



From experimental data to FY evaluation :

APRENDE

JEFF4.0 and future program

<u>Ces</u>

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APRENDE Subtask 4.3.1 Fission yield evaluation



Theoretically

Experimentally

 $Y(A^*, Z, E^*, J^{\pi}) = Y(A^*, Z) \times P(E_K | A^*, Z) \times P(E^*, J^{\pi} | A^*, Z, EK) \leftrightarrow Y(A, Z, E_K, I) = Y(A) \times P(Z | A, E_K) \times P(E_k | A, Z) \times P(m | A, Z, E_K)$

Pre-neutrons Mass, charge, excitation energy Mass Charge Kinetic Energy Isomeric

Applications : Y(A, Z, m) independent fission yields \rightarrow Decay data \rightarrow C(A, Z, m) Cumulative fission yields

In JEFF evaluation, independent and cumulative yields are two different evaluations due to the precise knowledge of chain yields (by radiochemical methods)

Full statistical description of fission observables : mean value, variance, covariance , PDF

- Evaluations / measurements : no/ rare available covariance
 - Major constraint for covariance matrix
- Variance(Mass) = \sum Var(Isotope) + \sum Cov (Isotopes) \rightarrow expected < \sum Var(Isotope)
- In current evaluations Variance(Mass) > Var(major Isotope)

Mass = \sum Isotope

JEFF-4 Goal → New methodology : complete and consistent



Gaussian compatibility tests and sorting of data

Example of re-interpretation of experimental data: reproducibility

Fickel1959 Chain yields

TABLE IX Mass spectrometric and isotope dilution data for Cs133 produced in the thermal neutron					ermal neutron
Sample	Isotope	Ratio before isotope dilution	No. of atoms of isotope added per g of Pu ²³⁹ , ×10 ¹⁹	Ratio after isotope dilution	Calculated fission yield, atoms×10 ¹⁸ /g Pu ²²⁹
9	133 137	$1.000 \\ 0.9329 \pm 0.0089$	5.938	$1.000 \\ 0.1421 \pm 0.0008$	16.01
8	133 137	$1.000 \\ 0.9322 \pm 0.0089$	7.853	$1.000 \\ 0.1765 \pm 0.0010$	18.35
3	133 137	$1.000 \\ 0.9233 \pm 0.0135$	5.938	$^{1.000}_{0.02144\pm0.00028}$	1.145

TABLE X
Mass spectrometric and isotope dilution data for Sr^{90} produced in the thermal neutron fission of Pu^{239}

Sample	Isotope	Ratio before isotope dilution	No. of atoms of isotope added per g of Pu ²³⁹ , ×10 ¹⁹	Ratio after isotope dilution	Calculated fission yield, atoms×10 ¹⁸ /g Pu ²³⁹
9	88 90	${0.6595 {\pm 0.0062}\atop{1.000}}$	1.274	3.307 ± 0.022 1.000	4.846
8	88 90	0.6599 ± 0.0062 1.000	1.122	2.593 ± 0.011 1.000	5.849
3	88 90	${}^{1.191\pm0.012}_{1.000}$	0.6678	1.975 ± 0.035 1.000	0.3656

FICKEL AND TOMLINSON: LIGHT MASS FRAGMENTS

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TABLE XIII

Cumulative fission yields of the light fragments in the thermal neutron fission of Pu²²⁹ normalized to the 6.90% Cs¹³³ yield

	Sample 3		Sample 8		Sample 9		Average
Isotopic - mass	Atoms×1018	% yield	Atoms×1018	% yield	Atoms×1018	% yield	% yield
72-82							0.59*
Kr ⁸³							0.29
Kr ⁸⁴			1 460	0 5456	1 262	0 5251	0.535
Rb ⁸⁵ (Kr ⁸⁰)			1.400	0.0400	1.202	0.0101	0.75
RL87			2.487	0.9291	0.2150	0.8942	0.912
Sr ⁸⁸	0.2387	1.438	3.819	1.440	3.164	1.368	1.43
Sr ⁸⁹	0.2868	1.728	4.589	1.726	3.802	1.639	1.71
Sr90	0.3656	2.203	5.849	2.199	4.846	2.089	2.10
Zr ⁹¹							2.09
Zr ⁹²							3.94
Zr ³⁵ 7-94							4.45
Mo ⁹⁵ (Zr ⁹⁵)			13.37	5.025	11.58	4.991	4.99
Zr ⁹⁶							5.13
Mo ⁹⁷			14.97	5.630	12.97	5.590	5.61
Mo ⁹⁸			15.60	5.861	13.50	5.818	5.84 6 11*
99			1 000	7 079	1 690	7 020	7 05
Mo ¹⁰⁰			1.882	1.012	13 60	5.860	5.86
Rulo					13.78	5.939	5.94
Ru ¹⁰²					13.06	5.626	5.63
R11104					13.64	5.877	5.88
105							5.50*
Ru106					1,051	4.530	4.53
107							3.40
108							2.44*
109							0.76*
110							0.271
111							0.10†
112							0.080*
114							0.060*
115							0.041*
116 - 118		c 00	10.95	6 00	16 01	6.00	0.122^*
Cs133	1.45	6.90	18.35	0.90	10.01	0.90	
Total % yie	ld					:	100.12

