

# Electric dipole moment searches in atoms & molecules

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**TORONTO**

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# Permanent electric dipole moment of a particle

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Asymmetry of charge distribution

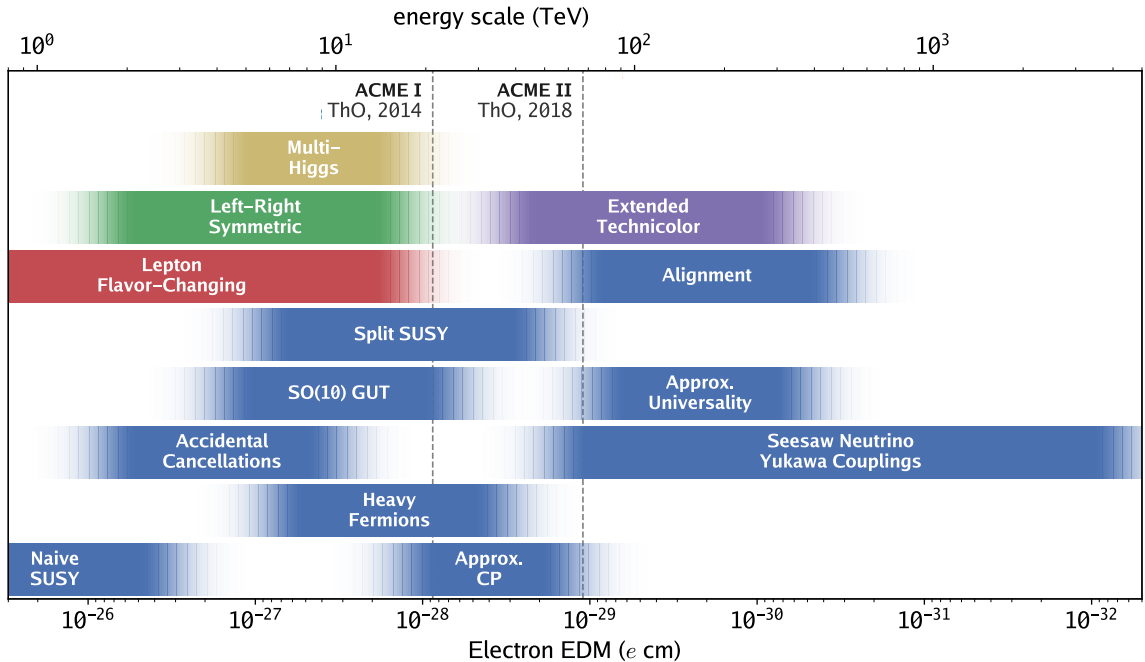
Has to be oriented along spin vector

*Wigner-Eckart theorem*

Low-energy observable which  
