

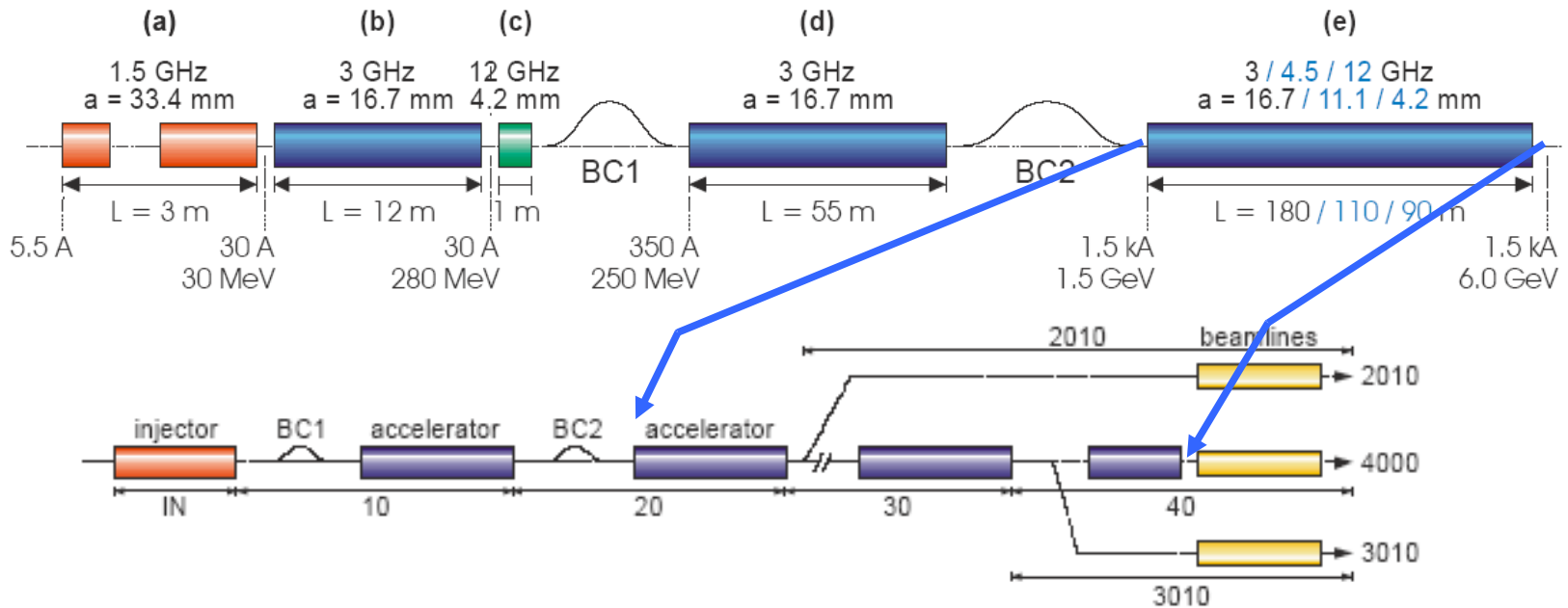
Beam Dynamics Study for PSI –XFEL Linac

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Beam Dynamics Study for PSI -XFEL Linac

- Beam parameters, machine layout
- Beam model for tracking calculations
- Wakefields and correlated energy spread
- Coherent oscillations. Emittance dilution
- Accelerating sections misalignments
- RF phase error
- Conclusion

