

# PIONIC HYDROGEN

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*PIONIC HYDROGEN collaboration*

*PSI experiments R-98.01 & R.06.03*

# **X-ray spectroscopy of exotic atoms**

***pionic and muonic hydrogen***

***pionic deuterium***

***goal - strong-interaction effects to  $\approx 1\%$***

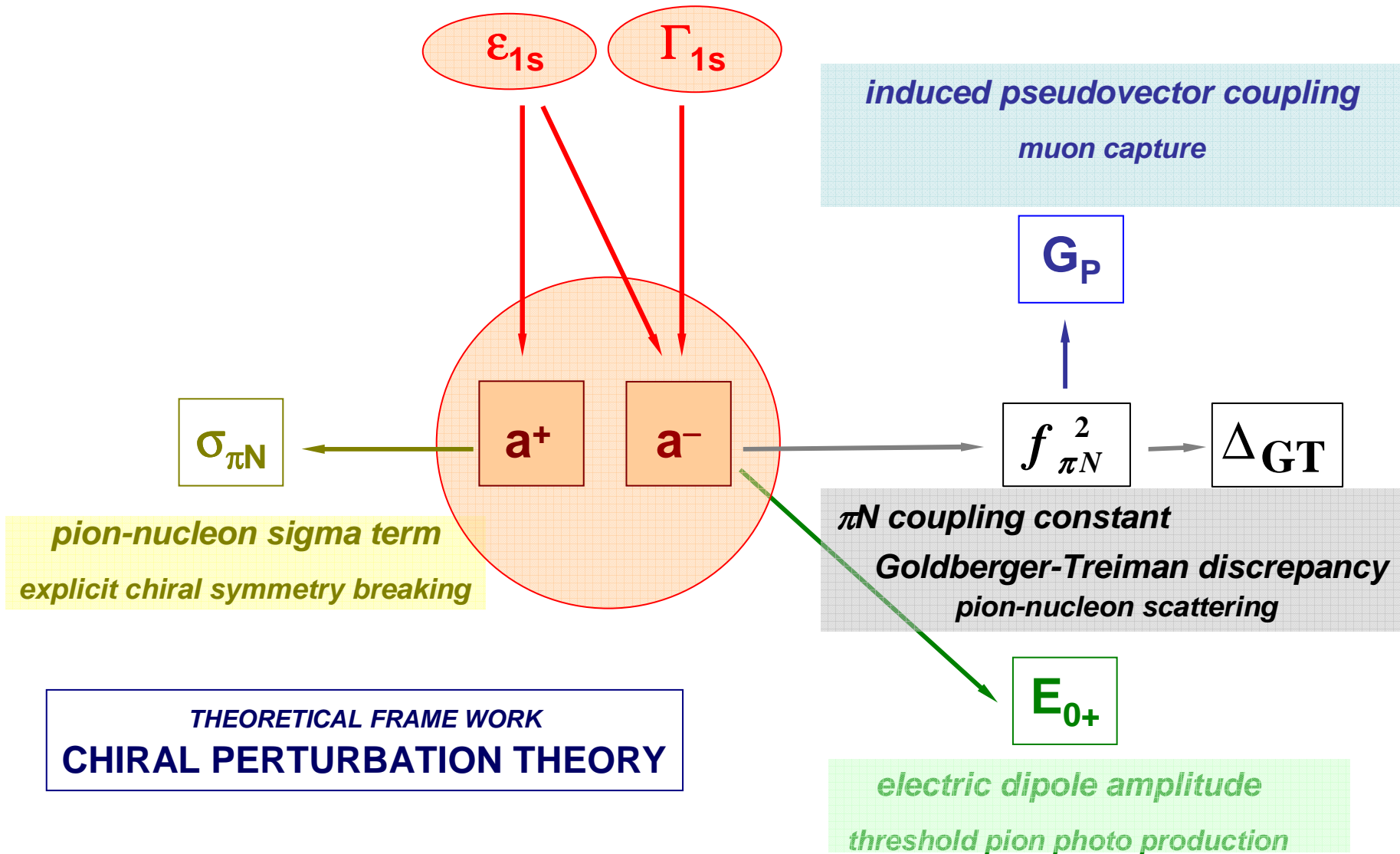


# PION-NUCLEON SCATTERING LENGTHS

$a^{\pm}$

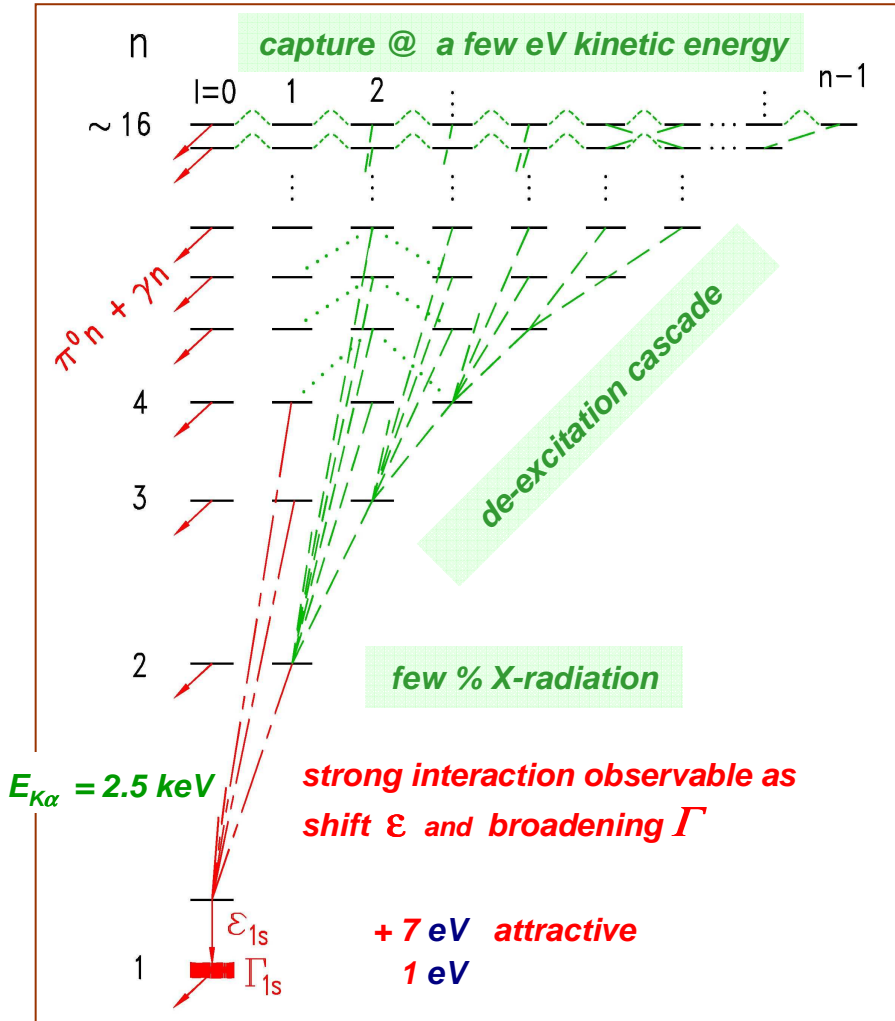
# PION-NUCLEON SCATTERING LENGTHS

related quantities



# PIONIC HYDROGEN - $\pi N$ scattering at „rest“

which scattering length where?



$$\pi H \epsilon_{1s} \propto a_{\pi-p \rightarrow \pi-p} \propto a^+ + a^- + \dots$$

$$\pi H \Gamma_{1s} \propto (a_{\pi-p \rightarrow \pi^0 n})^2 \propto (a^-)^2 + \dots$$

$$\pi D \epsilon_{1s} \propto a_{\pi-p \rightarrow \pi-p} + a_{\pi-n \rightarrow \pi-n} \propto 2 \cdot a^+ + \dots$$

