

Antognini<sup>\*</sup>, N. Ayres, I. Belosevic, V. Bondar, R. Iwai, K. Kirch<sup>\*</sup>, F. Piegsa<sup>‡</sup>, T. Yan, and D. Taqqu

Institute for Particle Physics and Astrophysics, ETH Zurich, Switzerland

M. Hildebrandt, A. Knecht, J. Nuber, A. Papa<sup>§</sup>, C. Petitjean, and A. Stoykov Paul Scherrer Institute, 5232 Villigen-PSI, Switzerland

> D. M. Kaplan and T.J. Phillips Illinois Institute of Technology, Chicago, IL 60616 USA

\* also at the PSI

<sup>‡</sup> presently at university Bern

§ also at the INFN and university of Pisa

#### muCool: a phase-space compressor





# **Working principle**



$$\vec{v}_D = \frac{\mu E}{1 + \omega^2 \tau_c^2} \left[ \hat{E} + \omega \tau_c \left( \hat{E} \times \hat{B} \right) + \omega^2 \tau_c^2 (\hat{E} \cdot \hat{B}) \hat{B} \right]$$

▶  $\tau_c$ : mean time between two  $\mu^+$ —He collisions

▶  $ω : μ^+$  cyclotron frequency



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### Trajectories in E- and B-fields with and without gas





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#### **Transverse compression: working principle**





#### **Transverse compression: simulations**





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#### **Transverse compression: simulations & measurements**



#### More .....



#### **Transverse compression: setup & target**





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A. Antognini et al., PRL 125, 164802 (2020) I. Belosevic, PhD Thesis ETH Zurich (2019)

#### Editors' Suggestion

# Demonstration of Muon-Beam Transverse Phase-Space

A. Antognini, N. J. Ayres, I. Belosevic, V. Bondar, A. Eggenberger, M. Hildebrandt, R. Iwai, D. M. Kaplan, K. S. Khaw, K. Kirch, A. Knecht, A. Papa, C. Petitjean, T. J. Phillips, F. M. Piegsa, N. Ritjoho, A. Stoykov, D. Taqqu, and G. Wichmann (muCool Collaboration) Phys. Rev. Lett. **125**, 164802 (2020) – Published 15 October 2020



An important step towards a high brightness, low energy, muon beam is achieved by compressing a positive muon beam from a vertical spread of 10 mm to 0.7 mm within a few microseconds.

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### Longitudinal compression: simulation









#### Longitudinal compression: measurements



Y. Bao et al., PRL 224801 (2014)

I. Belosevic et al., EPJC 79, 430 (2019)



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#### The general scheme





### **Mixed transverse-longitudinal compression**





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#### New target design





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#### **Mixed compression: measurements**





### **Mixed compression: discrepancy**



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#### New target design





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#### New target adaptable to extraction





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### Gas injection for extraction



destroy the vertical density gradient



Gas barrier for the target



#### **Extraction (base scheme)**





#### Extraction — pulsed re-acceleration



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#### Extraction — pulsed re-acceleration





Accumulation can be very complicated:

- degradation of beam quality
- muon decay

#### Extraction — cw re-acceleration





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### The muCool setup



## **Extraction from B-field**

Charge particles follow magnetic field lines

$$r_i \sim r_0 \sqrt{\frac{B_0}{B_i}}$$

$$\Delta E_{\perp i} \sim \Delta E_{\perp 0} \frac{B_i}{B_0}$$



The magnetic field can be terminated so that the beam transits from a region to another region with different field strengths. But in this process the charge particle receive an additional traverse momentum

,

$$\begin{split} \Delta p_{\perp} &= e \int_{0}^{t} v_{z} B_{\perp} dt \sim \frac{e w B_{i}}{2} \\ \Delta E_{\perp} &= \frac{e^{2}}{8m} w^{2} B_{i}^{2} \quad , \end{split}$$

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Gerola et al., Rev. Sci. Instrum. 66 (7) 1995

# **Extraction from B-field**



- Terminate B-field
- ▶ The radial component produces an azimuthal force  $F_{\theta} = -ev_z B_r(z)$
- ▶ The azimuthal force produces a divergence

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 $\alpha = \frac{eB_0}{2m\gamma} \frac{R}{v}$ 



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### **Extraction from B-field**

▶ At B = 4 T : beam diameter of 1mm

$$r_{i} \sim r_{0} \sqrt{\frac{B_{0}}{B_{i}}}$$
$$\Delta E_{\perp i} \sim \Delta E_{\perp 0} \frac{B_{i}}{B_{0}}$$

