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Advanced concepts for future SSMB storage rings

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Outline

- Introduction to SSMB (steady-state microbunching)
- The GLSF (generalized longitudinal strong focusing) scheme

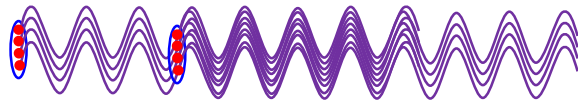


Synchrotron radiation sources:

High repetition rates; Good transverse coherence;
Poor longitudinal coherence (short-wavelength).



Incoherent radiation $P \propto N_e$

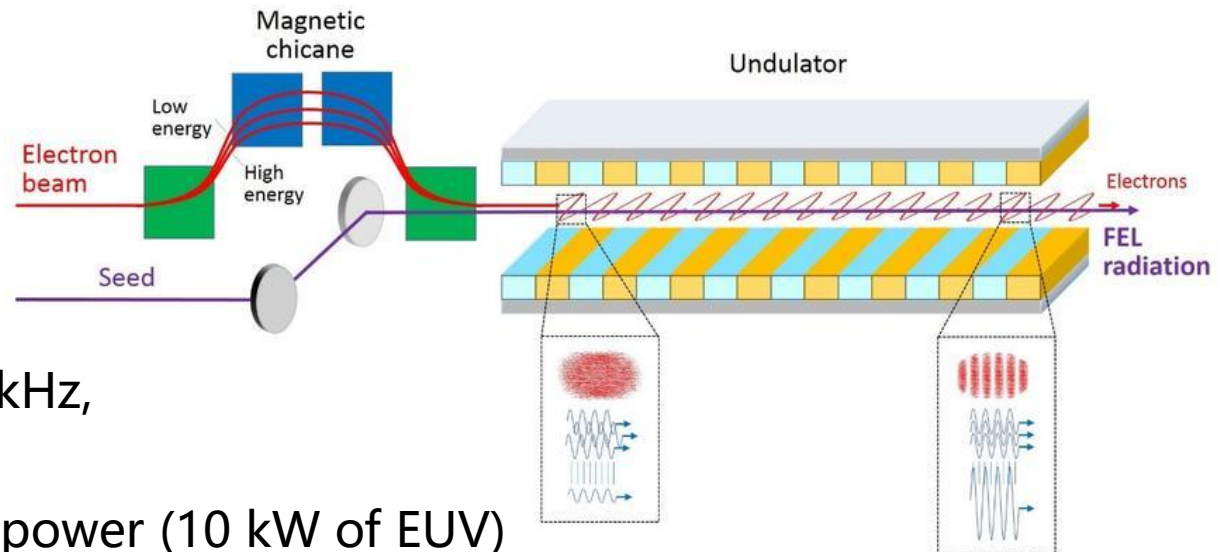


Coherent radiation $P \propto N_e^2$

For EUV, average power is around Watt in 2% b.w.

Free-electron lasers:

Good coherence;
(trans. AND long.)



Repetition rates:

NC: hundreds of Hz or kHz,

SC: up to the MHz

high average radiation power (10 kW of EUV)

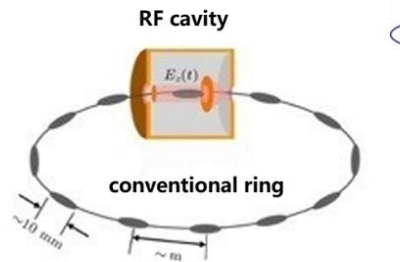
Concern is the cost.

A new mechanism of accelerator-driven light source

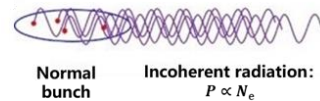
Generate microbunching and maintain it in storage rings, without destroying the bunch when radiation.

strong coherence
high repetition rate

Synchrotron radiation(SR)



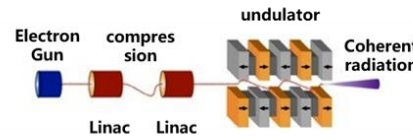
High repetition rate
Low peak power



$$P \propto N_e$$

$$f \sim 10^6 \text{ Hz}$$

Free electron laser(FEL)