*Interpolated values.

†Radiochemical yields.

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Fickel1959 Chain yields

A	Sample 1	Sample 2	Sample 3	Emirical Mean	Empirical Sandard Deviation	Student Standard deviation
83	0.29					
84	0.47					
85	0.5456	0.5251		0.53535	0.0145	4.9%
86	0.75					
87	0.9291	0.8942		0.91165	0.0247	4.9%
88	1.438	1.44	1.368	1.41533333	0.0580	5.4%
89	1.728	1.726	1.639	1.69766667	0.0719	5.6%
90	2.203	2.199	2.089	2.16366667	0.0915	5.6%
91	2.59					
92	3.12					
93	3.94					
94	4.45					
95	5.025	4.991		5.008	0.0240	0.9%
96	5.13					
97	5.63	5.59		5.61	0.0283	0.9%
98	5.861	5.818		5.8395	0.0304	0.9%
100	7.072	7.02		7.046	0.0368	0.9%
101	5.86					
102	5.94					
103	5.63					
104	5.88					
106	4.53					
109	1.5					
111	0.27					
112	0.1					
133	6.9					
			1			
				Mean S	Student Unc.	3.34%
				Min S	Student Unc.	0.9%

	А	Sample 1	Sample 2	Emirical Mean	Empirical Sandard Deviation	Student Standard deviation
	131	3.8	3.73	3.77	0.0495	2.4%
	132	5.3	5.21	5.26	0.0636	2.2%
	133	6.96	6.83	6.90	0.0919	2.4%
	134	7.52	7.39	7.46	0.0919	2.2%
	135	7.32	7.17	7.25	0.1061	2.7%
	136	6.69	6.56	6.63	0.0919	2.5%
	137	6.54	6.42	6.48	0.0849	2.4%
	138	0	6.25	6.25		3.0%
	140	5.5	5.66	5.58	0.1131	3.7%
	142	4.9	5.03	4.97	0.0919	3.4%
	143	4.5	4.61	4.56	0.0778	3.1%
	144	3.78	3.89	3.84	0.0778	3.7%
	145	3.08	3.16	3.12	0.0566	3.3%
	146	2.53	2.6	2.57	0.0495	3.5%
-	147	2.02	1.96	1.99	0.0424	3.9%
L	148	1.69	1.73	1.71	0.0283	3.0%
	149	1.32	1.28	1.30	0.0283	4.0%
	150	1	1.03	1.02	0.0212	3.8%
	151	0.814	0.79	0.80	0.0170	3.8%
	152	0.625	0.606	0.62	0.0134	4.0%
	154	0.297	0.289	0.29	0.0057	3.5%

Mean Student Unc.	3.2%
Min Student Unc.	2.2%

Example of re-interpretation of experimental data: experimental correlation matrix

