

A McStas Simulation Framework for Nested Mirror Optics *Method and Applications*

Workshop on Neutron Focusing Optics – NFO

Richard Wagner, ILL - 02.03.2023

PSI, Villigen



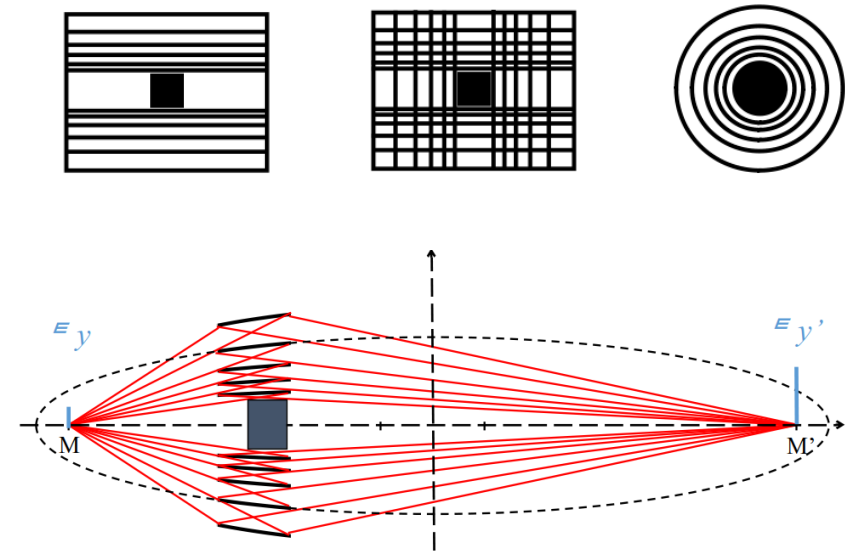
HighNess

Outline

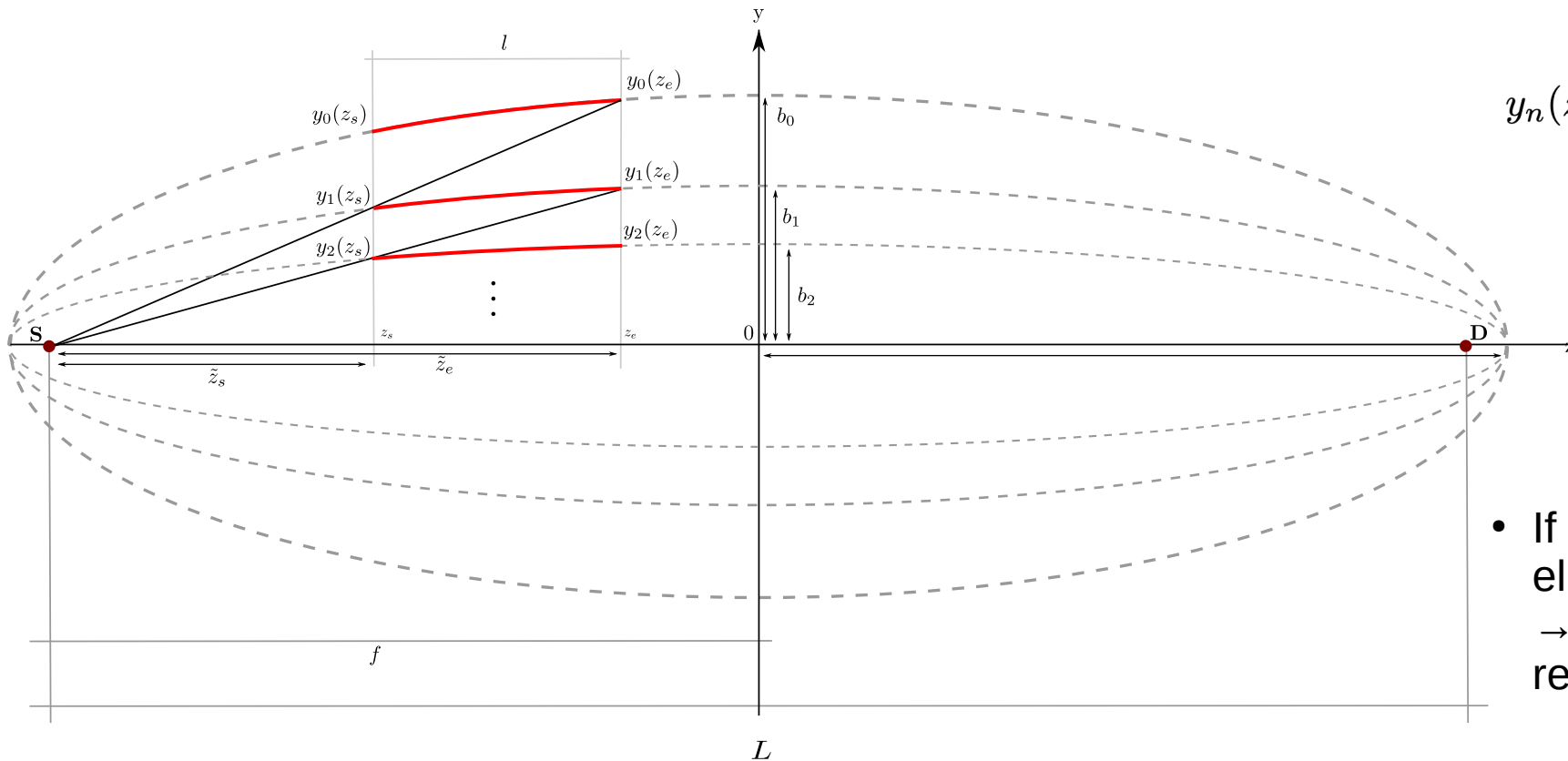
- Nested Mirror Optics
- McStas Components
- Applications
 - NNBAR
 - In-Beam UCN Source

Nested Mirror Optics - NMO

- Elliptical guide: possible architecture to transport neutrons diverging from a source to a detector (sample)
- Elliptical shaped mirror - has the property to reflect a beam that emanates from one of its focal points directly to the other one
- The layers of several guides can be nested to build up a spatial tight optical component
→ Focusing reflector in (compact) nested arrangement
- Elliptical mirrors in planar or cylindrical arrangement possible
- Verify & quantify performance of these optical systems in McStas Simulations



Nested optic Construction principle



$$y_n(z) = \sqrt{\left(1 - \frac{z^2}{f^2 + b_n^2}\right)} \cdot b_n$$

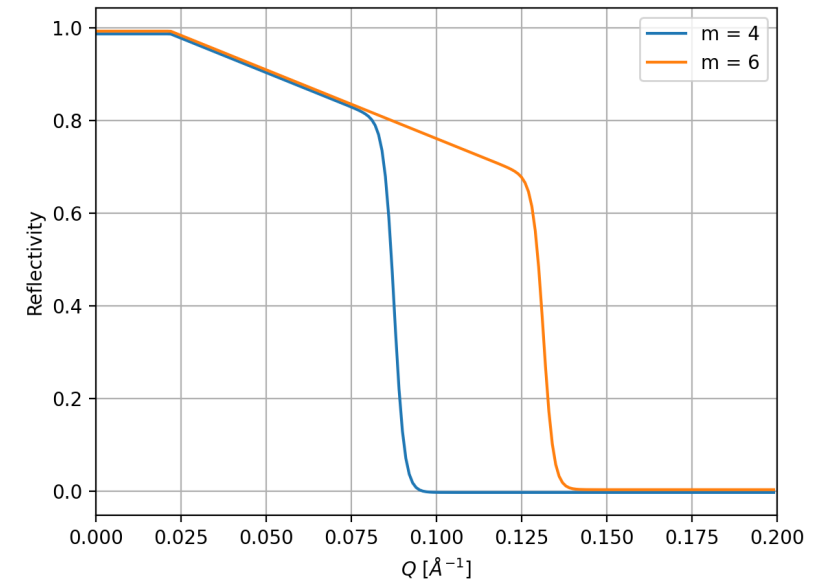
$$y_n(z_s) = \frac{\tilde{z}_s}{\tilde{z}_e} y_{n-1}(z_e)$$

- If the outer layer of a nested elliptical guide is given,
→ inner layers can be recursively constructed

- *Guide_anyshape.instr*
- Constitutes a reflecting surface of arbitrary shape defined by an OFF-File
- Reflectivity parametrized by R_0, Q_c, α, W, m

