

Spectroscopy of hydrogen molecular ions

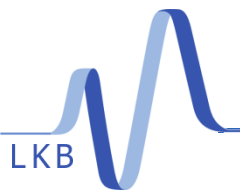
Jean-Philippe Karr^{1,2}

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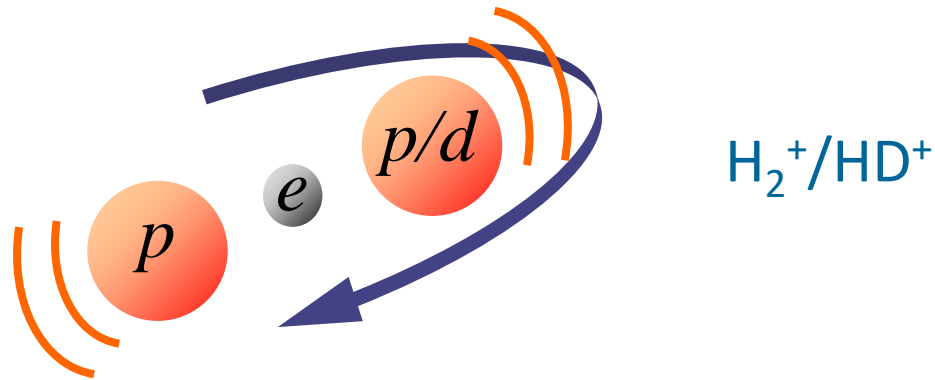
² *Université d'Evry – Val d'Essonne*



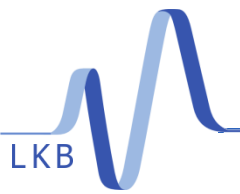
*Muonic Atoms at PSI2022
Satellite Workshop "Proton structure in and out of
muonic hydrogen — the ground-state hyperfine splitting"
15 October 2022*



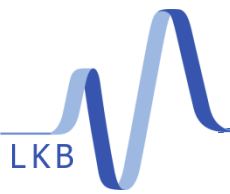
Hydrogen molecular ions (HMI)



- **Simple** (one-electron, three-body) quantum systems
Energy levels and other properties **calculable** with high accuracy.
- Many **ultra-narrow** ro-vibrational transitions
natural lifetimes from tens of ms (HD^+) to weeks (H_2^+)
- High-accuracy techniques as in optical ion clocks:
ion traps, laser cooling, Hz-linewidth laser, femtosecond comb...

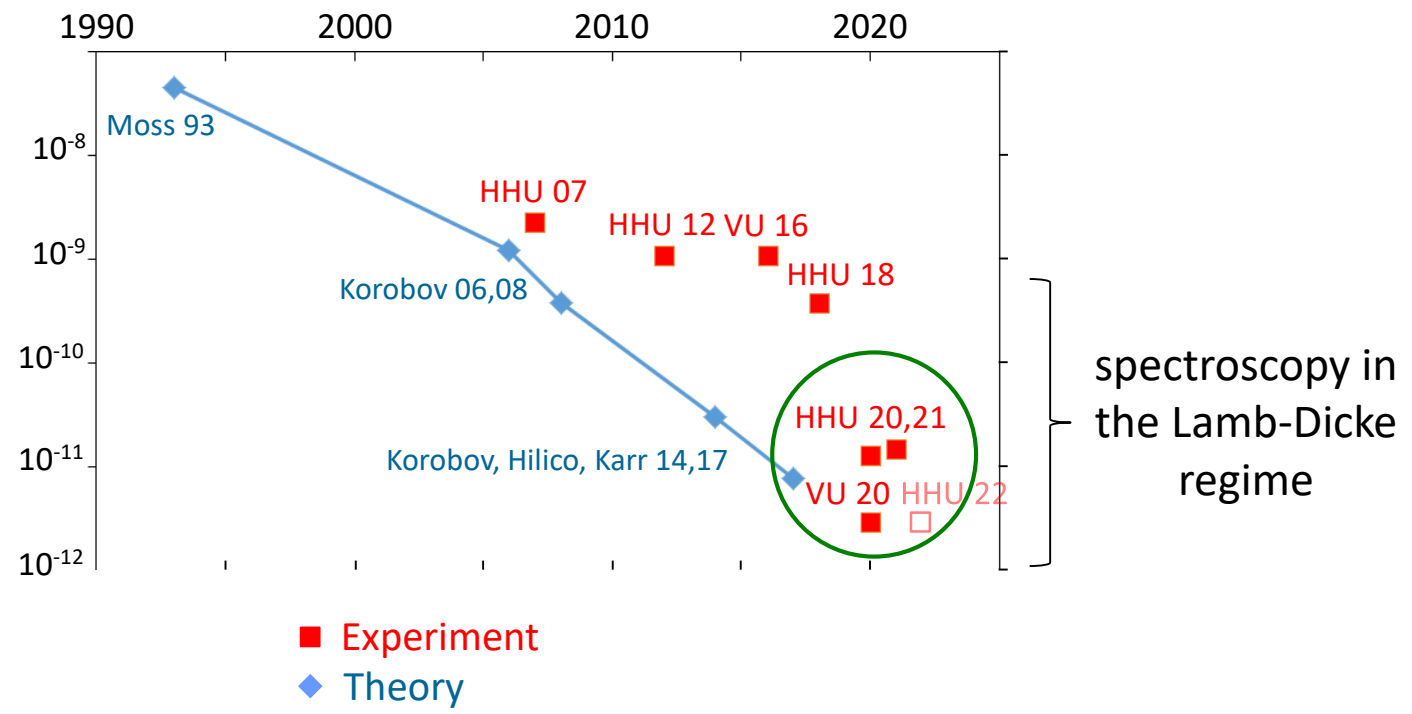


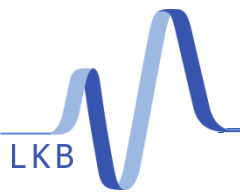
- Experiments : recent developments, ongoing projects
- Theory : hyperfine structure, energy levels
- Comparing theory with experiments
 - determination of fundamental constants
 - constraints on “new physics”



Progress in HD⁺ spectroscopy

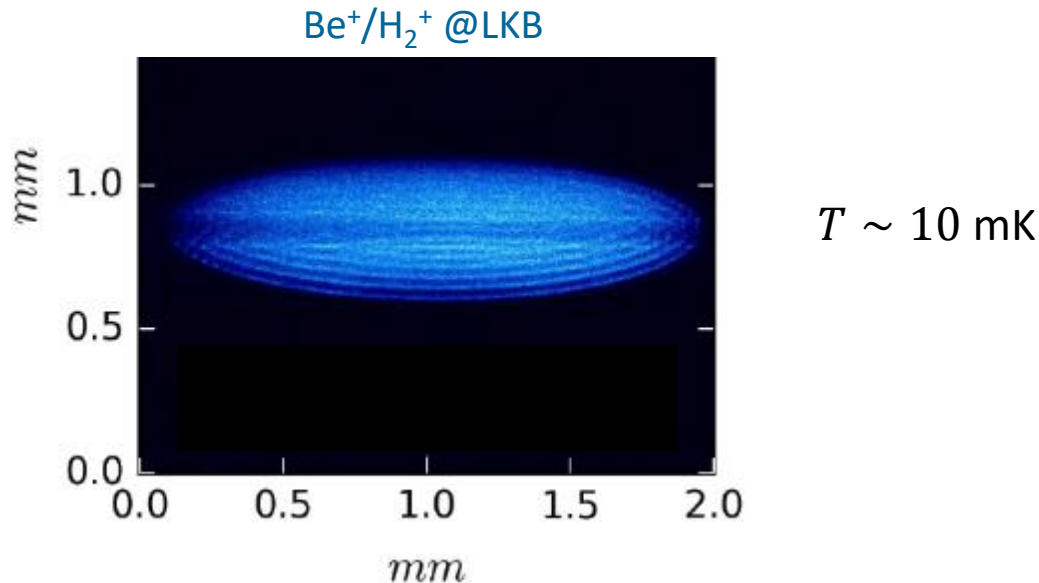
Precision of “Spin-averaged”
rovibrational transition frequencies





Experimental methods

- Ensembles of $\sim 50 - 100$ HD⁺ ions sympathetically cooled by laser-cooled Be⁺

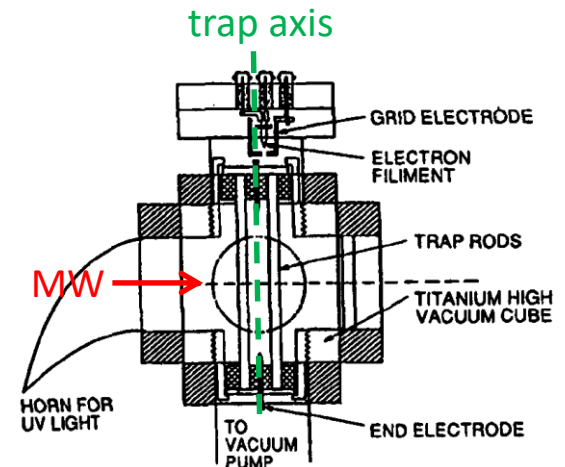


- **HD⁺ ion creation** by electron-impact ionization
 - relax to $v = 0$, but distributed in many rotational/hyperfine states
 - rotational cooling (T. Schneider et al., Nature Phys. 2010)
 - rf fields to transfer population between hyperfine levels
- **Detection** by selective photodissociation of excited state (REMPD)
 - signal = ion loss, measured from Be⁺ fluorescence change after secular excitation of HD⁺