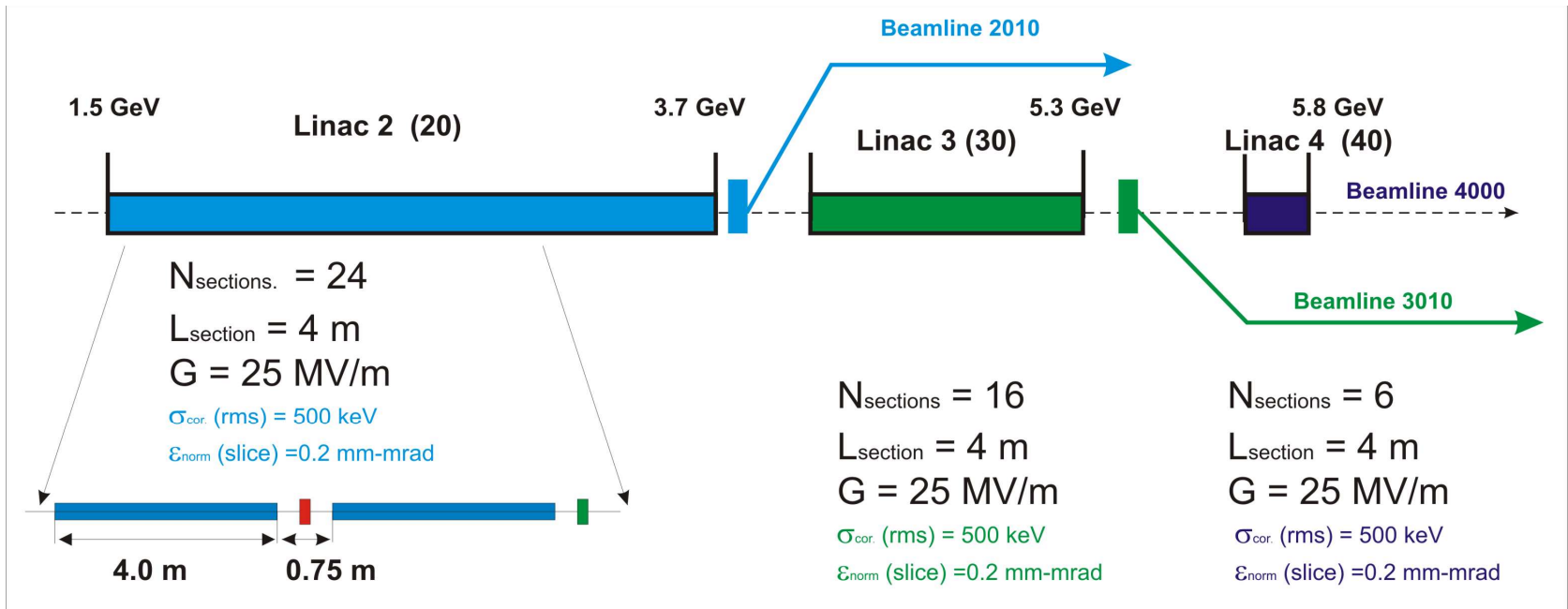
Beam parameters and machine layout



section	(a)	(b)	(c)	(d)	(e)	total	
average gradient	11.2	21.2	30.5	22.7	25.0	6.0	MV/m
phase	-25	-10.2	170	0	0		deg
bunch length	2.7	2.0	2.0	0.17	0.04		mm
linac induced energy chirp	1.1	5.7	-0.7	0.0	0.0	6.0	MV
wakefield induced energy chirp	-0.0	-0.2	-0.1	-1.3	-4.5	-6.0	MV

R. J. Bakker "PSI XFEL Specifications for CANDLE". FEL-BR06-014-2

Beam parameters and machine layout



	domain label	n^*	energy (GeV) target / max		current (kA)
electron gun	INEG	-	0.001	0.001	0.0055
injector	IN	4	0.25	0.35	0.030
linac-1	10	14	1.5	1.7	0.35
linac-2	20	24	3.7	4.1	1.5
linac-3	30	16	5.3	5.7	1.5
linac-4	40	6	5.8	6.3	1.5

* number of 4-m long S-band accelerating structures

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 FEL-BR06-014-2

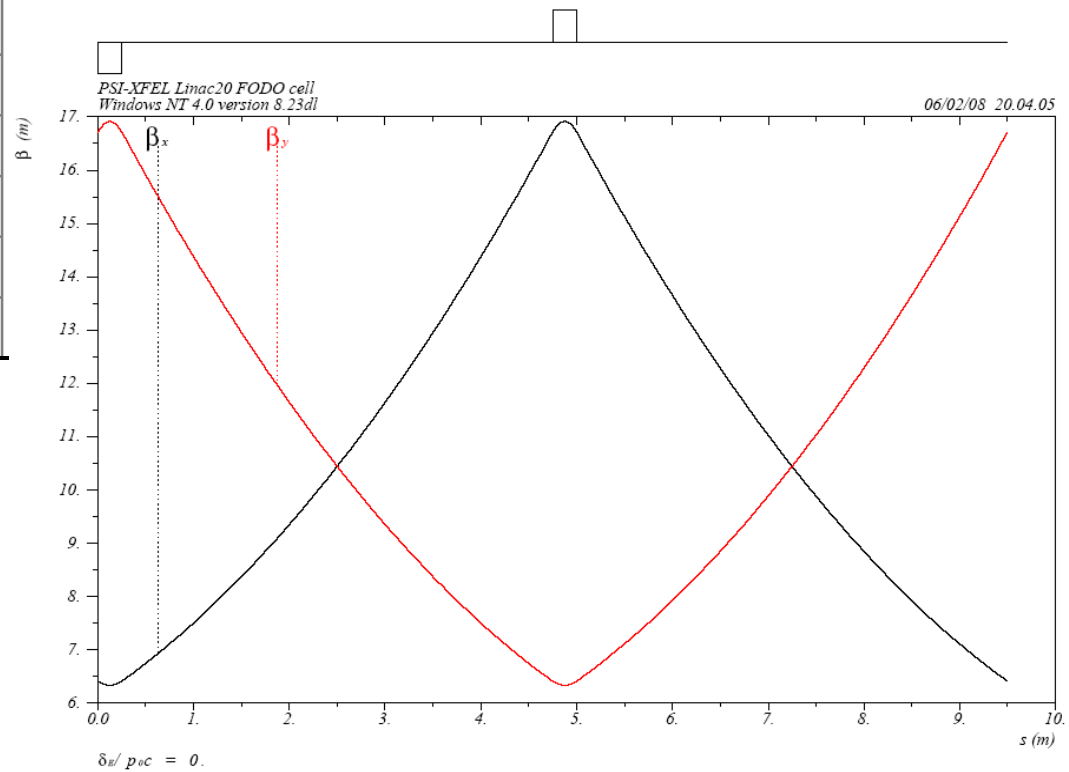
Beam parameters and machine layout

Parameter Linac 20		entrance	exit
Bunch Charge	[pC]	200	200
Energy	[GeV]	1.5	5.8 (max 6.1)
Slice energy spread rms	[keV]	500	500
Norm. transv. emit.	[mm-mrad]	0.2	0.2
Bunch Length	[mm]	40	40
Acc. Grad.	[MeV/m]	25	
RF frequency	[GHz]	3	
Acc Sections		46	
FODO Cells		23	
FODO cell length	[m]	9.5*	
Linac total length	[m]	218.5*	

