

muEDM in the landscape of storage ring EDM searches

– *LTPHD Seminar (26 September 2023)* –

Tim Hume, Muon Physics Group

Supervised by Dr. Philipp Schmidt-Wellenburg

ETH zürich

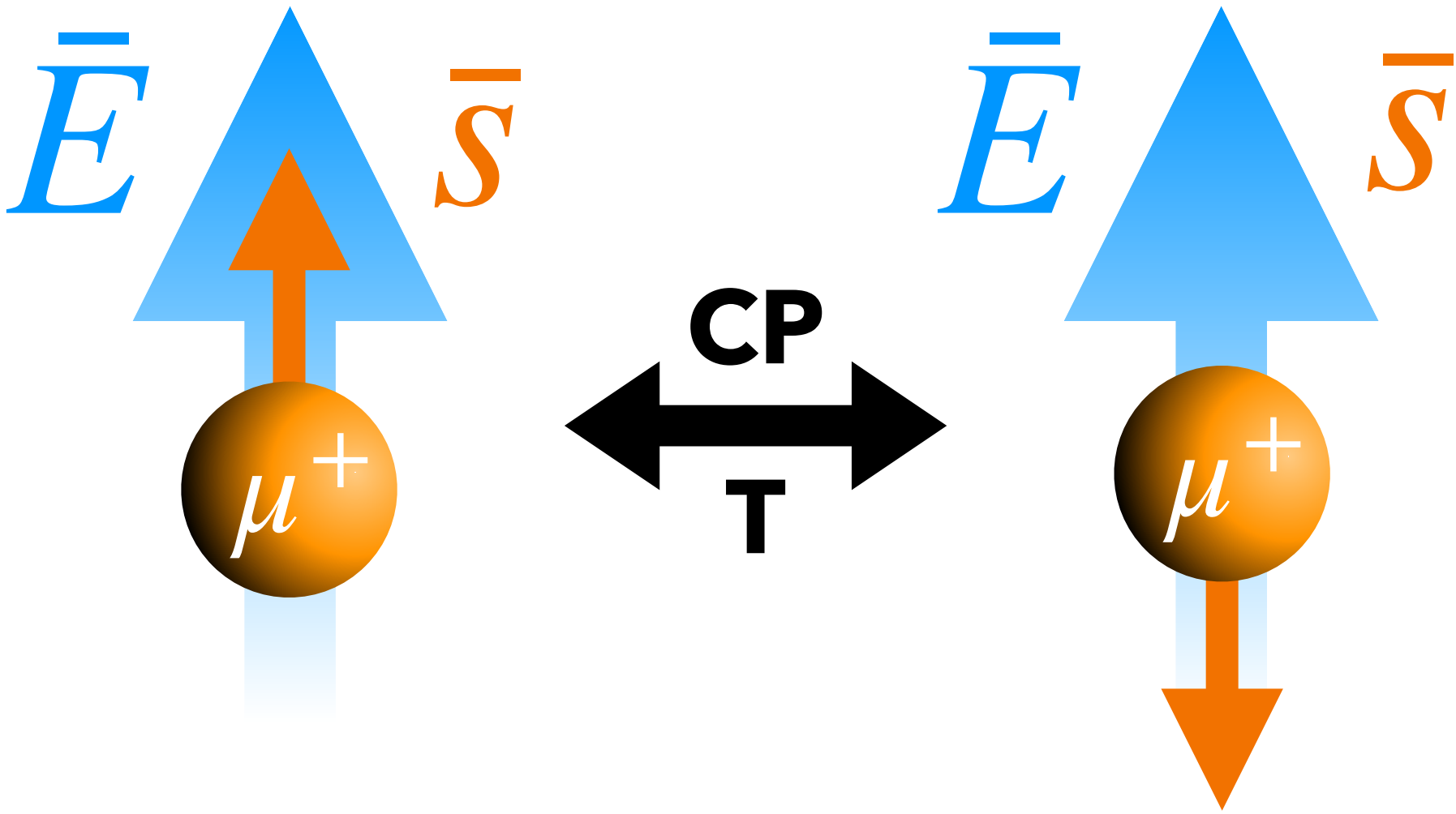
PAUL SCHERRER INSTITUT



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Muon Electric Dipole Moment

A permanent EDM requires T violation,
equivalently CP violation by the CPT Theorem.



$$H_{\mu}^{EDM} \stackrel{\beta \rightarrow 0}{\propto} d_{\mu} \bar{\sigma} \cdot \bar{E}$$

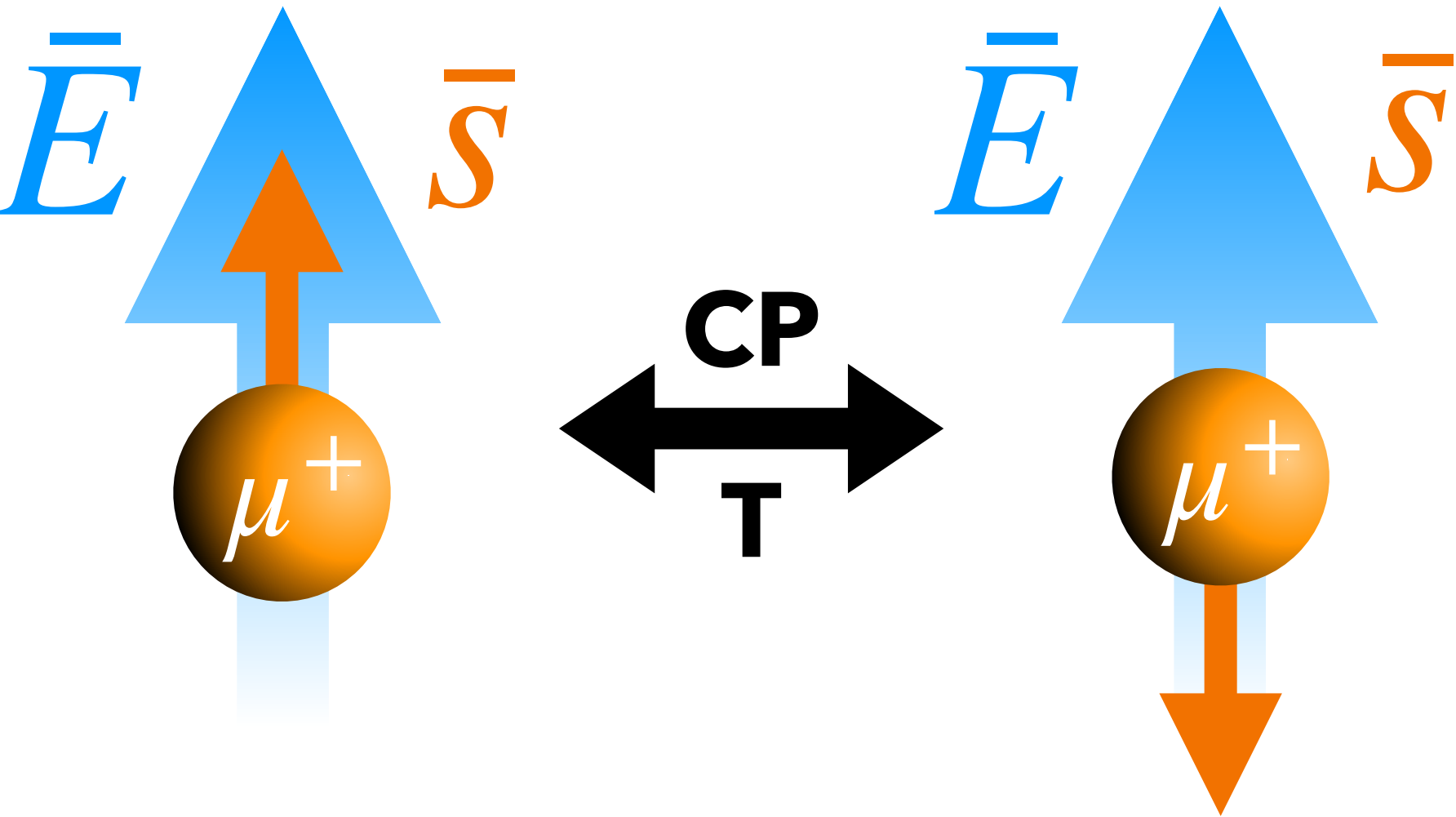
Hamiltonian EDM term is CP violating

SM Prediction: $d_{\mu}^{SM} = 1.4 \times 10^{-38} e \cdot \text{cm}$

(Yamaguchi & Yamanaka, 2020)

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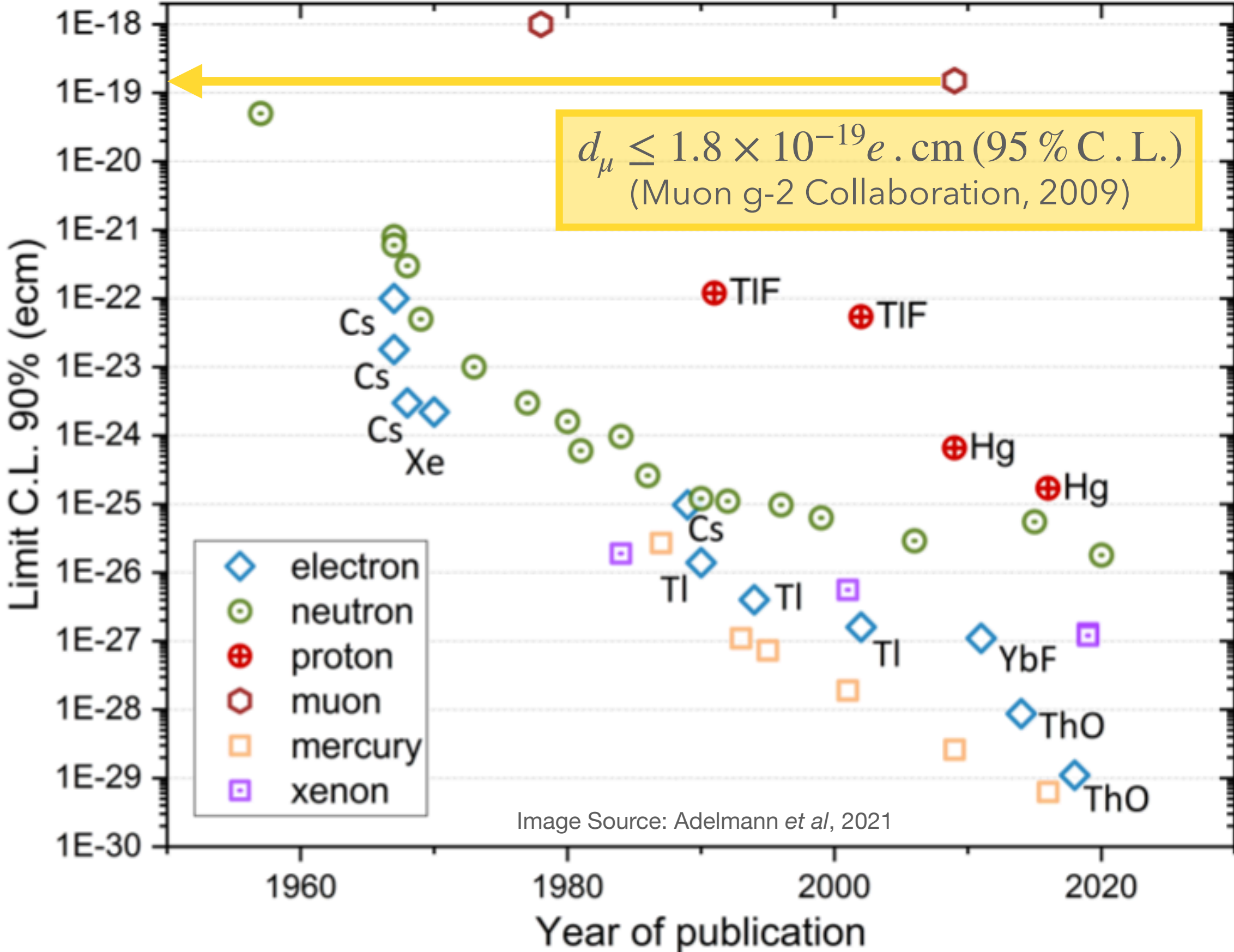
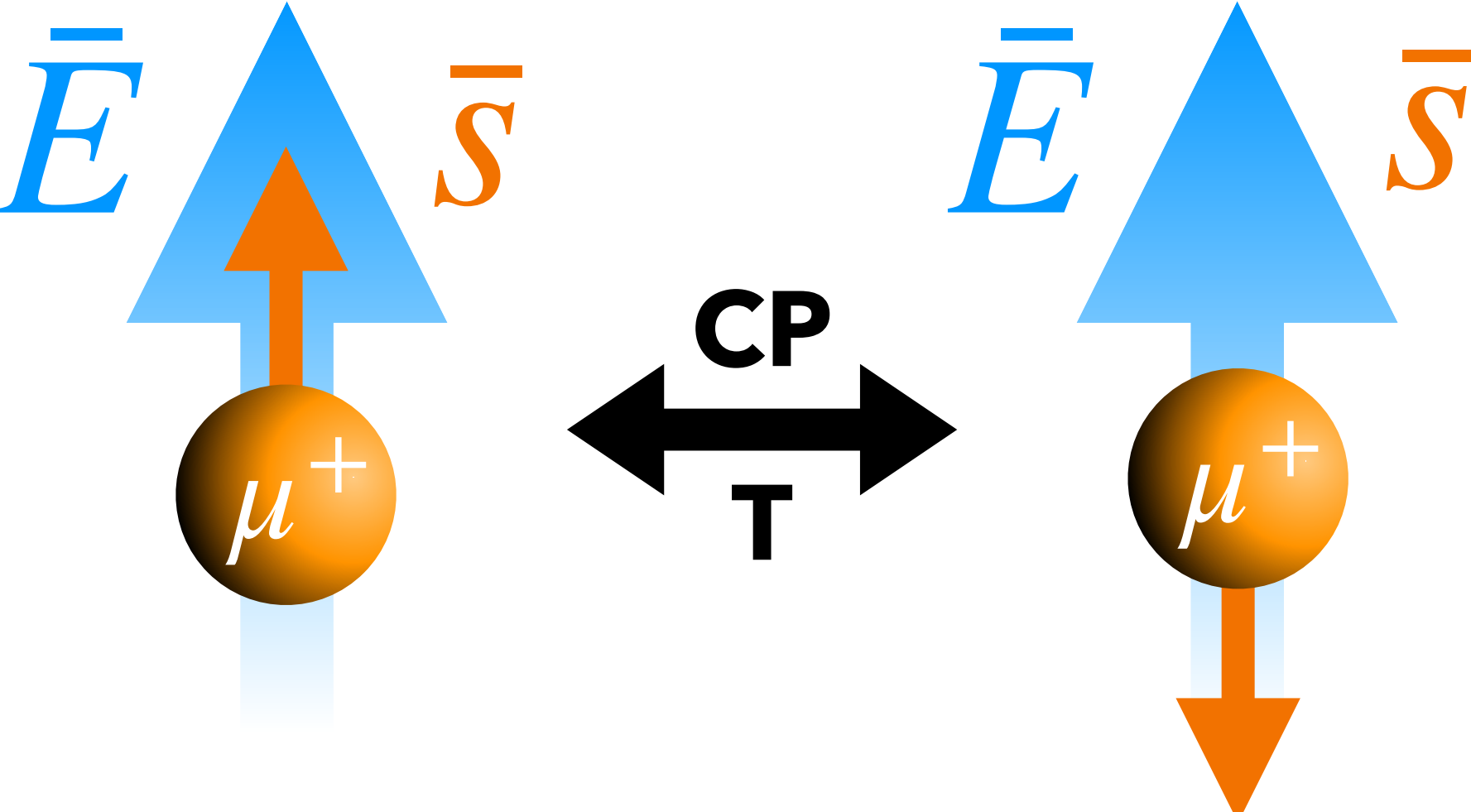