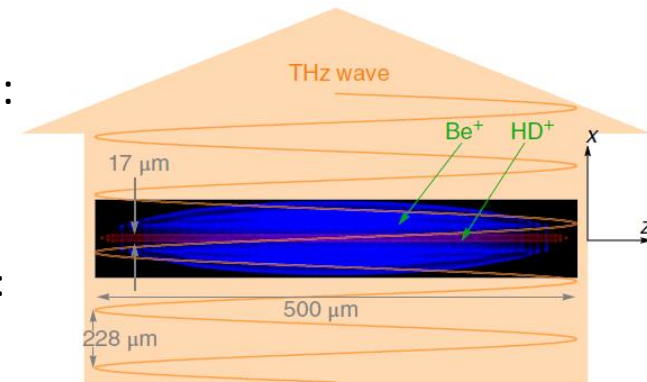
- Lamb-Dicke regime : $\delta x < \lambda/2\pi$
- Easy in the microwave domain (even at 300 K)
Ex: Hg⁺ ion clock ($\nu = 40.5$ GHz, $\lambda = 7.4$ mm) @JPL
- More challenging in the optical domain
(requires tightly confining trap)
- Easier for rotational/vibrational transitions in molecular ions (MIR/THz domain)

Sympathetic cooling ($T \sim 10$ mK), weakly confining trap:
 $\delta x \sim 1 - 10 \mu\text{m}$

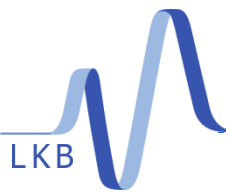
HD⁺ rotational transition ($\nu = 0, L = 0$) \rightarrow ($\nu' = 0, L' = 1$):
 $\lambda = 228 \mu\text{m}$



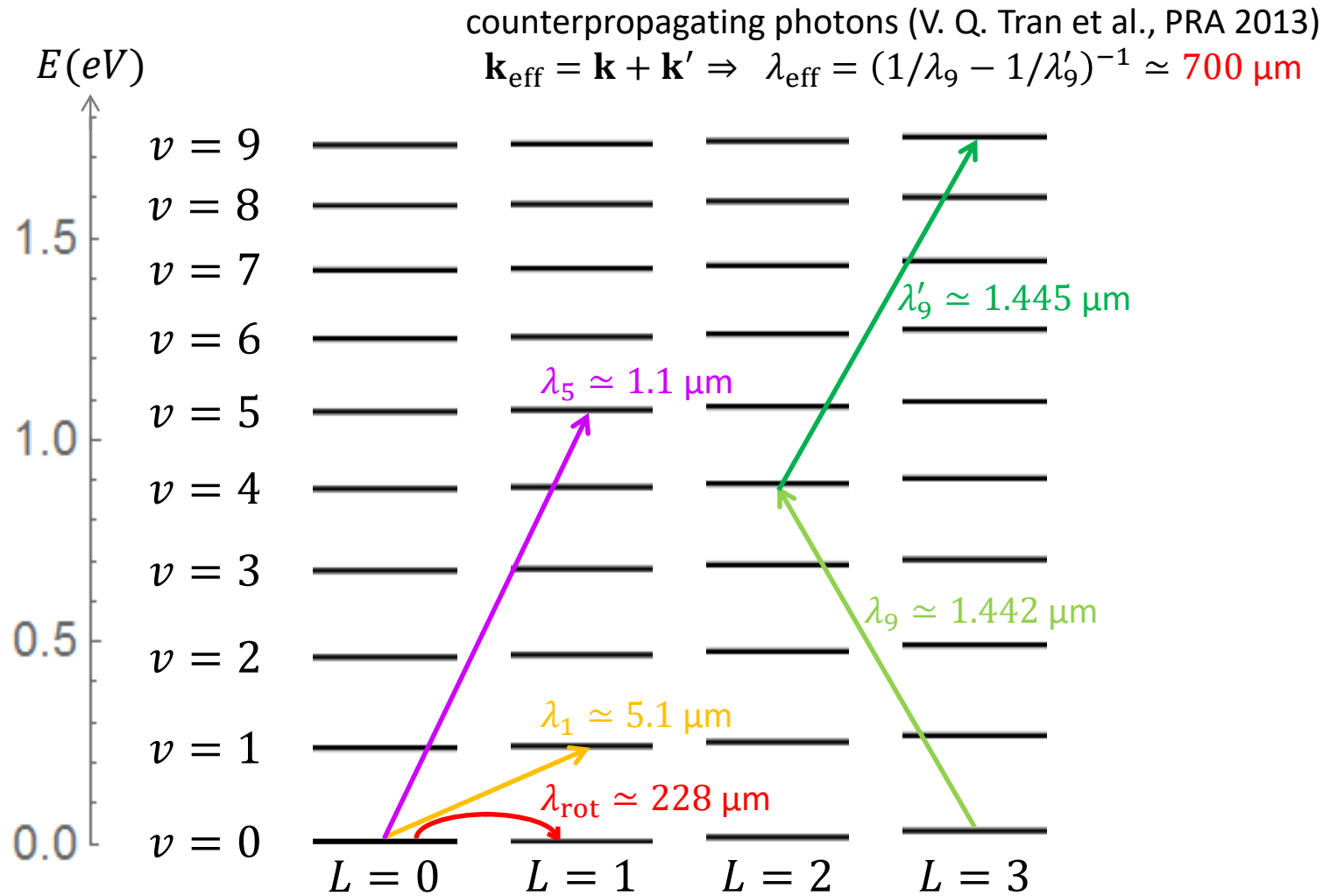
J.D. Prestage et al., IEEE 1990



S. Alighanbari et al., Nature Phys. 2018



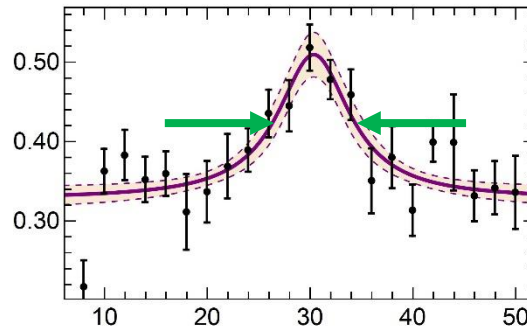
HD⁺ high-precision measurements ($\sim 10^{-11} - 10^{-12}$)



S. Alighanbari et al., Nature 2020
I. Kortunov et al., Nature Phys. 2021

S. Patra et al., Science 2020

$\nu = 0 \rightarrow 9$ transition (one hyperfine component)



Linewidth < 10 kHz

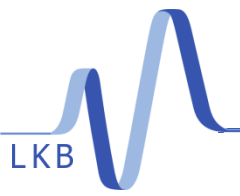
$$\nu_{\text{exp}} = 415\,264\,862\,249.2(0.4)_{\text{syst}}(0.5)_{\text{stat}} \text{ kHz}$$

S. Patra et al., Science 2020

- 2 hyperfine components measured
- Theoretical hyperfine structure required to extract spin-averaged transition frequency

Outlook

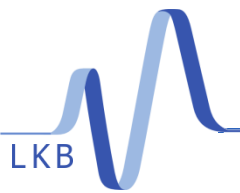
- H_2^+ two-photon spectroscopy (LKB) → see next slides
- Quantum-logic spectroscopy
 - Be^+/HD^+ Ch. Wellers et al., Mol. Phys. 2021
 - Be^+/H_2^+ D. Kienzler, ETH Zürich
- Spectroscopy of a single molecular ion in a Penning trap
 - Proposal for $\text{H}_2^+/\text{anti-H}_2^+$ E.G. Myers, PRA 2018 ; J.-Ph. Karr, PRA 2018 and 2021
 - Ongoing experiment: HD^+ (hfs) S. Sturm, MPIK Heidelberg



Complications with respect to HD⁺

Ro-vibrational transitions are not dipole-allowed, thus...