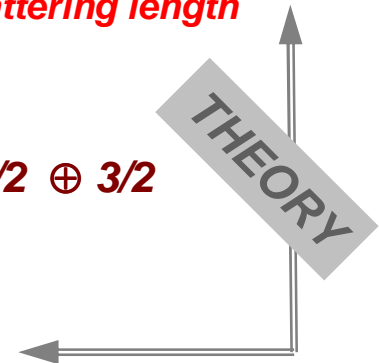
$a^\pm =$  isospin even/odd scattering length

$$\text{isospin } 1 \otimes 1/2 \Rightarrow 1/2 \oplus 3/2$$

isospin breaking corrections  
few-body effects etc,  
under control !!!

different

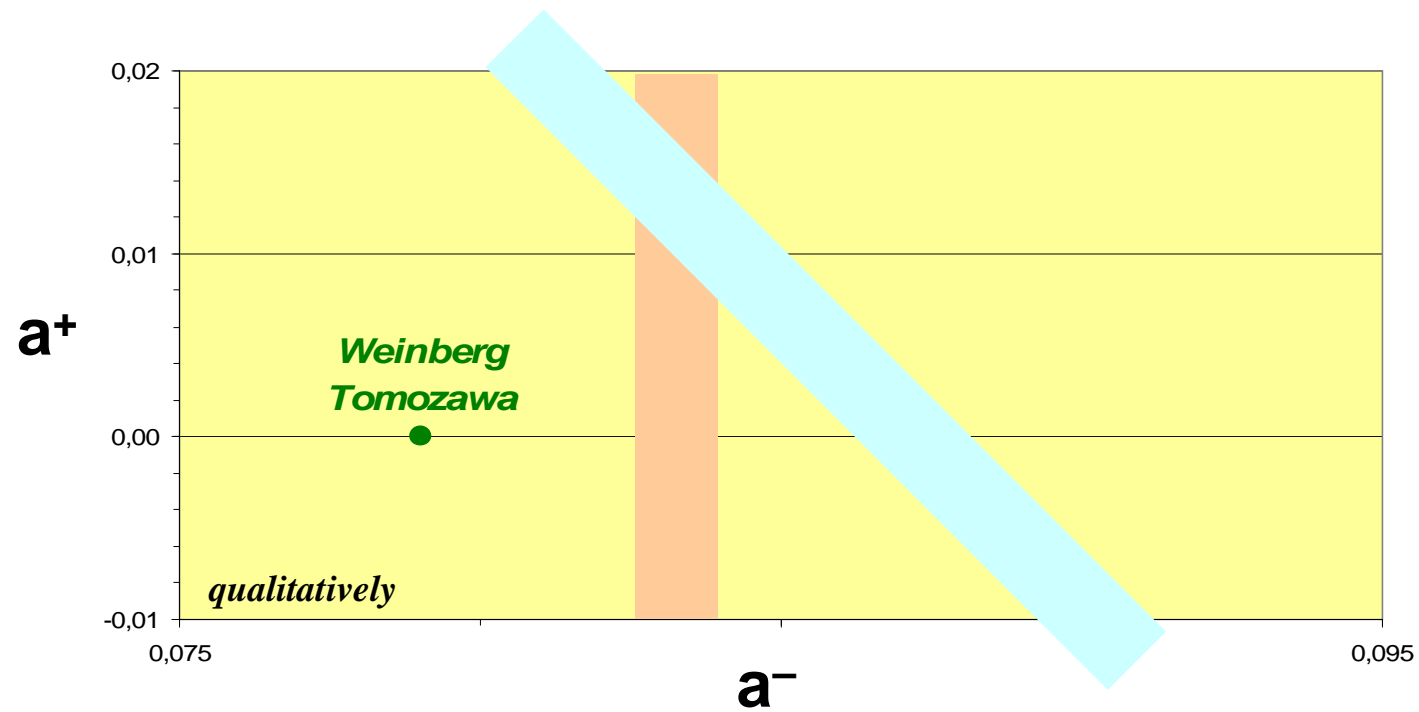
$$\text{!!! } \pi D \Gamma_{1s} \propto \Im a_{\pi-d \rightarrow nn+nny}$$