Image Source: Adelmann et al, 2021

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SM Prediction: $d_{\mu}^{SM} = 1.4 \times 10^{-38} e \cdot cm$

(Yamaguchi & Yamanaka, 2020)

$d_e \leq 4.1 \times 10^{-30} e \cdot cm$ LFU
⇒ $d_{\mu} \leq \frac{m_{\mu}}{m_e} d_e = 6.0 \times 10^{-28} e \cdot cm$?

(Roussy et al., 2023)

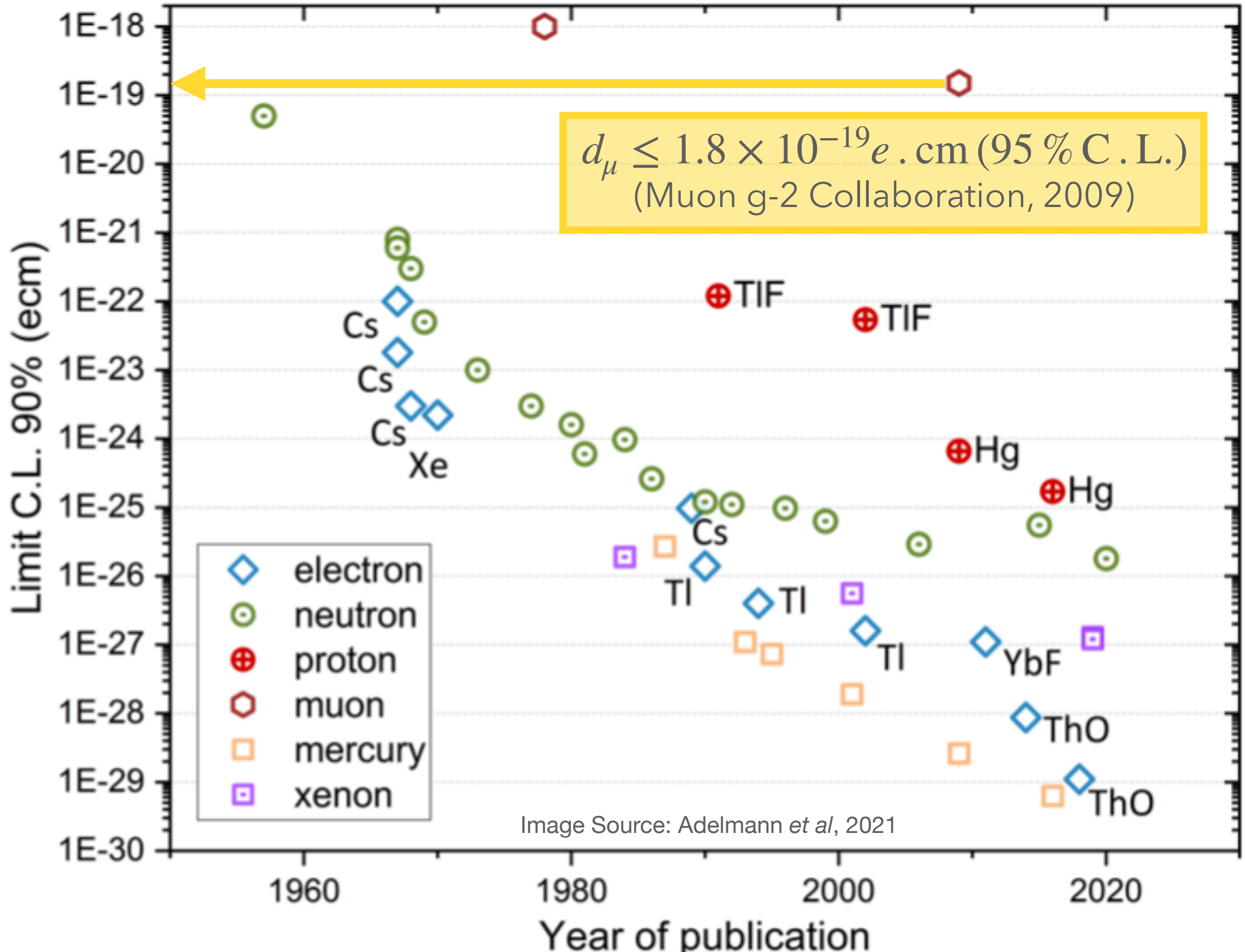
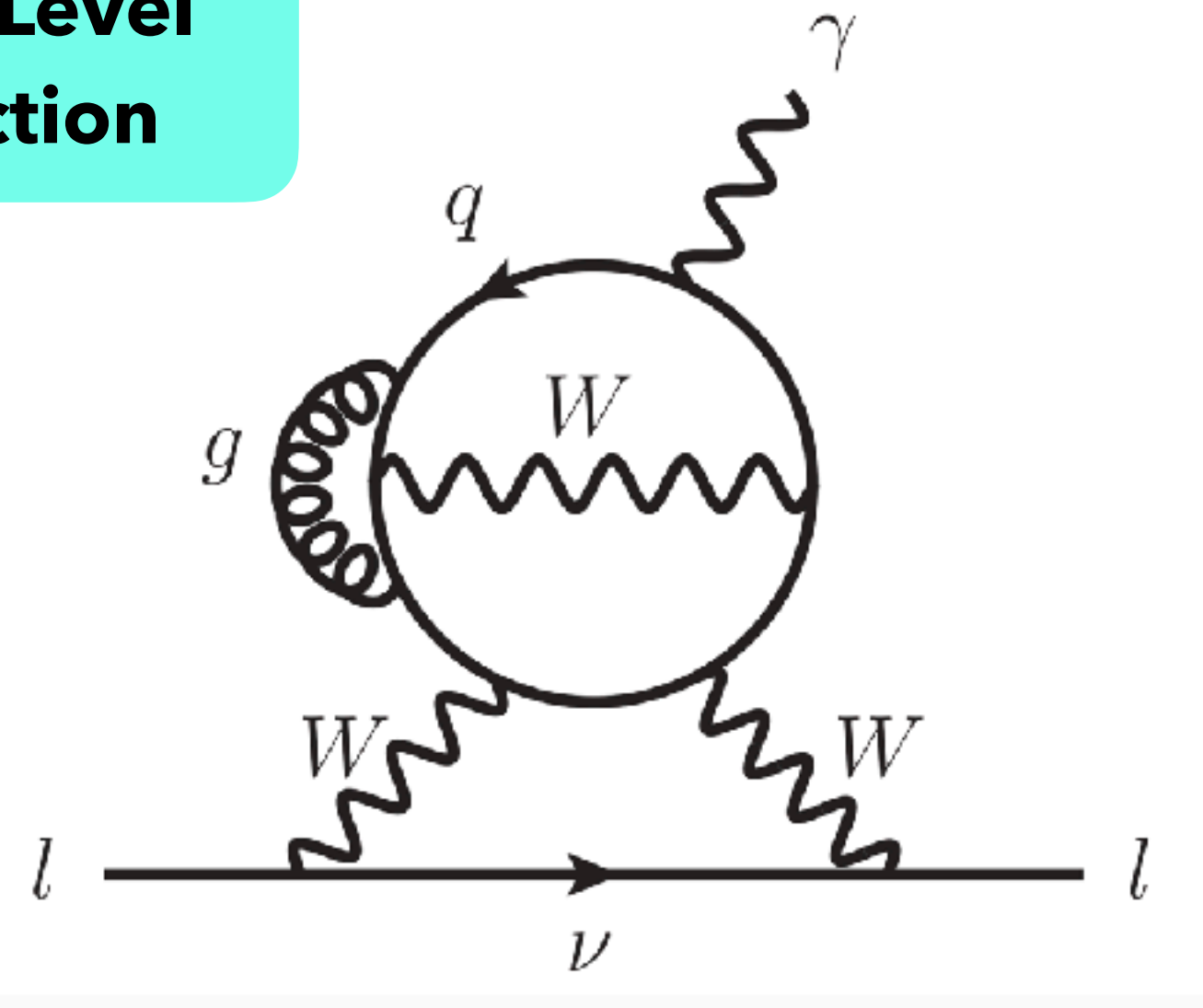


Image Source: Adelmann et al, 2021

Standard Model Prediction

The muon EDM is heavily suppressed in the SM.
 With current sensitivity $\sim 10^{19}$ larger, we essentially perform a "background-free" search.

Quark Level Prediction



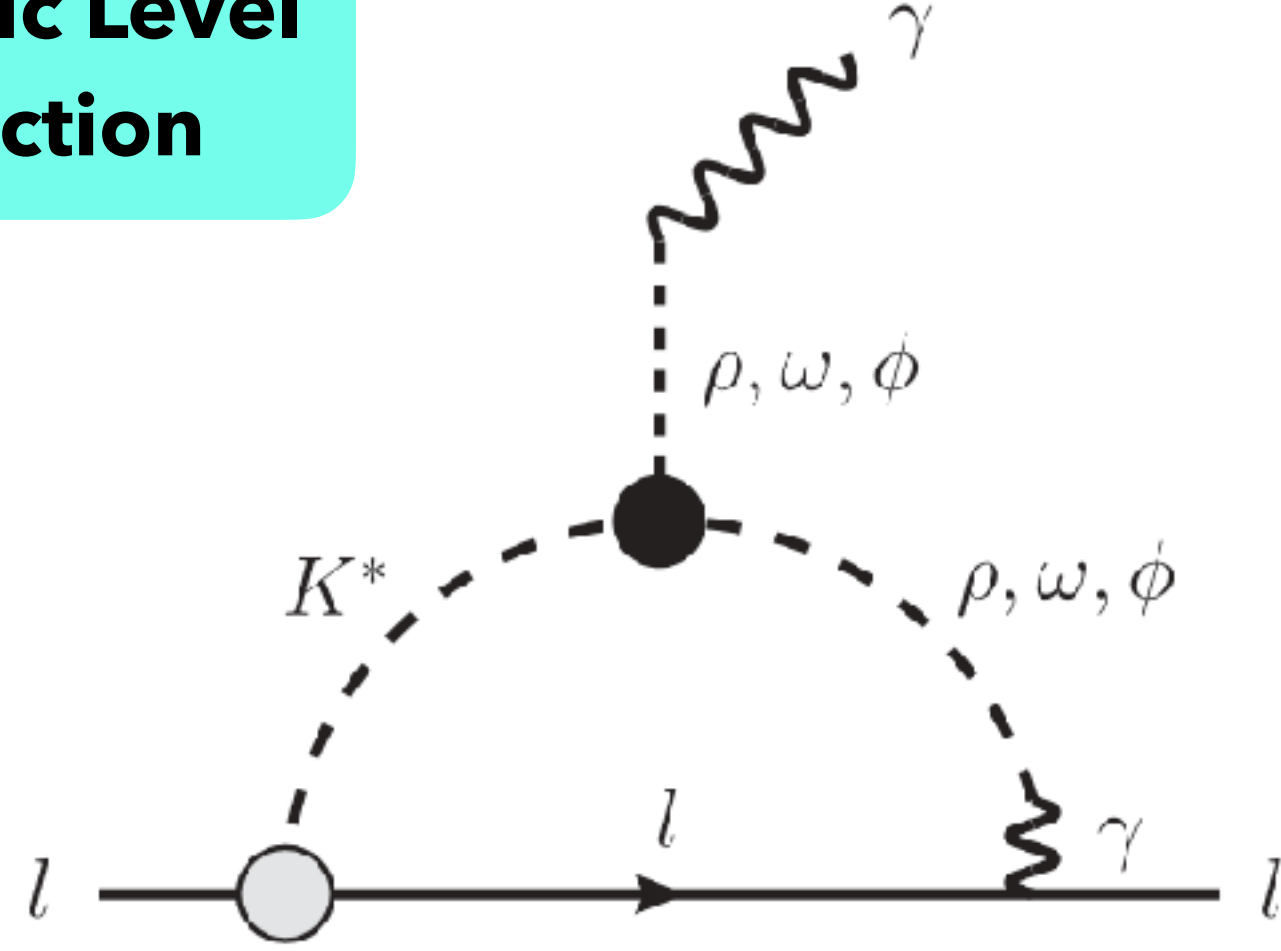
4-loop effect
 Cancellation through GIM Mechanism
 $d_\mu \sim \mathcal{O}(10^{-48} ecm)$

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(Received 4 June 2020; accepted 9 November 2020; published 10 December 2020)

Hadronic Level Prediction



1-loop effect
 Less cancellation due to different momenta
 $d_\mu = 1.4 \times 10^{-38} ecm$