- Worse population problem
 - long-lived excited vibrational states (~ 1 week)
 - Our solution : state-selective production of H₂⁺ by multiphoton (3+1) ionization (REMPI) from a pulsed H₂ molecular beam J. Schmidt et al., PR Appl. 2020
- Weaker transitions
 - Doppler-free two-photon transition : $(v = 0, L = 2) \rightarrow (v' = 1, L' = 2)$, $\lambda = 9.17 \mu\text{m}$
 - No enhancement from quasi-resonant intermediate states
 - In-vacuum enhancement cavity required
- ✓ Trapped, sympathetically cooled, state-selected H₂⁺
- ✓ Selective photodissociation (213 nm) + ion counting for REMPD spectroscopy
- ✓ Ultrastable laser source @ 9.17 μm : QCL phase-locked to single-mode CO₂ laser, injected in-vacuum cavity
- Lastly: absolute frequency measurements in the mid-infrared



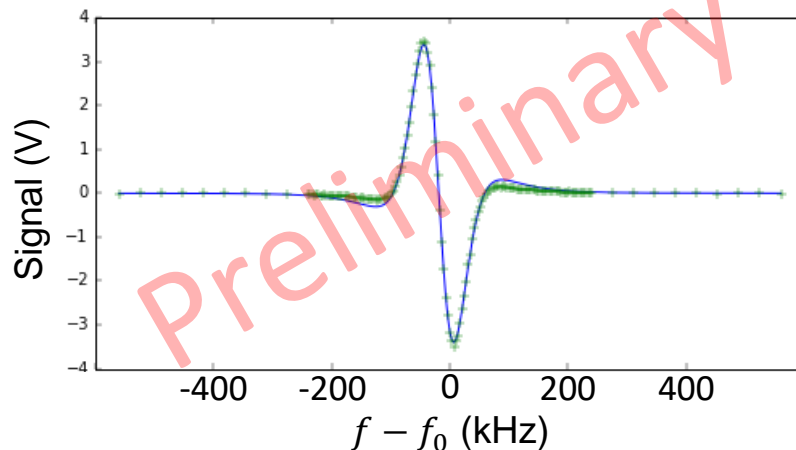
Frequency measurement setup

- ✓ Frequency comb centered at $1.56 \mu\text{m}$, locked on ultrastable signal T-REFIMEVE from SYRTE at $1.542 \mu\text{m}$
- ✓ Extension around $1.89 \mu\text{m}$
- ✓ SFG in AgGaSe_2 : $1.89 \mu\text{m} + 9.17 \mu\text{m} \rightarrow 1.56 \mu\text{m}$
- ✓ Beat note SFG signal/comb used to lock CO_2 laser
- ✓ QCL locked to CO_2 laser with tunable frequency offset ($\pm 2 \text{ GHz}$)

See B. Argence et al.,
Nature Photon. 2015

Characterization : spectroscopy of formic acid (HCOOH)

Intracavity saturated absorption, 3rd harmonic detection



Repeatability of line center :
 $\pm 37 \text{ Hz}$ ($\sim 10^{-12}$)

- Nonrelativistic Quantum Electrodynamics (NRQED)
 - effective Hamiltonian approach
 - expansion of corrections in powers of $\alpha, Z\alpha, m/M$.

- Resolution of the three-body Schrödinger equation by a variational method

Separation of radial and angular variables:

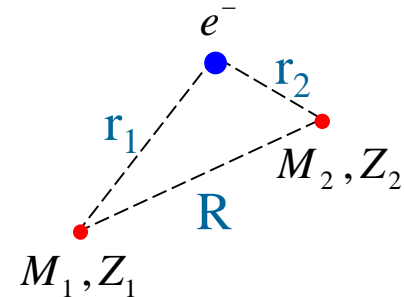
$$\psi_{LM}^{\Pi}(\mathbf{R}, \mathbf{r}_1) = \sum_{l_1+l_2=L \text{ or } L+1} \Upsilon_{LM}^{l_1 l_2}(\hat{\mathbf{R}}, \hat{\mathbf{r}}_1) F_{l_1}(R, r_1, r_2)$$

C. Schwartz, Phys. Rev. **123**, 1700 (1961)

Radial wavefunctions:

$$F(R, r_1, r_2) = \sum_{n=1}^N \left(C_n \operatorname{Re} \left(e^{-\alpha_n R - \beta_n r_1 - \gamma_n r_2} \right) + D_n \operatorname{Im} \left(e^{-\alpha_n R - \beta_n r_1 - \gamma_n r_2} \right) \right)$$

V.I. Korobov, Phys. Rev. A **61**, 064503 (2000)



- ✓ Extremely accurate energy levels (10^{-15} - 10^{-20} or better) and wavefunctions

- Some higher-order corrections are evaluated in the adiabatic approximation

$$\Psi^{\text{BO}} = \phi_{\text{el}}(\mathbf{r}; R)\chi_{\text{BO}}(R)$$

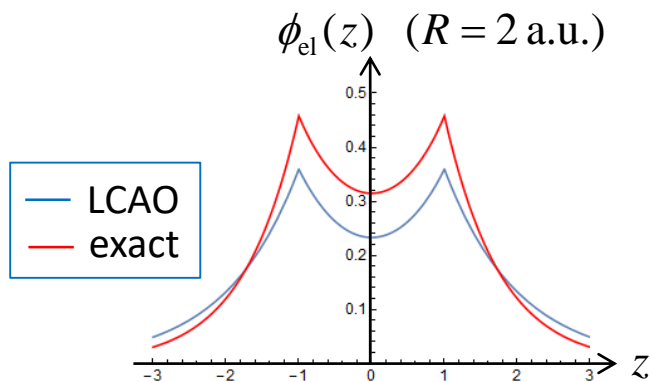
Variational expansion:

$$\phi_{\text{el}}(r_1, r_2) = \sum_{i=1}^N C_i (e^{-\alpha_i r_1 - \beta_i r_2} + e^{-\beta_i r_1 - \alpha_i r_2})$$

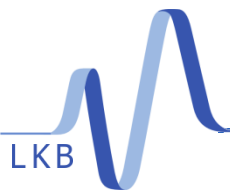
Ts. Tsogbayar and V.I. Korobov, J. Chem. Phys. **125**, 024308 (2006)

- LCAO approximation :

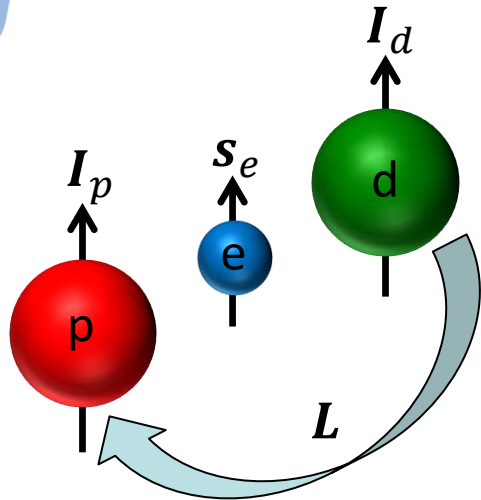
$$\phi_{\text{LCAO}}(r_1, r_2) = \frac{1}{\sqrt{2(1+S)}} [\phi_{1s}(r_1) + \phi_{1s}(r_2)]$$



