

# Status of OPAL Boundary Geometry Feature and Surface Emission Models for Dark current and Multipacting Simulation

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- 1 New geometry feature: particle-boundary collision test model
  - Basic idea: line segment-triangle intersection (LSTI) test
  - Early rejection strategy
- 2 Surface emission physics models
  - Field emission model
  - Secondary emission model
- 3 Current results
  - Dark current simulation with field emission model
  - Benchmark of secondary emission module
- 4 Plan for the next step

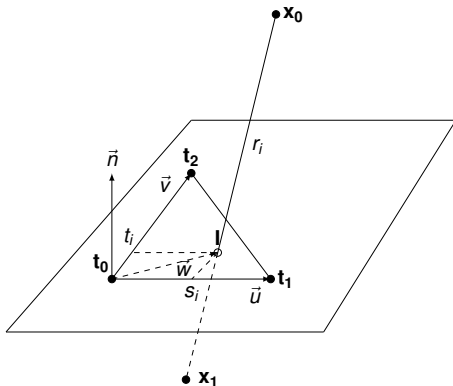
# THE GOAL OF THE WORK

- Extend OPAL to handle the complex boundary.
- Provide field emission model and a reduced model with randomly generated electrons for dark current study (CTF3 gun, new gun...)
- Provide feasible multipacting model primarily for cyclotrons, including models of field emission, secondary emission...

# Outline

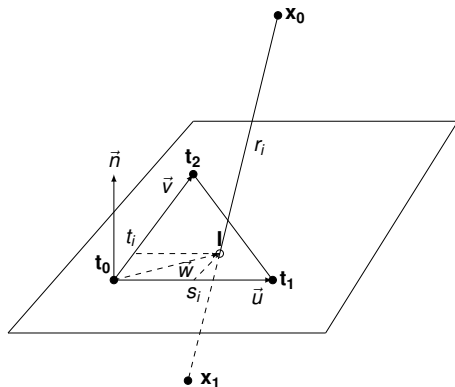
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# LINE SEGMENT-TRIANGLE INTERSECTION TEST



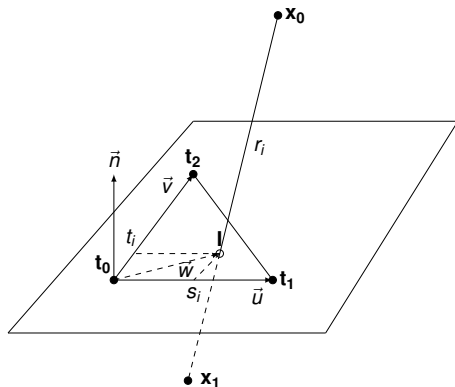
- $\mathbf{x}_0, \mathbf{x}_1$  are position of a particle.
- Triangle  $\mathbf{t}_0, \mathbf{t}_1, \mathbf{t}_2$  is one piece of triangulated boundary surface.
- Using [D.Sunday's] Line-Triangle intersect algorithm.
- Precomputed triangle normal.

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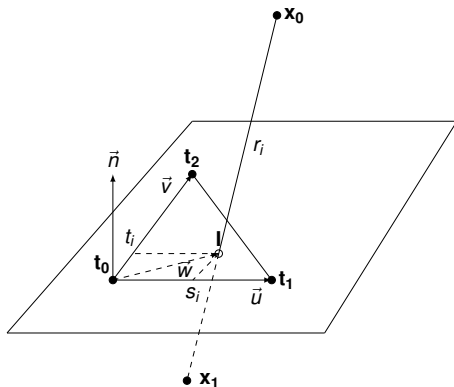
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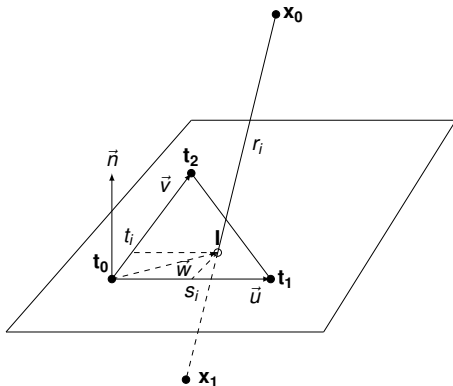
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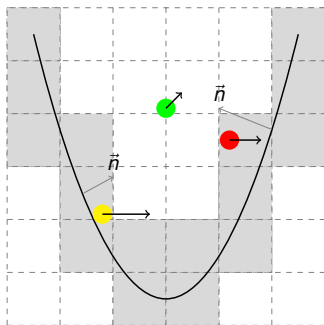
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- LSTI test is accurate but time consuming.
- Solution: early rejection strategy.