Andreas Crivellin,¹ Martin Hoferichter,² and Philipp Schmidt-Wellenburg¹¹Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland²Institute for Nuclear Theory, University of Washington, Seattle, Washington 98195-1550, USA (Received 3 August 2018; published 7 December 2018)

Lepton Flavour Violation

A BSM model assuming Minimal Flavour Violation (MFV) leads to a scaling of the lepton EDMS with mass, as expected with Lepton Flavour Universality (LFU):

$$d_e \leq 4.1 \times 10^{-30} e \cdot \text{cm} \quad \begin{array}{c} \text{MFV} \\ \Rightarrow \end{array} \quad d_\mu \leq \frac{m_\mu}{m_e} d_e = 6.0 \times 10^{-28} e \cdot \text{cm}$$

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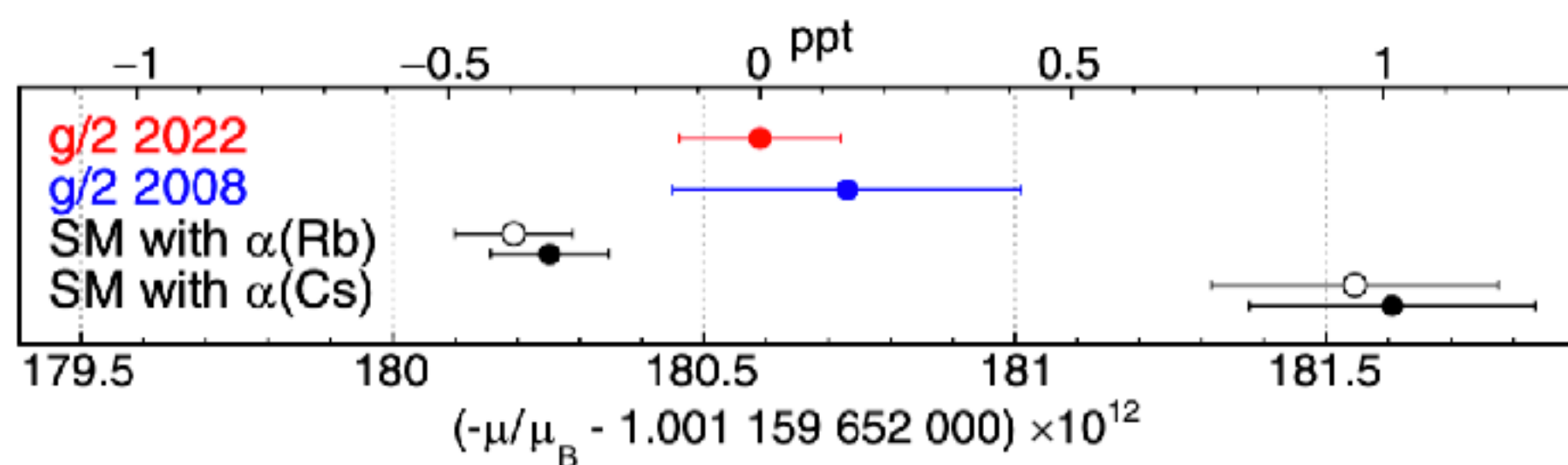
$$\text{Br}[\mu \rightarrow e\gamma] < 4.2 \times 10^{-13} \quad (90\% \text{ C.L.})$$

(MEG Collab., 2016)

Exp. Avg. 2023
BNL + FNAL (R1-3)

Th. Calculation 2020
Muon g-2 Theory Init.

5σ discrepancy



$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$$

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}}$$

Muon g-2 Anomaly

Electron g-2 Anomaly

MEG Limit

MFV insufficient

Given the constraints from MEG, and while the g-2 anomalies persist, a BSM theory addressing such anomalies should decouple e and μ sectors, accommodating a large muon EDM.

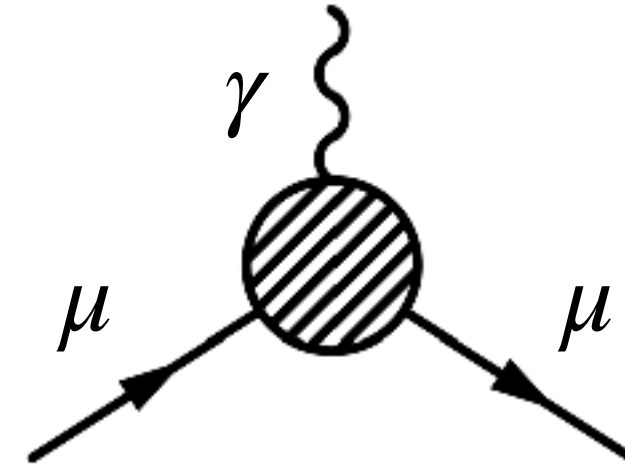
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Lepton Flavour Violation

The EFT includes terms for the magnetic ($\sigma_{\alpha\beta}$) and electric ($\sigma_{\alpha\beta}\gamma^5$) dipole moments:

$$H_{\text{eff}} = c_R^{\ell_f \ell_i} \bar{\ell}_f \sigma_{\alpha\beta} P_R \ell_i F^{\alpha\beta} + \text{h.c.}$$



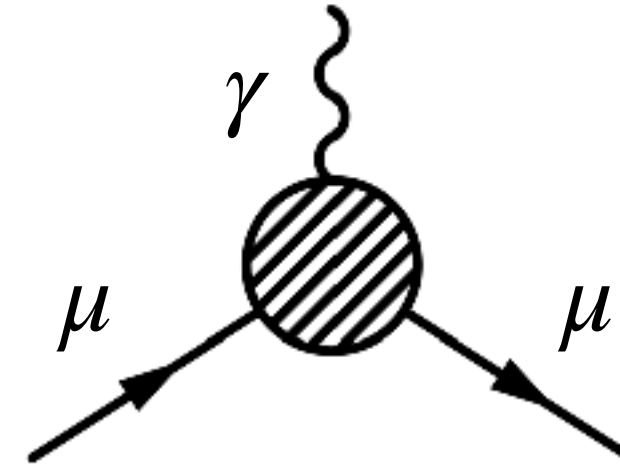
Expanding the terms ($P_R = (1 + \gamma^5)/2$) and reducing to low energy limit (dipole form factors as $q^2 \rightarrow 0$), gives:

$$a_{\mu}^{(\text{eff})} = \frac{4m_{\mu}}{e} \text{Re}(c_R^{\mu\mu}) \quad d_{\mu}^{(\text{eff})} = -2\text{Im}(c_R^{\mu\mu})$$

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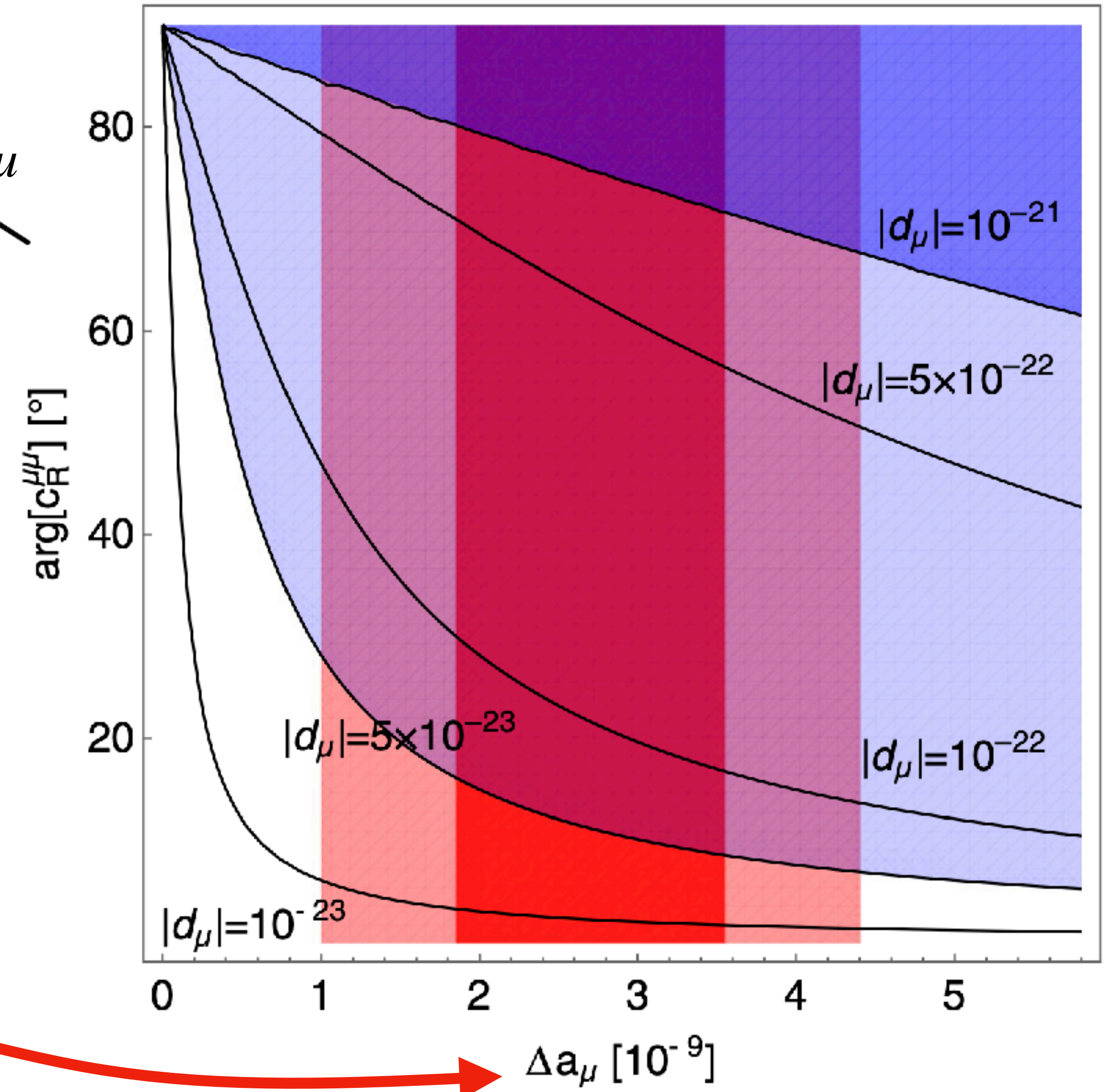


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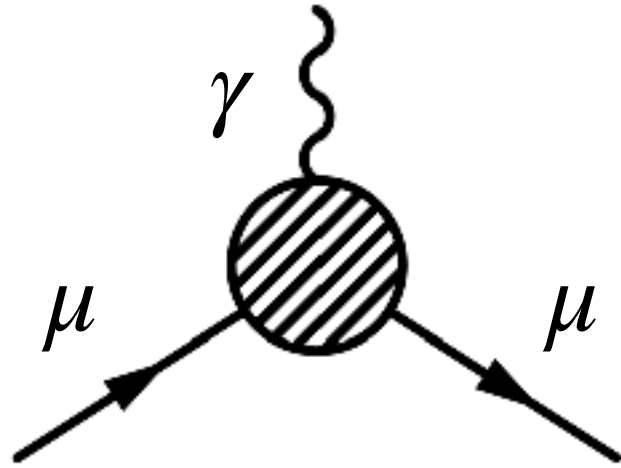
$$\arg(c_R^{\mu\mu}) = \arctan \left(\frac{2m_{\mu} d_{\mu}^{(\text{eff})}}{e a_{\mu}^{(\text{eff})}} \right)$$



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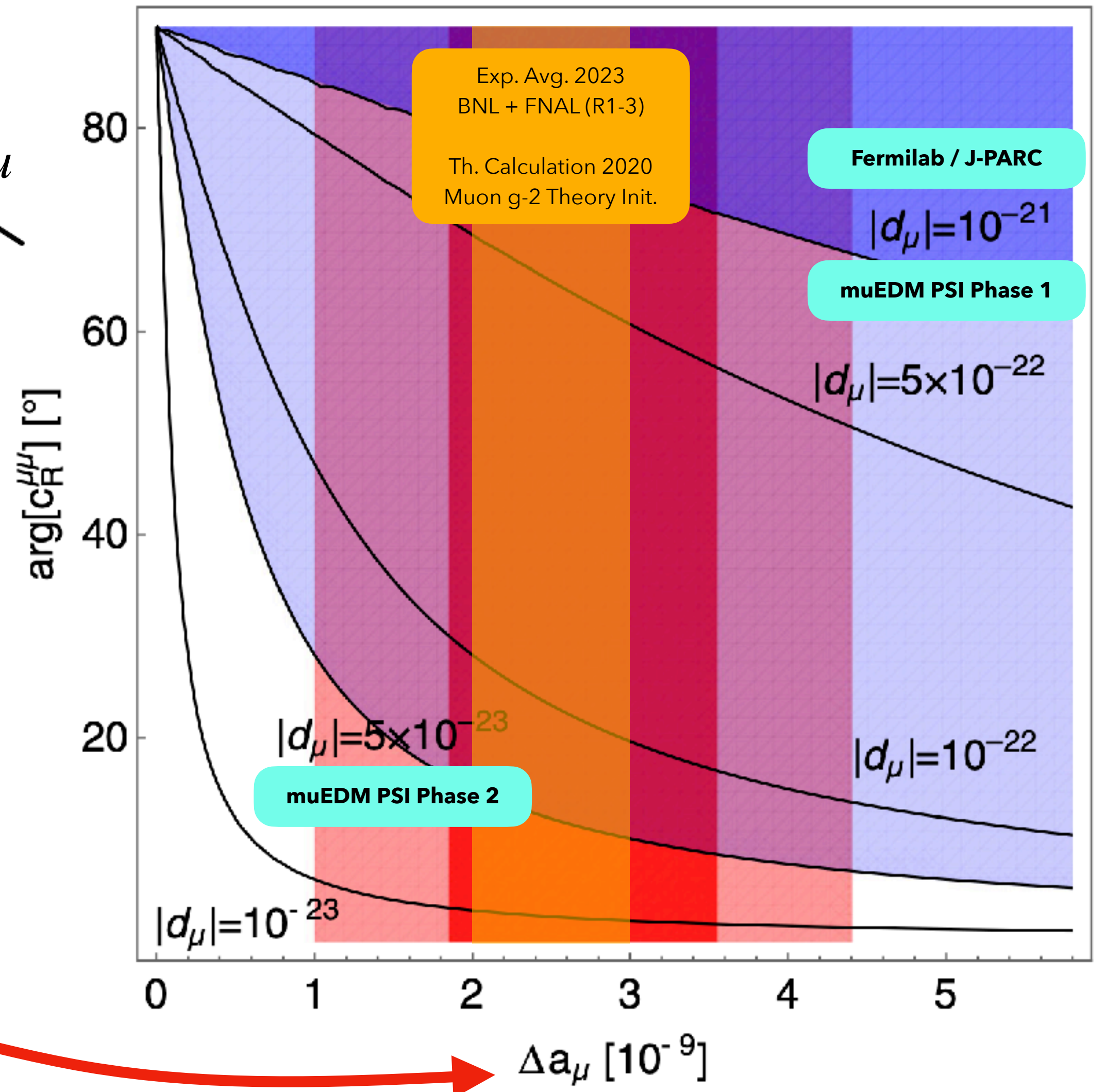
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Indirect Limits