## constraints for $a^\pm$ from $\pi\text{H}$

$$\pi\text{H} \quad \varepsilon_{1s} \propto f(a^+, a^-, \text{LEC}(c_1, f_1, f_2))$$

$$\pi\text{H} \quad \Gamma_{1s} \propto [f(a^-, \text{LEC}(c_1, f_2))]^2$$

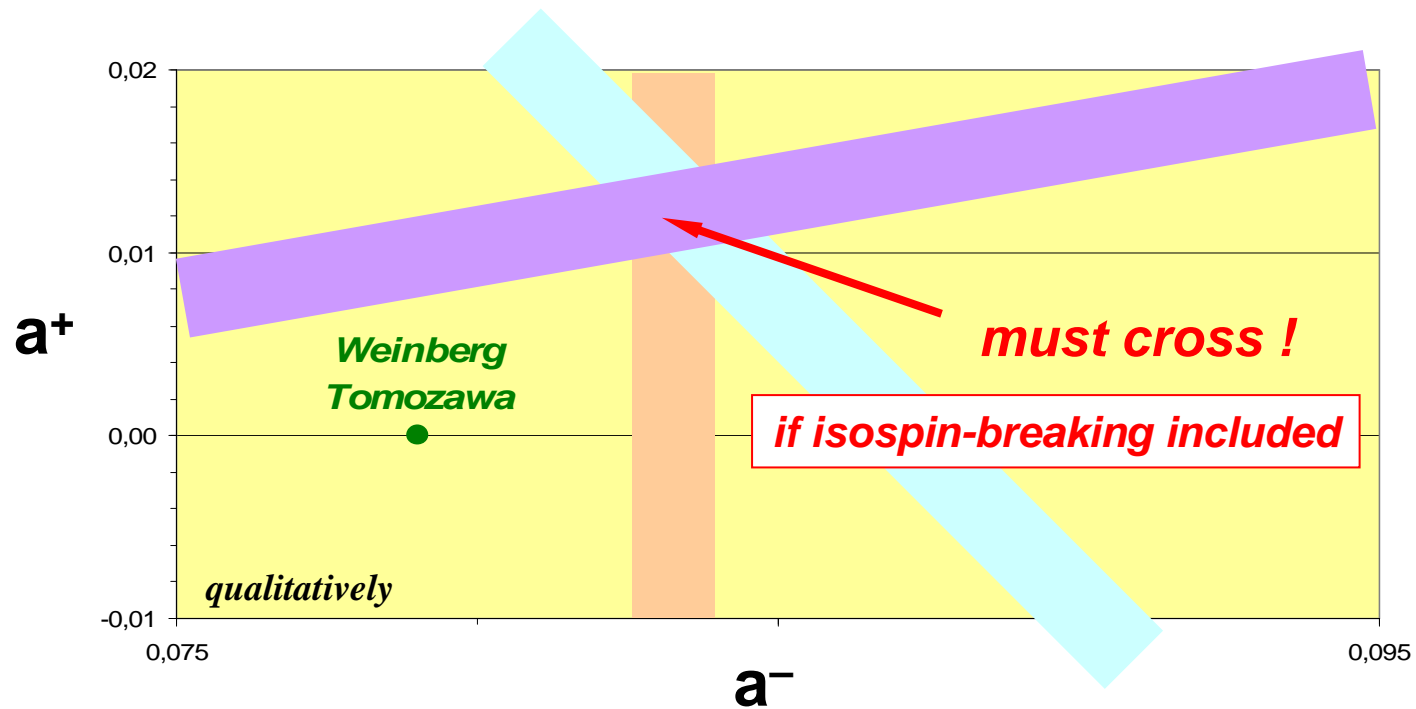


## constraints for $a^\pm$ from $\pi\text{H}$ and $\pi\text{D}$

$$\pi\text{H} \quad \varepsilon_{1s} \quad \propto f(a^+, a^-, \text{LEC}(c_1, f_1, f_2))$$

$$\pi\text{H} \quad \Gamma_{1s} \quad \propto [f(a^-, \text{LEC}(c_1, f_2))]^2$$

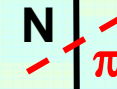
$$\pi\text{D} \quad \varepsilon_{1s} \quad \propto f(a^+, a^-, \text{LEC}(c_1, f_1, f_2))$$