probes extremely high-energy physics

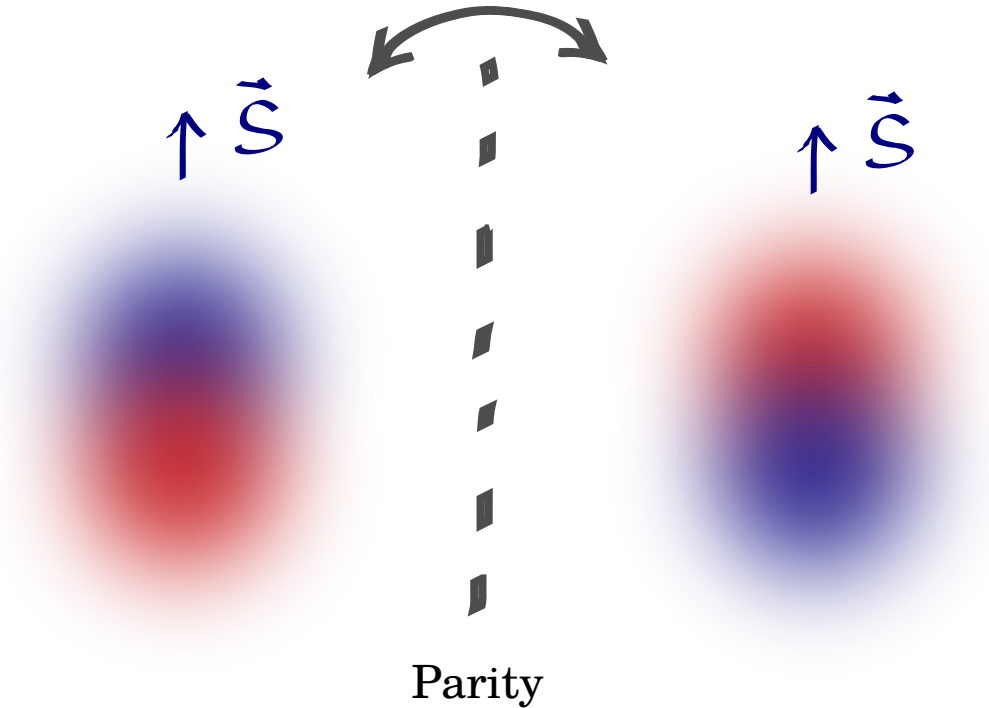


# High energy reach



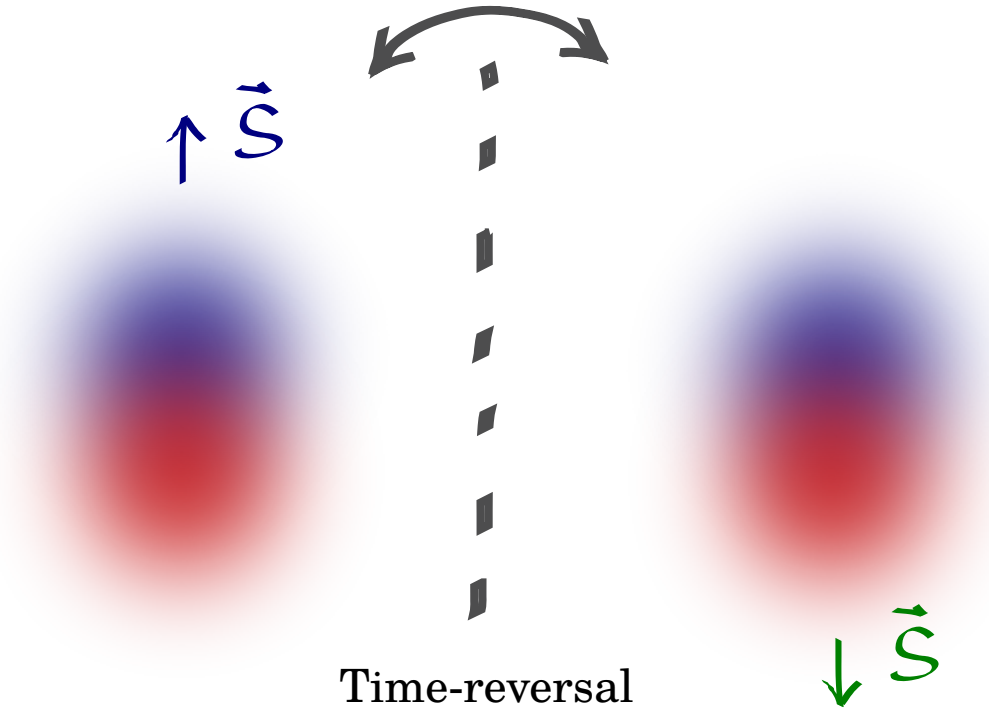
# EDMs violate parity symmetry

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# EDMs violate time-reversal symmetry

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# Permanent electric dipole moment of a particle

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Asymmetry of charge distribution