Atomic EDMs can also constrain CP-violating observables. The atomic EDM (due to relativistic corrections that counter the Schiff Theorem) is scaling as $d_{\text{atom}} \propto \alpha^2 Z^3$

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Low photon momenta inside nucleus: $q_\gamma \sim 30 \text{ MeV} < m_\mu$

Treat only the dominant $\mathbf{E}^3\mathbf{B}$ interaction inside the nucleus

$$\mathcal{L} = -\frac{d_\mu e^3}{12\pi^2 m_\mu^3} (\mathbf{E} \cdot \mathbf{B})(\mathbf{E} \cdot \mathbf{E} - \mathbf{B} \cdot \mathbf{B})$$

Nuclear $\mathbf{E}(r)$ field based on collective charge properties

Nuclear $\mathbf{B}(r, I)$ field estimated using shell model

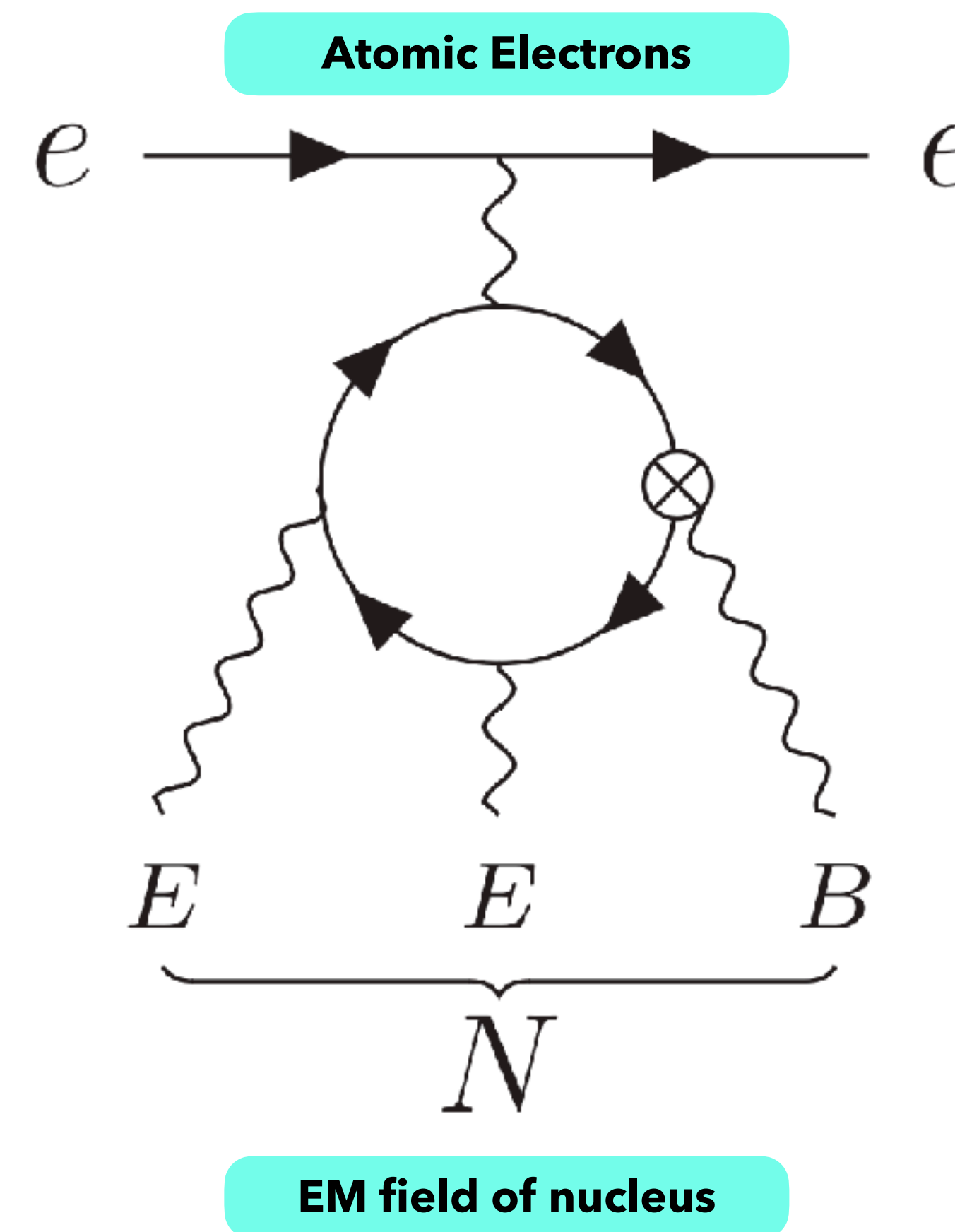
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Nuclear $\mathbf{E}(r)$ field based on collective charge properties

Nuclear $\mathbf{B}(r, I)$ field estimated using shell model

Calculate the Schiff moment S_N of the nucleus in terms of d_μ and compare to measurement.

$$S_N = (\text{Nuc. Struct.}) \times -\frac{d_\mu Z^2}{m_\mu^3 \alpha^3} m_p R_N^2$$

$$|S_{199\text{Hg}}^{(\text{exp})}| < 3.1 \times 10^{-13} \text{ efm}^3 \implies d_\mu < 6.4 \times 10^{-20} \text{ ecm}$$

Better than BNL direct limit

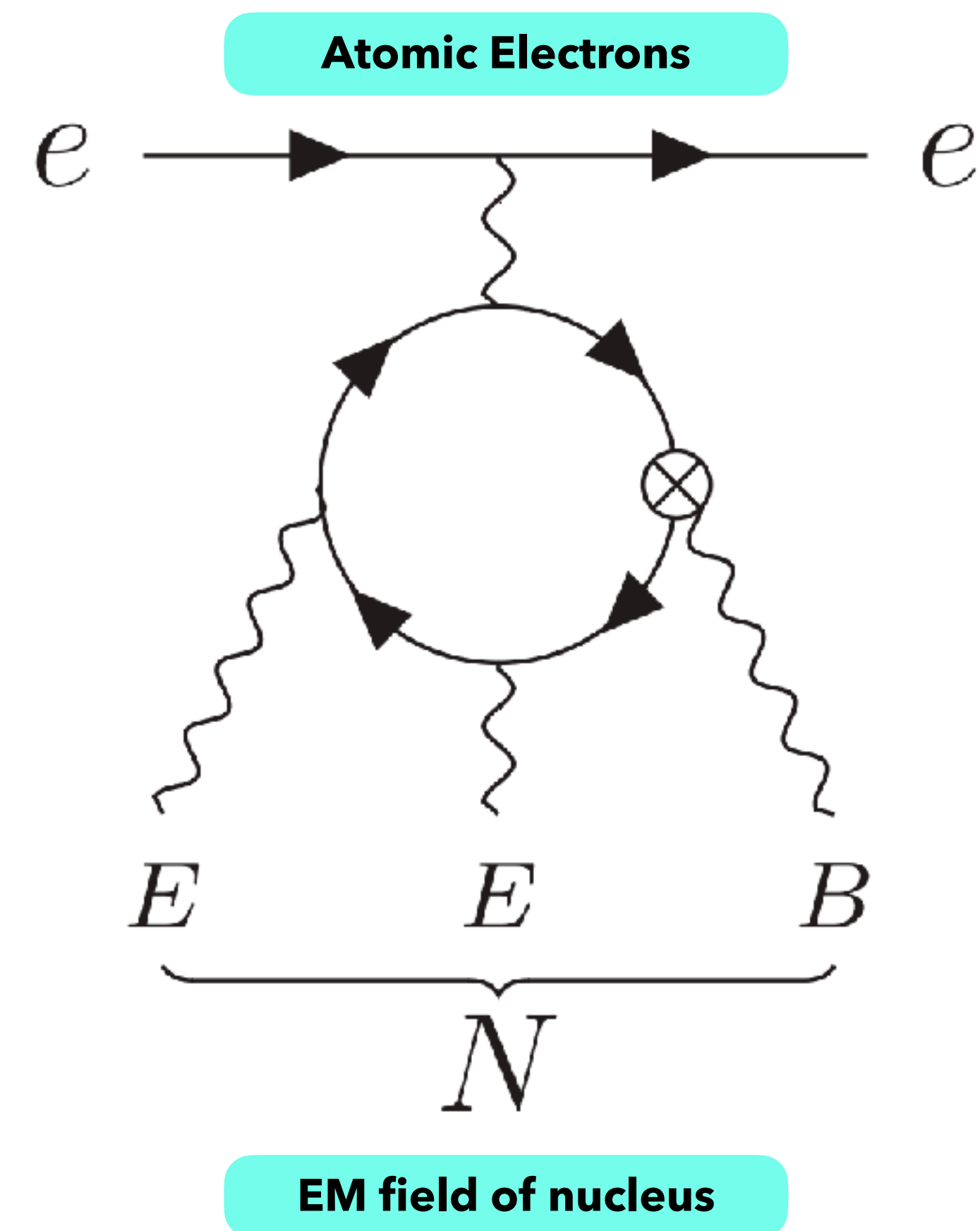
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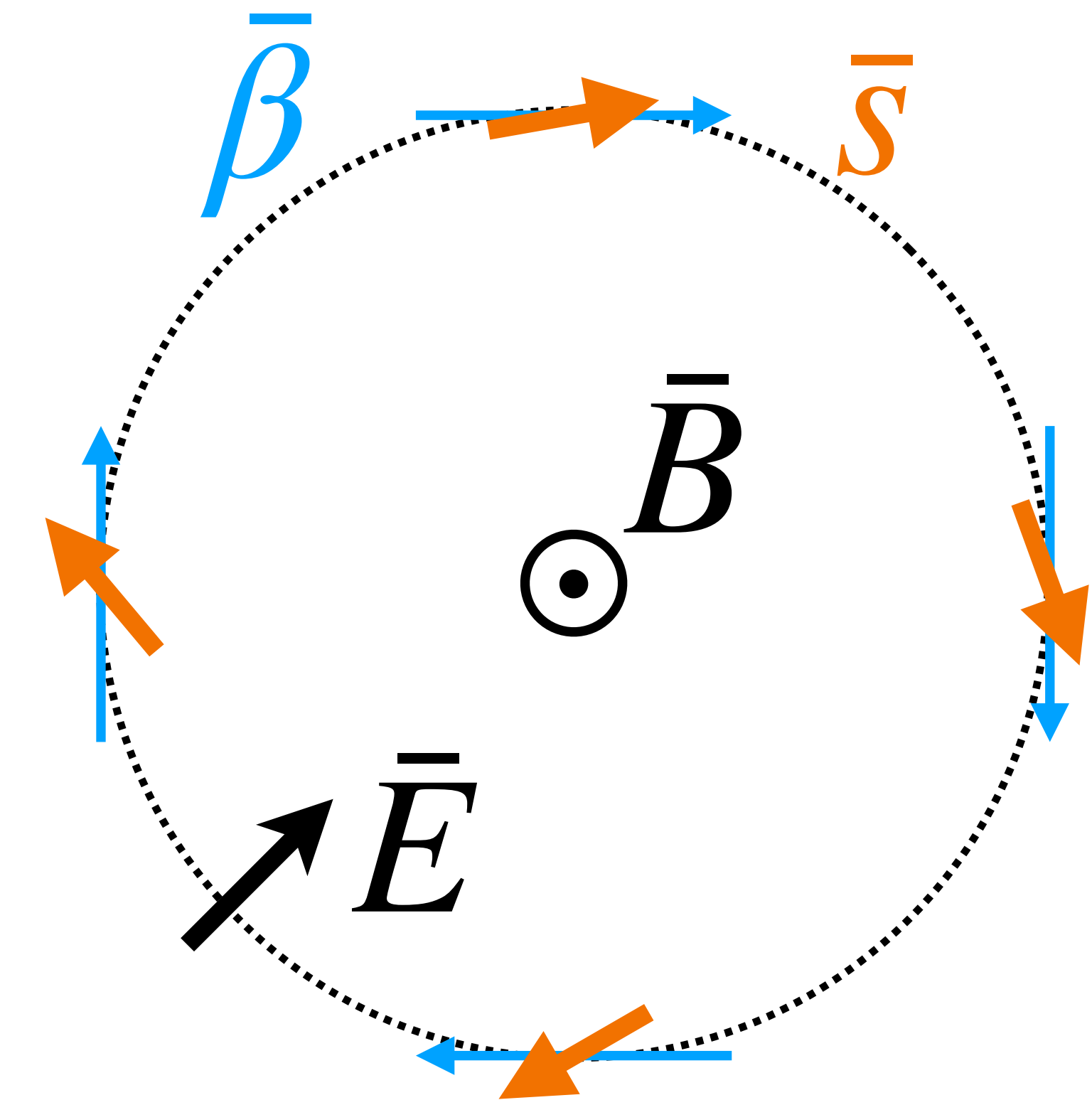


Spin Precession in a storage ring

$$\left(\vec{d}_\mu = \frac{\eta e}{2mc} \vec{s} \right)$$

Velocity : $\frac{d\vec{\beta}}{dt} = \vec{\Omega}_c \times \vec{\beta}$ $\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c$