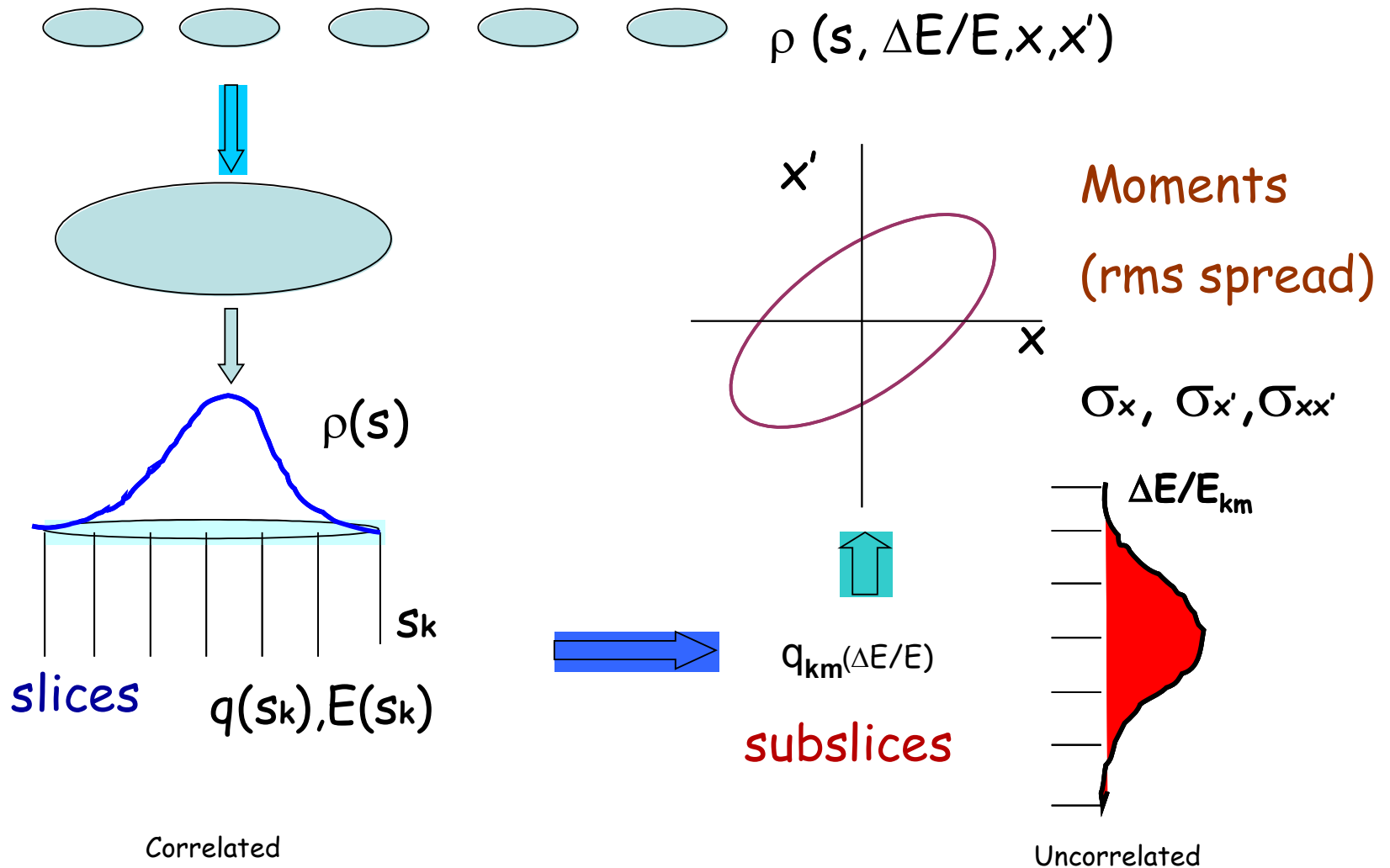
* Physical length (the interspacing is a subject for further optimization)

Main Twiss parameters.

β_{\max} x / y [m]	16.719
Phase adv. per cell μ	$\pi/2$
Cell Length [m]	9.5
K1 (QD / QF) [m ⁻²]	0.787



Beam model for tracking calculations



Longitudinal and transverse wake functions for S-Band structure

K. L. Bane, M. Timm, T. Weiland, SLAC-PUB-9798

Transverse and longitudinal
point wake functions
for S-band structure

$$W_x = 4.10 \cdot \left[1 - \left(1 + 1.15 [s / mm]^{\frac{1}{2}} \right) \cdot \exp \left(-1.15 [s / mm]^{\frac{1}{2}} \right) \right] \cdot \left[\frac{V}{pC \cdot mm \cdot m} \right]$$



$$W_z = 200 \cdot \exp \left[-0.77 (s / mm)^{\frac{1}{2}} \right] \cdot \left[\frac{V}{pC \cdot m} \right]$$