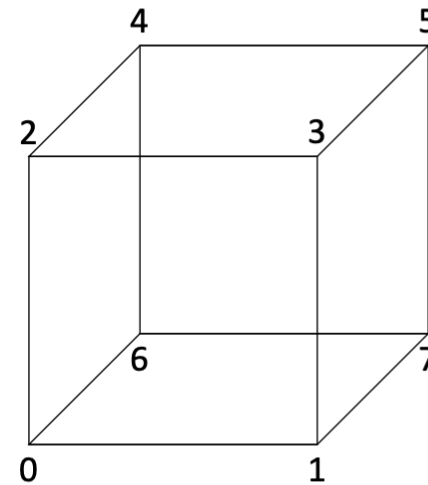
Table 1: Input parameters for the *Guide_anyshape* component

| Parameter | Description |
|-----------|---|
| geometry | name of the OFF-file that defines the geometry of the optic |
| m | m-value of the optics material (zero is completely absorbing) |



OFF(object file format)-Files

```
1 OFF
2 # A cube of size 1x1x1 centred
3 8 6 0
4 -0.500000 -0.500000 0.500000
5 0.500000 -0.500000 0.500000
6 -0.500000 0.500000 0.500000
7 0.500000 0.500000 0.500000
8 -0.500000 0.500000 -0.500000
9 0.500000 0.500000 -0.500000
10 -0.500000 -0.500000 -0.500000
11 0.500000 -0.500000 -0.500000
12 4 0 1 3 2
13 4 2 3 5 4
14 4 4 5 7 6
15 4 6 7 1 0
16 4 1 7 5 3
17 4 6 0 2 4
18
```



Example of an OFF-File describing a cube of side length one and its representation

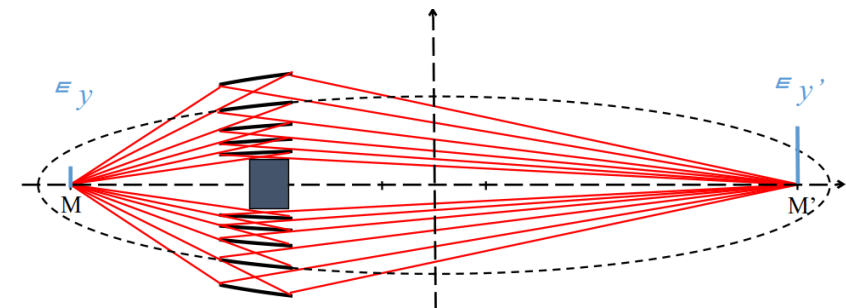
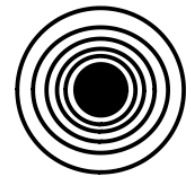
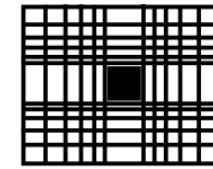
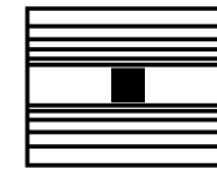
NMO - component creation library

- Collection of Python functions for OFF File Generation of Nested Mirror Optics

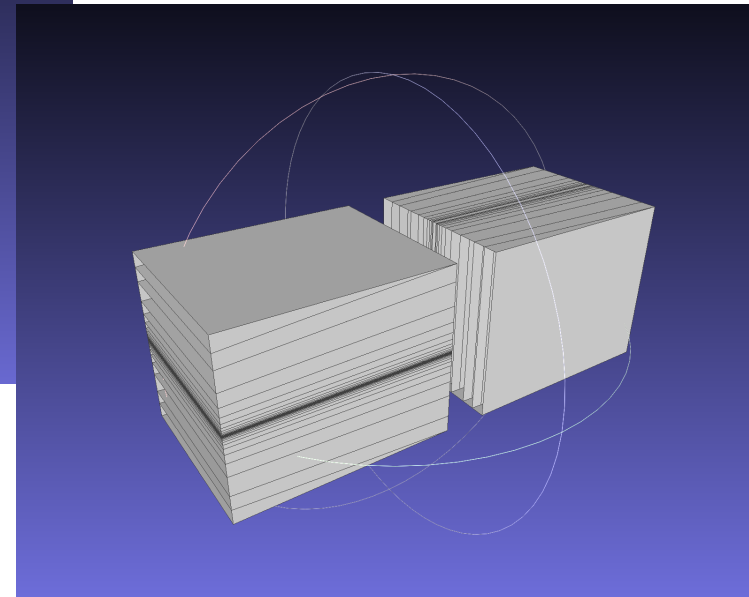
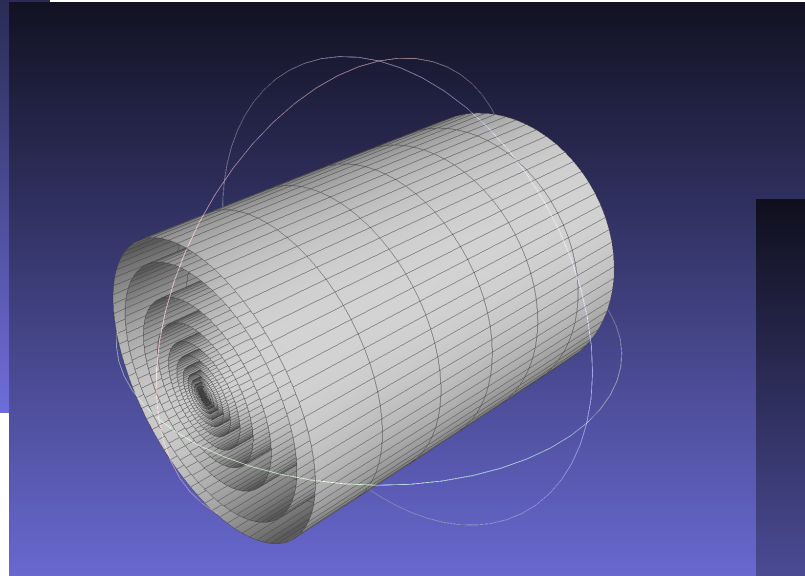
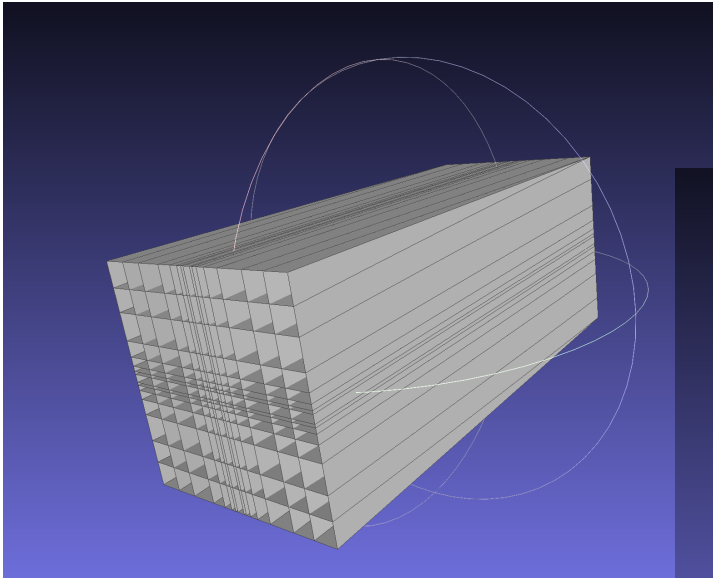
- Example

Table 5: Input parameters for the createToroidalNestedOFFwArray() function

| Parameter | Description |
|----------------|---|
| L | distance between focal points of the ellipses |
| b_array | array containing the minor axes of the nested ellipses |
| z_start | starting point of the optic, relative to the focal point |
| l | length of the optic |
| nb_segments | number of segments by which the ellipses are approximated |
| nb_segments_T | number of segments the circumferences of the toroidal sections are approximated with |
| filename | name of the generated OFF-file |
| opticHalfWidth | limit for extent of the optic. The area the optic can occupy is between \pm opticHalfWidth |
| bBoundingBox | outer level is surrounded by a bounding box (true/false) |



Example NMOs: Elliptical Guides



Example NMOs: Wolter optics (type I)