Spin : $\frac{d\vec{s}}{dt} = \vec{\Omega}_0 \times \vec{s}$



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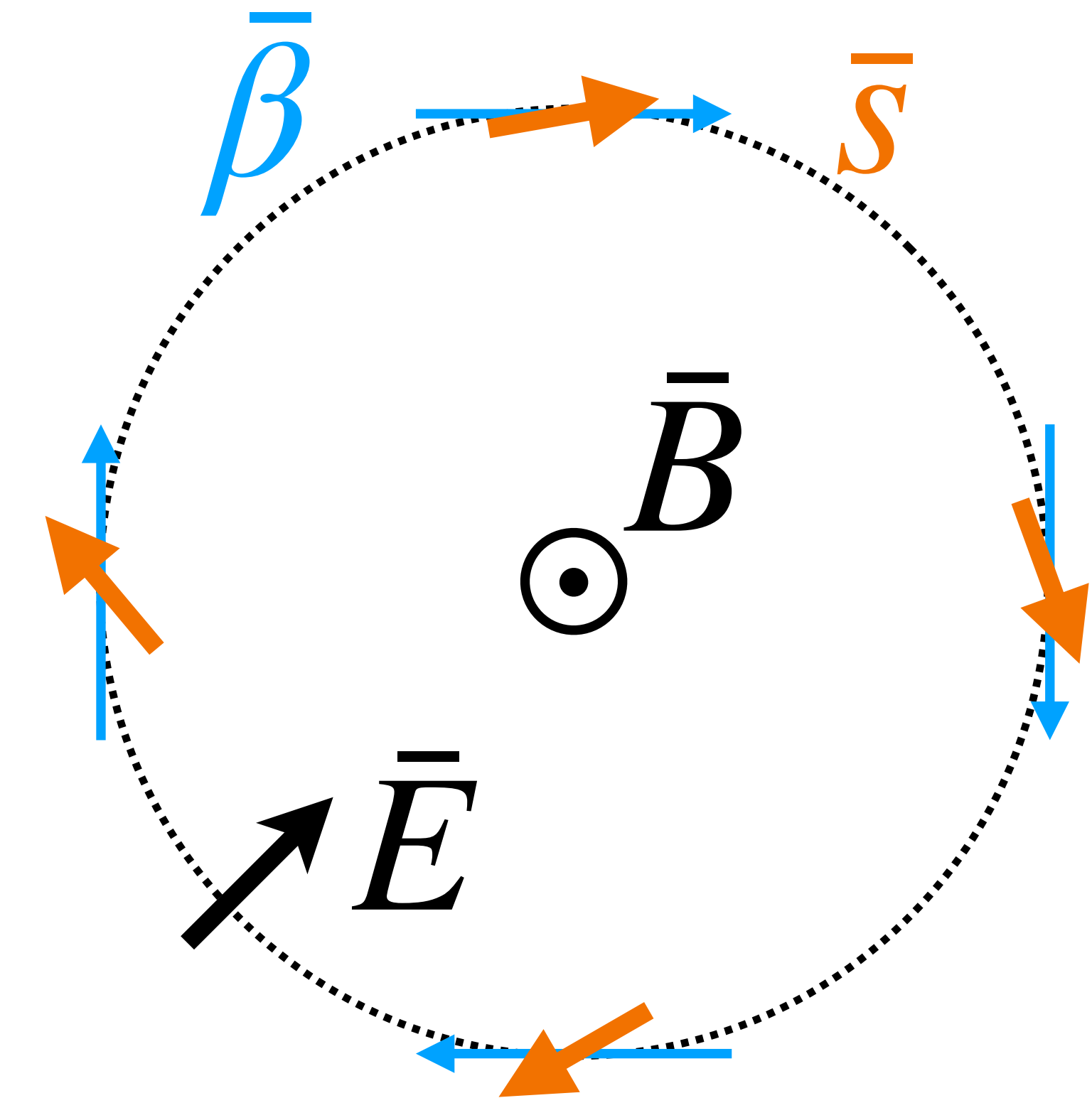
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$$= \frac{aq}{m} \left(\vec{B} - \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(1 + \frac{1}{a(1 - \gamma^2)} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right)$$

$$+ \frac{\eta q}{2m} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma/c}{\gamma + 1} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right)$$



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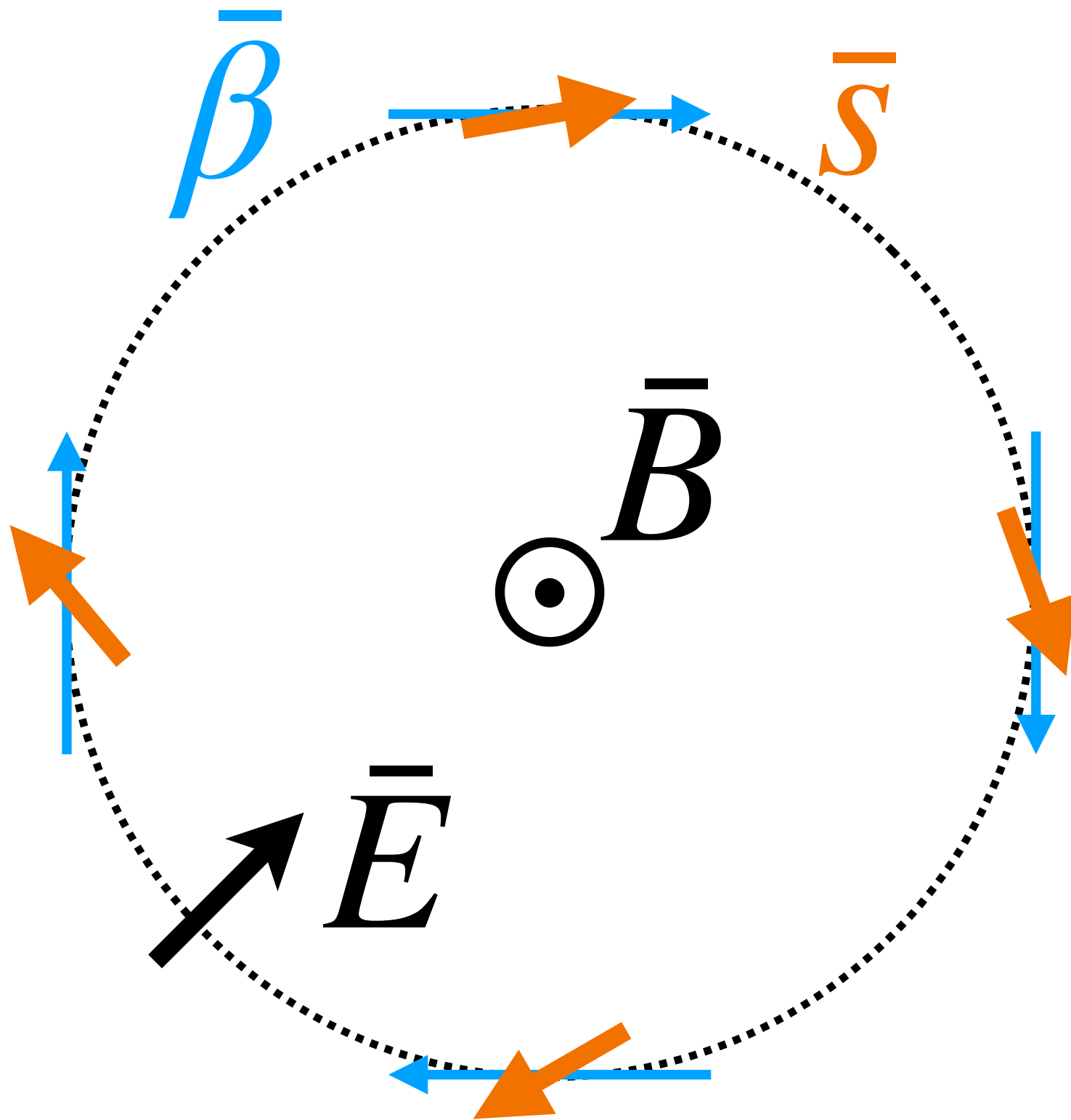
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Experimental Approaches

Fermilab
$$\bar{\Omega} = \frac{aq}{m} \left(\bar{B} - \left(1 + \frac{1}{a(1-\gamma^2)} \right) \frac{\bar{\beta} \times \bar{E}}{c} \right) + \frac{\eta q}{2m} \left(\bar{\beta} \times \bar{B} + \frac{\bar{E}}{c} \right)$$

"magic momentum"

J-PARC
$$\bar{\Omega} = \frac{aq}{m} \left(\bar{B} - \left(1 + \frac{1}{a(1-\gamma^2)} \right) \frac{\bar{\beta} \times \bar{E}}{c} \right) + \frac{\eta q}{2m} \left(\bar{\beta} \times \bar{B} + \frac{\bar{E}}{c} \right)$$

"E field shielding"

PSI
$$\bar{\Omega} = \frac{aq}{m} \left(\bar{B} - \left(1 + \frac{1}{a(1-\gamma^2)} \right) \frac{\bar{\beta} \times \bar{E}}{c} \right) + \frac{\eta q}{2m} \left(\bar{\beta} \times \bar{B} + \frac{\bar{E}}{c} \right)$$

"frozen spin"

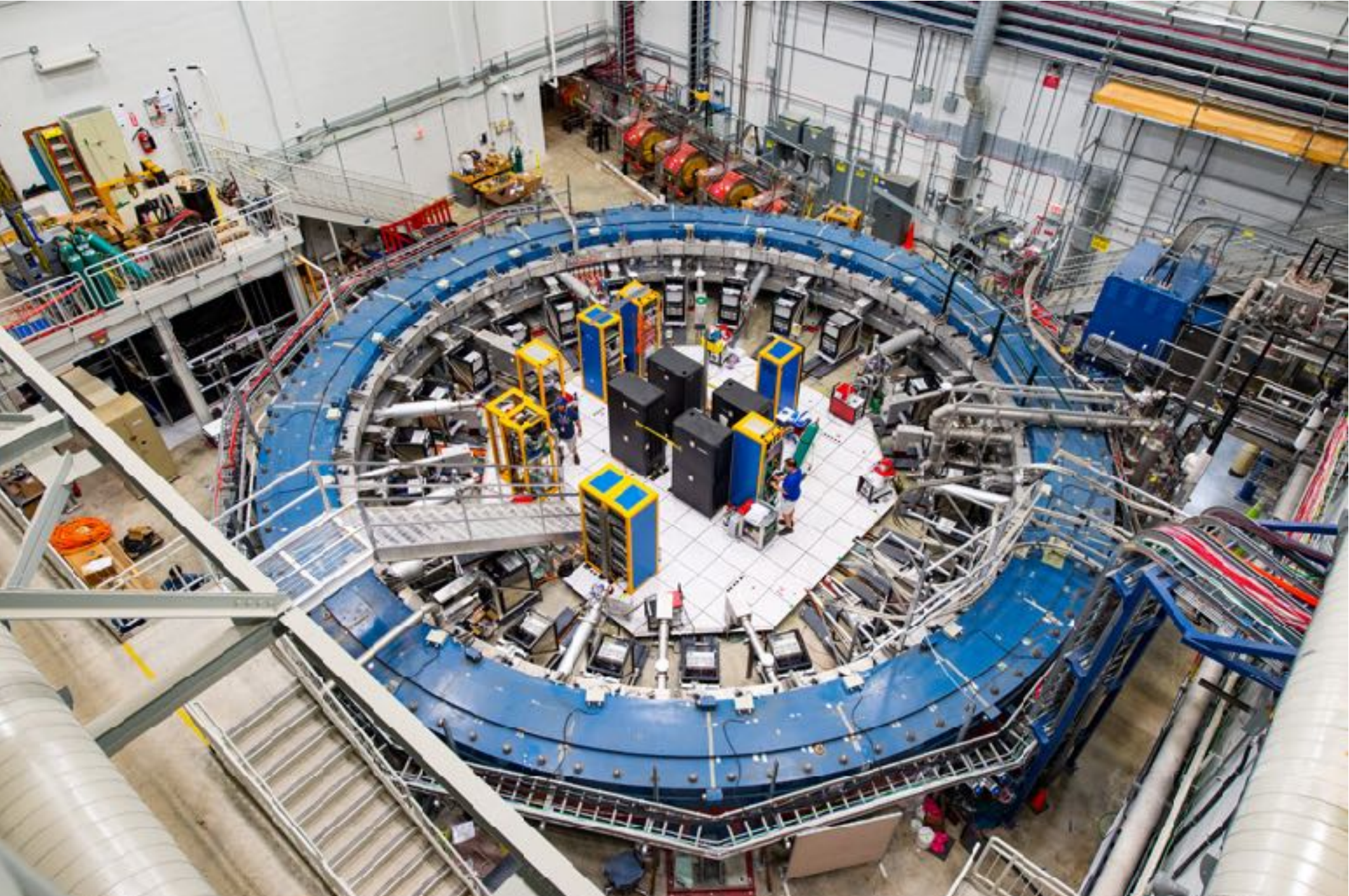
Muon g-2 at BNL & Fermilab

Pulsed (avg. bunch freq. 11.4 s^{-1}) muon beam with magic momentum $3.1 \text{ GeV}/c$