Transverse and longitudinal
wake potentials of bunch

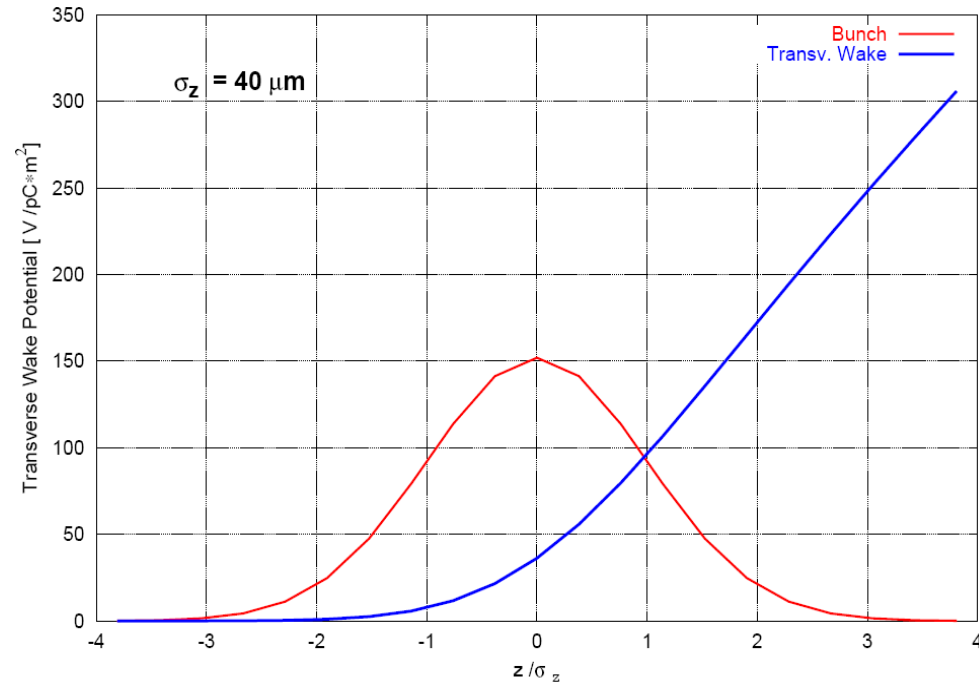


$$W_{\perp}(s) = \int_{-\infty}^s P(s') w_x(s - s') ds'$$

$$W_{\parallel}(s) = \int_{-\infty}^s P(s') w_z(s - s') ds'$$

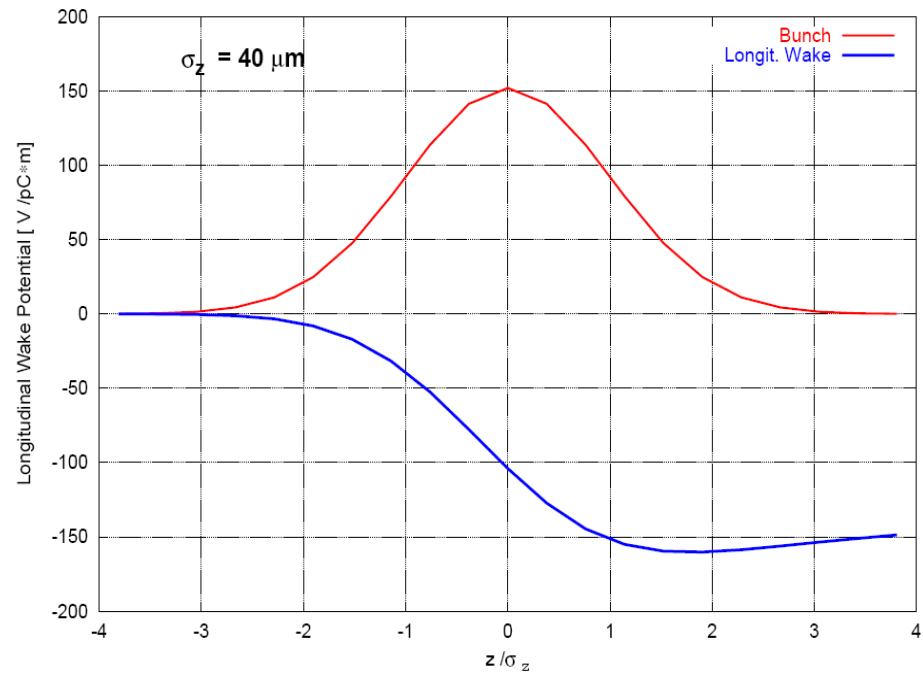
Longitudinal and transverse wake functions for S-Band structure

Single Bunch Transverse Wake Potential



Bunch charge [pC]	200
Bunch length [μm]	40
λ_{RF} [m]	0.1

Single Bunch Longitudinal Wake Potential



Induced correlated energy spread in linac

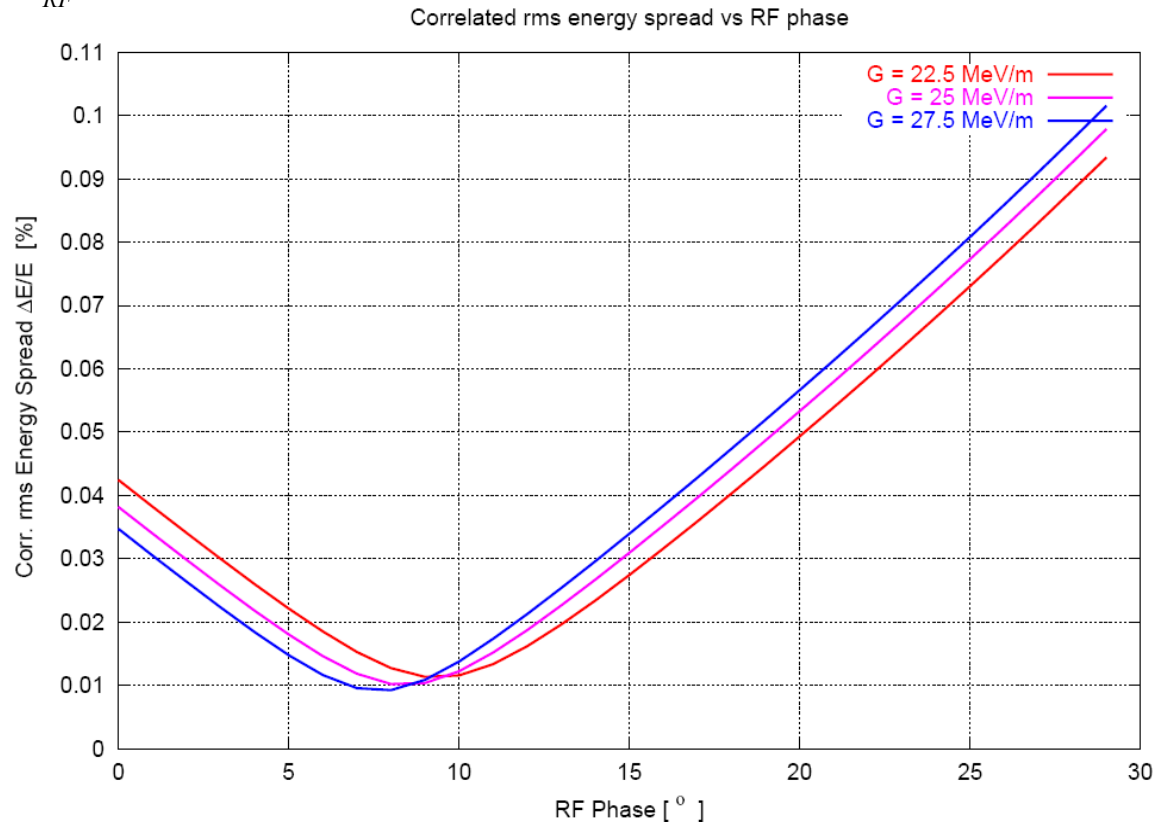
Correlated Energy Spread :