Terminate B-field at B=0.01 T with 2 mm grid spacing Far field divergence 2 mrad Beam diameter is 20 mm Transmission 70%



E:	10 keV		
ΔΕ:	100 eV		
Diameter:	20 mm		
Divergence:	2 mrad		



## **Preliminary simulations of extraction**



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# Preliminary simulations: density

Cryogenic Target He injection Continuous flow simulations with ANSYS ⊳ (accurate till 5 mm from last wall) Pumped region Differentially pumped region will be ⊳ simulated with Monte Carlo approaches Density Contour 1 9.046e-02 3.565e-02 1.405e-02 He injection 5.536e-03 2.182e-03 8.597e-04 3.388e-04 1.335e-04 5.261e-05 2.073e-05 8.170e-06 3.220e-06 1.269e-06 5.000e-07 [kg m^-3]



### **Preliminary simulations: temperature**



![](_page_30_Picture_2.jpeg)

### **Preliminary simulations: density**

![](_page_31_Figure_1.jpeg)

![](_page_31_Picture_2.jpeg)

# Preliminary simulations: density gradient in target

Density gradient is only minimally affected by gas injection

[K]

![](_page_32_Figure_2.jpeg)

![](_page_32_Figure_3.jpeg)

1.250

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3.750

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# Efficiency for cw acceleration using mixed target

	2.5 x 10⁻⁵	Total efficiency
	7 x 10 <sup>-1</sup>	Transmission through grid
	8 x 10 <sup>-1</sup>	Muon decay till end of solenoid
		Accumulation and pulsing
	4 x 10 <sup>-1</sup>	Drift from orifice to re-acceleration region
	6 x 10 <sup>-1</sup>	Extraction from orifice
	1.0 x 10 <sup>-1</sup>	Compression towards orifice (in about 5 µs)
HIMB	6 x 10 <sup>-3</sup>	Stopping in active region of gas target (10 mbar, 14 K
HIMB	3 x 10 <sup>-1</sup>	Injection into solenoid and coupling into gas target

![](_page_33_Figure_2.jpeg)

Using demonstrated mixed target

- 10% (FWHM) momentum bite is a big problem
- ▶ Stopping probability in 10 mbar He @ 14 K, 5 T:

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- ▶ 2.1% FWHM= 1%
- ▶ 1.6% FWHM= 3%
- ▶ 0.6% FWHM= 10%

![](_page_33_Picture_9.jpeg)

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# Efficiency for cw acceleration using mixed target

			1
5 x 10 <sup>-1</sup>	3 x 10 <sup>-1</sup>	Injection into solenoid and coupling into gas target	4
1 x 10 <sup>-2</sup>	6 x 10 <sup>-3</sup>	Stopping in active region of gas target (10 mbar, 14 K)	
1.5 x 10 <sup>-1</sup>	1.0 x 10 <sup>-1</sup>	Compression towards orifice (in about 5 $\mu$ s)	
6 x 10 <sup>-1</sup>	6 x 10 <sup>-1</sup>	Extraction from orifice	
4 x 10 <sup>-1</sup>	4 x 10 <sup>-1</sup>	Drift from orifice to re-acceleration region	
		Accumulation and pulsing	
8 x 10 <sup>-1</sup>	8 x 10 <sup>-1</sup>	Muon decay till end of solenoid	Potential
7 x 10 <sup>-1</sup>	7 x 10 <sup>-1</sup>	Transmission through grid	
1.0 x 10 <sup>-4</sup>	2.5 x 10⁻⁵	Total efficiency	
U	U Oper limit v	sing demonstrated mixed target vith this mixed layout	
"A	djabatic" e	fficiency improvements	
E-field de	esign, colde d orifice, ma	r T, larger active region, smaller B, aterial that allows larger field strengths	0

![](_page_34_Picture_2.jpeg)

# **Applications**

Assume an efficiency of **5 x 10**-5 (cw extraction)

⇒ Muon rate of 5 x 10<sup>5</sup> µ/s

 $\mu SR$ 

- Focus the beam to have > 100 mrad
  ⇒ beam diameter of < 1 mm (@ 10 keV)</li>
- Beam could be switched between multiple spectrometers operating in parallel to avoid pile-up losses.
  - Including 60% losses to transport the muons to the various spectrometer
     3 beamlines (left, center, right) with
     5x10<sup>4</sup> µ/s each and sub-mm size could be operated
- Well suited also for post-acceleration to hundreds of keV
   A. Masamitsu