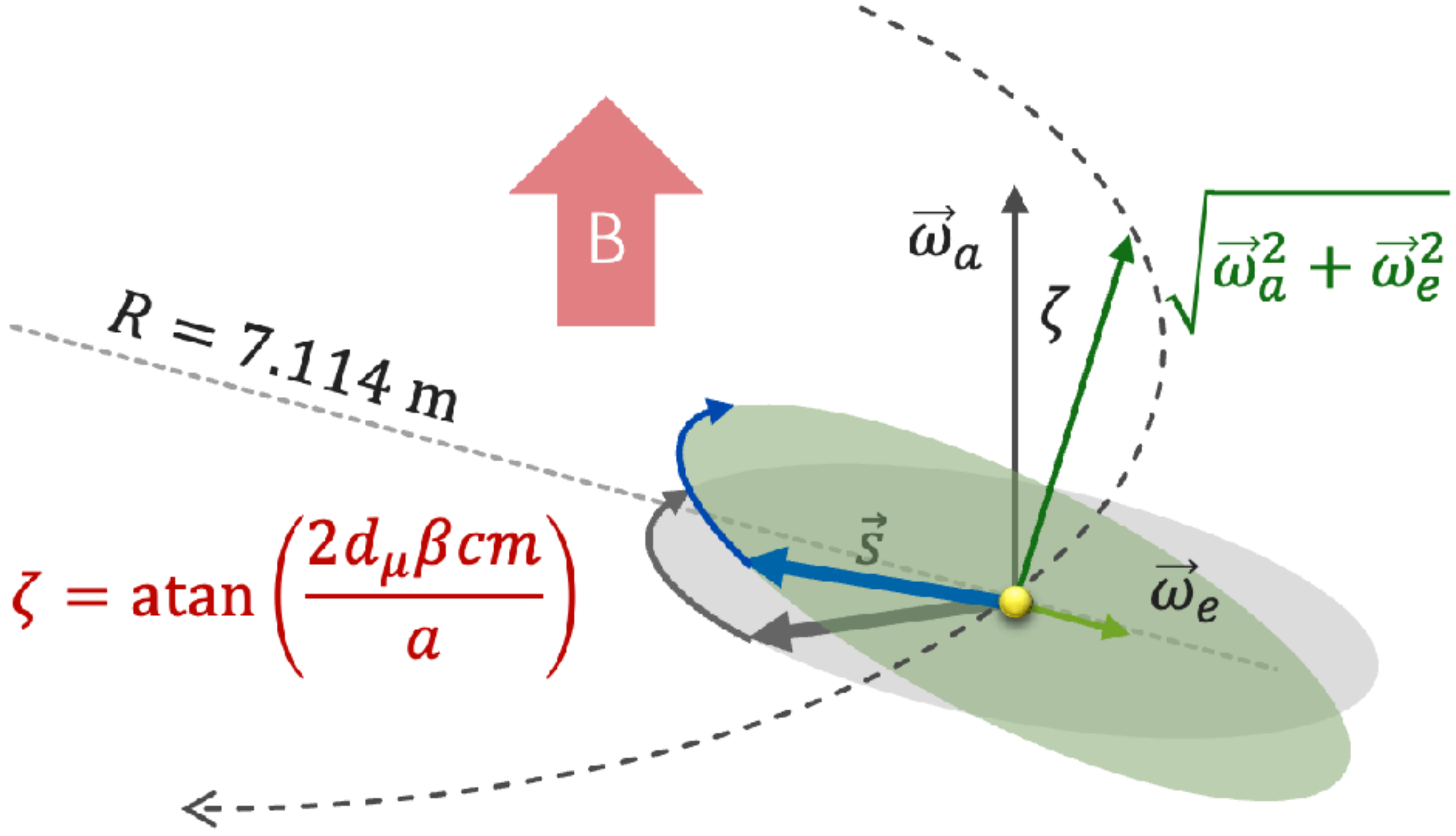
$$1 + \frac{1}{a_\mu(1 - \gamma^2)} \stackrel{!}{=} 0 \implies \gamma = 29.3$$

$$\bar{\Omega} \approx \frac{aq}{m} \bar{B} + \frac{\eta q}{2m} \bar{\beta} \times \bar{B}$$

2 simultaneous precession axes!



Credit: FNAL, DoE muon-g-2.fnal.gov



Credit: P. Schmidt-Wellenburg

Frozen Spin Technique

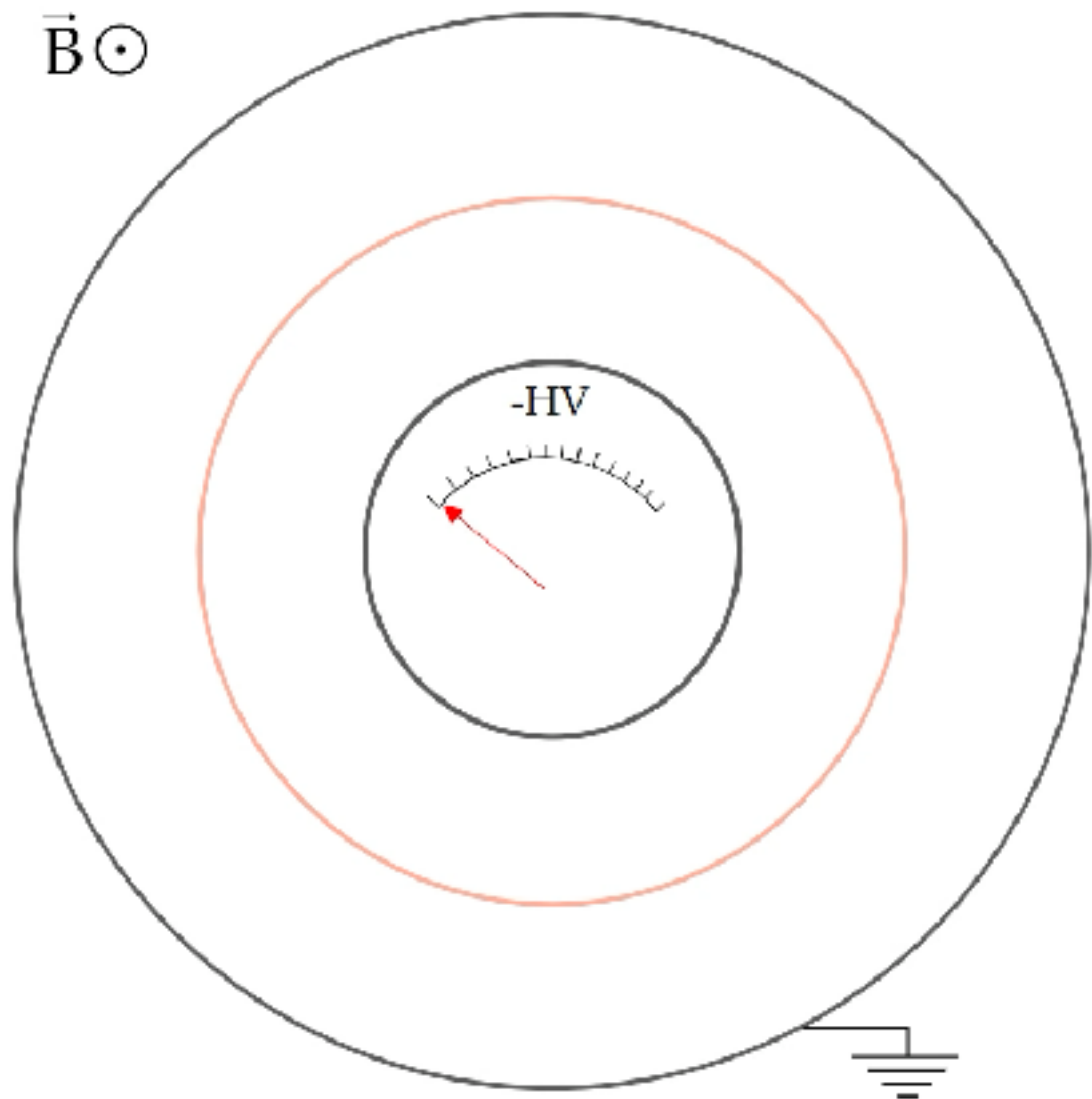
Goal: Configure E, B fields such that spin follows velocity vector and EDM is the only inherent source of spin precession.

$$\begin{aligned}\bar{\Omega} = \bar{\Omega}_0 - \bar{\Omega}_c = & \frac{aq}{m} \left(\bar{B} - \frac{\gamma}{\gamma+1} (\bar{\beta} \cdot \bar{B}) \bar{\beta} - \left(1 + \frac{1}{a(1-\gamma^2)} \right) \frac{\bar{\beta} \times \bar{E}}{c} \right) \\ & + \frac{\eta q}{2m} \left(\bar{\beta} \times \bar{B} + \frac{\bar{E}}{c} - \frac{\gamma/c}{\gamma+1} (\bar{\beta} \cdot \bar{E}) \bar{\beta} \right)\end{aligned}$$

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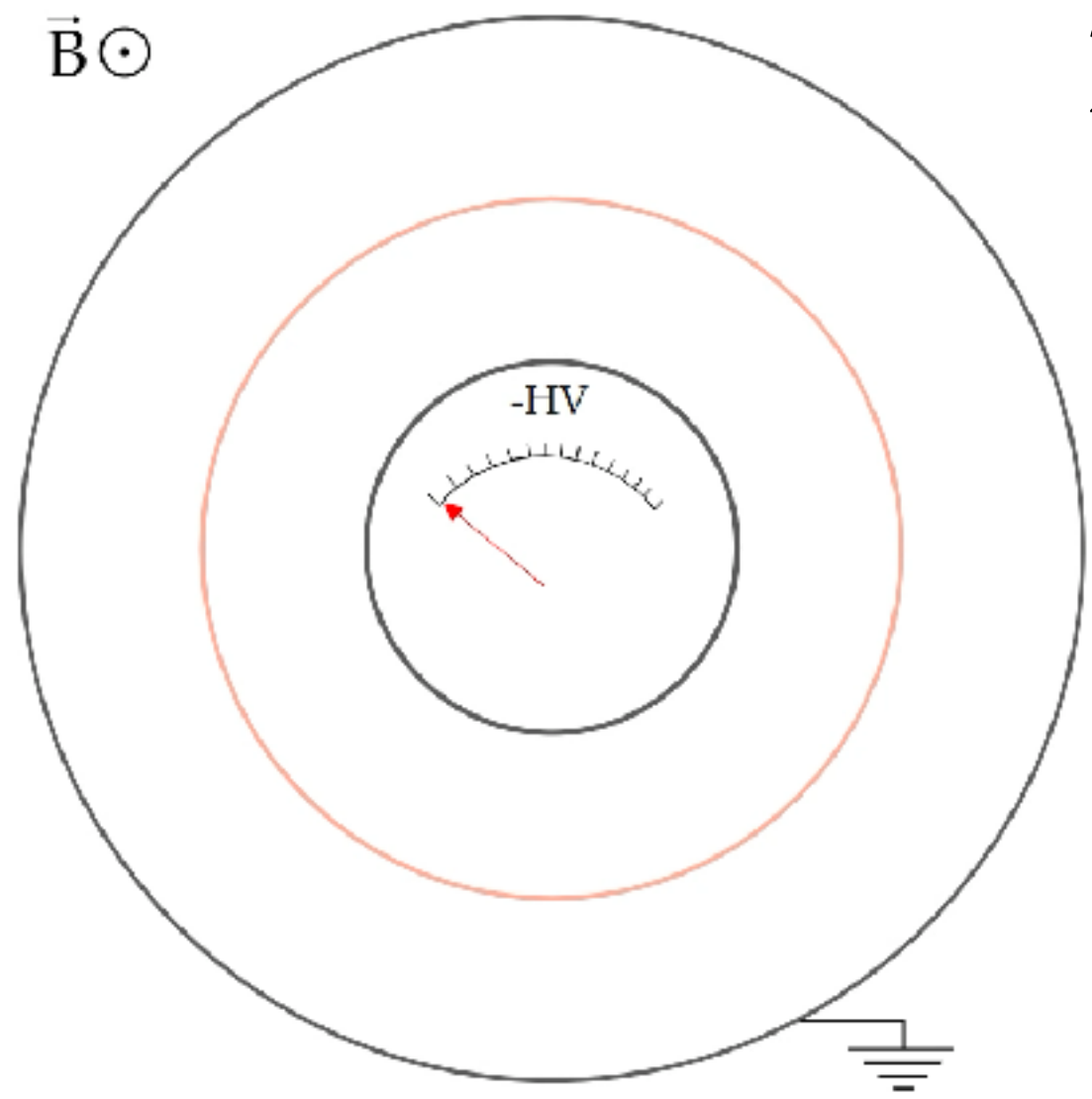


Frozen Spin Condition : $E_f \stackrel{a \ll 1}{\approx} aB\beta c\gamma^2$

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Frozen Spin Condition : $E_f \stackrel{a \ll 1}{\approx} aB\beta c\gamma^2$

Experimental Requirements:

1. Fields \perp Velocity
2. Precisely tuned $E = E_f$
3. Constrained B_r (radial), E_z (axial)

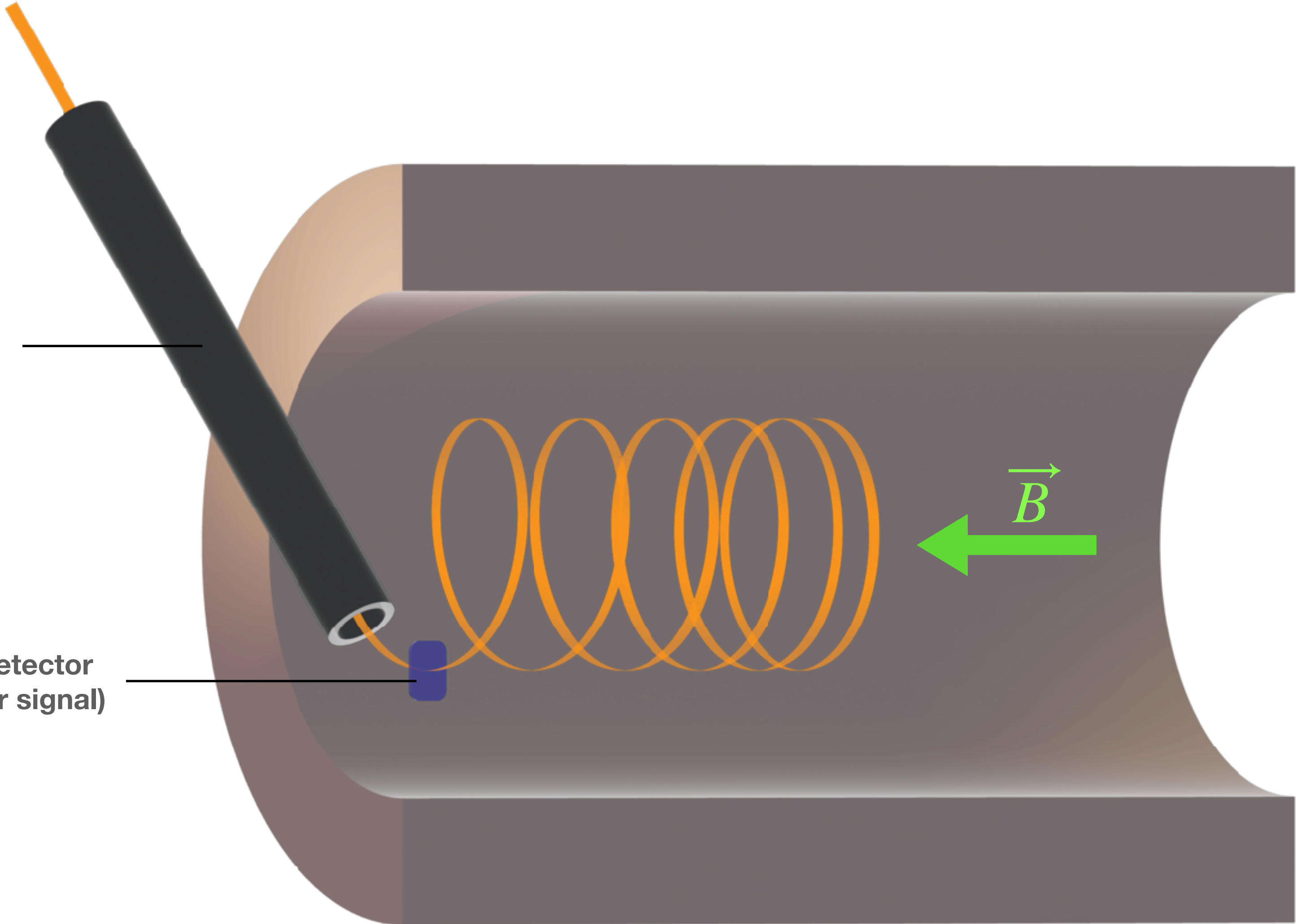
Any periodic deviations must be stable over the timescale of τ_μ .