- Interaction with external accelerating RF voltage
- Interaction with accelerating structure - wakefields

$$\Delta E(z, s) = eQzW_z(s) + e\hat{G}z \cos(\phi_0 + \frac{2\pi}{\lambda_{RF}} s) - eGz$$

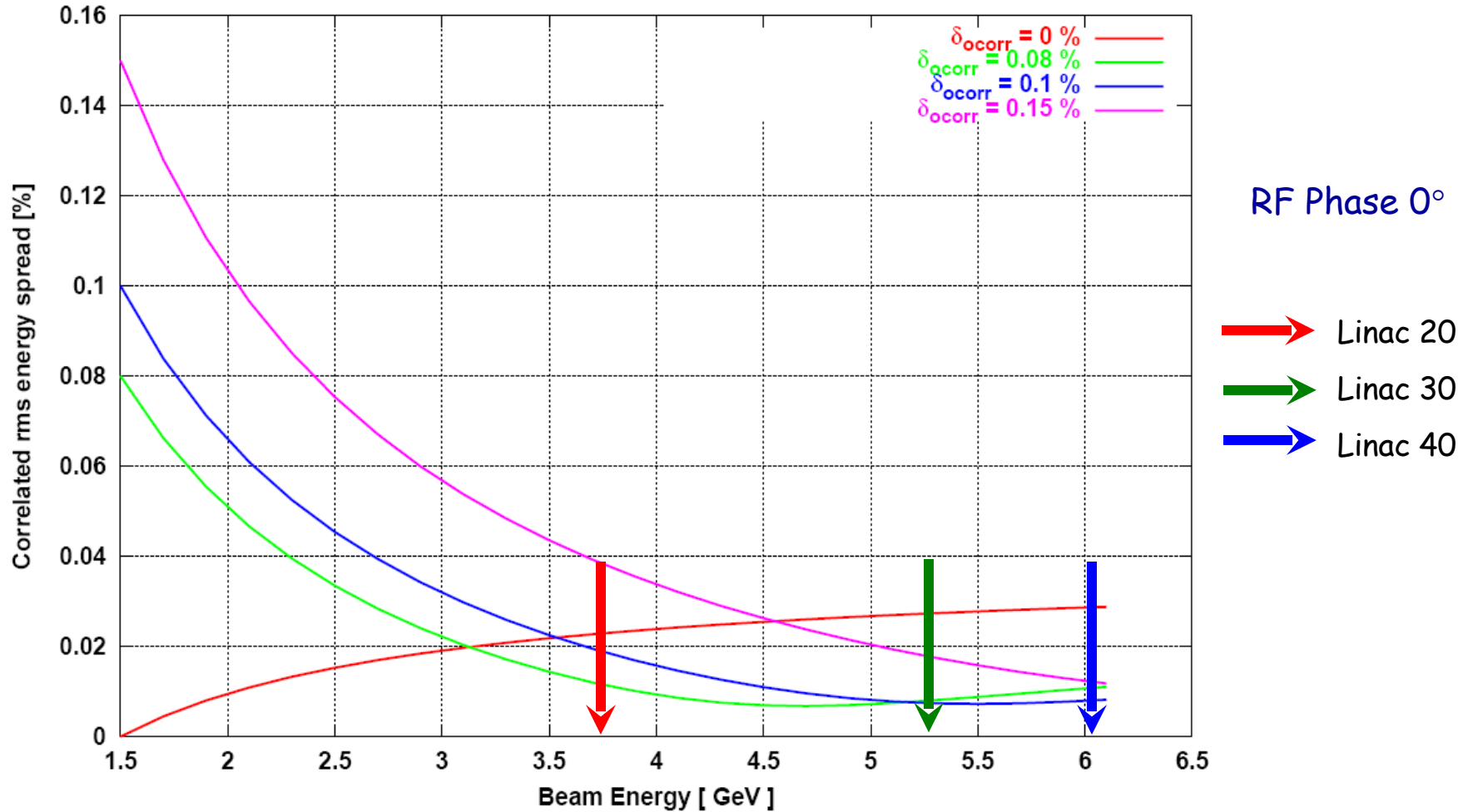
RMS relative energy spread at the linac end (Upper limit)

For $G = 25 \text{ MeV/m}$ 8° off-crest is
 $G = 24.75 \text{ MeV/m}$. For 46 cells total energy gain is $\sim 4554 \text{ MeV}$ with rms corr. energy spread 0.01% (600 keV for 6 GeV)