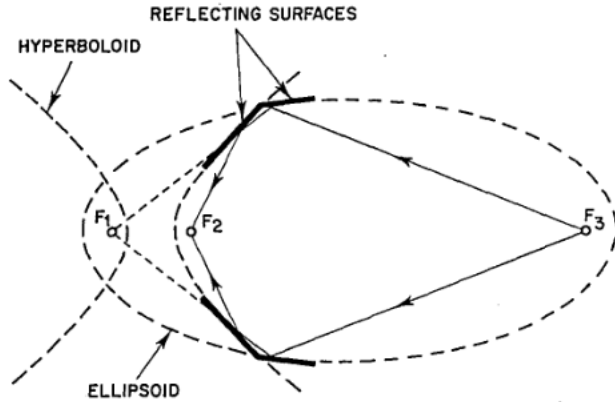
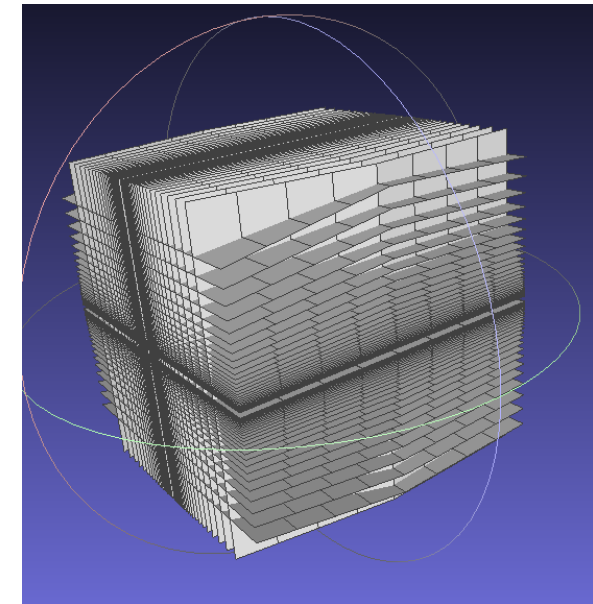
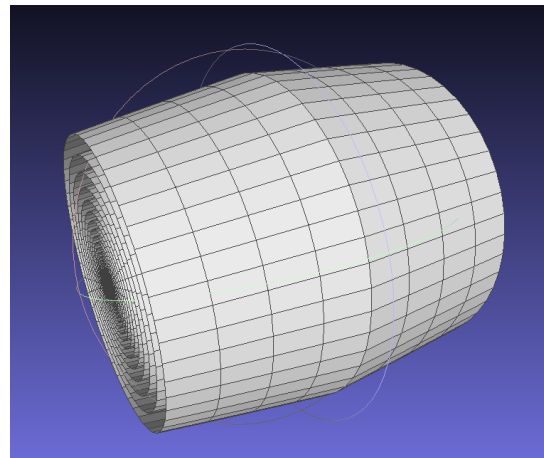
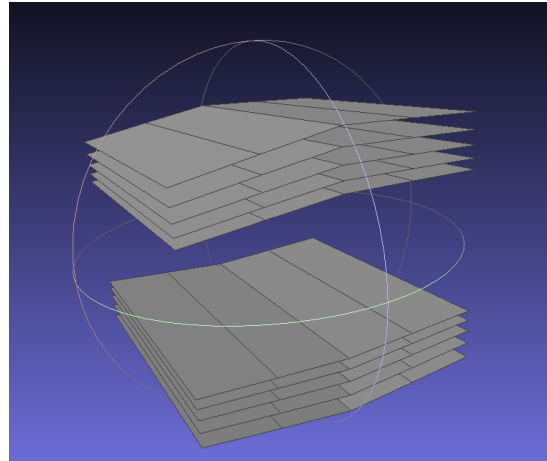


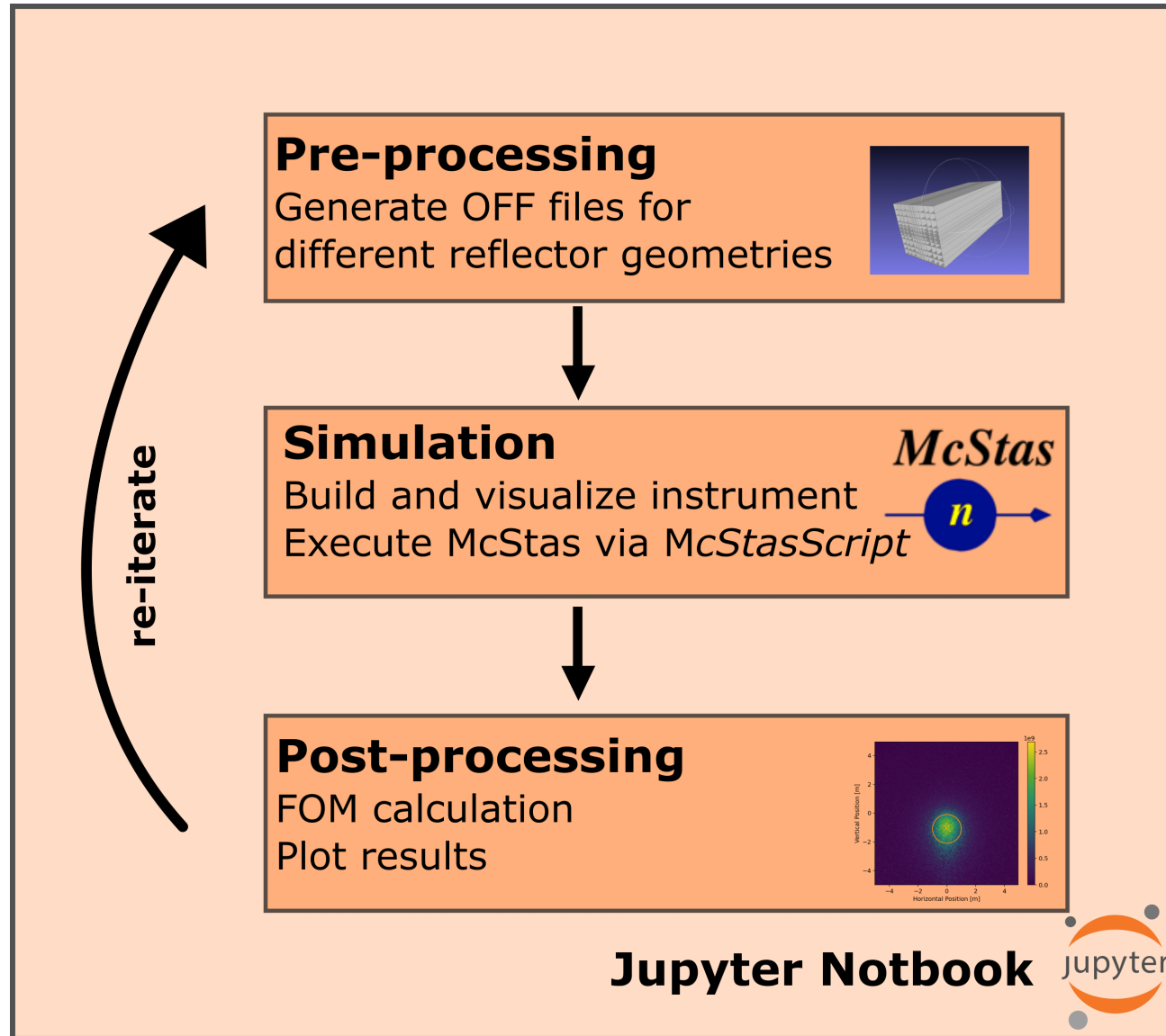
Fig. 1. Schematic representation of the ellipsoid-hyperboloid mirror. A source at one focus of the ellipsoid (F_3) is imaged at the focus of the hyperboloid (F_2) after two reflections.