Has to be oriented along spin vector

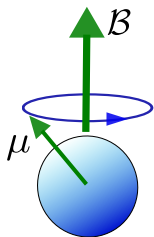
*Wigner-Eckart theorem*

Low-energy observable which  
probes extremely high-energy physics

*model-independent signature  
of some new  $P,T$ -violation*

# Measuring an electric dipole moment

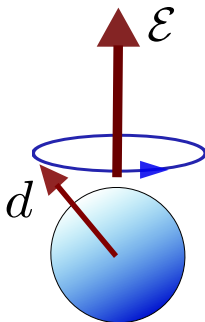
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[] B-field exerts torque on magnetic moment

[] Spin precession angle per unit time is proportional to the magnetic moment

Similarly ....

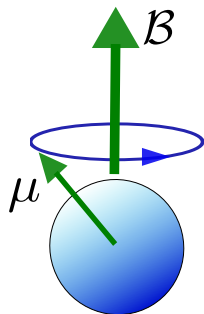


[] E-field exerts torque on electric dipole moment

[] Spin precession angle per unit time is proportional to the EDM

# Quantum mechanical version

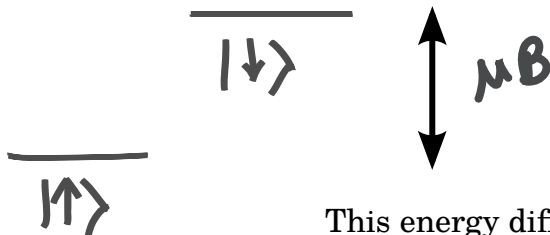
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Zero magnetic field:



Non-zero magnetic field:

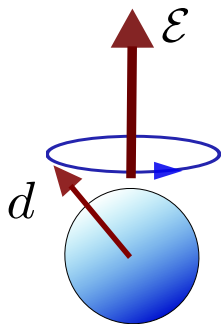


This energy difference  
gives the magnetic moment



# Quantum mechanical version

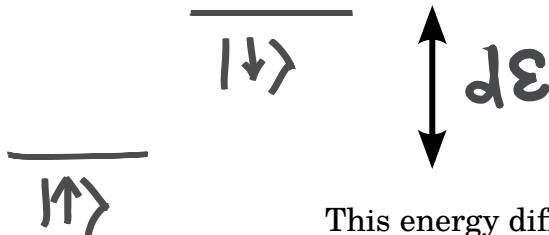
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Zero electric field:



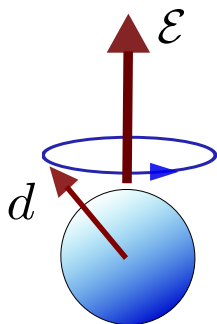
Non-zero electric field:



This energy difference  
gives the EDM

# Quantum mechanical version

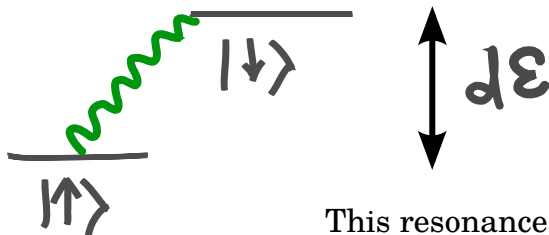
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Zero electric field:

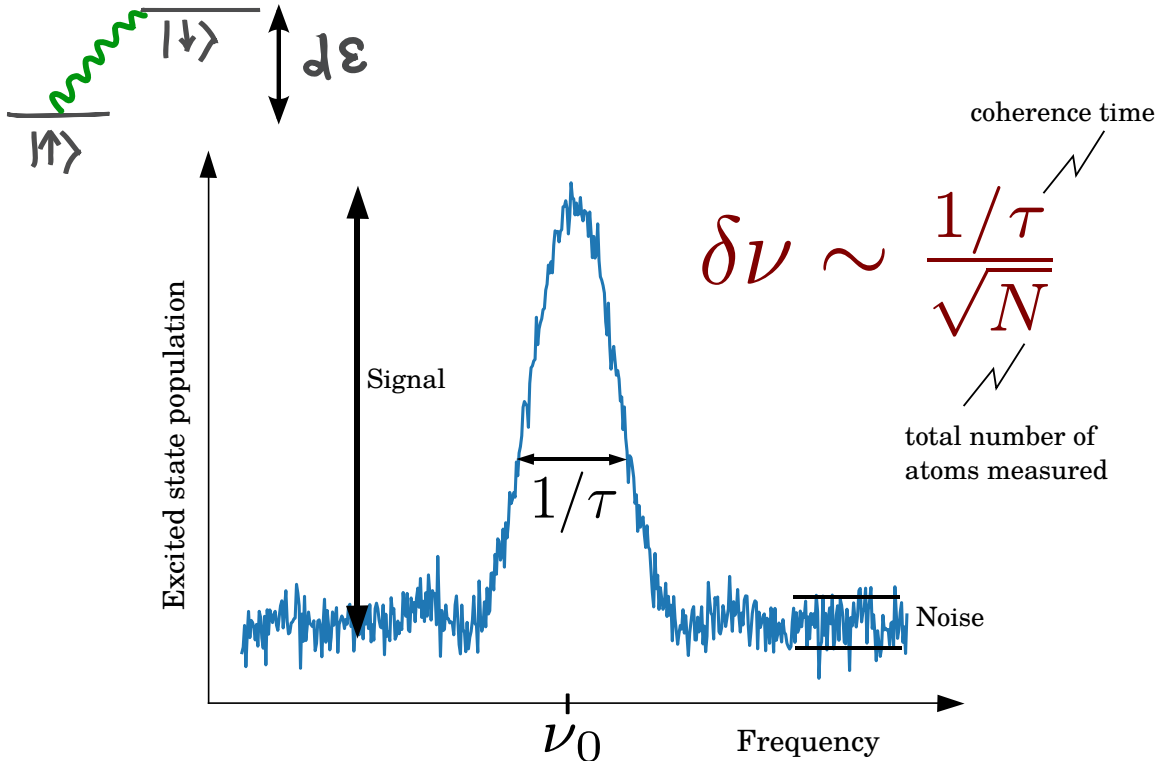


Non-zero electric field:

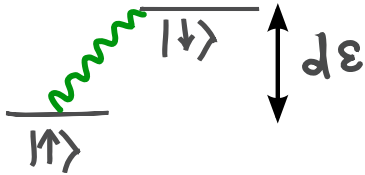


This resonance frequency  
gives the EDM

# Electron spin resonance



# Precision of EDM experiments



$$\delta d = \frac{1}{\varepsilon \tau \sqrt{N}}$$

$$\delta \nu \sim \frac{1/\tau}{\sqrt{N}}$$

coherence time

total number of  
particles measured

So we always want:

- ... the largest electric field
- ... the longest coherence time
- ... lots and lots of particles

# Ongoing EDM searches with atoms & molecules

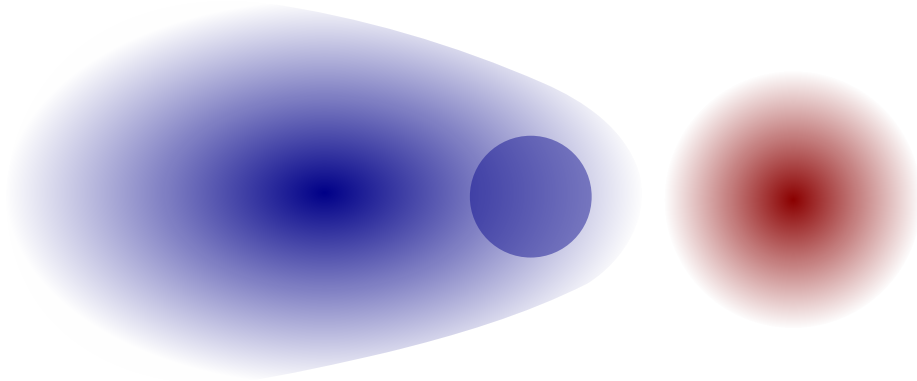
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ThO	electron	(ACME) Chicago + Harvard + Northwestern)
HfF <sup>+</sup> , ThF <sup>+</sup>	electron	JILA
YbF	electron	Imperial College
YbOH	electron	(PolyEDM) CalTech + Harvard
BaF	electron	multiple groups
Hg	nuclear	Washington
Ra	nuclear	Argonne
Xe	nuclear	multiple groups
TlF	nuclear	(CENTREX) Chicago + Columbia + Yale