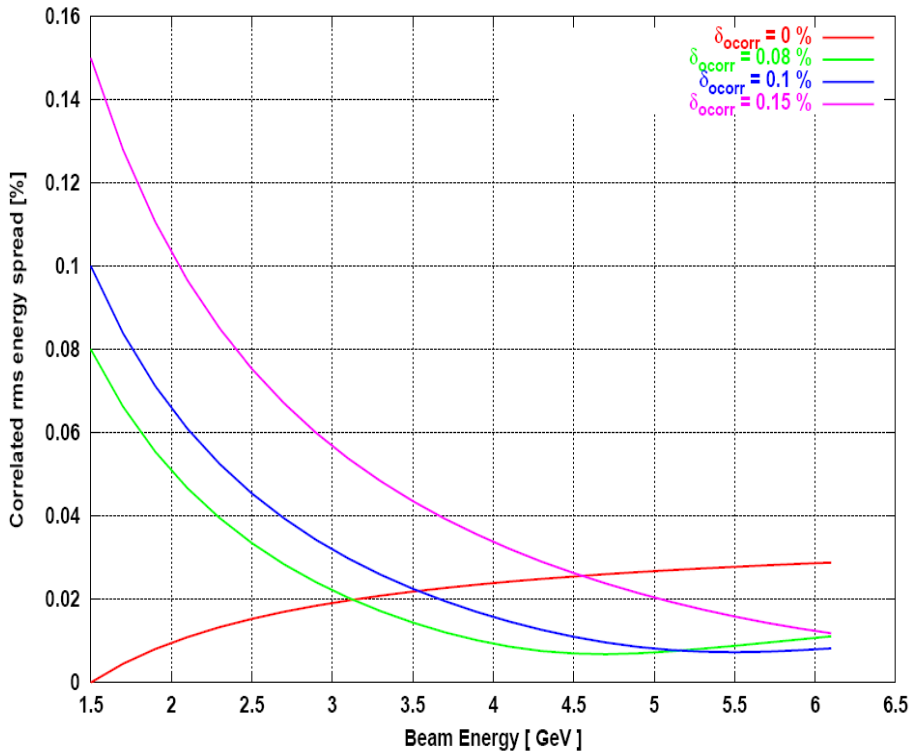
Correlated energy variation along the linac

$$\delta_{cor}(s, z) = \frac{\Delta E(s, z)}{E(z)} = \frac{U(s)}{G} \left[1 - \frac{\gamma_0}{\gamma(z)} \right]$$

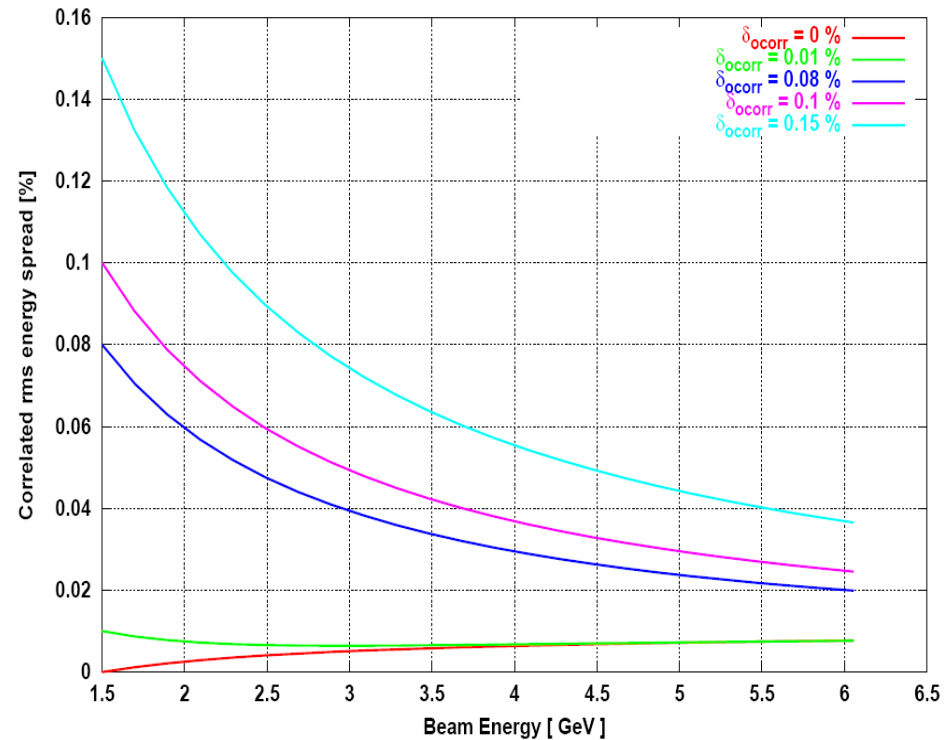


Effect of Initial Correlated Energy Spread (BC)