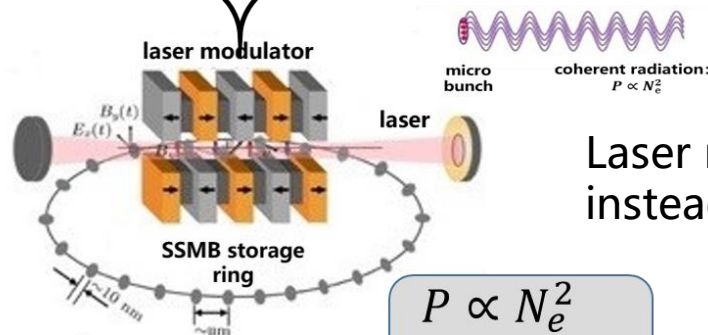


$$P \propto N_e^2$$

$$f \sim 10^2 \text{ Hz}$$

Low repetition rate
High peak power

Steady state microbunching (SSMB)



Laser modulator
instead of RF cavity

$$P \propto N_e^2$$

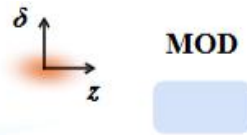
$$f \sim 10^6 \text{ Hz}$$

High average power
(kW of EUV)

High repetition rate
High peak power

Approaches to realize **eigenstate** nanometer-long bunches in storage rings?

Longitudinal weak focusing (LWF): laser modulator + low- α lattice



longitudinal weak focusing
storage ring

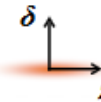
RAD

1064 nm, MW-level $\sim 1e-6$

tens-of-nanometer-long
bunch can be achieved;
hard to get coherent radiation
at 13.5 nm (EUV).

Longitudinal strong focusing (LSF):
Laser modulators as 'long. quads'

Notable variation of bunch length
At radiation point nanometer-long bunches
Coherent 13.5-nm EUV radiation
Hundreds of MW laser power is required to
modulate the beam \rightarrow pulsed mode



longitudinal strong focusing
storage ring

MOD1

RAD

MOD2

Generalized longitudinal strong focusing (GLSF):
Strong beam manipulation, yet within 4-D coupled phase space

Vertical-longitudinal coupling
Laser modulator placed at dispersive location

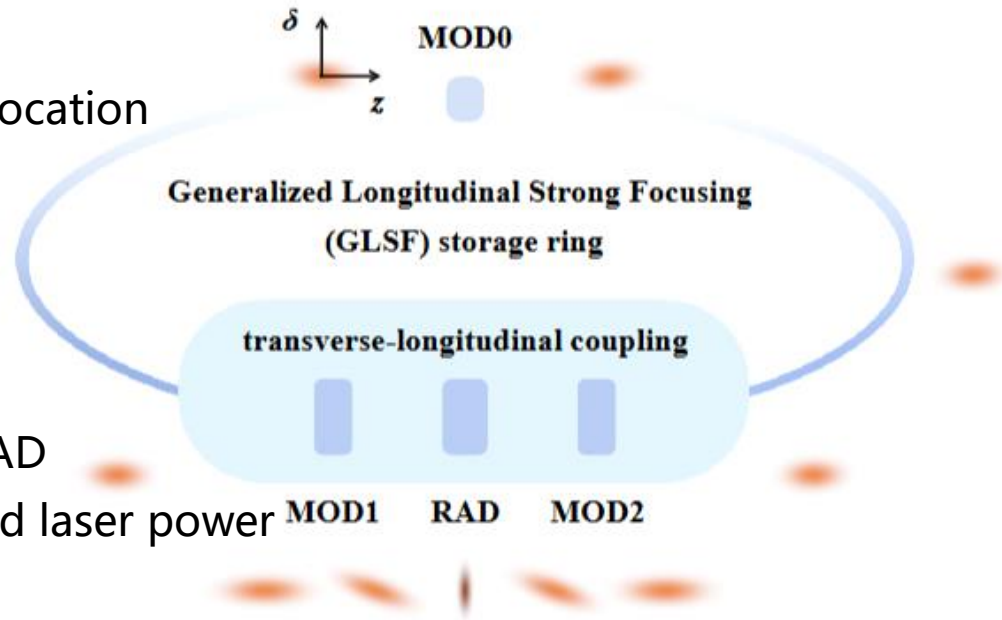
$$(\epsilon_x, \epsilon_y, \epsilon_z) \quad \sigma_{z_RAD} \propto \sqrt{\epsilon_y}$$