# HYDROGEN & DEUTERIUM - ORIGIN OF $\Gamma_{1s}$

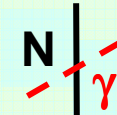
$\pi H$  scattering  $\pi^- p \rightarrow \pi^0 n + n \gamma$

CEX scattering



$\pi D$  absorption  $\pi^- d \rightarrow nn + nn \gamma$

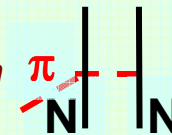
radiative capture



BR are well known from experiment

$NN \leftrightarrow NN\pi$   
s-wave pion production/absorption

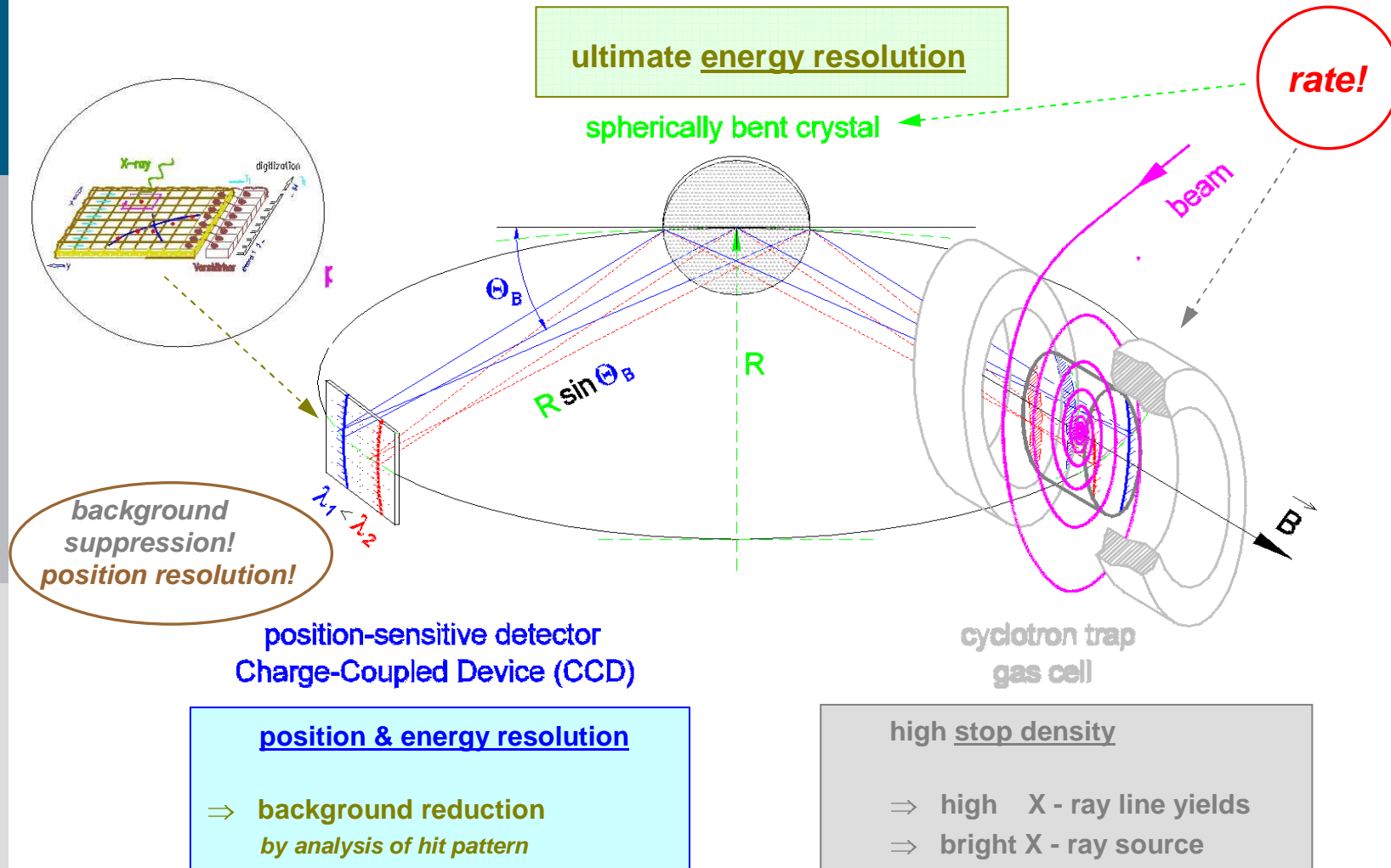
„true“ absorption



# EXPERIMENT

- *How to produce a suitable X-ray source?*
- *What about background?*
- *Resolution of the crystal spectrometer ?*