RF phase 0°

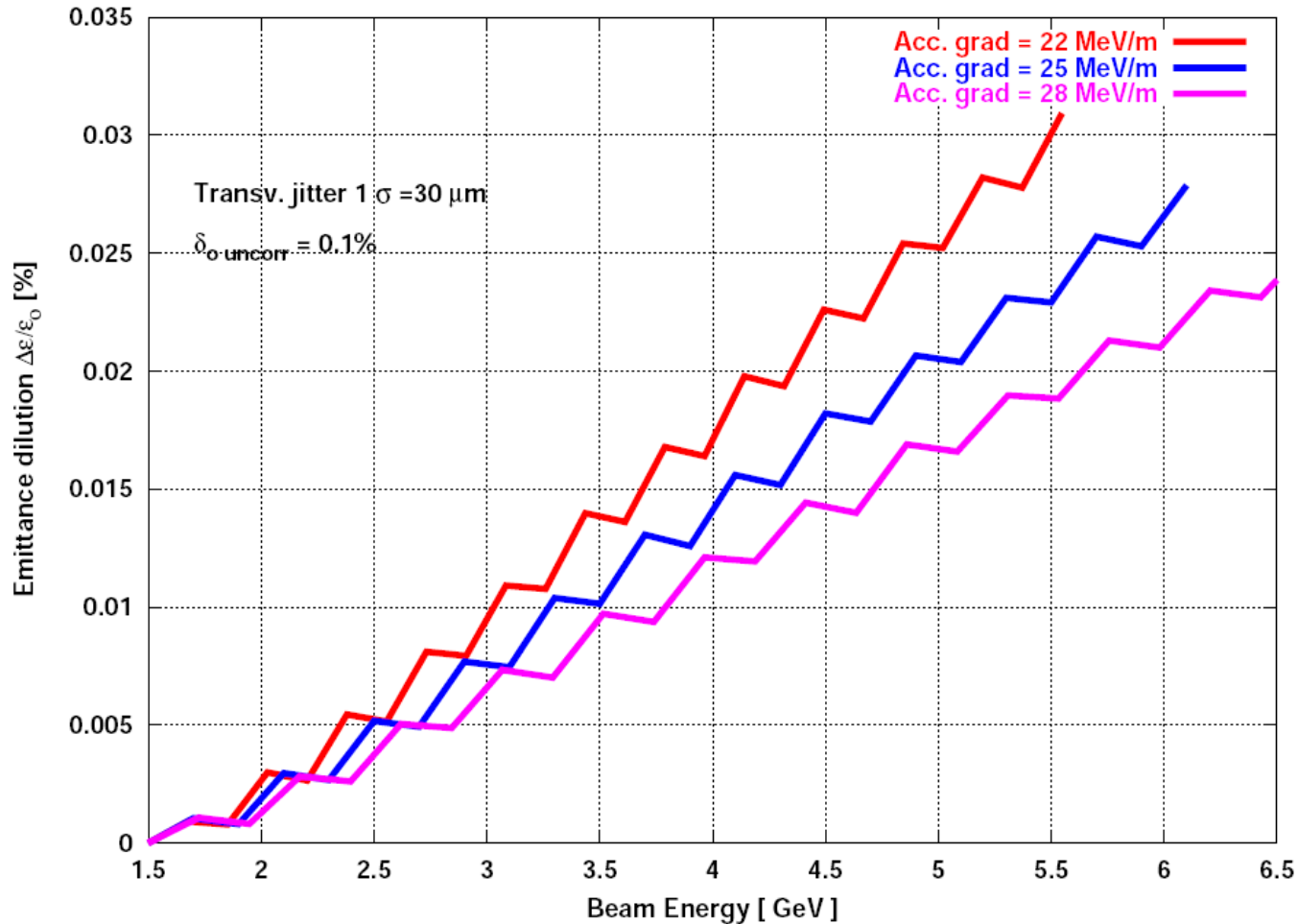


RF phase 8°

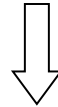


Coherent betatron oscillations. Chromatic Effect.

- Initial transverse jitter - $1\sigma \sim 30 \mu\text{m}$
- Initial uncorrelated energy spread (BC20) - 0.1%



Obtained results could be scaled for other energy spread:



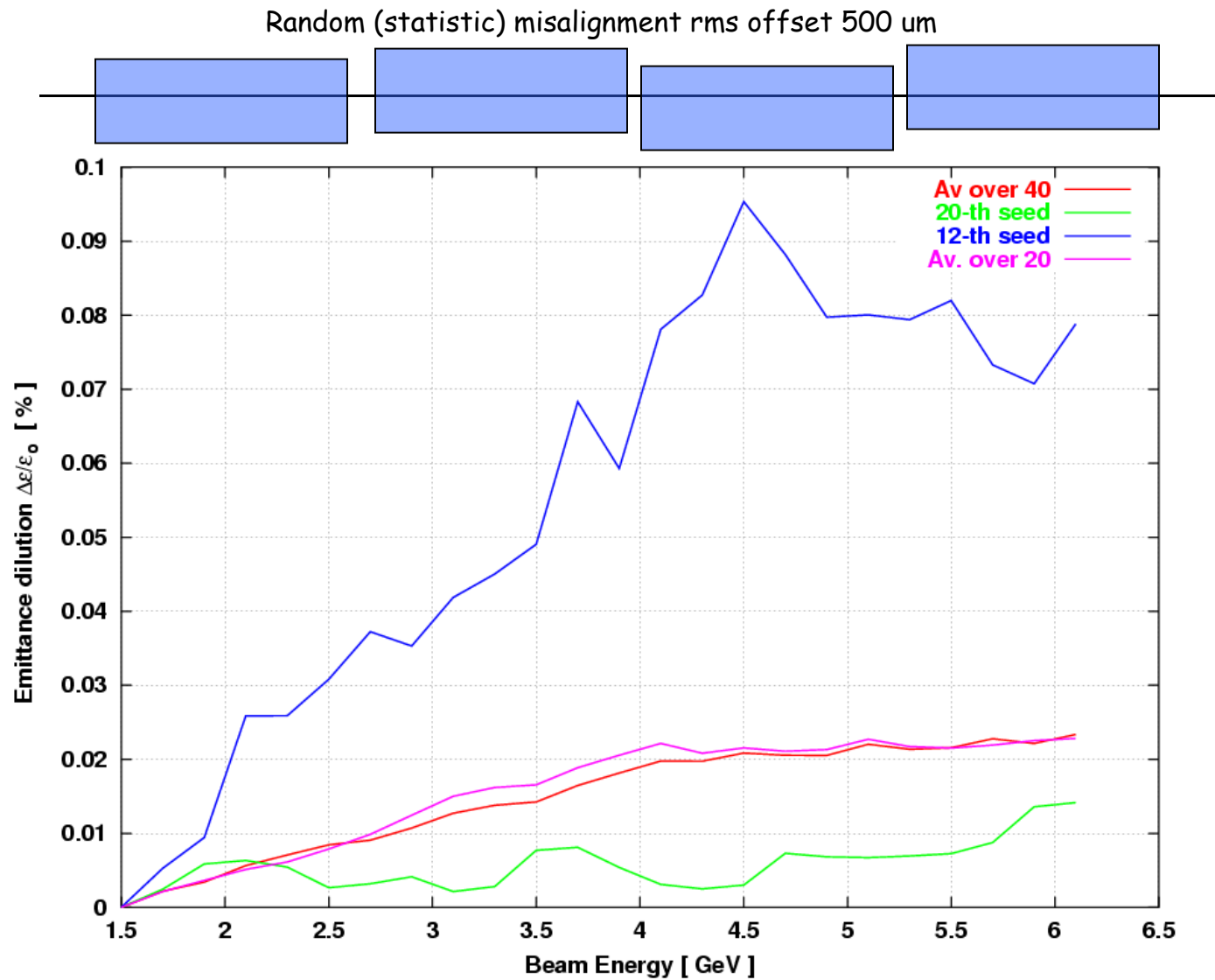
$$\frac{\Delta\varepsilon_1}{\Delta\varepsilon_0} \sim \frac{\delta_1^2}{\delta_0^2}$$

Coherent betatron oscillations. Wakefield effect.