From: R. C. Chase and J. K. Silk,
Appl. Opt. 14, 2096-2098 (1975)

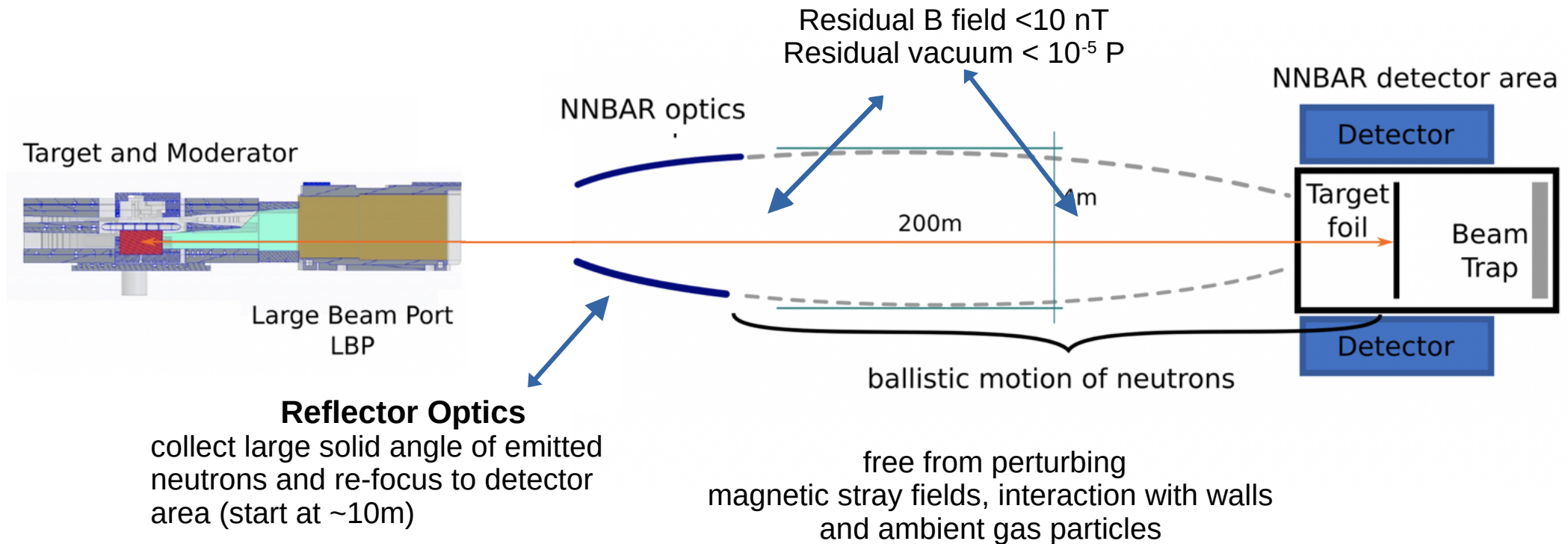
- Hyperboloid and ellipsoid segment
- Design fulfills the Abbé sine condition in good approximation
- Produce sharp and aberration free images.



- Library extended to create Wolter NMOs



Application Example NNBAR Experiment at ESS



Transition probability

for quasi free condition

$$P_{n\bar{n}} = \left(\frac{t}{\tau} \right)^2$$

t ... uninterrupted flight time

τ ... free oscillation time

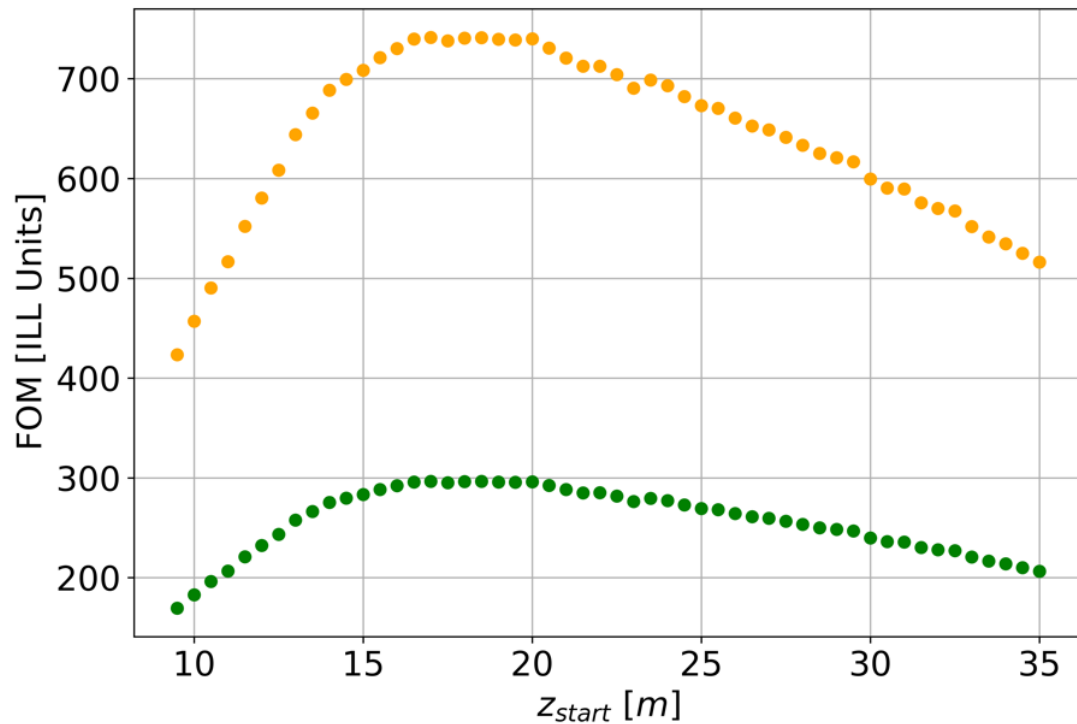
Figure of Merit - FOM

$$FOM = \sum_i \overbrace{N_i}^{\text{neutrons}} * \overbrace{t_i^2}^{\text{(uninterrupted) flight time}} / \underbrace{(4 \times 10^9)}_{\text{normalization factor}}$$

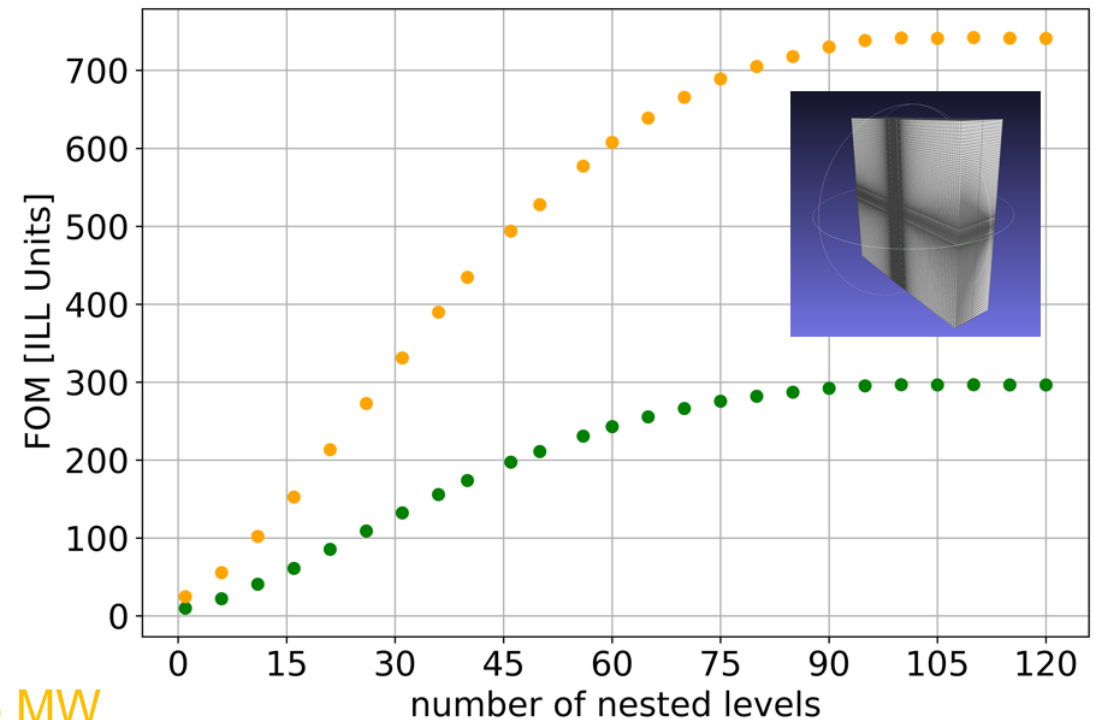
HighNess

Application Example NNBAR Experiment at ESS

Find the optimum optic by varying parameters
(e.g. starting point, # of nested levels, ...)
Example: Simulations for a 1m long nested Reflector