	Fickel1959_a
	A 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 100 101 102 103 104 106 109 111 112 133
	83 1.000 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.064 0.064 0.064 0.064 0.179 0.064 0.175 0.172 0.171 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.253 1
	84 0.064 1.000 0.044 0.064 0.044 0.041 0.039 0.039 0.054 0.064 0.064 0.064 0.179 0.064 0.172 0.171 0.064 0.0
Lowest possible	85 0.044 0.0
	87 0.044 0.044 0.871 0.044 1.000 0.028 0.027 0.027 0.044 0.044 0.044 0.044 0.123 0.044 0.120 0.118 0.118 0.044 0.044 0.044 0.044 0.044 0.044 0.044 0.175 0.6
estimation of the	88 0.041 0.041 0.028 0.041 0.028 1.000 0.612 0.789 0.041 0.041 0.041 0.041 0.113 0.041 0.110 0.109 0.108 0.041 0.041 0.041 0.041 0.041 0.041 0.041 0.041 0.041 0.160 0.5
	89 0.039 0.039 0.027 0.039 0.027 0.612 1.000 0.776 0.039 0.039 0.039 0.039 0.110 0.039 0.107 0.105 0.105 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.155 0.4
correlation matrix	90 0.039 0.039 0.027 0.039 0.027 0.789 0.776 1.000 0.039 0.039 0.039 0.039 0.110 0.039 0.107 0.105 0.105 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.039 0.155 0.3
	91 0.064 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 1.000 0.344 0.713 0.482 0.346 0.508 0.175 0.172 0.171 0.064 0.0
	93 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.713 0.482 1.000 0.677 0.626 0.713 0.172 0.171 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.253 0
	94 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.482 0.326 0.677 1.000 0.423 0.482 0.175 0.172 0.171 0.064 0.0
	95 0.179 0.179 0.123 0.179 0.123 0.113 0.110 0.110 0.146 0.302 0.626 0.423 1.000 0.345 0.488 0.241 0.411 0.179 0.1
	96 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.508 0.344 0.713 0.482 0.345 1.000 0.175 0.348 0.595 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.064 0.253 -0.3
	97 0.175 0.175 0.120 0.175 0.120 0.110 0.107 0.107 0.175 0.175 0.175 0.175 0.175 1.000 0.467 0.467 0.475 0.17
	100 0.172 0.172 0.118 0.172 0.118 0.109 0.105 0.105 0.172 0.172 0.172 0.172 0.241 0.348 0.467 1.000 0.386 0.172 0.17
	101 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.064 0.064 0.064 0.064 0.179 0.064 0.175 0.172 0.171 1.000 0.701 0.794 0.698 0.363 0.064 0.064 0.064 0.253 -0.7
Fickal1959 b	102 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.064 0.064 0.064 0.064 0.064 0.179 0.064 0.175 0.172 0.171 0.701 1.000 0.557 0.489 0.254 0.064 0.064 0.064 0.253 -0.8
D	103 0.064 0.064 0.044 0.064 0.044 0.041 0.039 0.039 0.064 0.064 0.064 0.064 0.179 0.064 0.175 0.172 0.171 0.794 0.557 1.000 0.554 0.288 0.064 0.064 0.064 0.253 -0.9
0 131 132 133 134 135 136 137 138 140 142 1	43 144 145 146 147 148 149 150 151 152 154 4 0.064 0.179 0.064 0.175 0.172 0.171 0.698 0.489 0.554 1.000 0.253 0.064 0.064 0.064 0.253 -1
131 1.000 0.105 0.772 0.131 0.113 0.118 0.124 0.101 0.084 0.091 0.0	98 0.083 0.093 0.087 0.080 0.101 0.078 0.081 0.080 0.078 0.087 0.084 0.179 0.064 0.175 0.172 0.171 0.565 0.254 0.255 1.000 0.064 0.064 0.064 0.253
132 0.105 1.000 0.081 0.141 0.121 0.127 0.134 0.109 0.090 0.098 0.1	05 0.090 0.100 0.094 0.086 0.108 0.084 0.087 0.086 0.084 0.094 0.094 0.064 0.179 0.064 0.172 0.171 0.064 0.06
133 0.772 0.081 1.000 0.130 0.111 0.117 0.123 0.100 0.082 0.090 0.0	97 0.082 0.092 0.086 0.079 0.100 0.077 0.080 0.079 0.077 0.086 4 0.064 0.179 0.064 0.175 0.172 0.171 0.064 0.064 0.064 0.064 0.064 0.064 0.064 1.000 0.253
134 0.131 0.141 0.130 1.000 0.119 0.493 0.132 0.802 0.088 0.096 0.1	04 0.088 0.098 0.092 0.084 0.107 0.083 0.086 0.085 0.082 0.092 3 0.253 0
135 0.113 0.121 0.111 0.119 1.000 0.108 0.113 0.092 0.076 0.083 0.0	89 0.076 0.084 0.080 0.072 0.092 0.071 0.074 0.073 0.071 0.079
136 0.118 0.127 0.117 0.493 0.108 1.000 0.119 0.615 0.080 0.087 0.0	93 0.080 0.088 0.083 0.076 0.096 0.074 0.077 0.076 0.074 0.083
137 0.124 0.134 0.123 0.132 0.113 0.119 1.000 0.102 0.084 0.091 0.0	98 0.084 0.093 0.088 0.080 0.101 0.078 0.081 0.080 0.078 0.088
138 0.101 0.109 0.100 0.802 0.092 0.615 0.102 1.000 0.068 0.074 0.0	80 0.068 0.076 0.071 0.065 0.082 0.064 0.066 0.065 0.064 0.071
140 0.084 0.090 0.082 0.088 0.076 0.080 0.084 0.068 1.000 0.802 0.68	69 0.056 0.062 0.059 0.054 0.068 0.053 0.055 0.054 0.052 0.059
142 0.091 0.098 0.090 0.096 0.083 0.087 0.091 0.074 0.802 1.000 0.8	35 0.061 0.068 0.064 0.058 0.074 0.057 0.059 0.059 0.057 0.064
143 0.098 0.105 0.097 0.104 0.089 0.093 0.098 0.080 0.669 0.835 1.0	00 0.782 0.787 0.724 0.063 0.682 0.062 0.743 0.063 0.062 0.069
144 0.083 0.090 0.082 0.088 0.076 0.080 0.084 0.068 0.056 0.061 0.7	82 1.000 0.616 0.566 0.054 0.533 0.053 0.581 0.054 0.052 0.059
145 0.093 0.100 0.092 0.098 0.084 0.088 0.093 0.076 0.062 0.068 0.7	87 0.616 1.000 0.570 0.060 0.537 0.058 0.585 0.060 0.058 0.065
146 0.087 0.094 0.086 0.092 0.080 0.083 0.088 0.071 0.059 0.064 0.7	24 0.566 0.570 1.000 0.056 0.494 0.055 0.538 0.057 0.055 0.062
147 0.080 0.086 0.079 0.084 0.072 0.076 0.080 0.065 0.054 0.058 0.0	63 0.054 0.060 0.056 1.000 0.065 0.520 0.052 0.367 0.410 0.316
148 0.101 0.108 0.100 0.107 0.092 0.096 0.101 0.082 0.068 0.074 0.6	82 0.533 0.537 0.494 0.065 1.000 0.064 0.506 0.065 0.063 0.071
149 0.078 0.084 0.077 0.083 0.071 0.074 0.078 0.064 0.053 0.057 0.0	62 0.053 0.058 0.055 0.520 0.064 1.000 0.051 0.660 0.737 0.567
150 0.081 0.087 0.080 0.086 0.074 0.077 0.081 0.066 0.055 0.059 0.7	43 0.581 0.585 0.538 0.052 0.506 0.051 1.000 0.052 0.051 0.057
151 0.080 0.086 0.079 0.085 0.073 0.076 0.080 0.065 0.054 0.059 0.0	63 0.054 0.060 0.057 0.367 0.065 0.660 0.052 1.000 0.521 0.401
152 0.078 0.084 0.077 0.082 0.071 0.074 0.078 0.064 0.052 0.057 0.0	62 0.052 0.058 0.055 0.410 0.063 0.737 0.051 0.521 1.000 0.448
154 0.087 0.094 0.086 0.092 0.079 0.083 0.088 0.071 0.059 0.064 0.0	69 0.059 0.065 0.062 0.316 0.071 0.567 0.057 0.401 0.448 1.000