#### Muonium spectroscopy

#### P. Crivelli

- Focus the beam to 1 mm diameter (@ 5 keV), better overlap with lasers
- Improve laser excitation rates by > 200 compared to present experiment at LEM

![](_page_35_Figure_12.jpeg)

![](_page_35_Picture_13.jpeg)

## **Applications**

#### Muonium gravity

A. Soter

Assume an efficiency of **5 x 10**-5 (cw extraction)

 $\Rightarrow$  Muon rate of 5 x 10<sup>5</sup>  $\mu$ /s @ 10 keV, sub-mm size

![](_page_36_Figure_5.jpeg)

Measure g with an accuracy of 1 m/s<sup>2</sup> in 2 weeks 100 nm grating pitch

- The low energy improves muon to vacuum muonium conversion
- The small size simplifies grating production (pitch, size, precision)

Alternative with Whispering Gallery setup is explored where the size of the muCool beam is even more important (A. Soter & V. Nesvizhevsky)

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# Applications (push muCool performance)

#### μEDM P. Schmidt-Wellenburg

- ▶ To have  $d_{\mu} < 10^{-23}$  e cm
  - ▶ 5 x 10<sup>5</sup> µ/s @ 125 MeV/c,
  - 100 kHz rep. rate pulsing
  - Phase-space V: 2 mm mrad
  - Phase-space H: 20 mm mrad
  - 4 ns timing
- ▶ Presently using  $\mu$ E1
  - ▶ 5x 10<sup>4</sup> µ/s @ 125 MeV/c
- Requires post-acceleration from 1.5 MeV/c to 125 (200) MeV/c
  - A. Masamitsu

- Alternative: cw extraction + entrance detector
  - ▶ Assume cw extraction efficiency of **5 x 10**-5
  - ▶ 20% losses in post-acceleration stage
    ⇒ Muon rate: 4 x 10<sup>5</sup> µ/s
    - Improve  $d_{\mu}$  limit (relative to  $\mu$ E1) by  $\leq 2$  (pileup !)
    - Less background?

- Next improvement 2 muons per bunch at 200 kHz pulsing
  - leads to a muon rate of 4 x 10<sup>5</sup> μ/s
  - with a factor of 3 losses during accumulation an extraction efficiency of about 1.5 x 10<sup>-4</sup> is needed
  - beam size increase during accumulation?

![](_page_37_Picture_21.jpeg)

![](_page_37_Picture_22.jpeg)

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# Summary

#### Long way to go

Injection into solenoid and target

#### Compression in target

- Extraction from gas target
- Drift from orifice to re-acceleration region
- Acceleration
- Extraction from B-field

#### Many challenges & risks

- Mechanical stability
- Discharge issues (could increase at the HIMB rates, target tested only at 10 kHz)
- Gas, vacuum and thermal management
- Beam degradation in drift-region, accumulations and re-acceleration

Total estimated efficiency for CW-extraction HIMB output  $\rightarrow$  muCool outside solenoid:

2 x 10<sup>-5</sup> – 1 x 10<sup>-4</sup>

#### For pulsed extraction there are additional losses

E:	10 keV	
ΔE:	100 eV	
Diameter:	20 mm	
Divergence:	2 mrad	

#### Larger improvements ?

- If dispersion could be obtained at target position the stopping probability could be increased by a factor of 2 (inhomogeneous degrader)
- Other target layout & material?
- Concatenation of two mixed compression regions could be used to double stopping efficiency.
   Issues: evacuation / µ-He-collisions

# Is possible to decrease phase space?

![](_page_39_Picture_1.jpeg)

- Superconductor that cancel or decrease B-field
- Freeze desired amount of B-field to keep polarisation, e.g. 0.1 T
- ▶ 6 mm thickness needed to shield 5 T, 5 K operation
- Super-conducting shield could be used also to accelerate muons
- Injection through a tiny slit or hole
- Use strips as before to drift atoms into shield with ExB
- ▶ grad B effect on muon motion ?
- Collisions in injection region

![](_page_39_Picture_10.jpeg)

 $\boldsymbol{v}_D = \frac{mc}{2q} (v_\perp^2 + 2v_\parallel^2) \frac{\boldsymbol{B} \times \nabla |\boldsymbol{B}|}{|\boldsymbol{B}|^3}.$ 

![](_page_39_Picture_11.jpeg)