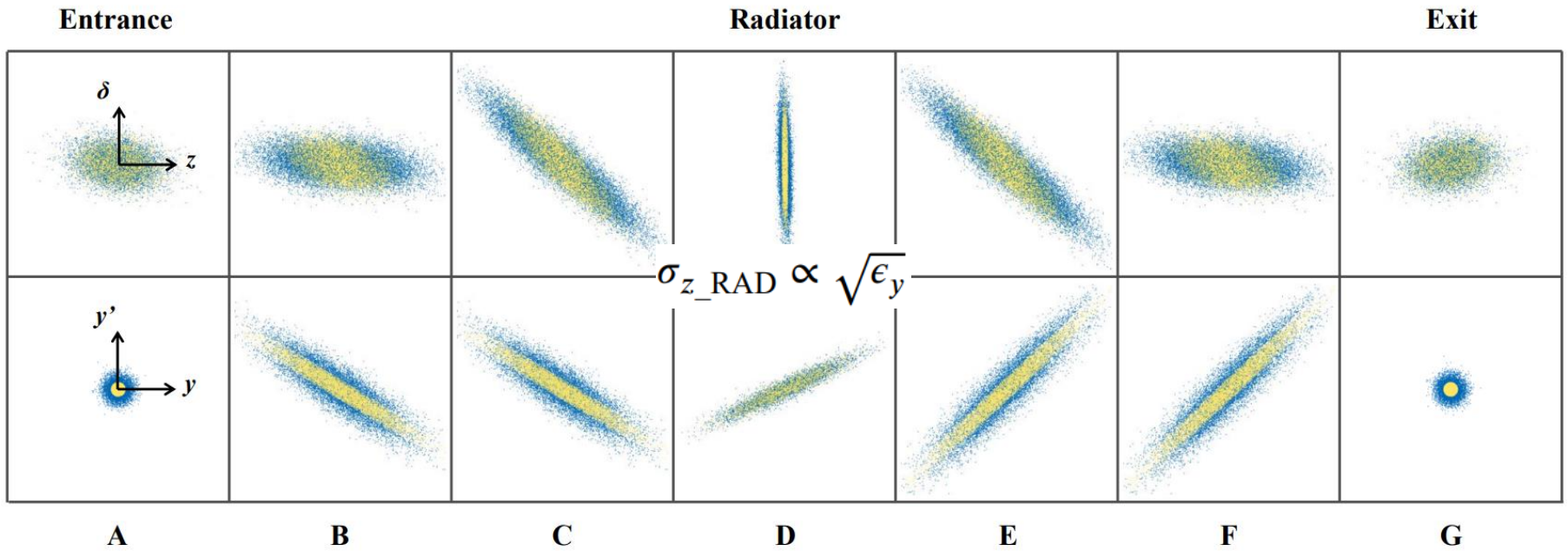
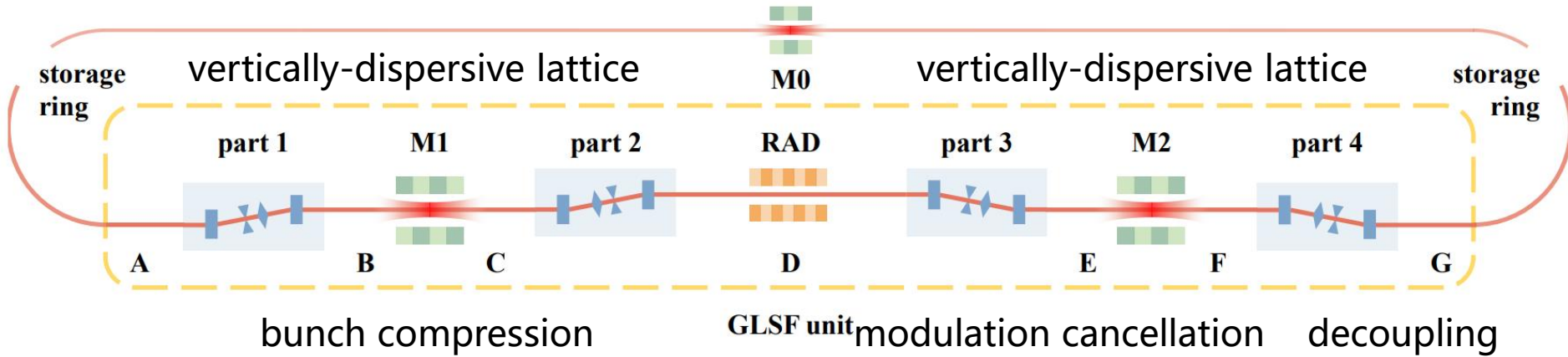
$$P_{laser} \quad \downarrow$$