Uncertainty estimation form Lohengrin of historical method

Fig. 10 Impact of the correlation (E_k, q) on the estimation of the relative mass yields. The bias rises from 5 to 17% when the scan is performed at a charge state q that differs more from q_{mean} is observed. See text for details

A. Chebboubi Eur. Phys. J. A (2021) 57: 335

Test and sorting of available experimental data for the 4 main fissile nuclei

Only mass yields and chain yields used in these analyses

• S.-M. Cheikh, PhD thesis, UGA, 18 Oct. 2023

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 S.-M. Cheikh, G. Kessedjian et al., Covariance Workshop 2022, Tokyo, Japan, EPJ Web of Conferences 281, 00023 (2023)

Gaussian compatibility tests and sorting of data

JEFF-4 Goal \rightarrow New methodology : complete and consistent

- Previous FY evaluations :
- Independent and Cumulative FY evaluations are two different evaluations : only mean values follow conservation laws
- Driven by the cumulative data
- Uncertainties of Ind. FY are overestimated due to the lack of correlation matrix as by-product of the analysis
- Covariance/correlation matrix of Ind FY is extrapolated assuming the
 C. Devillers methodology : Assumption Corr (C, C') = I

• JEFF-4 Evaluation

- Independent and Cumulative FY come from a unique evaluation
- Take into account the experimental correlation matrix available or deduced from literature
- Complete description of the fission yield observables
- Consistent according to the conservation laws for : mean values, uncertainties and correlation matrices