5 MW
2 MW

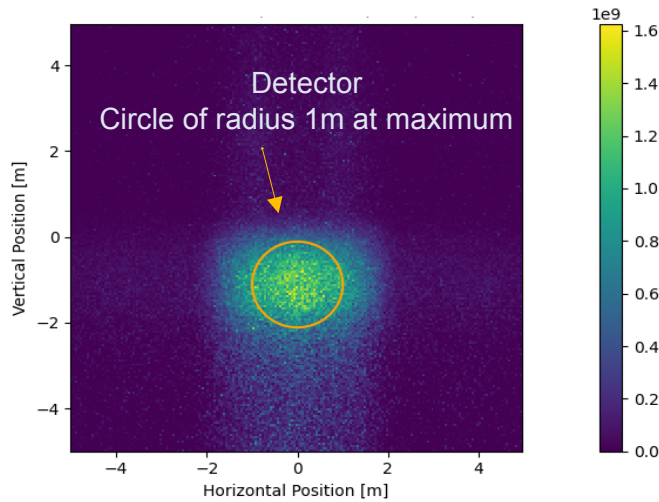


HighNess

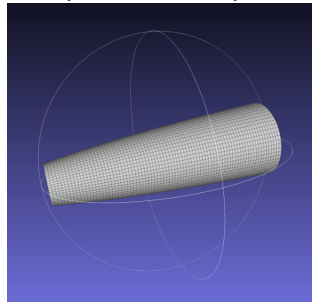
Application Example

NNBAR Experiment at ESS

Example: Simulations for a 10m Nested Reflector

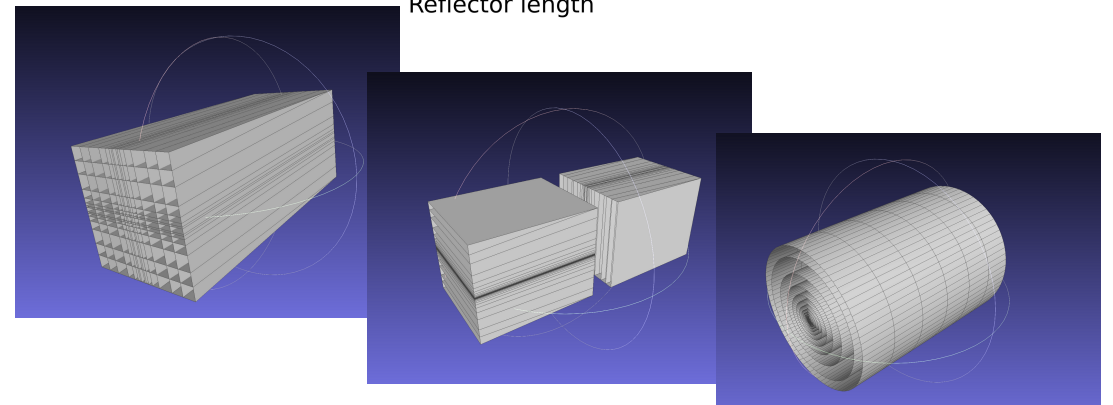
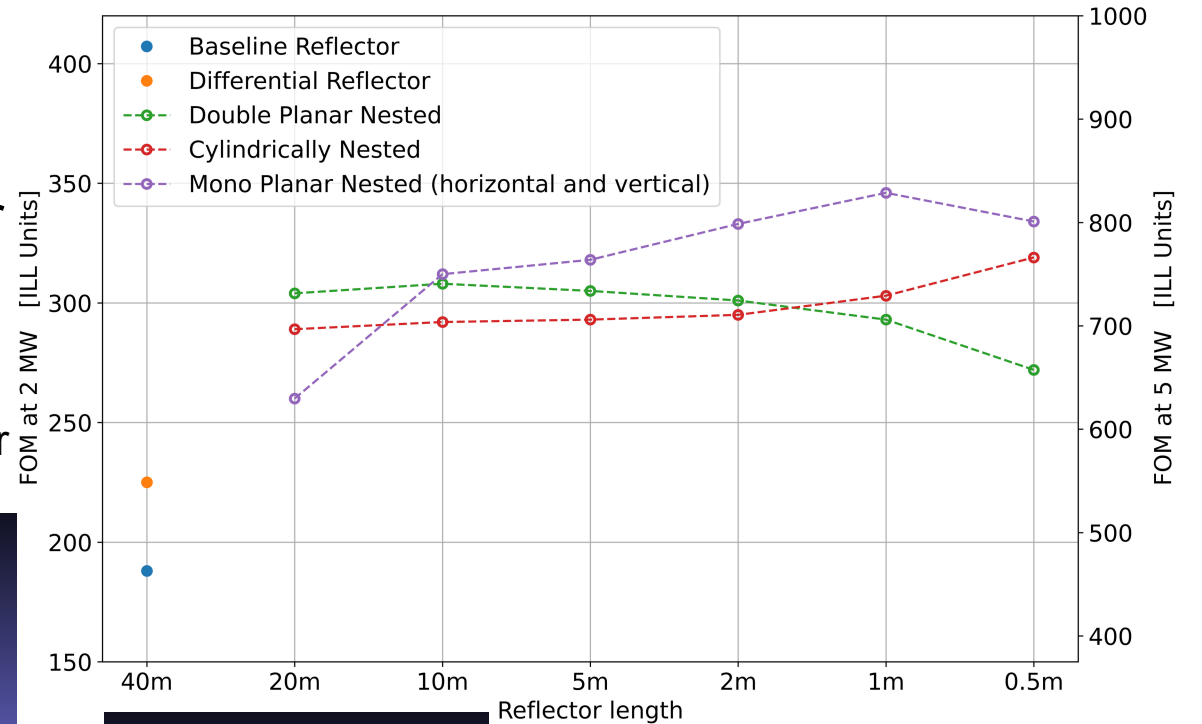


40m single layer (baseline)

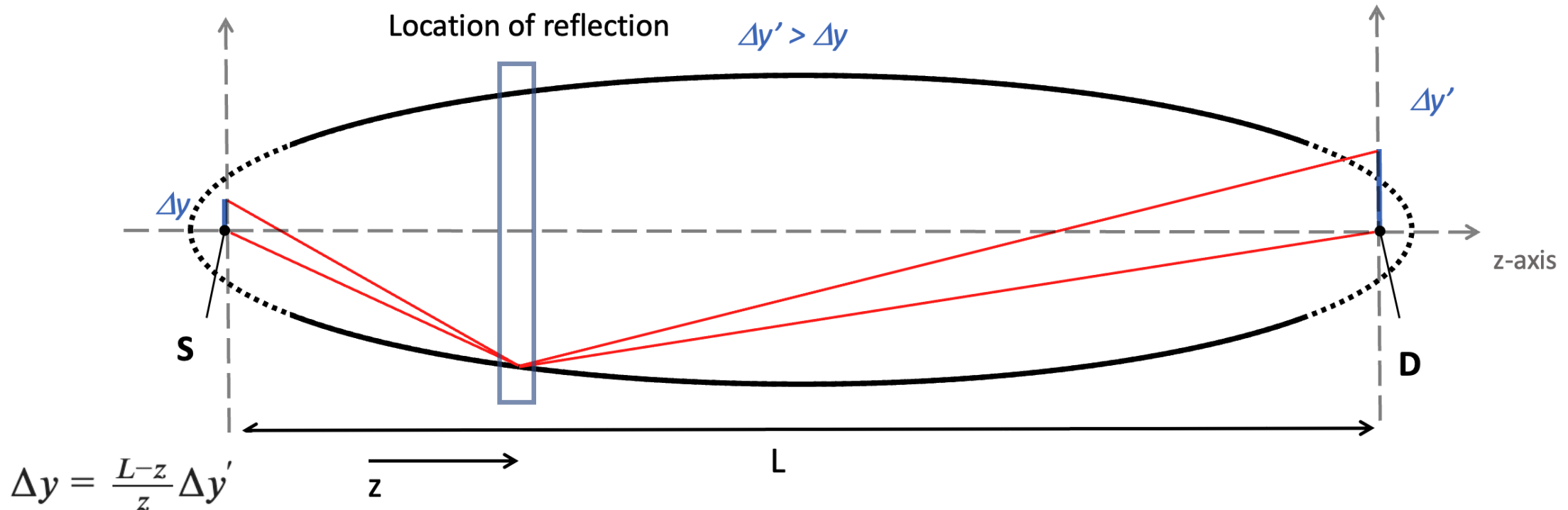


FOM: 308 (nested levels=13, 2 MW)

Collected results for different reflector systems



Off-Axis magnification for an elliptical reflector



$$M = \Delta y / \Delta y' = \frac{L-z}{z}$$

Examples:

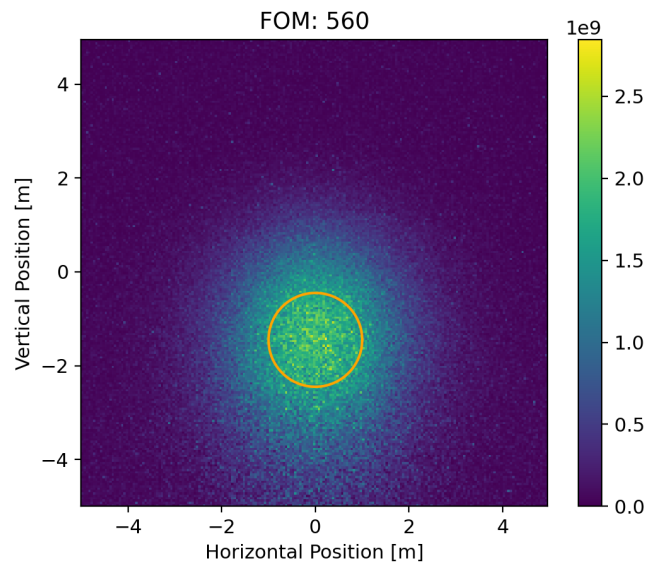
$$L = 200, z = 10 \rightarrow M = 19$$

$$L = 200, z = 20 \rightarrow M = 9$$

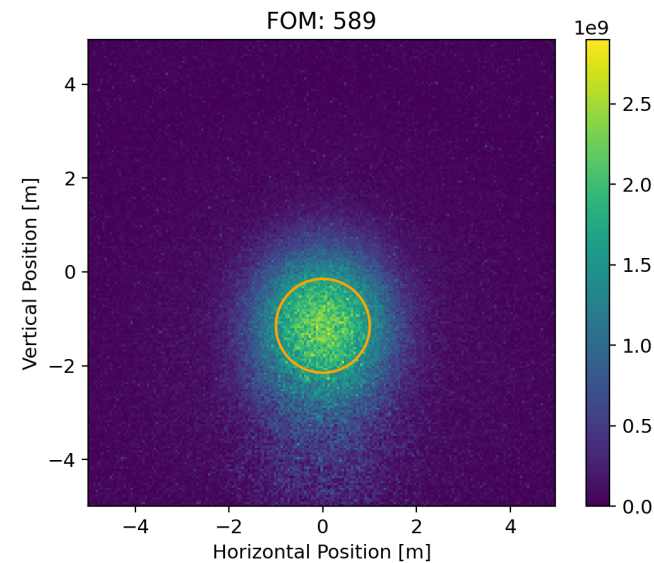
$$L = 200, z = 100 \rightarrow M = 1$$

NNBAR: cylindrical, 10m, 4 levels (5MW) Start of reflector: 10m, 15m, 20m

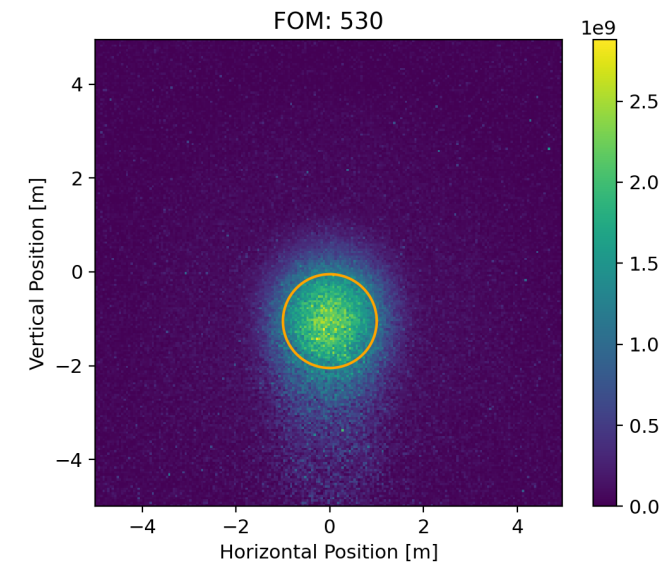
10m



15m



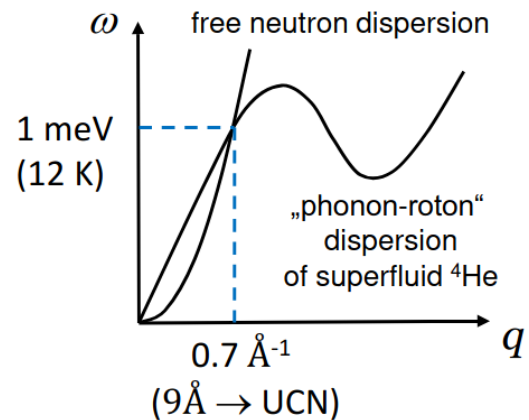
20m



Position of optic has to fulfill trade off between
focusing and covering of solid angle

Application Example In-Beam UCN Source ESS

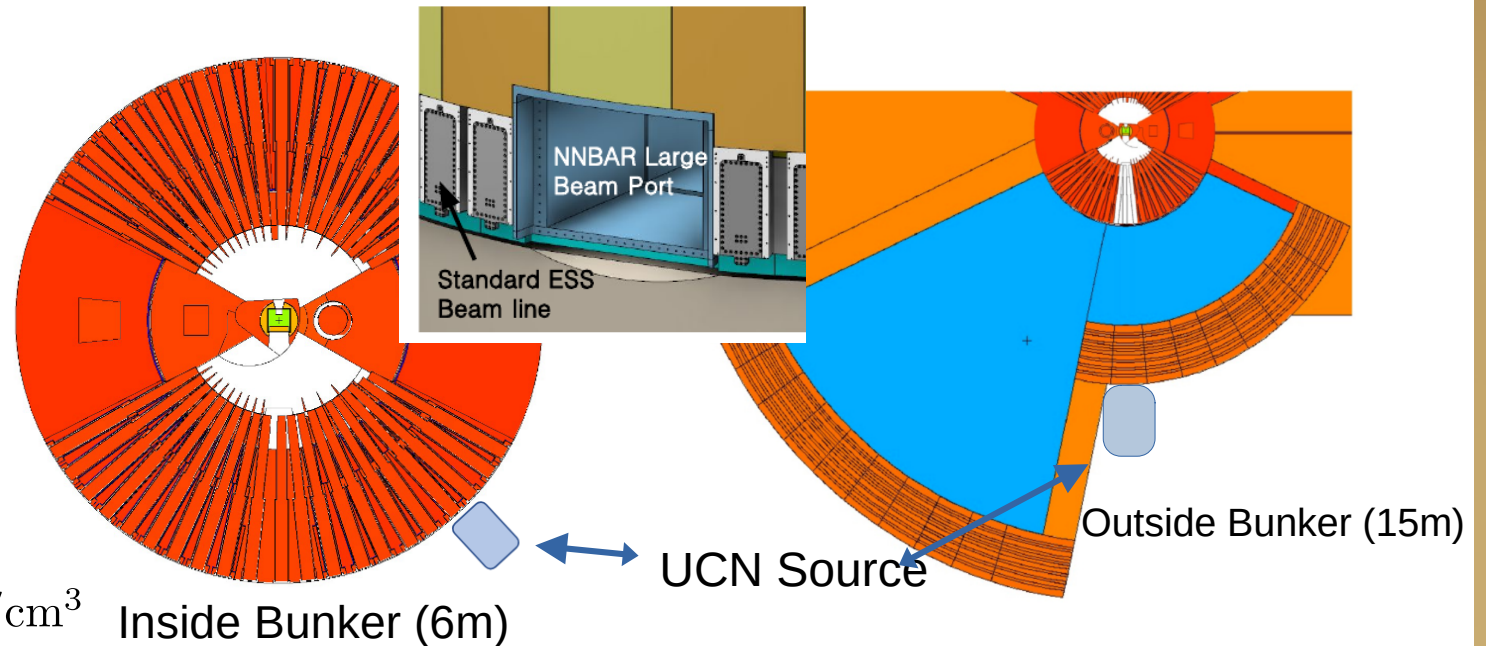
Ultra - cold neutron UCN production in superfluid Helium



Production Rate:

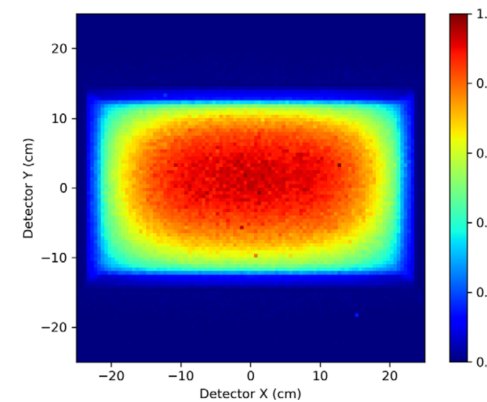
$$P(E_{\text{UCN}}) = \frac{d\phi(E^*)}{dE} \cdot 1.44 \times 10^{-7} \text{ UCN/sec/cm}^3$$