$1\sigma_g$ electronic wavefunction



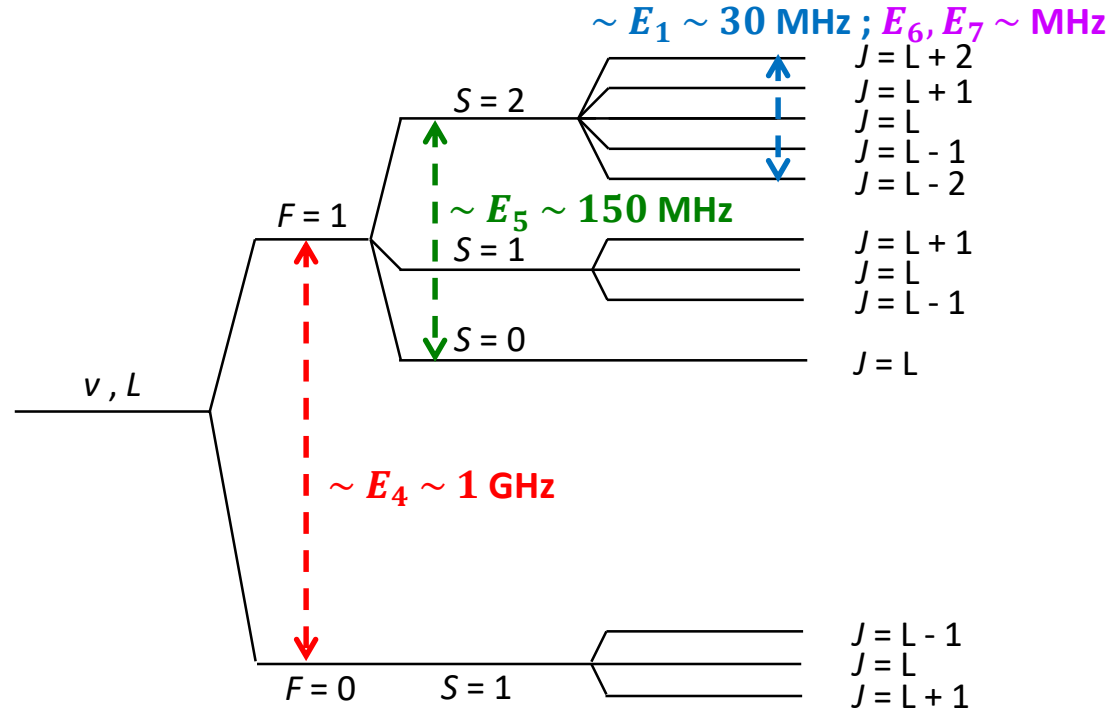
Effective spin Hamiltonian: HD⁺



$$\mathbf{F} = \mathbf{s}_e + \mathbf{I}_p$$

$$\mathbf{S} = \mathbf{F} + \mathbf{I}_d$$

$$\mathbf{J} = \mathbf{S} + \mathbf{L}$$



Electronic spin-orbit Nuclear spin-rotation

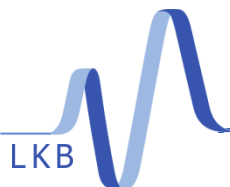
$$H_{\text{eff}} = E_1(\mathbf{L} \cdot \mathbf{s}_e) + E_2(\mathbf{L} \cdot \mathbf{I}_p) + E_3(\mathbf{L} \cdot \mathbf{I}_d) + E_4(\mathbf{I}_p \cdot \mathbf{s}_e) + E_5(\mathbf{I}_d \cdot \mathbf{s}_e) \quad \text{"Fermi" interaction}$$

$$+ E_6 \left\{ 2\mathbf{L}^2(\mathbf{I}_p \cdot \mathbf{s}_e) - 3[(\mathbf{L} \cdot \mathbf{I}_p)(\mathbf{L} \cdot \mathbf{s}_e) + (\mathbf{L} \cdot \mathbf{s}_e)(\mathbf{L} \cdot \mathbf{I}_p)] \right\}$$

$$+ E_7 \left\{ 2\mathbf{L}^2(\mathbf{I}_d \cdot \mathbf{s}_e) - 3[(\mathbf{L} \cdot \mathbf{I}_d)(\mathbf{L} \cdot \mathbf{s}_e) + (\mathbf{L} \cdot \mathbf{s}_e)(\mathbf{L} \cdot \mathbf{I}_d)] \right\} \quad \text{Spin-spin tensor interactions}$$

$$+ E_8 \left\{ 2\mathbf{L}^2(\mathbf{I}_p \cdot \mathbf{I}_d) - 3[(\mathbf{L} \cdot \mathbf{I}_p)(\mathbf{L} \cdot \mathbf{I}_d) + (\mathbf{L} \cdot \mathbf{I}_d)(\mathbf{L} \cdot \mathbf{I}_p)] \right\}$$

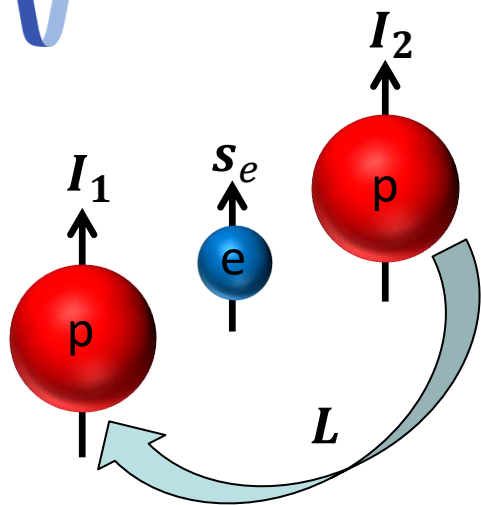
$$+ E_9 \left\{ \mathbf{L}^2 \mathbf{I}_d^2 - (3/2)(\mathbf{L} \cdot \mathbf{I}_d) - 3(\mathbf{L} \cdot \mathbf{I}_d)^2 \right\} \quad \text{Deuteron Quadrupole moment}$$



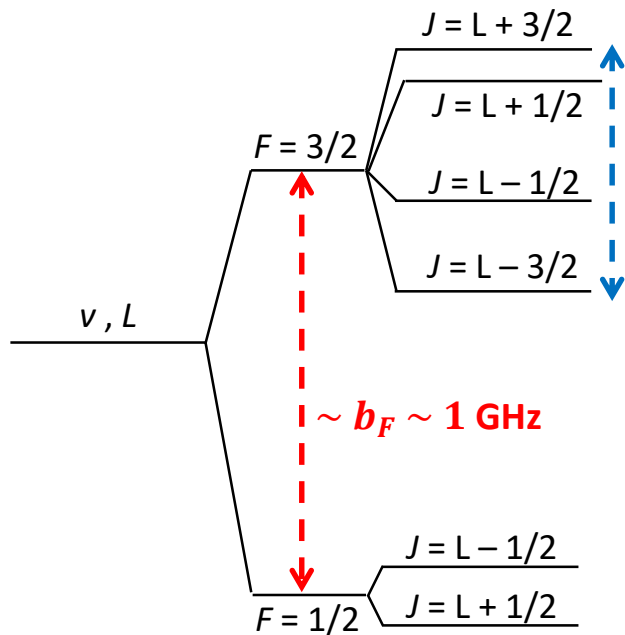
Effective spin Hamiltonian: H_2^+

Odd $L: I = 1$ (ortho)

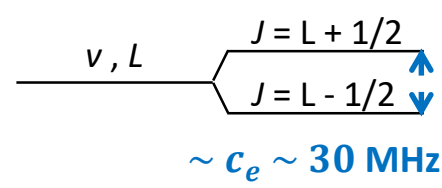
Even $L: I = 0$ (para)



$$\begin{aligned} \mathbf{I} &= \mathbf{I}_1 + \mathbf{I}_2 \\ \mathbf{F} &= \mathbf{s}_e + \mathbf{I} \\ \mathbf{J} &= \mathbf{S} + \mathbf{L} \end{aligned}$$



$\sim c_e \sim 30 \text{ MHz}$
 $d_1 \sim \text{MHz}$



Electronic spin-orbit

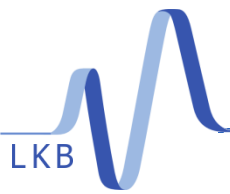
Nuclear spin-rotation

$$H_{\text{eff}} = c_e (\mathbf{L} \cdot \mathbf{s}_e) + c_I (\mathbf{L} \cdot \mathbf{I}) + b_F (\mathbf{I} \cdot \mathbf{s}_e) \quad \text{"Fermi" interaction}$$

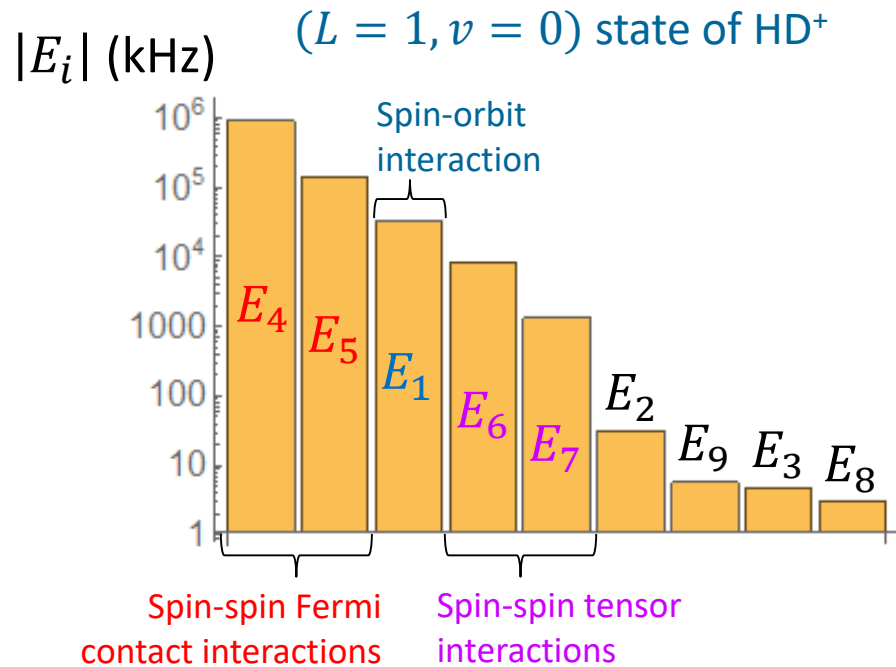
$$+ \frac{d_1}{3(2L-1)(2L+3)} \left\{ 2\mathbf{L}^2 (\mathbf{I} \cdot \mathbf{s}_e) - 3[(\mathbf{L} \cdot \mathbf{I})(\mathbf{L} \cdot \mathbf{s}_e) + (\mathbf{L} \cdot \mathbf{s}_e)(\mathbf{L} \cdot \mathbf{I})] \right\}$$

$$+ \frac{d_2}{3(2L-1)(2L+3)} \left\{ \mathbf{L}^2 \mathbf{I}^2 - \frac{3}{2} (\mathbf{L} \cdot \mathbf{I}) - 3(\mathbf{L} \cdot \mathbf{I})^2 \right\}$$