Project exclusively low emit_y to σ_{z_RAD}
Less demand on modulation depth and laser power
A partial emittance-exchange scheme

De-modulation and de-coupling are needed to match beam status with the rest of the ring outside the GLSF unit → Ring-based eigen-state

works also for RF-pre-bunched and coasting beam





Bunching factor for pre-bunched beam at the radiation point in GLSF approach

$$b = e^{-\frac{1}{2}k_r^2\sigma_{z_RAD}^2} \left| \sum_{p=-\infty}^{\infty} J_p(n) e^{-\frac{1}{2}(n-p)^2k_m^2\sigma_{z_MOD}^2} \right|$$

$J_p(n)$ p-th order Bessel function of first kind
 n: harmonic number
 kr/km: radiation/modulation wave number

$\sigma_{z_RAD}/\sigma_{z_MOD}$: bunch length at RAD/MOD

modulation depth h

$$|h| \geq \frac{\epsilon_y}{\sigma_{z_y_MOD}\sigma_{z_RAD}} \quad P_{RAD} \propto b^2$$

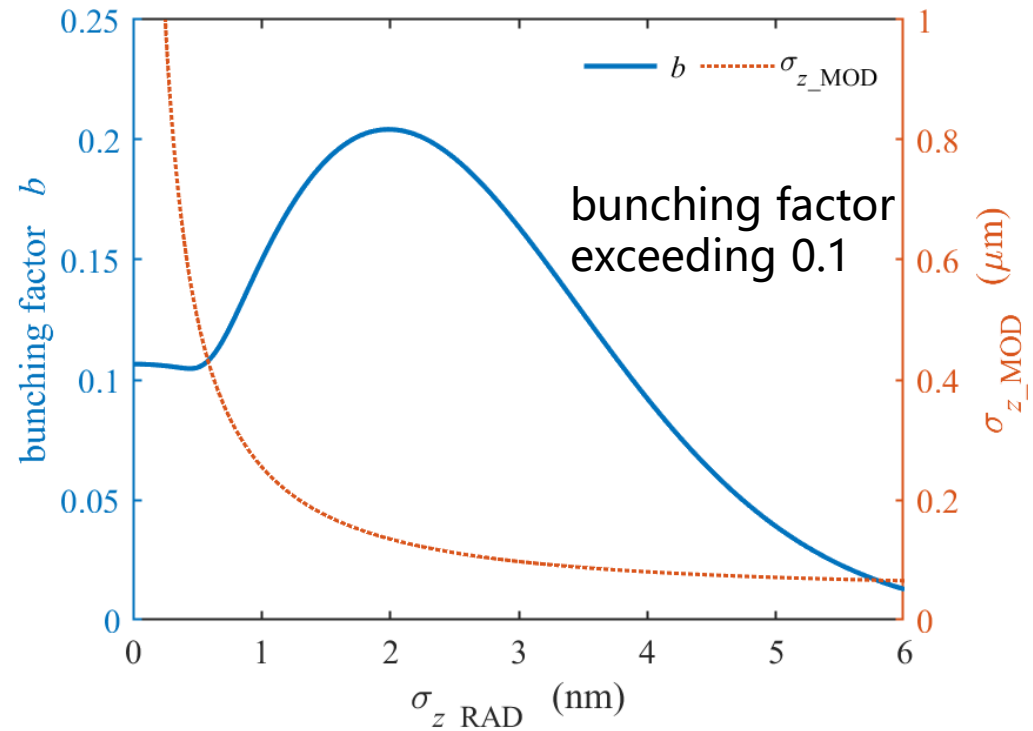
$$P_{laser} \propto h^2$$

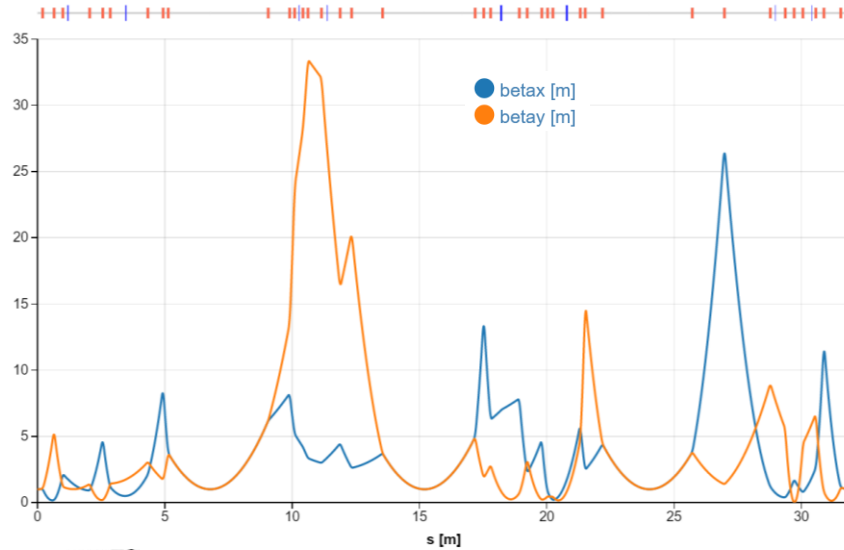
Low emit_y → low h and P_{laser}

This is why GLSF is preferred

Assuming

$P_{laser} = 1 \text{ MW}$, $|h| = 4000 \text{ m}^{-1}$,
 $E = 400 \text{ MeV}$, $\text{emit}_y = 1 \text{ pmrad}$,
 $\lambda_r = 13.5 \text{ nm}$, $\lambda_m = 1 \mu\text{m}$,
 $\sigma_{z_y_MOD} = \text{emit}_y / (|h| * \sigma_{z_RAD})$