9Å flux at source will convert to UCN flux

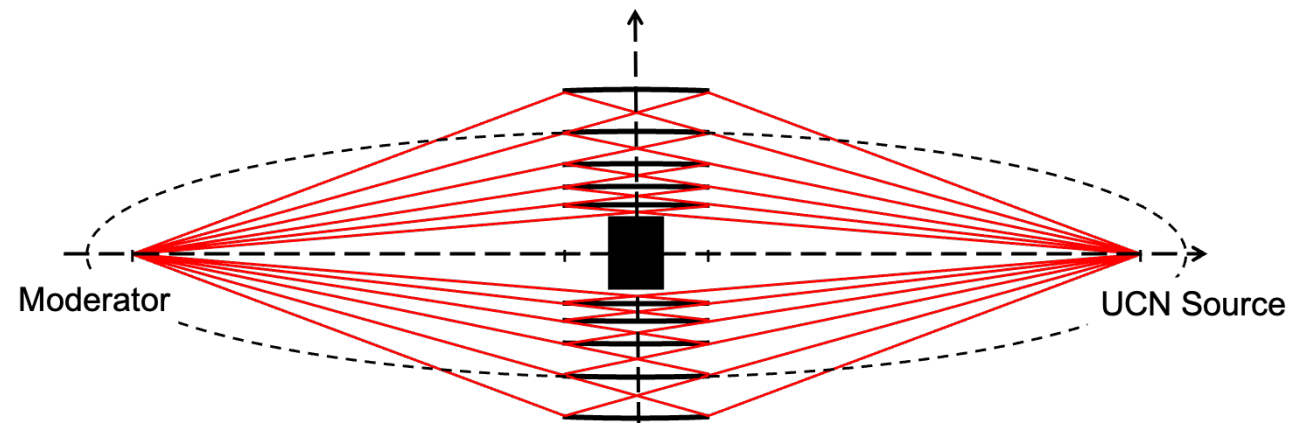


Application Example In-Beam UCN Source ESS

- Need a neutron delivery system with high brilliance transfer from moderator to UCN source, with largest technically possible solid angle
- Neutron imaging from the moderator to the UCN source via NMOs has been identified as possible solution



Intensity map (simulated) at the ESS LD2 moderator surface of neutrons with WL near 9 Å



In-beam superfluid-helium ultracold neutron source for the ESS

Oliver Zimmer^{a,*}, Thierry Bigault^a, Skyler Degenkolb^b, Christoph Herb^c, Thomas Neulinger^a, Nicola Rizzi^d, Valentina Santoro^d, Alan Takibayev^a, Richard Wagner^a and Luca Zanini^d

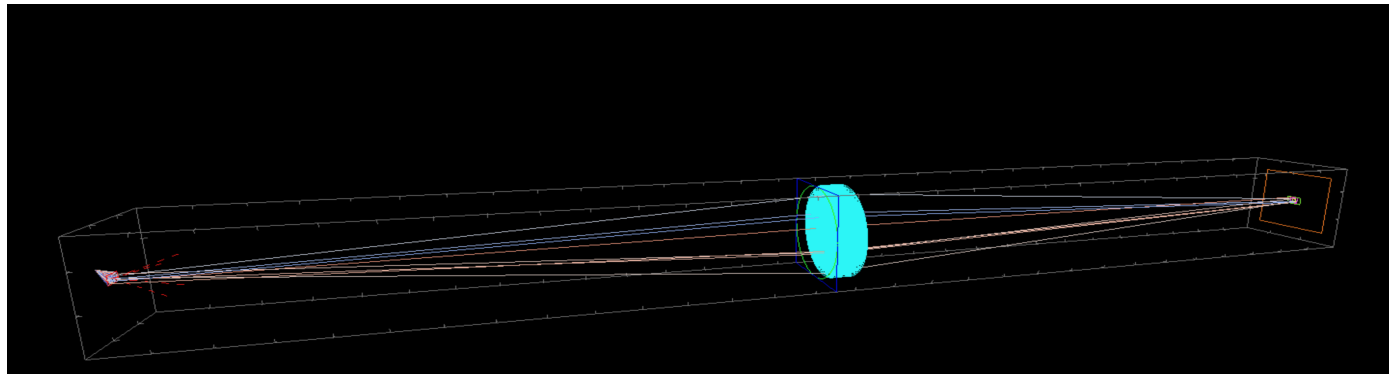
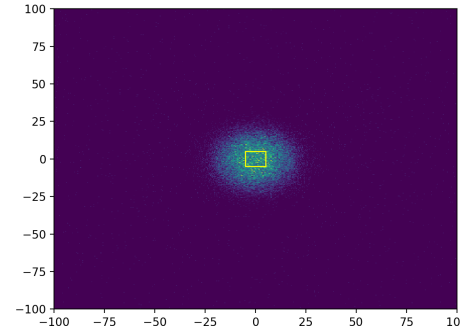
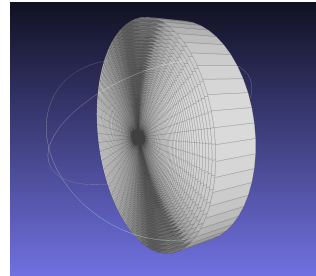
Journal of Neutron Research 24 (2022) 95–110 95
DOI 10.3233/JNR-220045



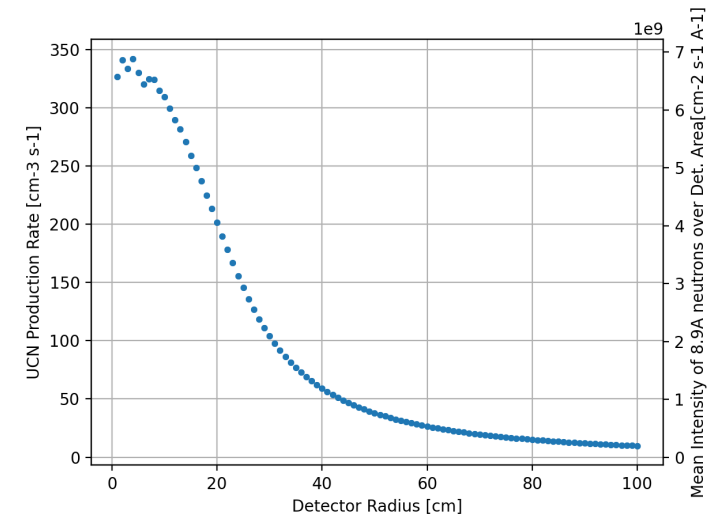
Application Example In-Beam UCN Source ESS

NMO at 15m:
length 0.5m, 119 levels

Distance Source-Detector
30m

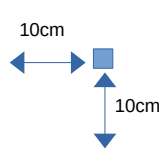


Production Rate

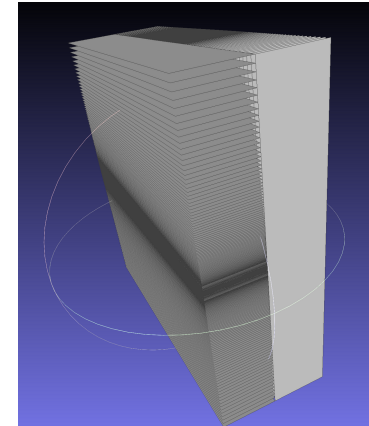
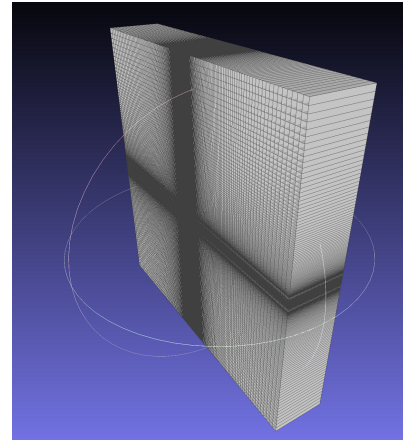