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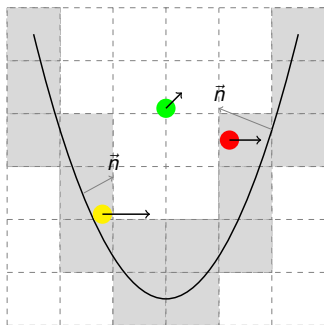
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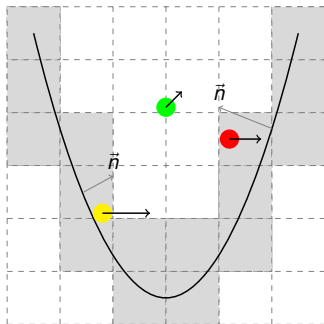
- Use uniformed boxes to facilitate the particle searching.
- Shield like boundary box.
- Direction of momentum and triangle normal are also evaluated.

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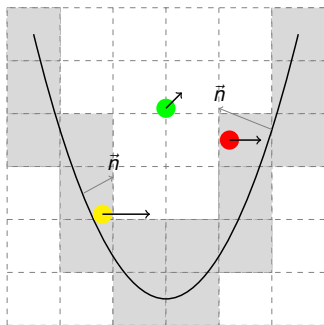
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# ELECTRON QUANTUM TUNNELING AT HIGH FIELD

- Fowler-Nordheim formula induced by [R. H. Fowler, L. Nordheim] and implemented for dark current simulation by [J. H. Han]:

$$J(\mathbf{r}, t) = \frac{A(\beta E)^2}{\varphi t(y)^2} \exp\left(\frac{-Bv(y)\varphi^{3/2}}{\beta E}\right)$$

- $J(\mathbf{r}, t)$ : current density in position  $\mathbf{r}$  and time  $t$ ;  $\varphi$ : work function;  $\beta$ : field enhancement factor;  $E$ : electric field in the normal direction of surface;  $A$  and  $B$  are empirical constants;
- Functions  $v(y)$  and  $t(y)$  represents the image charge effects, detailed in [Y. Feng and J. P. Verboncoeur's paper]

$$\text{with: } y = \sqrt{\frac{e^3}{4\pi\epsilon}} \frac{\sqrt{\beta E}}{\varphi} = 3.795 \times 10^{-5} \frac{\sqrt{\beta E}}{\varphi}.$$

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# SPACE CHARGE CONSIDERATION

- Child-Langmuir law

$$\begin{aligned} J(\mathbf{r}, t) &= \frac{4\epsilon_0}{9} \sqrt{2 \frac{e}{m}} \left( \frac{V^{3/2}}{d^2} \right) \\ &= \frac{4\epsilon_0}{9} \sqrt{2 \frac{e}{m}} \left( \frac{E^{3/2}}{d^{1/2}} \right) \end{aligned}$$

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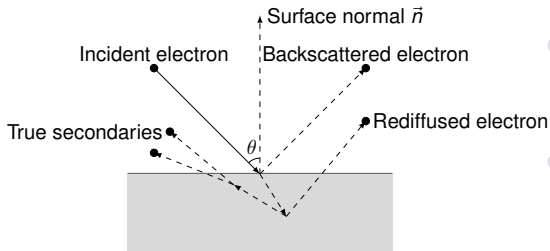
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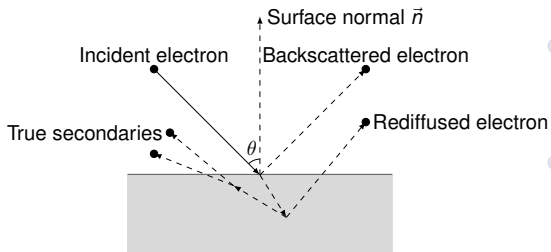
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A Probabilistic model developed by  
[M. A. Furman and M. Pivi]

- Mathematically self-consistent
- Phenomenological- don't involve secondary physics but fit the data.
- A serial of parameters to fit the measured SEY data.
- The Monte Carlo technique has been used