Spin-spin tensor interactions



Calculation of hyperfine coefficients



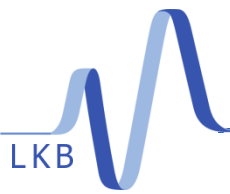
- All coefficients calculated within Breit-Pauli approximation, taking into account electron anomalous magnetic moment
All terms of order $m\alpha^4$ and $m\alpha^5$ included \Rightarrow relative uncertainty $\sim \alpha^2$
D. Bakalov et al., PRL 2006
- Sufficient for small coefficients (E_2, E_3, E_8, E_9) at present level of exp. accuracy
- For the largest coefficients, higher-order corrections need to be considered
 $E_4, E_5 \rightarrow$ see next slide
 E_1, E_6, E_7 : V.I. Korobov et al., PRA 2020 ; M. Haidar et al., arXiv:2209.02382, to appear in PRA

Spin-spin contact interactions

Type of contribution	H atom $\Delta E_{hfs}(1S)$	HD ⁺ molecule $E_4(v=0, L=0)$	
Fermi splitting E_F [$m\alpha^4$ order]	1 418 840.093	924 383.973	} Breit-Pauli
Anomalous magnetic moment [αE_F]	1 645.361	1 071.964	
Relativistic (“Breit”) correction [$(Z\alpha)^2 E_F$]	113.333	66.936(61)	} State-independent
One-loop radiative correction [$\alpha(Z\alpha)E_F$]	-136.517	-88.942	
One-loop radiative correction [$\alpha(Z\alpha)^2 E_F$]	-11.330	-7.381	
Higher-order nonrecoil QED	1.089(1)	-2.241(432)	
Nuclear correction = $E_{hfs}^{exp} - E_{hfs}^{QED}$	-46.276(1)	-30.150(424)	
TOTAL	1 420 405.752 (exp.)	925 394.159(860)	0.93 ppm

J.-Ph. Karr et al., PRA **102**, 052827 (2020)

- $(Z\alpha^2)E_F$ relativistic correction calculated in the adiabatic approximation.
- Nuclear correction in H atom determined from the difference between experimental value and total nonrecoil QED prediction.
- Higher-order QED & nuclear correction added in HD⁺ theory under the approximation that they are entirely described by a **delta function**.



Comparison with experiments : H_2^+

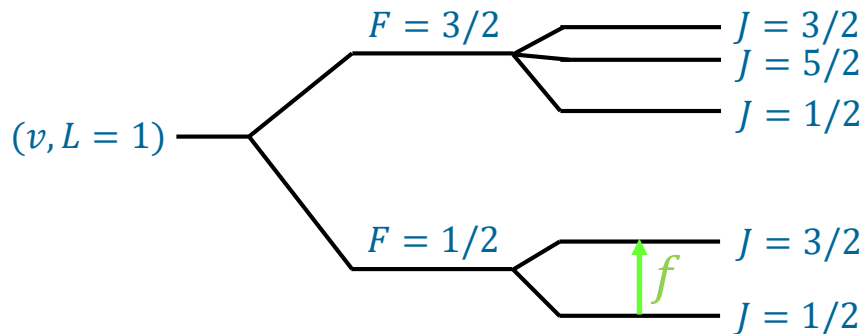
- Complete measurements of the hyperfine splitting
K. B. Jefferts, PRL **23**, 1476 (1969)
- ⇒ spin-spin contact interaction coefficient b_F ($\leftrightarrow E_4$ in HD^+)
- ✓ Good agreement at ~ 1 ppm level

Unit: MHz L = 1

ν	b_F (theory)	b_F (experiment)
4	836.7287(8)	836.7292(8)
5	819.2267(8)	819.2273(8)
6	803.1745(7)	803.1751(8)
7	788.5075(7)	788.5079(8)
8	775.1712(7)	775.1720(8)

J.-Ph. Karr et al., PRA **102**, 052827 (2020)

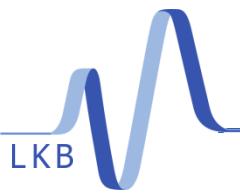
- High-precision measurements ($\sim 10^{-7}$) for a few hyperfine intervals
S. C. Menasian and H. G. Dehmelt, Bull. Am. Phys. Soc. **18**, 408 (1973)
- Sensitive to c_e, d_1 ($\leftrightarrow E_1, E_6$ in HD^+)
- ✓ Small deviations of 60-80 Hz (3-5 ppm) $\sim 1.2-1.6 \sigma_c$



Unit: MHz

(L, ν)	f (theory)	f (experiment)
(1,4)	15.371 316(56)	15.371 407(2)
(1,5)	14.381 453(52)	14.381 513(2)
(1,6)	13.413 397(48)	13.413 460(2)

M. Haidar et al., PRA **106**, 022816 (2022)



Comparison with experiments : HD⁺

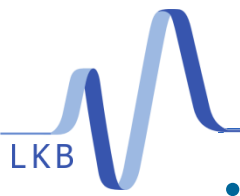
Unit: kHz

Transition	f_{hfs}^{exp}	f_{hfs}^{theor}	Δf	$\Delta f/\sigma_c$	
$(v = 0, L = 0) \rightarrow (v' = 1, L' = 1)$	41 294.06(32)	41 293.66(12)	0.40	1.2	E_1, E_6
$(v = 0, L = 0) \rightarrow (v' = 5, L' = 1)$	126 092.6(1.2)	126 092.02(10)	0.58	0.5	E_4, E_5
$(v = 0, L = 3) \rightarrow (v' = 9, L' = 3)$	178 254.4(9)	178 245.89(28)	8.5	9.0	E_4, E_5

➤ Rotational transition : 6 hyperfine components measured → extract E_1, E_6, E_7

coefficient	E_k^{exp}	E_k^{theor} (this work)	ΔE_k	$\Delta E_k/\sigma_c$
E_1	31 984.9(1)	31 985.41(12)	-0.5	-3.3
E_6	8 611.17(5)	8 611.299(18)	-0.13	-2.4
E_7	1 321.72(4)	1 321.7960(28)	-0.08	-2.0

- No contribution(s) identified that could have the required order of magnitude to explain discrepancies
- Take discrepancies into account by expanding error bars



HD⁺ energy levels: overview and comparison with H atom

- Unit: kHz, CODATA 2018 values of FC
- Only theoretical uncertainties are shown

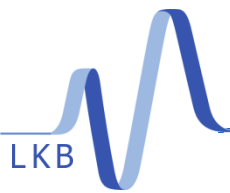
Type of contribution	H atom $\Delta E(1S)$	HD ⁺ molecule $\Delta E(v = 0, L = 0)$
1. Relativistic energy	-3 288 095 029 857.92	-3 934 027 681 033.9(1.1)
2. Relativistic-recoil	2 402.35	2 229.6(0.6)
3. One-loop self-energy	8 383 339.47	10 891 032.6(17.4)
4. One-loop vacuum polarization	- 214 816.61	-280 113.6
Muonic VP	-5.07	-6.6
Hadronic VP	-3.40(8)	-4.4(0.1)
5. Two-loop radiative corrections	727.19(66)	944.6(11.8)
6. Three-loop radiative corrections	1.72(34)	2.4(0.6)
7. Nuclear finite size and polarizability (+ rad. corr.)	1 107.98(39)	5 330.2(0.5)
8. Radiative-recoil corrections	-12.32(74)	-13.5(2.2)
9. Nuclear self-energy	4.62(16)	3.8(0.1)
TOTAL	-3 288 086 857 111.4(1.1)	-3 934 017 061 629(21)

E. Tiesinga et al., Rev. Mod. Phys. **93**, 025010 (2021)

S. Karshenboim et al., Phys. Lett. B **795**, 432 (2019)

3.5×10^{-13}

5.3×10^{-12}



One-loop self-energy

$$E_{se} = m\alpha^5 \left[(A_{41} \ln(\alpha^{-2}) + A_{40}) \langle Z_1 \delta(\mathbf{r}_1) + Z_2 \delta(\mathbf{r}_2) \rangle \right. \\ + A_{50} \alpha \langle Z_1^2 \delta(\mathbf{r}_1) + Z_2^2 \delta(\mathbf{r}_2) \rangle \\ + (A_{62} \ln^2(\alpha^{-2}) + A_{61} \ln(\alpha^{-2}) + A_{60}) \alpha^2 \langle Z_1^3 \delta(\mathbf{r}_1) + Z_2^3 \delta(\mathbf{r}_2) \rangle \\ \left. + (A_{71} \ln(\alpha^{-2}) + A_{70}) \alpha^3 \langle Z_1^4 \delta(\mathbf{r}_1) + Z_2^4 \delta(\mathbf{r}_2) \rangle + \dots \right]$$

- Some coefficients ($A_{41}, A_{50}, A_{62}, A_{71}$) are state-independent and can be taken from H-like atom theory.