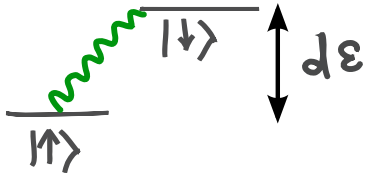
*+ more brewing ....*

# A molecule is complicated

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# Precision of EDM experiments



$$\delta d = \frac{1}{\varepsilon \tau \sqrt{N}}$$

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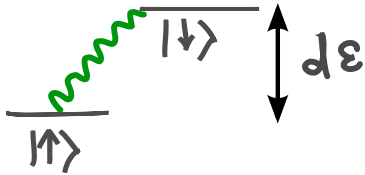
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So we always want:

- ... **the largest electric field**  $\longrightarrow$  *this is why we use atoms & molecules*
- ... the longest coherence time
- ... lots and lots of particles

# Precision of EDM experiments



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$$\delta \nu \sim \frac{1/\tau}{\sqrt{N}}$$

coherence time

total number of  
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So we always want:

... the largest electric field	] →	this is why we use atoms & molecules could also be improved using AMO techniques (cooling & trapping)
... the longest coherence time		
... lots and lots of particles		



# Ongoing EDM searches with atoms & molecules

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ThO	electron	(ACME) Chicago + Harvard + Northwestern)
HfF <sup>+</sup> , ThF <sup>+</sup>	electron	JILA
YbF	electron	Imperial College
YbOH	electron	(PolyEDM) CalTech + Harvard
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Xe	nuclear	multiple groups
TlF	nuclear	(CENTREX) Chicago + Columbia + Yale

*+ more brewing ....*

The periodic table is color-coded by groups: Group 1 (pink), Group 2 (yellow), Groups 3-10 (purple), Groups 11-18 (light blue), and Groups 19-20 (yellow). Red circles highlight the following elements: Rb, Sr, Y, Zr, Nb, Mo, Tc, Ru, Rh, Pd, Ag, Cd, In, Sn, Sb, Te, I, Xe, Cs, Ba, Lu, Hf, Ta, W, Re, Os, Ir, Pt, Au, Hg, Tl, Pb, Bi, Po, At, Rn, Fr, Ra, Lr, Rf, Db, Sg, Bh, Hs, Mt, Ds, Rg, Cn, Nh, Fl, Mc, Lv, Ts, Og, La, Ce, Pr, Nd, Pm, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb, Ac, Th, Pa, U, Np, Pu, Am, Cm, Bk, Cf, Es, Fm, Md, No.

# Why is the E-field so large in atoms & molecules ?

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In fact, the field experienced by the EDMs of electrons or nuclei inside atoms & molecules is ZERO !

*(non-relativistic point particles: Schiff's theorem)*

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Electrons move ~relativistically inside heavy atoms (Salpeter, Sandars)

*⇒ electron EDM leads to  $P, T$ -violating energy shifts in atoms / molecules*

# Why is the E-field so large in atoms & molecules ?

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In fact, the field experienced by the EDMs of electrons or nuclei inside atoms & molecules is ZERO !