NMOs as (non)-imaging device

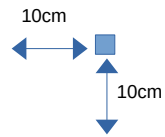
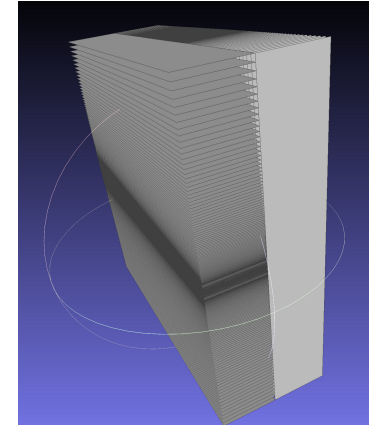
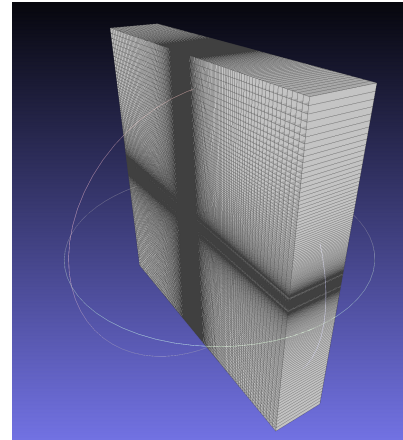
1 Double- or
2 Monoplanar
elliptical NMOs
at 15m
focal length 15m



off-axis "point" source

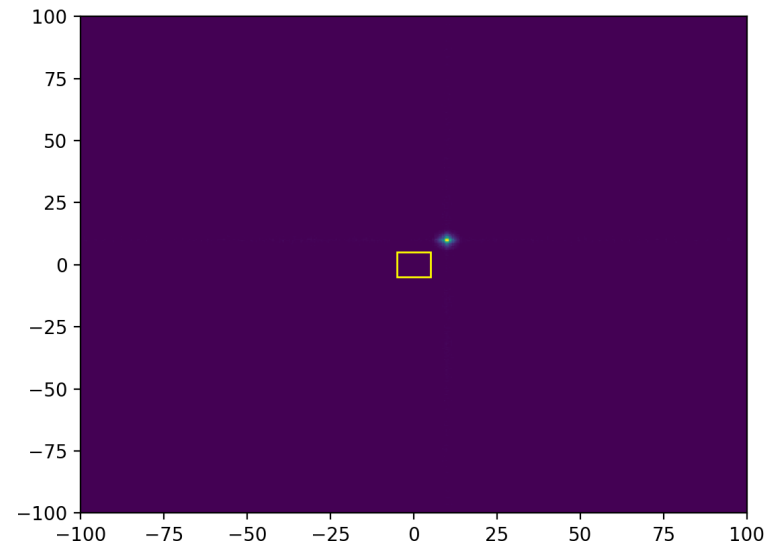


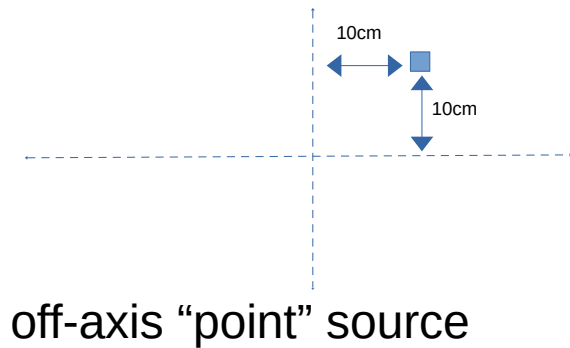
1 Double- or
2 Monoplanar
elliptical NMOs
at 15m
focal length 15m



off-axis “point” source

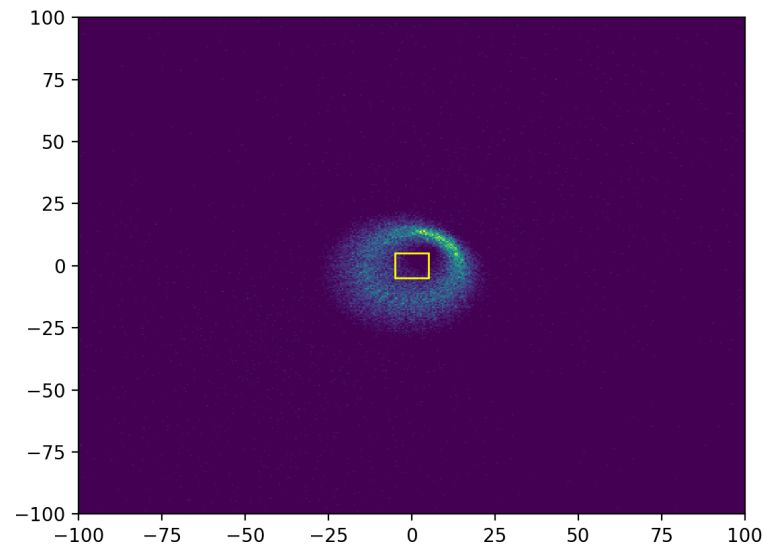
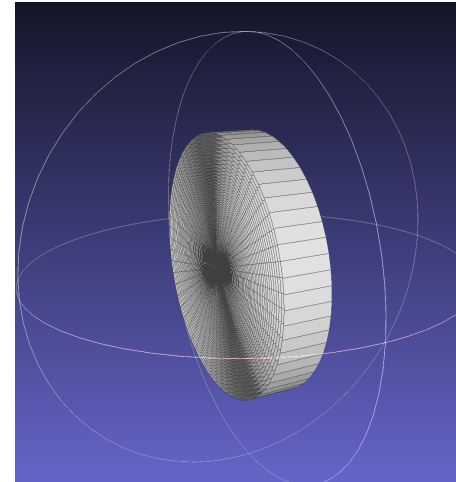
Detector at 30m



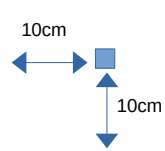
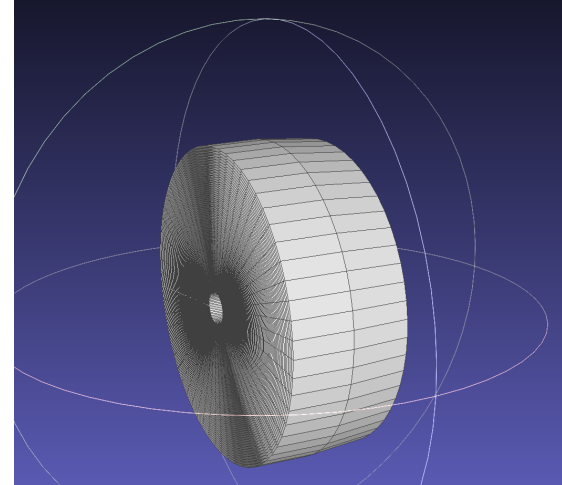


Toroidal (cylindrical)
elliptical NMO
at 15m
focal length 15m

Detector at 30m

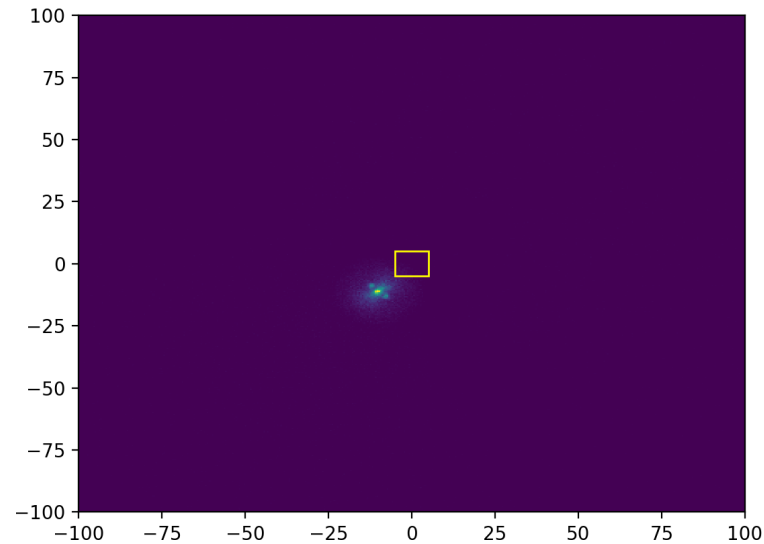


Wolter optic NMO
at $\sim 15\text{m}$
 $f_s = 14.9\text{m}$



off-axis "point" source

Detector at 30m



- Support nested layers with different m-values:
 - Guide_anyshape_r.instr
- Asymmetric NMOs: i.e. different half-axis arrays for upper and lower half
- Nested parabolic NMOs (stand-alone or as part of Wolter optic)
- Take into account losses:
 - Thickness of mirrors
 - Waviness, roughness of mirrors
 - Off-specular reflection



Thank you for your attention!

Credits: Jonathan Collin, Nyia Petkova, Gautier Daviau, Alexandra Karabasova,
Nicola Rizzi, Luca Zanini, Oliver Zimmer