- $m\alpha^5$ order: Bethe logarithm calculated with 8-9 significant digits

V.I. Korobov, PRA **85**, 042514 (2012) ; V.I. Korobov and Z.-X. Zhong, PRA **86**, 044501 (2012)

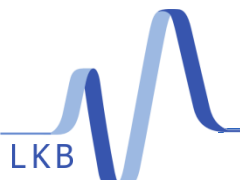
- $m\alpha^7$ order: calculated in the adiabatic approximation

V.I. Korobov, L. Hilico, J.-Ph. Karr, PRL **112**, 103003 and PRA **89**, 032511 (2014)

- Higher-order remainder ($m\alpha^8$ and above): estimated from H(1S) results using the LCAO approximation

$$E_{se}^{(8+)} = m\alpha^7 (G_{SE}(1S) - A_{60}(1S)) \langle Z_1^3 \delta(\mathbf{r}_1) + Z_2^3 \delta(\mathbf{r}_2) \rangle$$

V.I. Korobov and J.-Ph. Karr, PRA **104**, 032806 (2021)



Comparison with experiments

$(L, v) \rightarrow (L', v')$	Theory	Experiment
$(0, 0) \rightarrow (1, 0)$	1 314 925 752.932(<u>19</u>)(<u>61</u>)	1 314 925 752.910(17)
$(0, 0) \rightarrow (1, 1)$	58 605 052 163.9(<u>0.5</u>)(<u>1.3</u>)	58 605 052 164.24(86)
$(3, 0) \rightarrow (3, 9)$	415 264 925 502.8(<u>3.3</u>)(<u>6.7</u>)	415 264 925 501.8(1.3)

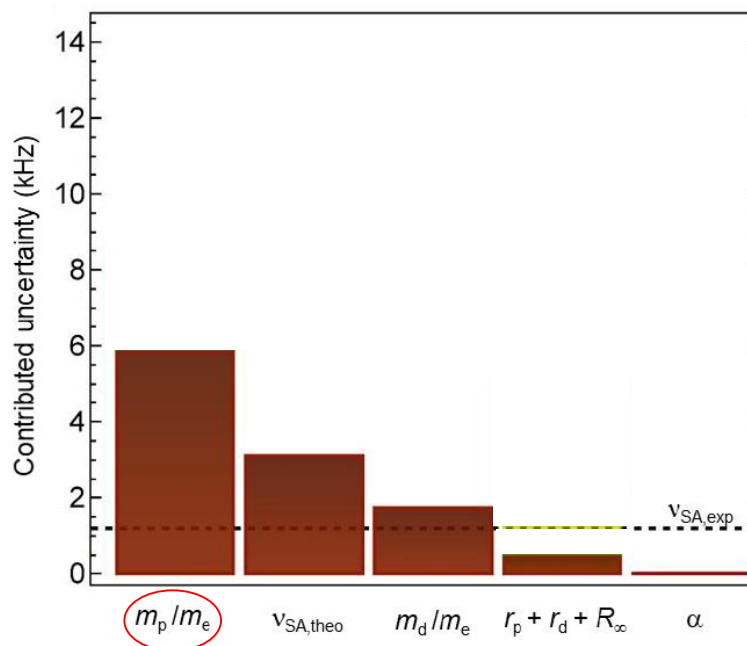
V.I. Korobov and J.-Ph. Karr,
PRA **104**, 032806 (2021)

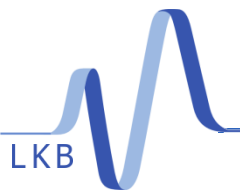
Theoretical uncertainties
Uncertainties from FC (CODATA 2018)

Uncertainty contributions

Example : $v = 0 \rightarrow 9$ transition

S. Patra et al., Science **369**, 1238 (2020)





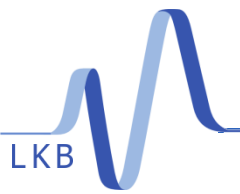
- Theoretical uncertainty $\sim 7.5 \cdot 10^{-12}$ ($1.5 \cdot 10^{-11}$) for vibrational (rotational) transitions
- Satisfactory agreement with experimental data
- Next step : nonperturbative calculation of the one-loop self-energy using highly precise solutions of two-center Dirac equation:
 - H.D. Nogueira, V.I. Korobov, J.-Ph. Karr, PRA **105**, L060801 (2022)
 - O. Kullie, S. Schiller, PRA **105**, 052801 (2022)

\Rightarrow reduce uncertainty by a factor of ~ 2 .

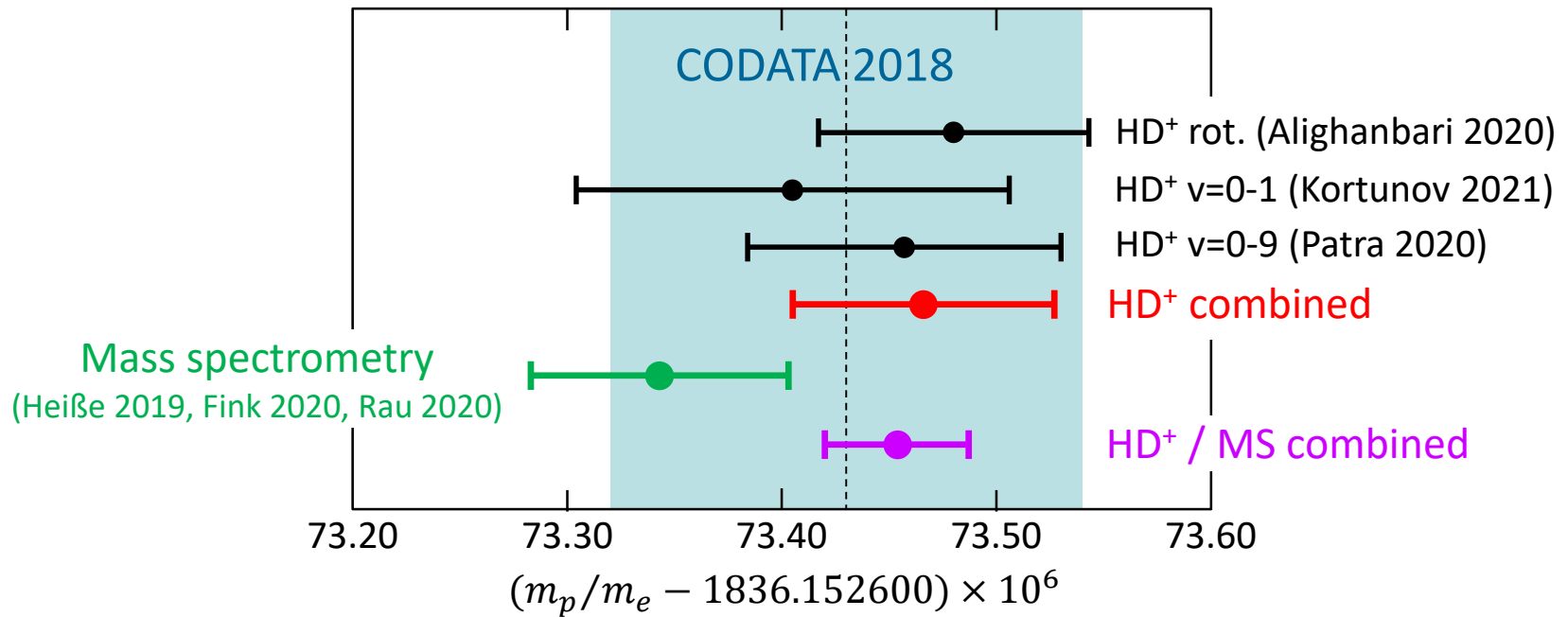
} 10^{-20} accuracy
(in agreement!)

Applications

- Determination of fundamental constants
- Constraining “new physics”



Determination of the proton-electron mass ratio



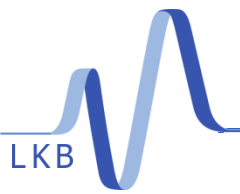
- From HD⁺ data alone:

$$m_p/m_e = 1836.152\,673\,466(61) \quad [3.3 \times 10^{-11}]$$

Good agreement with CODATA 2018 and recent mass spectrometry results.