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Electrons move ~relativistically inside heavy atoms (Salpeter, Sandars)

*⇒ electron EDM leads to  $P,T$ -violating energy shifts in atoms / molecules*

Nuclei are extended objects (Schiff)

*⇒ nuclear EDM leads to  $P,T$ -violating energy shifts in atoms / molecules*

# P,T-violating energy shifts

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So we never directly measure particle EDMs in atoms & molecules

What we measure are **P,T-violating energy level shifts**  
that depend on the *spin orientation* relative to *electrical polarization*

$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}}$$

**Electrons:**

$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}} \longrightarrow \vec{d}_{\text{atom}} \cdot \vec{\mathcal{E}}_{\text{lab}} \quad (\text{atoms})$$

$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}} \longrightarrow d_e \vec{\mathcal{E}}_{\text{eff}} \vec{S} \cdot \hat{n} \quad (\text{molecules})$$

**Nuclei:**

$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}} \longrightarrow \vec{d}_{\text{atom}} \cdot \vec{\mathcal{E}}_{\text{lab}} \quad (\text{atoms})$$

$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}} \longrightarrow (d_n R + 6\mathfrak{S}) \vec{I} \cdot \hat{n} \quad (\text{molecules})$$

# Electron "EDM" experiments

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???

**Particle theory:**

Electron coupling  
to new physics

**Quantum chemistry:**

Electron-nucleus  
interaction

**Experiment:**

P,T-violating shifts

# Nuclear "EDM" experiments

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???

<b>Particle theory:</b>	QCD coupling to new physics
<b>Nuclear theory:</b>	Nucleon-nucleon interactions, QCD
<b>Quantum chemistry:</b>	Electron-nucleus interaction
<b>Experiment:</b>	P,T-violating shifts



# P,T-violating energy shifts

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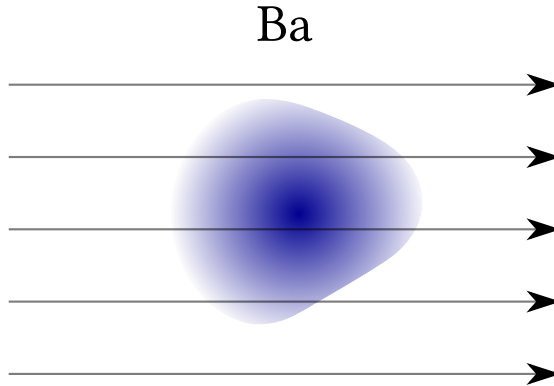
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$$\Delta\nu = \Upsilon_{\text{PT}} \vec{J} \cdot \hat{\mathcal{D}} \longrightarrow (d_n R + 6\mathfrak{S}) \vec{I} \cdot \hat{n} \quad (\text{molecules})$$

# Why polar molecules?

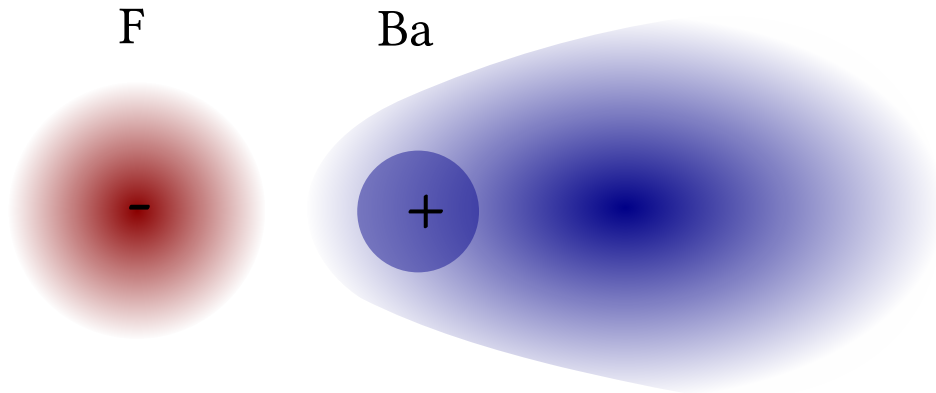
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Neutral atom in lab E-field