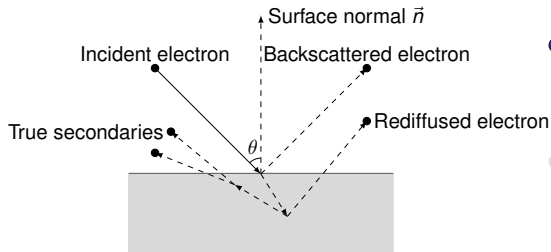
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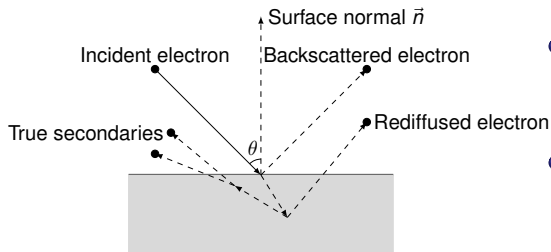
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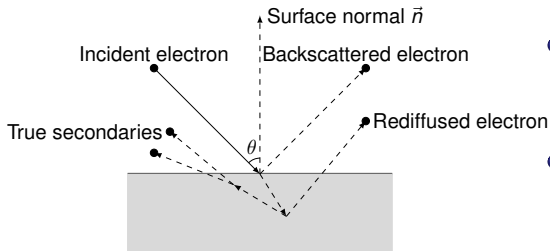
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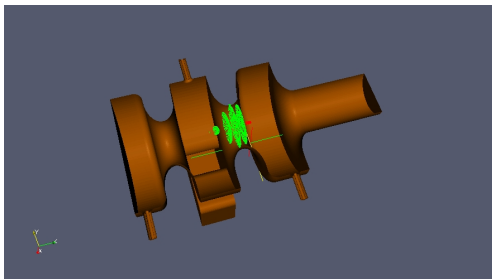
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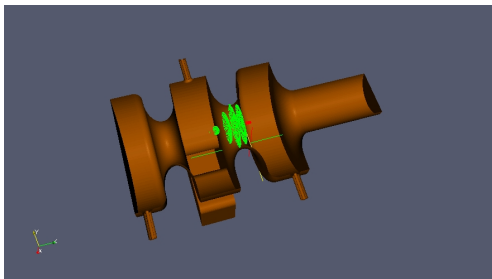
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- We add a post processing feature which shows the origin positions and phase of dark current particles which are alive beyond user specified positions.
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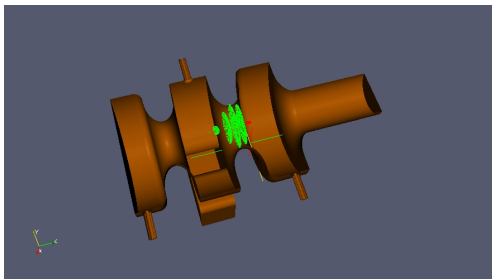
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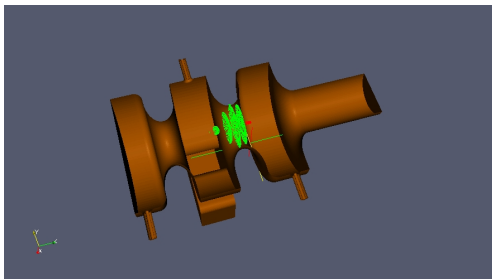
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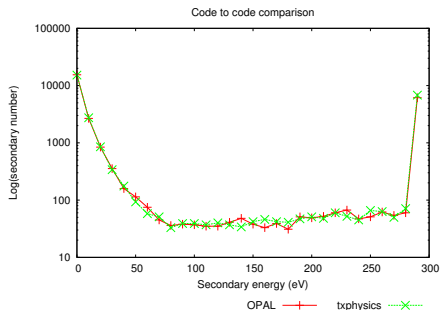
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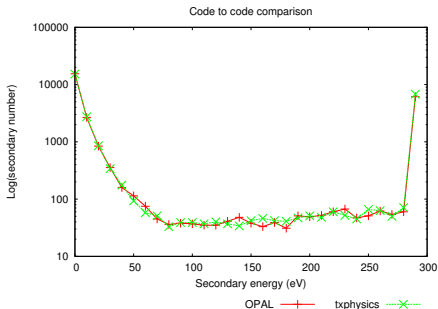
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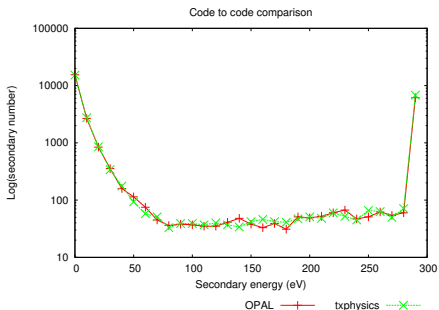
- Large samples: 10000 incident electrons.
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# ACKNOWLEDGEMENT

I wish to thank Andreas, Benedikt, Yves, Hua, Christof and all other AMAS members, also thank Dr.Lukas Stingelin and Mr.Falone Antonio.

# REFERENCES

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