muEDM Experiment at PSI

28 MeV/c μ^+
(π E1 Beamline, PSI)

Superconducting
Injection Chanel

Entrance Detector
(t=0 & trigger signal)



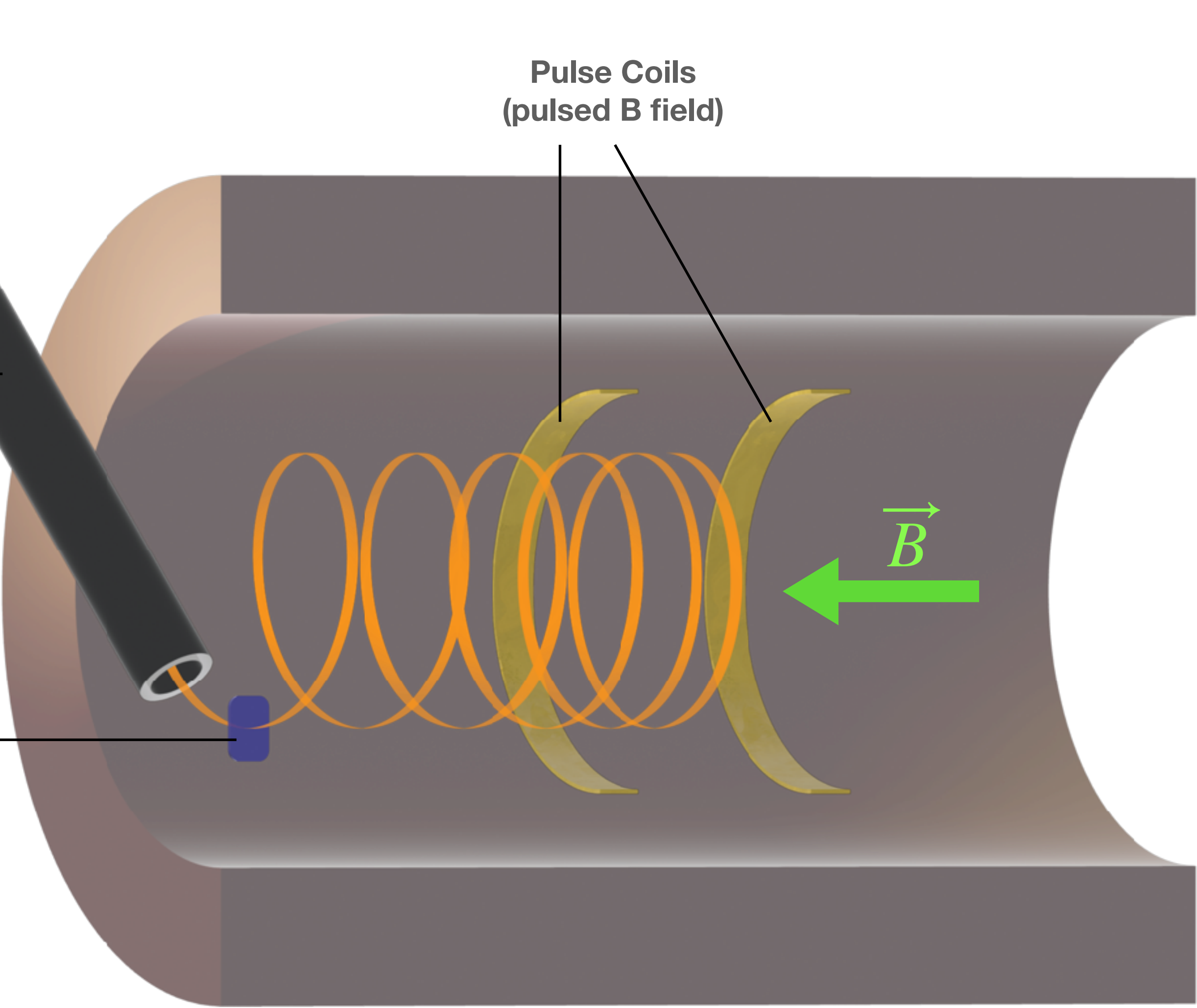
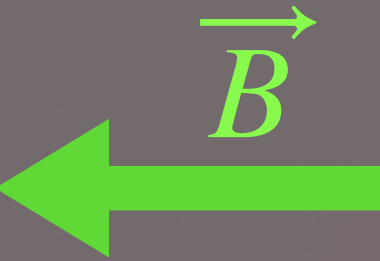
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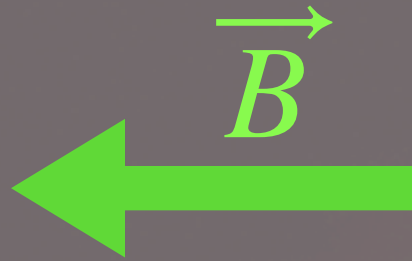
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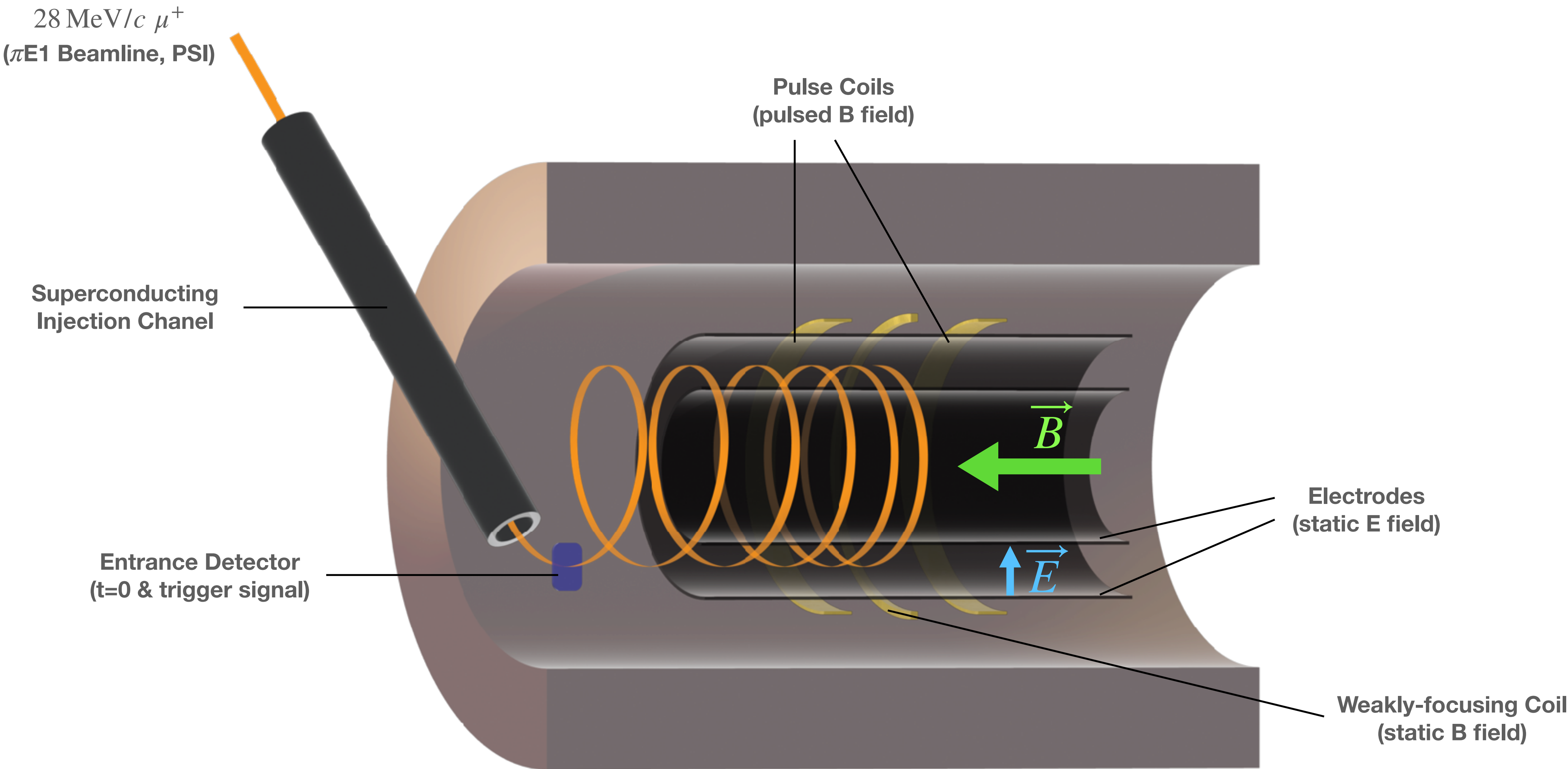
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Pulse Coils
(pulsed B field)

Weakly-focusing Coil
(static B field)



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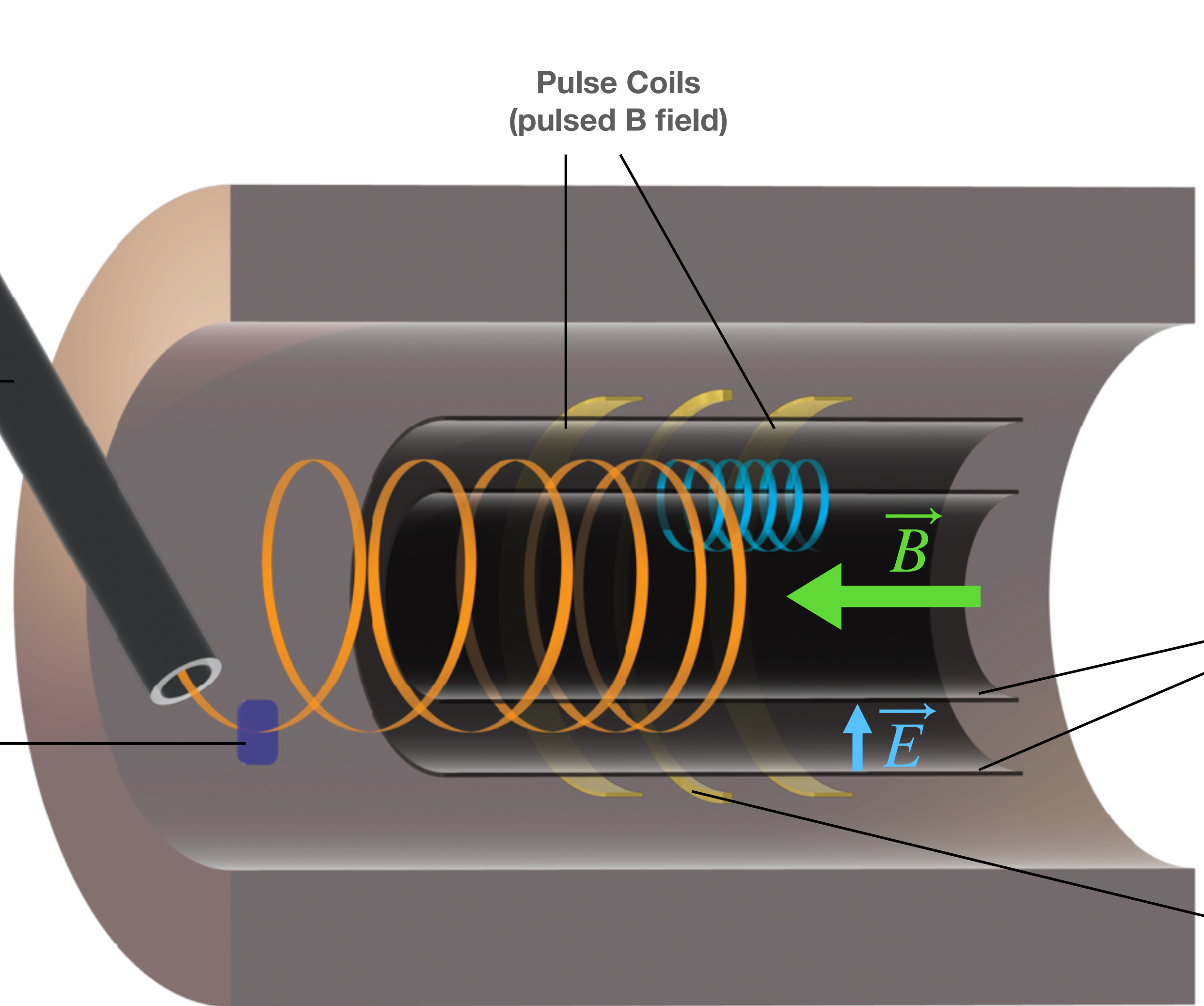
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Superconducting
Injection Chanel