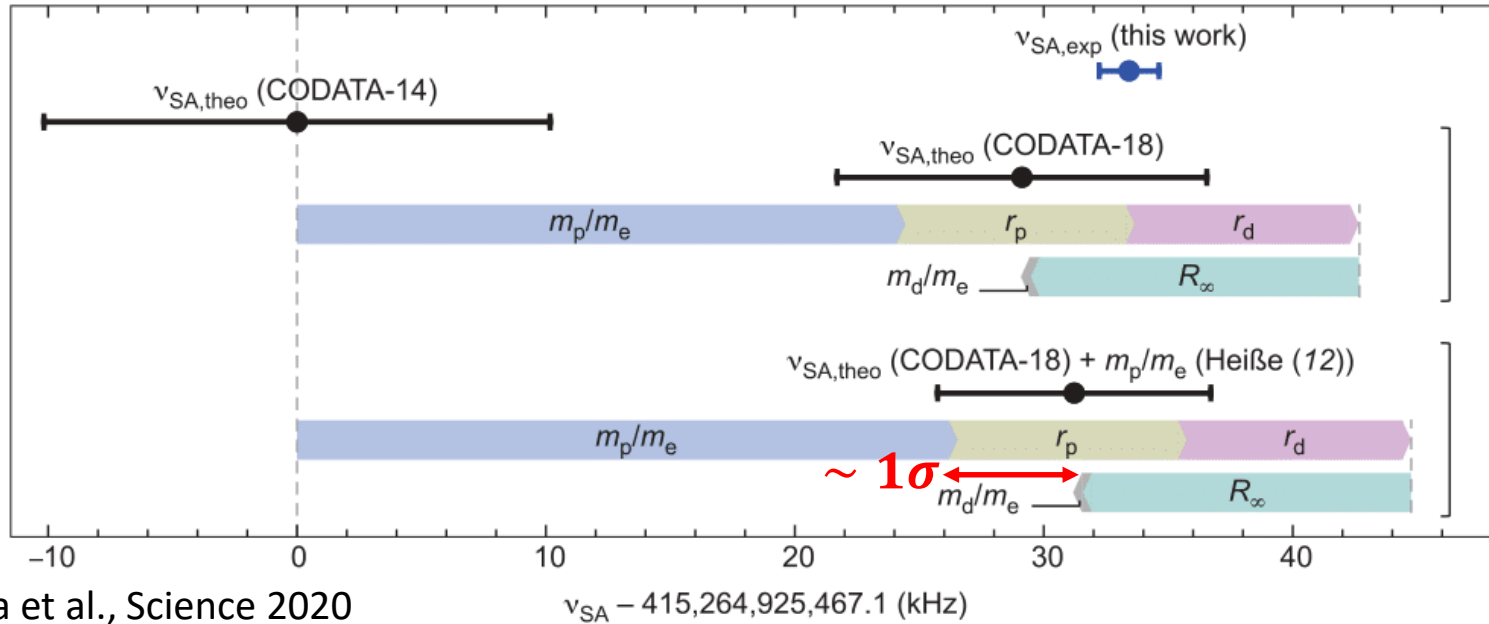
- From HD⁺ and mass spectrometry combined:

$$m_p/m_e = 1836.152\,673\,454(33) \quad [1.8 \times 10^{-11}]$$



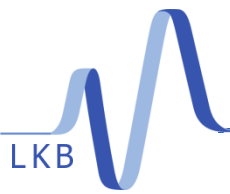
Is HD⁺ spectroscopy sensitive to the proton radius ?

Example : ($\nu = 0, L = 3$) \rightarrow ($\nu' = 9, L' = 3$) transition

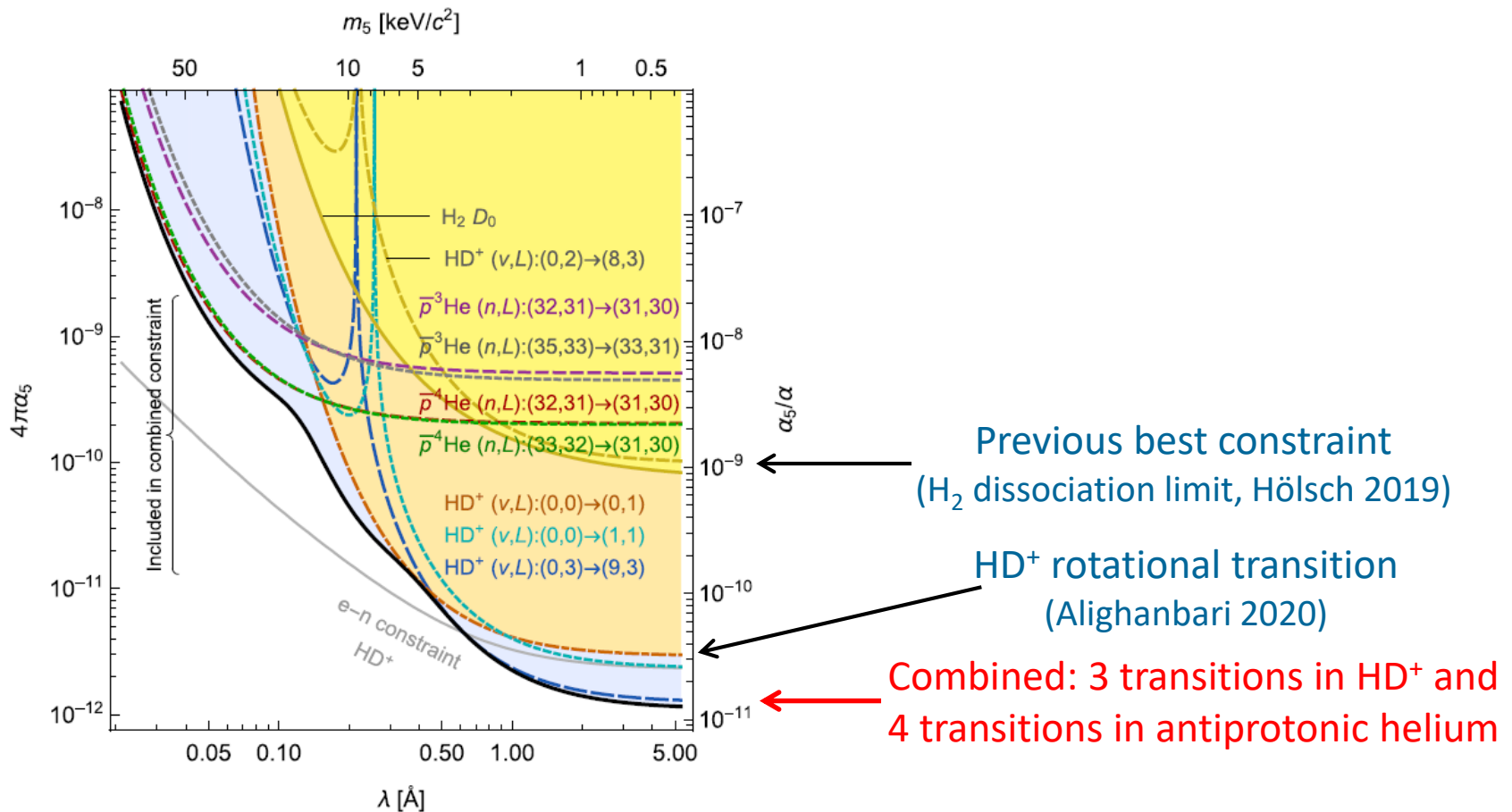


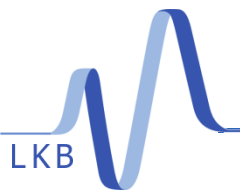
- r_p, r_d, R_∞ are strongly correlated (H/D 1S-2S)
- With measurements at 10^{-12} precision level, theory improvement to $3 \cdot 10^{-12}$: $u(r_p) < 0.01$ fm

J.-Ph. Karr et al., PRA 94, 050501(R) (2016)



Constraint on “fifth force” between hadrons





Self-consistent approach to constrain new physics (NP)

C. Delaunay, JPK, T. Kitahara, J. Koelemeij, Y. Soreq, J. Zupan (soon on arXiv)

- Precision measurements (e.g. spectroscopy of simple atoms/molecules) can be used for NP searches by comparing with Standard Model (SM) prediction.
- SM predictions use accepted (CODATA) values of fundamental constants, which are obtained under the assumption that no NP exists. The presence of NP would affect the extraction of fundamental constants !
- Self-consistent approach: global fit of precision data in the presence of NP, simultaneously extracting fundamental constants and NP parameters.