# Why polar molecules?

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Polar molecule = +ion subjected to large electric field  
from the -ion

# Ongoing EDM searches with atoms & molecules

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ThO	electron	molecular beam, laser spectroscopy
HfF <sup>+</sup> , ThF <sup>+</sup>	electron	ion trap, laser spectroscopy
YbF	electron	molecular beam, rf+laser spectroscopy
YbOH	electron	laser-cooled molecules
BaF	electron	molecular beam; matrix isolation
Hg	nuclear	vapour cell, rf spectroscopy
Ra	nuclear	optical trap
Xe	nuclear	cells, rf spectroscopy
TlF	nuclear	molecular beam, rf+laser spectroscopy

# Recent results: electron EDM

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## Precision Measurement of the Electron's Electric Dipole Moment Using Trapped Molecular Ions

William B. Cairncross, Daniel N. Gresh, Matt Grau, Kevin C. Cossel, Tanya S. Roussy, Yiqi Ni, Yan Zhou, Jun Ye, and Eric A. Cornell

Phys. Rev. Lett. **119**, 153001 – Published 9 October 2017

## Improved limit on the electric dipole moment of the electron

[ACME Collaboration](#)

[Nature](#) **562**, 355–360 (2018) | [Cite this article](#)

$$|d_e| \lesssim 10^{-29} \text{ e cm}$$

# Recent results: nuclear EDMs

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## Reduced Limit on the Permanent Electric Dipole Moment of $^{199}\text{Hg}$

B. Graner, Y. Chen ((陳宜)), E. G. Lindahl, and B. R. Heckel

Phys. Rev. Lett. **116**, 161601 – Published 18 April 2016; Erratum [Phys. Rev. Lett. 119, 119901 \(2017\)](#)

## New Limit on the Permanent Electric Dipole Moment of $^{129}\text{Xe}$ Using $^3\text{He}$ Comagnetometry and SQUID Detection

N. Sachdeva, I. Fan, E. Babcock, M. Burghoff, T. E. Chupp, S. Degenkolb, P. Fierlinger, S. Haude, E. Kraegeloh, W. Kilian, S. Knappe-Grüneberg, F. Kuchler, T. Liu, M. Marino, J. Meinel, K. Rolfs, Z. Salhi, A. Schnabel, J. T. Singh, S. Stüiber, W. A. Terrano, L. Trahms, and J. Voigt

Phys. Rev. Lett. **123**, 143003 – Published 4 October 2019

## Measurement of the permanent electric dipole moment of the $^{129}\text{Xe}$ atom

F. Allmendinger, I. Engin, W. Heil, S. Karpuk, H.-J. Krause, B. Niederländer, A. Offenhäusser, M. Repetto, U. Schmidt, and S. Zimmer

Phys. Rev. A **100**, 022505 – Published 7 August 2019

## Improved limit on the $^{225}\text{Ra}$ electric dipole moment

Michael Bishof, Richard H. Parker, Kevin G. Bailey, John P. Greene, Roy J. Holt, Mukut R. Kalita, Wolfgang Korsch, Nathan D. Lemke, Zheng-Tian Lu, Peter Mueller, Thomas P. O'Connor, Jaideep T. Singh, and Matthew R. Dietrich

Phys. Rev. C **94**, 025501 – Published 3 August 2016

# Where next?

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Techniques will continue to improve (larger coherence times, more atoms)

Creative choices of experimental systems to maximize amplification of P,T-violation (e.g., radioactive molecules @ TRIUMF, FrAg @ Chicago)

Nuclear theory improvements to better connect experimental measurements with new physics parameters

# Work in my group

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Developing new techniques for electron EDM measurements

*... trapping large quantities of molecules in neon ice crystals*  
eg, arXiv: 2207.07279

Exploring new experimental systems

*... octupole-deformed nuclei doped in non-centrosymmetric crystals*

**Please talk to me** if you are interested.

We have openings for students & postdocs!



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