# Johann-type SET-UP



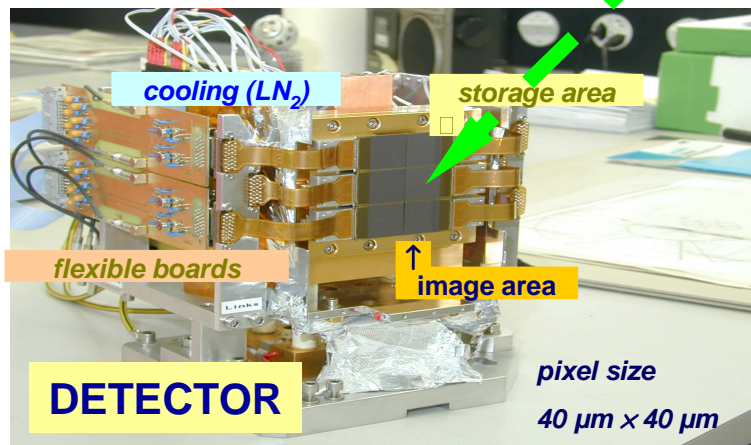
L. Simons, *Physica Scripta* 90 (1988), *Hyperfine Int.* 81 (1993) 253



*spherically curved*

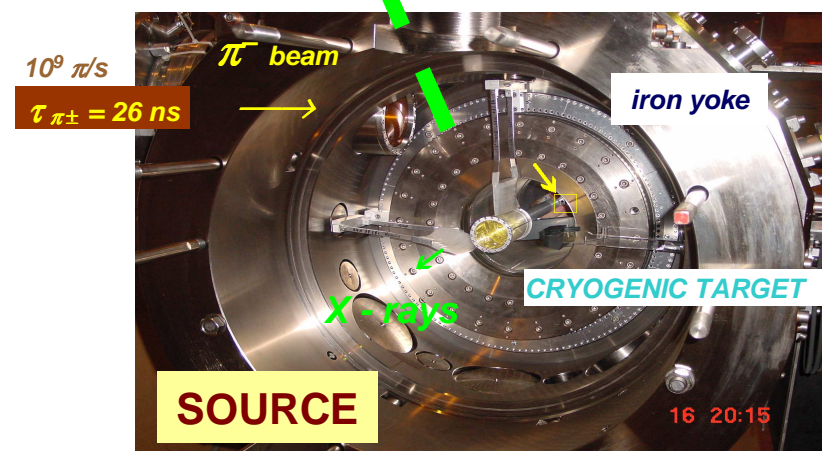
$R = 3\text{ m}$   
 $\Phi = 10\text{ cm}$