Emittance dilution *Wakefields contribution*

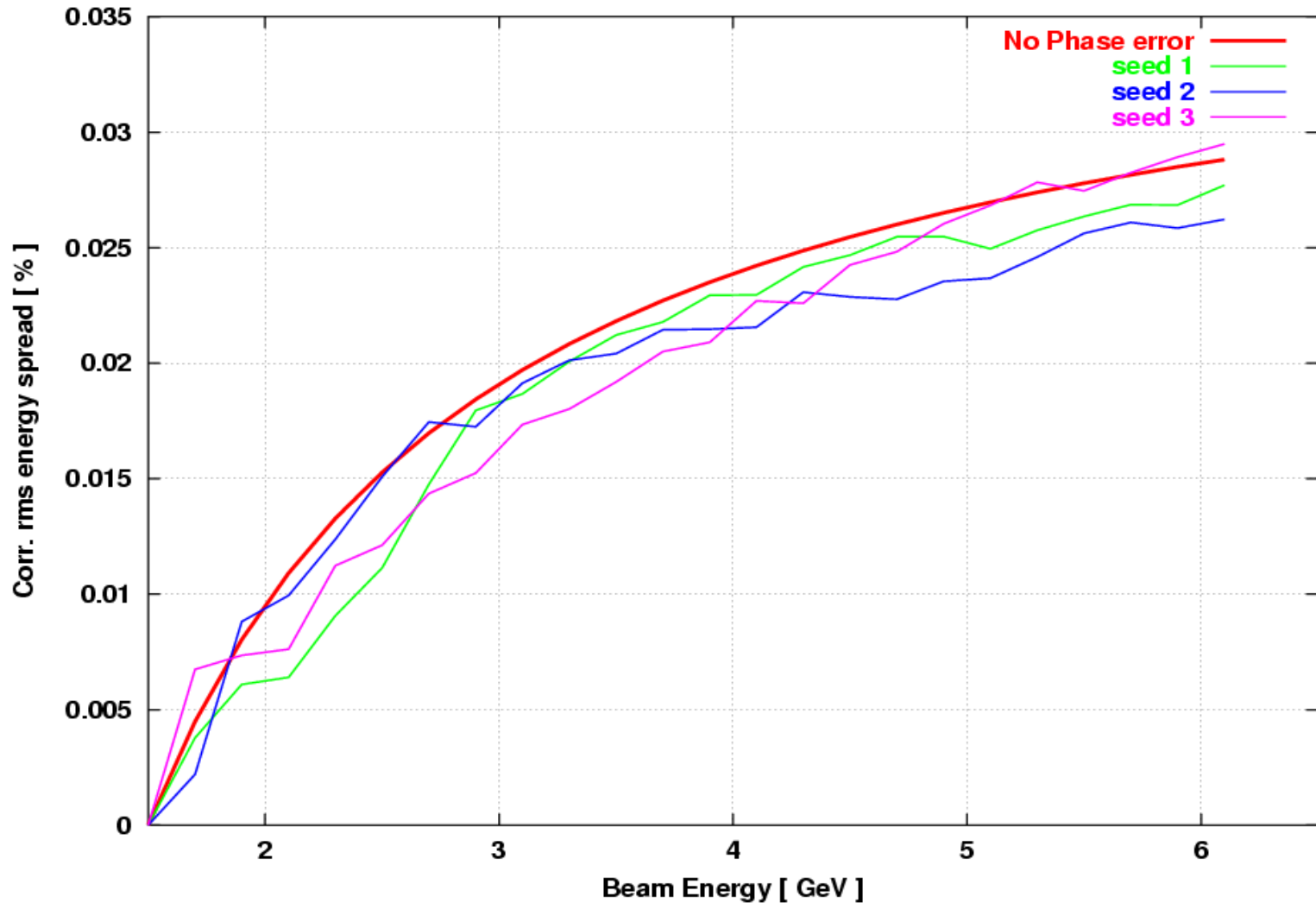


Misalignments. Accelerating section



Misalignments. RF phase

Correlated rms energy spread for RF phase (statistic) random error of 5°



Conclusion.

- Coherent oscillations.
 - Chromatic emittance dilution $<0.04\%$
 - Wakefield emittance dilution $<0.003\%$
- Correlated energy Spread.
 - 0.01% correlated energy spread is achievable
 - Need further optimizations for initial corr. energy spread, RF phase and BC design.
- Accel. Sections misalignments. For $500\ \mu\text{m}$ rms offset rms emittance dilution $<0.025\%$
- For rms RF phase errors $5\ \text{degree}$ rms corr. energy spread deviation is $<0.005\%$

Conclusion 2

- Energy spread in BC10/BC20.
 - Parameters for bunch compressors
 - Reduce number of FODO cells by factor 2-3
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Under Study

- Quadrupole misalignments and trajectory correction
- Accel. section tilts.
- Emittance dilution in low-energy part of S-band accelerator (0.25-1.5 GeV)
- Optimization of machine performance and beam optics