$E = 400 \text{ MeV}$

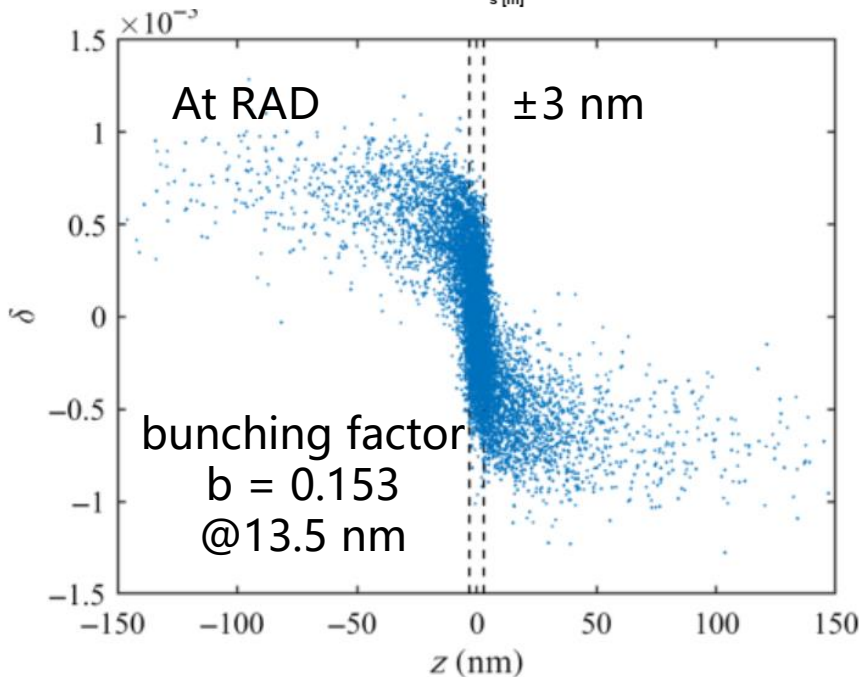
$I_{\text{avg}} = 1 \text{ A}$

$\text{emit}_y = 1 \text{ pmrad}$

$\lambda_m = 1064 \text{ nm}$

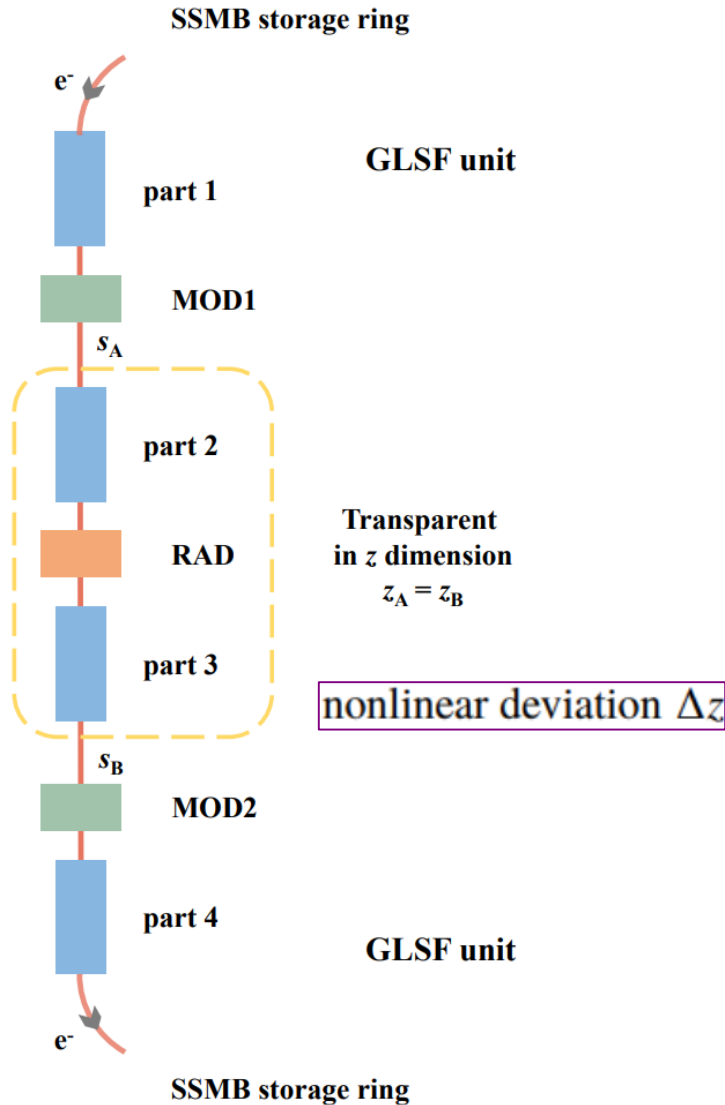
$\lambda_r = 13.5 \text{ nm}$

$P_{\text{laser}} = 1 \text{ MW}$



EUV radiation within $\pm 2\%$ b.w.
@ 13.5 nm: $P = 1.2 \text{ kW}$

With the linear design of the GLSF unit completed, an output of kilowatt-level EUV radiation is attained for the first time within the current technical capabilities of laser cavities.



- Express Δz in terms of the particle coordinates at s_A using the Taylor-map representation.
- Derive the expressions for $\langle \Delta z \rangle$ and $\sigma_{\Delta z}$.
- Evaluate the 2nd and 4th-order beam moments at s_A and substitute them into $\langle \Delta z \rangle$ and $\sigma_{\Delta z}$ expressions.
- Sort expressions for $\langle \Delta z \rangle$ and $\sigma_{\Delta z}$ by beam parameters, namely ϵ_x , ϵ_y , σ_{δ_0} , as well as h .