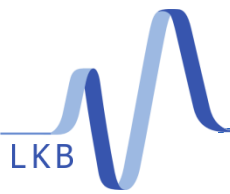
Datasets

1) “Control” dataset = subset of CODATA 2018

- H, D, μH , μD spectroscopy (R_∞, r_p, r_d)
- $a_e, h/m_X$, bound electron g -factors, mass spectrometry (α, m_e, m_p, m_d)
- 78 observational equations, 44 adjusted constants
(CODATA 2018: 105/62 without G and d_{220})

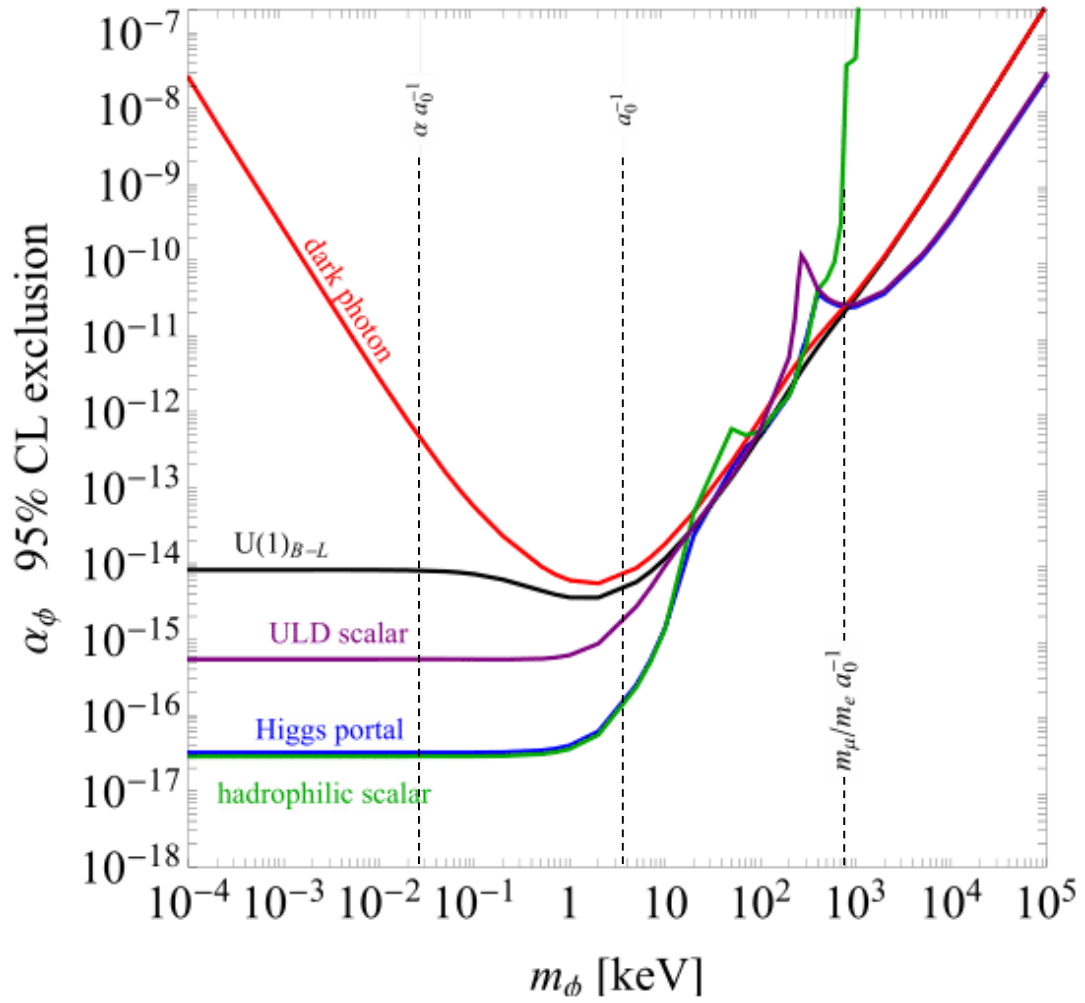
2) 2022 dataset: with most recent data and theory improvements

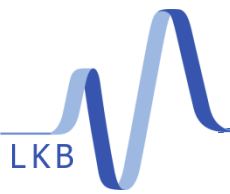
and HD^+ , $\bar{p}\text{He}$ spectroscopy (more sensitive to some NP models)



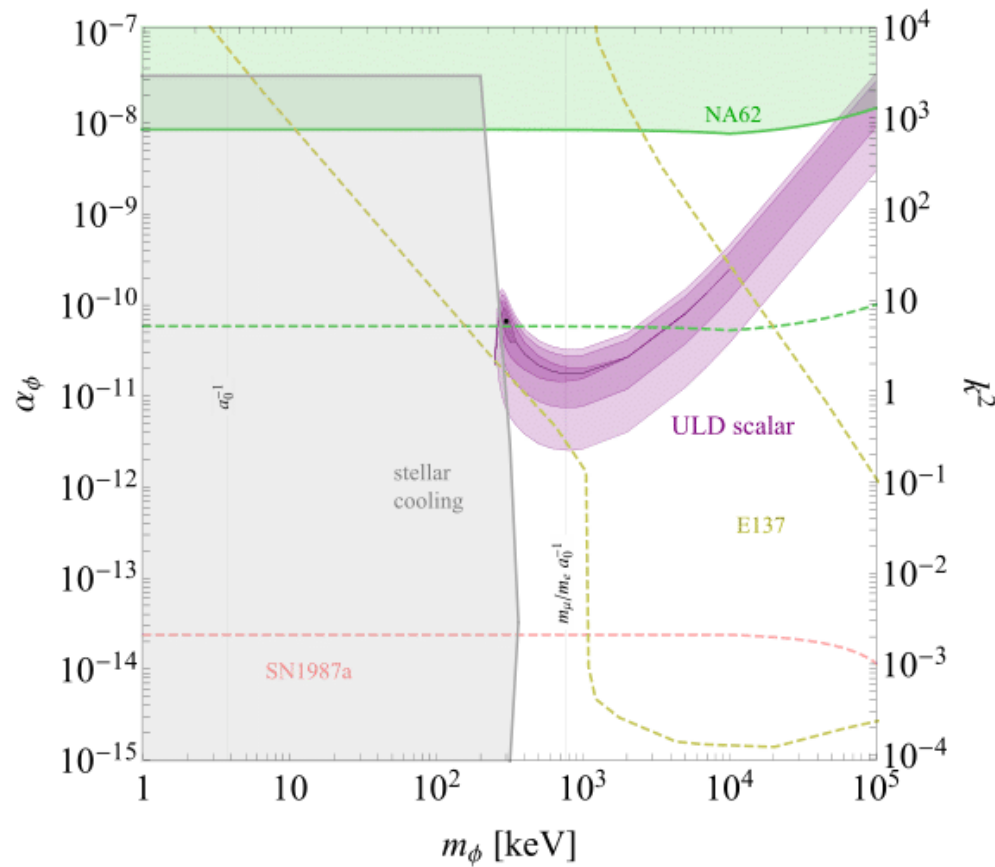
Bounds on NP coupling constant

$$V_{NP}^{ij}(r) = (-1)^{s+1} \alpha_\phi q_i q_j \frac{e^{-m_\phi r}}{r}$$

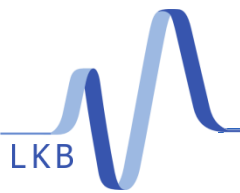




NP model favored over SM



- Tensions related to the proton radius favor nonzero e-p coupling
- “Up-Lepto-Darko-philic” scalar model statistically favored at $\sim 5\sigma$ level, not excluded by other constraints



Summary

- Several HD⁺ rovibrational transitions measured with 10⁻¹¹/10⁻¹² precision
More - and more precise - data to come.
- Improved hyperfine structure theory
 - Good agreement in H₂⁺
 - HD⁺ : good agreement or big discrepancy, depending on transition
 - Affects the precision of extracted spin-averaged transition frequencies, but no big impact on m_p/m_e determination.
- Theoretical precision : 7.5 10⁻¹² (1.5 10⁻¹¹) for vibrational (rotational) transitions
Next step: nonperturbative calculation of the one-loop self-energy, using accurate solutions of the two-center Dirac equation.
- Final data for CODATA 2022 adjustment under study
Preliminary estimate : m_p/m_e uncertainty reduced to $\sim 2 \cdot 10^{-11}$, combining HD⁺ spectroscopy with mass spectrometry.
- Self-consistent bounds on NP : check arXiv !

Acknowledgements

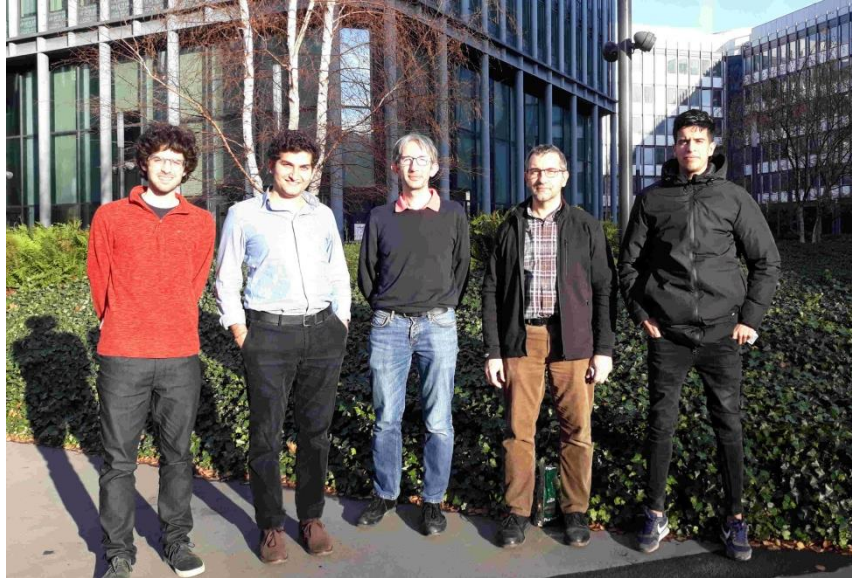
Bérangère Argence

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