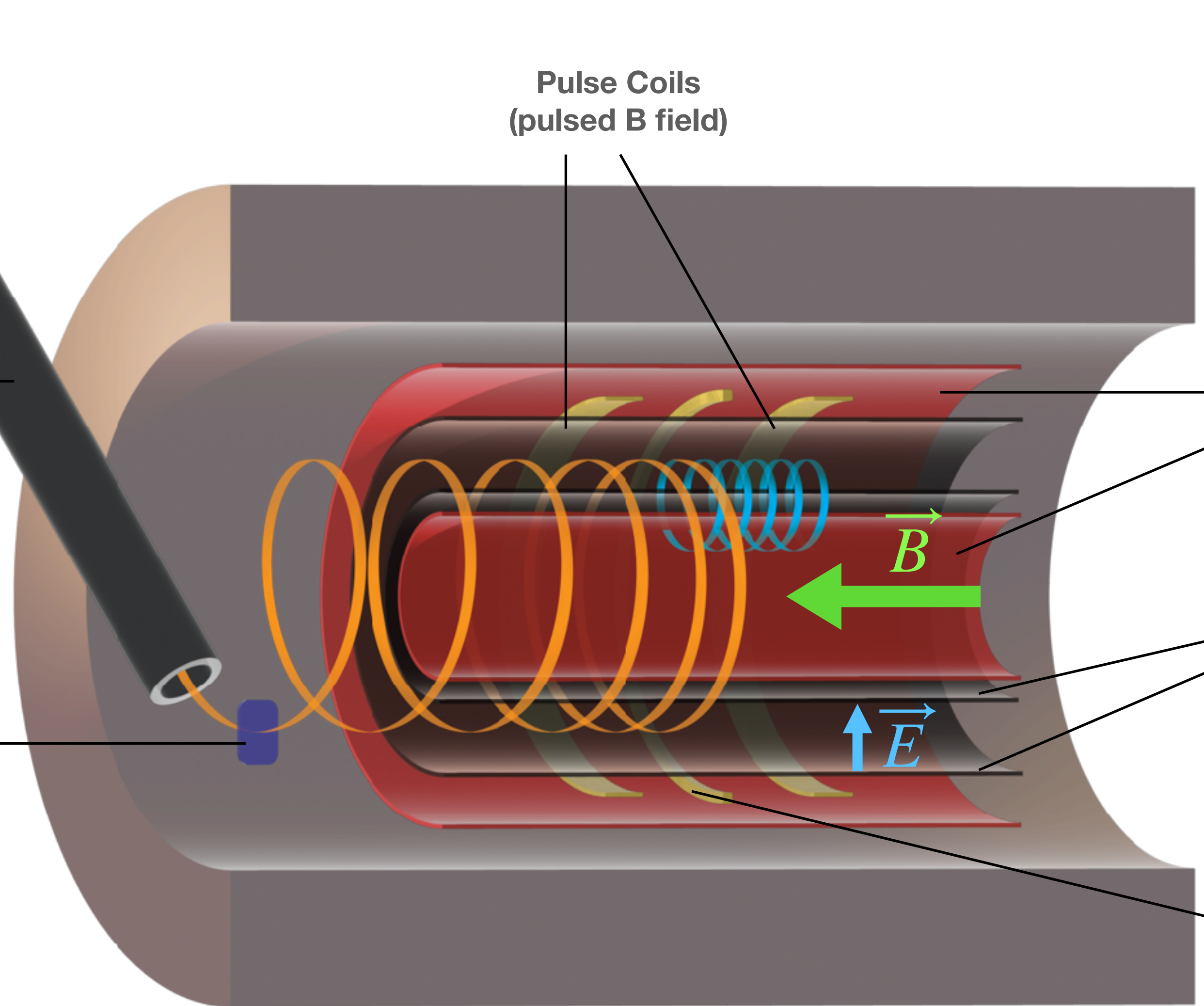
Entrance Detector
(t=0 & trigger signal)

Pulse Coils
(pulsed B field)

Positron Trackers

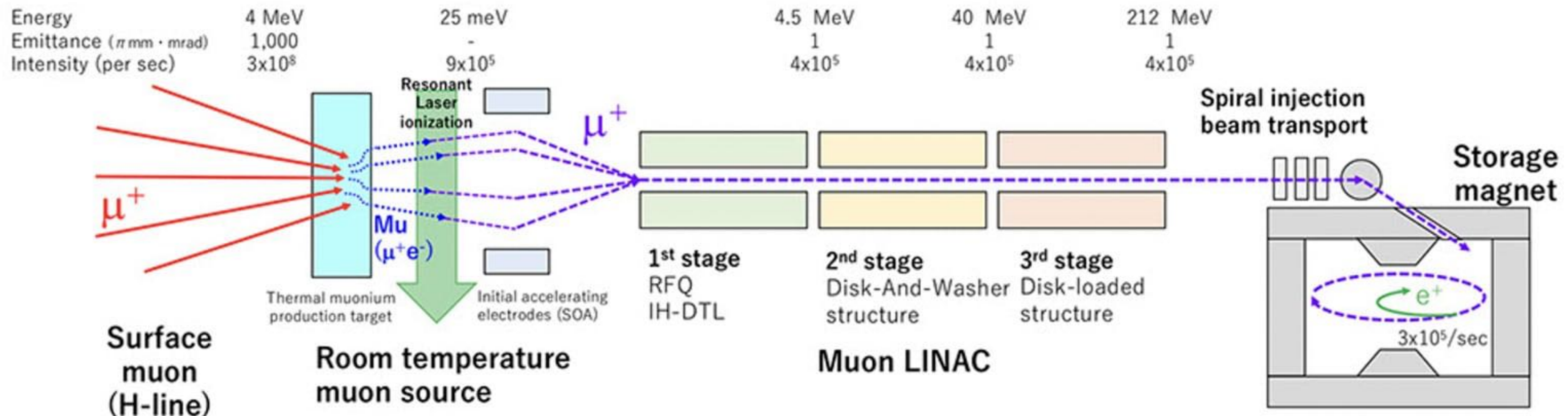
Electrodes
(static E field)

Weakly-focusing Coil
(static B field)



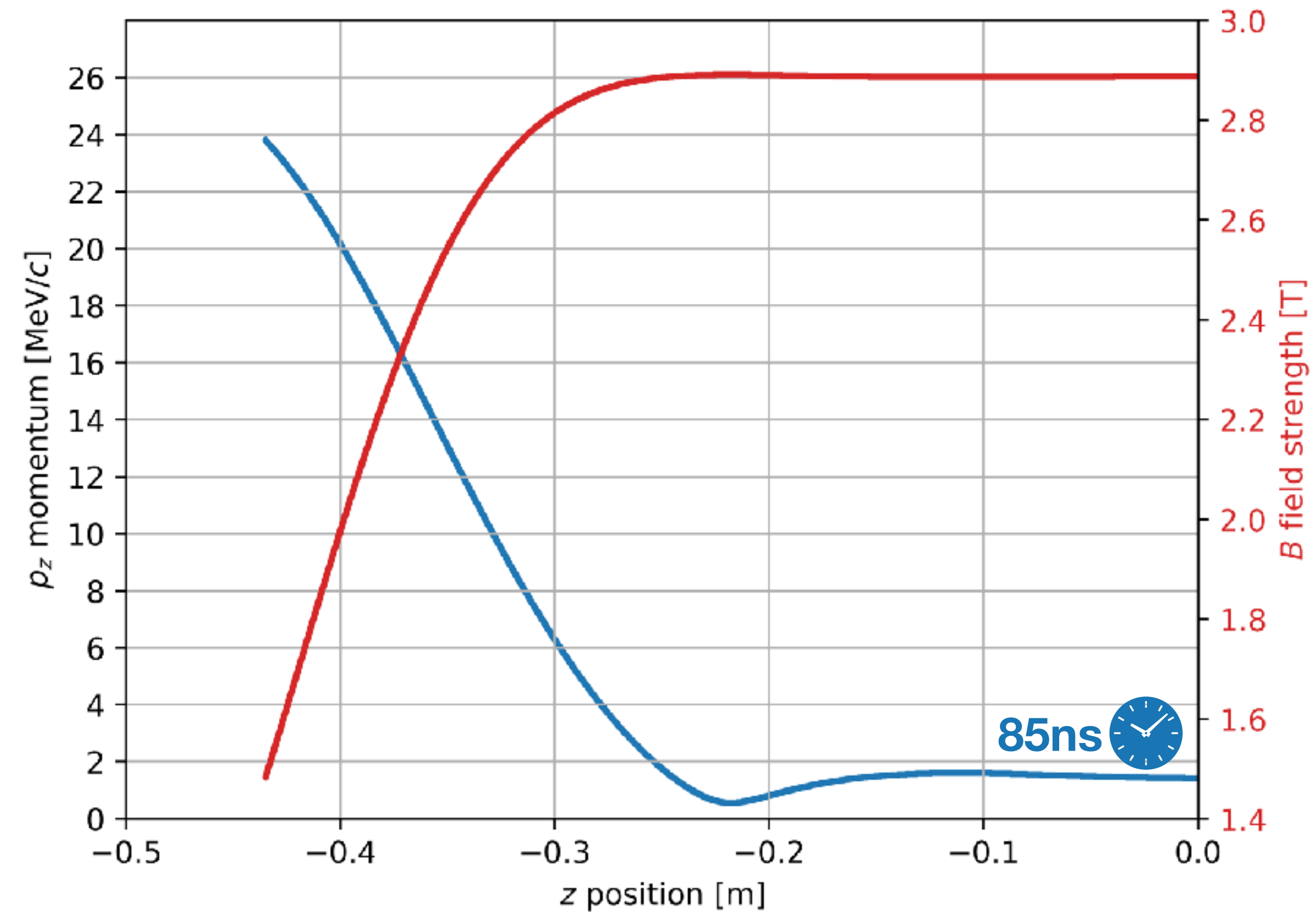
Muon g-2/EDM at JPARC

- Pulsed (bunch rate 25 Hz) muon beam with momentum 30 MeV/c.
- Longitudinal injection (similar to PSI)
- Electric field cancellation means narrow acceptance phase space.
- Pulsed beam demands bunched injection and measurement
- Ultra-cold muon beam developed for phase space compression.

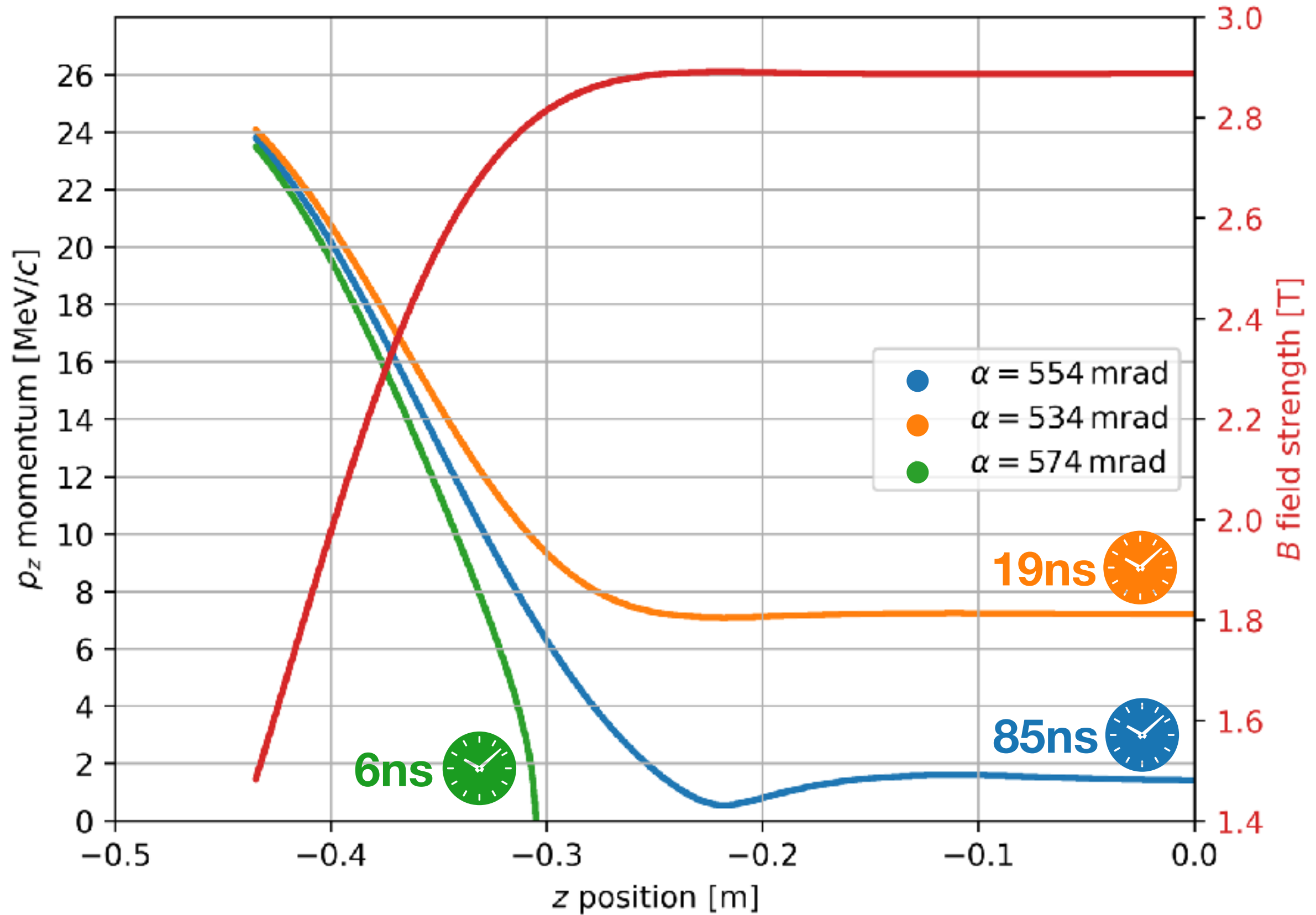


Credit: J-PARC g-2.kek.jp

Challenges: Injection & Storage



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Outlook for muEDM Phase I