S.-M. Cheikh, G. Kessedjian et al., Eur. Phys. J. A, 60 11 (2024) 222

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Test and sorting of available experimental data for the 4 main fissile nuclei

²³³U(n_{th},f): Mass yields

²³³U(n_{th},f): Exclusion plot

Mass Number

-0.2

G. Kessedjian et al. - JEFF Meeting Nov. 2024

(A,Z,m)

G. Kessedjian et al. - APRENDE WP2-WP4 workshop , 26-27 Fev. 2025

 \rightarrow New evaluated database – free of model input- – in order to test phenomenological fission models

²³⁵U(n_{th},f): From pre-n yields to post-n yields

$$Y_A = \sum_{\nu=0} Y_{A^*} \cdot P(\nu \mid A^*)$$
 with $A^* = A + \nu$

²³⁵U(n_{th},f): From Pre-neutron yields to post-neutron yields

A. Regonesi PhD Thesis (2024-2027)

$^{235}\text{U(n}_{th}\text{,f}\text{):}\,\,pre\text{-}n$ mass yield analysis \rightarrow MCMC method

G. Kessedjian et al. - APRENDE WP2-WP4 workshop, 26-27 Fev. 2025

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A. Regonesi PhD Thesis (2024-2027)

Perspectives : pre-n mass yield analysis \rightarrow MCMC method

Preliminary Results

Geltenbort's data : Exp. Resolution Res(A)~0.8 uma

Conclusion and perspectives

- Consistent evaluation of Mass Independant Cumulative Chain yields ^{233, 235}U(n_{th},f) & ^{229, 241}Pu(n_{th},f)
- ²³⁵U & ²³⁹Pu FY ENDF files are available in JEFF-4T4 Library
- ²³³U & ²⁴¹Pu FY ENDF files should be available in February 2025
- Tractability of the selected and used data is available

→ reinterpretation of EXP data with correlation matrix : must be preserved for the future !

- PhD thesis @ Cadarache (A. Regonesi 2024-2027) is ongoing :
 - \rightarrow Pre-n yield evaluation
 - \rightarrow prompt neutron emission evaluation per mass evaluation
 - \rightarrow neutron energy dependent fission yield studies : ²³⁵U, ²³⁸U ...

Combined analysis to post-n evaluation

- Middle term perspectives correspond to the use of the new Charge distribution per mass with the correlation matrix from the Direct-Zp model based on pre-neutron parameters (replacing the Wahl Systematics)
 - \rightarrow Results from Sidi. M. Cheikh Thesis \rightarrow JEFF-4.1
 - \rightarrow New PhD project (2025-2028) on P(Z|A) and cumulative yields should be start.

Perspectives : pre-n mass yield analysis \rightarrow **MCMC method**

Preliminary Results

JEFF-4 Goal \rightarrow New methodology : complete and consistent

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jefdoc-1902 jefdoc-2007 jefdoc-2038 jefdoc-2038 jefdoc-2056 jefdoc-2027 jefdoc-2203 jefdoc-2204 jefdoc-2205 jefdoc-2207 jefdoc-2295 jefdoc-2295 jefdoc-2370 jefdoc-2371 jefdoc-2372

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Thank you for your attention

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JEFF-4 Goal \rightarrow New methodology : complete and consistent

²³⁵U(n_{th},f): JEFF-4T4

²³⁵U(n_{th},f): JEFF-4T4

²³⁵U(n_{th},f): JEFF-4T4

²³⁵U(n_{th},f): Exclusion plot in reference to JEFF-4T4 evaluation

 \rightarrow New evaluated database – free of model input- – in order to test phenomenological fission models

G. Kessedjian et al. - APRENDE WP2-WP4 workshop , 26-27 Fev. 2025

→ New evaluated database – free of model input – in order to test phenomenological fission models

241Pu(n_{th},f) Chain Yields 2025

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241Pu(n_{th},f) Chain Yields 2025

²³⁵U(n_{th},f): Exclusion plot in reference to JEFF-4T4 evaluation

²³⁵U(n_{th},f): From pre-n yields to post-n yields

²³⁵U(n_{th},f): From Pre-neutron yields to post-neutron yields

235 U(n_{th},f): From Pre-neutron yields to post-neutron yields \rightarrow Sensitivity to Y(A*)

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²³⁵U(n_{th},f): From Pre-neutron yields to post-neutron yields \rightarrow Sensitivity to $\nu(A^*)$

Perspectives : pre-n mass yield analysis \rightarrow MCMC method

Geltenbort's data : Exp. Resolution Res(A)~0.8 uma

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Back-up