

# New Theory Initiative on Muonic Atom Spectroscopy

Theory consensus on the **Lamb shift and hfs** of muonic hydrogen, deuterium, ...; akin to the “*g*-2 Theory Initiative”

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## The anomalous magnetic moment of the muon in the Standard Model



Contribution	Section	Equation	Value $\times 10^{11}$	References
Experiment (E821)		Eq. (8.13)	116 592 089(63)	Ref. [1]
HVP LO ( $e^+e^-$ )	Section 2.3.7	Eq. (2.33)	6931(40)	Refs. [2–7]
HVP NLO ( $e^+e^-$ )	Section 2.3.8	Eq. (2.34)	−98.3(7)	Ref. [7]
HVP NNLO ( $e^+e^-$ )	Section 2.3.8	Eq. (2.35)	12.4(1)	Ref. [8]
HVP LO (lattice, <i>udsc</i> )	Section 3.5.1	Eq. (3.49)	7116(184)	Refs. [9–17]
HLbL (phenomenology)	Section 4.9.4	Eq. (4.92)	92(19)	Refs. [18–30]
HLbL NLO (phenomenology)	Section 4.8	Eq. (4.91)	2(1)	Ref. [31]
HLbL (lattice, <i>uds</i> )	Section 5.7	Eq. (5.49)	79(35)	Ref. [32]
HLbL (phenomenology + lattice)	Section 8	Eq. (8.10)	90(17)	Refs. [18–30,32]
QED	Section 6.5	Eq. (6.30)	116 584 718.931(104)	Refs. [33,34]
Electroweak	Section 7.4	Eq. (7.16)	153.6(1.0)	Refs. [35,36]
HVP ( $e^+e^-$ , LO + NLO + NNLO)	Section 8	Eq. (8.5)	6845(40)	Refs. [2–8]
HLbL (phenomenology + lattice + NLO)	Section 8	Eq. (8.11)	92(18)	Refs. [18–32]
Total SM Value	Section 8	Eq. (8.12)	116 591 810(43)	Refs. [2–8,18–24,31–36]
Difference: $\Delta a_\mu := a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$	Section 8	Eq. (8.14)	279(76)	

# Muonic Atom Spectroscopy Theory Summaries — MASTS

## Working groups, possible divisions

1.  $\mu\text{H}, \mu\text{D}, \dots, \mu\text{X}, \text{Mu}(?)$
2. *Lamb shift, fs, hfs*
3. *QED, QCD = (lattice, EFTs, data-driven)*

Main outcome: *full SM result!*

## The 1st workshop:

*Satellite to “Nucleon Structure at Low Q”, Crete, May 2022*

*Dedicated MITP workshop in 2024?*