$$\langle \Delta z \rangle = \epsilon_x \Omega_1 + \epsilon_y \Omega_2 + \sigma_{\delta_0}^2 \Omega_3 + \frac{h^2}{2k^2} \Omega_4$$

$$\sigma_{\Delta z}^2 = \epsilon_x^2 \Sigma_1 + \epsilon_y^2 \Sigma_2 + \epsilon_y \sigma_{\delta_0}^2 \Sigma_3 + \epsilon_y \frac{h^2}{k^2} \Sigma_4 + \sigma_{\delta_0}^4 \Sigma_5 + \sigma_{\delta_0}^2 \frac{h^2}{k^2} \Sigma_6 + \frac{h^4}{k^4} \Sigma_7$$

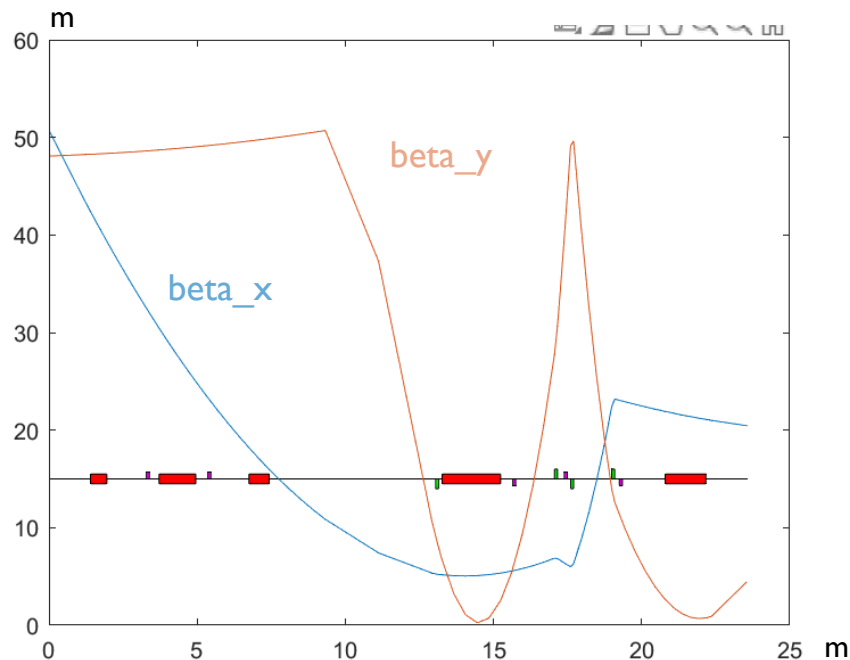
$$\Omega_1 = T_{511} \beta_x - 2T_{521} \alpha_x + T_{522} \gamma_x$$

$$\Omega_2 = T_{533} \beta_y - 2T_{543} \alpha_y + T_{544} \gamma_y$$

$$\Omega_3 = T_{533} D^2 + 2T_{543} DD' + T_{544} D'^2 + 2T_{563} D + 2T_{564} D' + T_{566}$$

$$\Omega_4 = T_{566}$$

Realization of lattice between modulators. Tried different layouts.
MOGA is used to find solutions. Goal is $\langle \Delta z \rangle$ and $\sigma_{\Delta z}$.



emit_x = 5.13 nmrads
emit_y = 4.60 pmrad
sigma_delta = 9.44e-4
 $\lambda_m = 532$ nm

E = 600 MeV
h = 2560 m⁻¹
Hy_rad = 0.87 μ m
Hy_mod = 0.19 m

beta_max = 50.7 m
beta_min = 0.25 m
eigen-emit_y = 1.19 pmrad
rho = 65.6 m

Sextuple off

Sextuple on

$\langle \Delta z \rangle = 13$ nm

$\langle \Delta z \rangle = \mathbf{0.06}$ nm

$\sigma_{\Delta z} = 17$ nm

$\sigma_{\Delta z} = \mathbf{0.09}$ nm



- SSMB is a novel light source with the capability of generating high-average-power short-wavelength coherent radiation.
- The GLSF approach can establish nanometer-long ring-stored bunches through beam manipulation in 4-D vertical-longitudinal coupled phase space. In linear demonstrations, an output of kilowatt-level EUV radiation can be realized within the current technical capabilities of laser cavities.

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**Generalized longitudinal strong focusing
in a steady-state microbunching storage ring**

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Thank you for your time.