**Large - Area Focal Plane Detector**

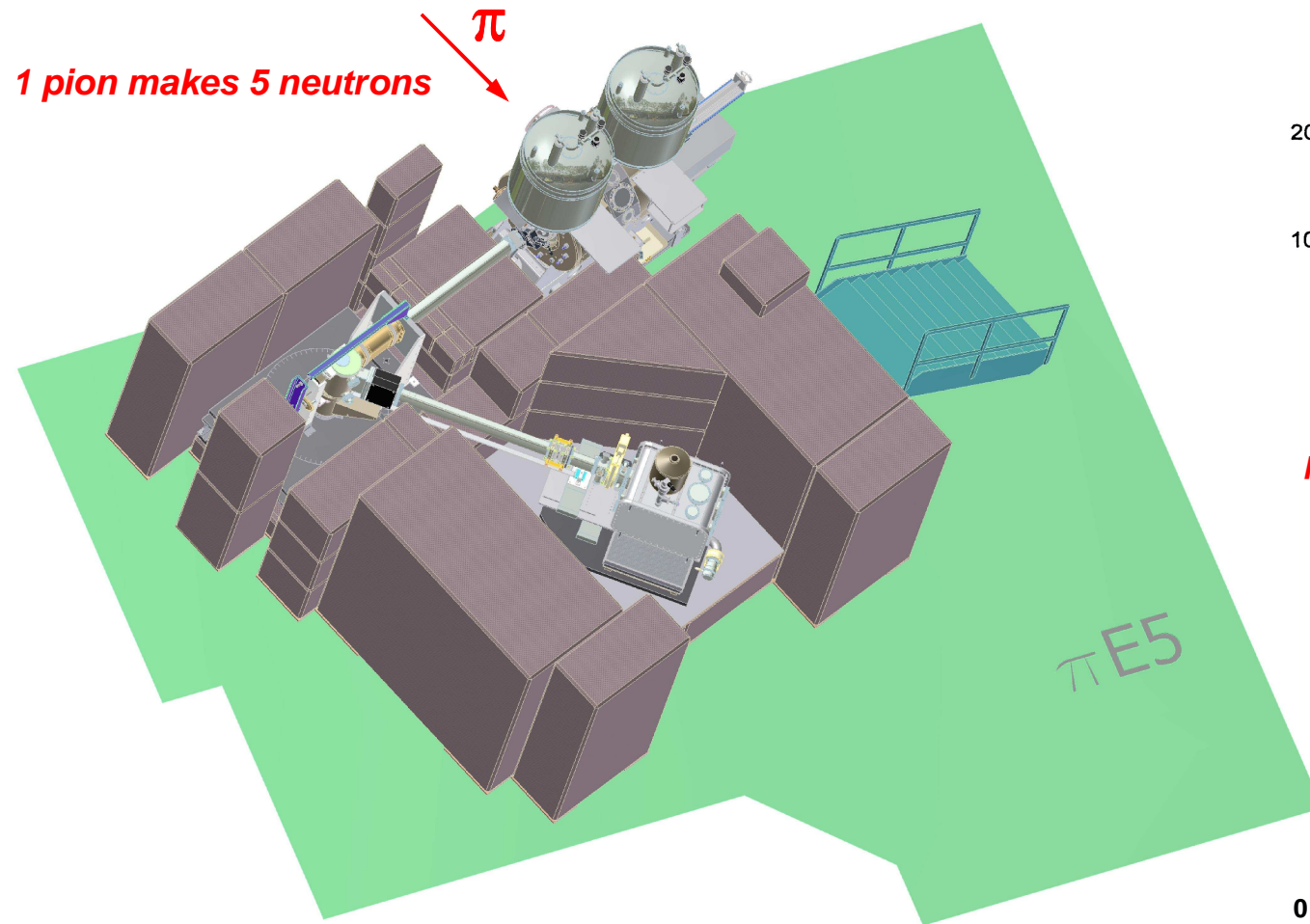


**CYCLOTRON TRAP**

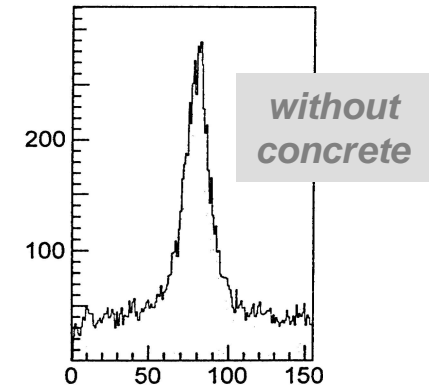
*one coil removed*



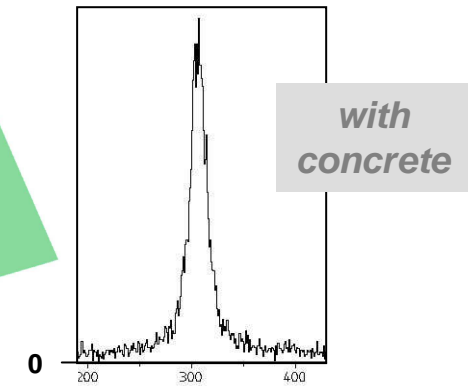
# TYPICAL SET-UP at PSI



*pionic hydrogen*



*peak/background x 10*

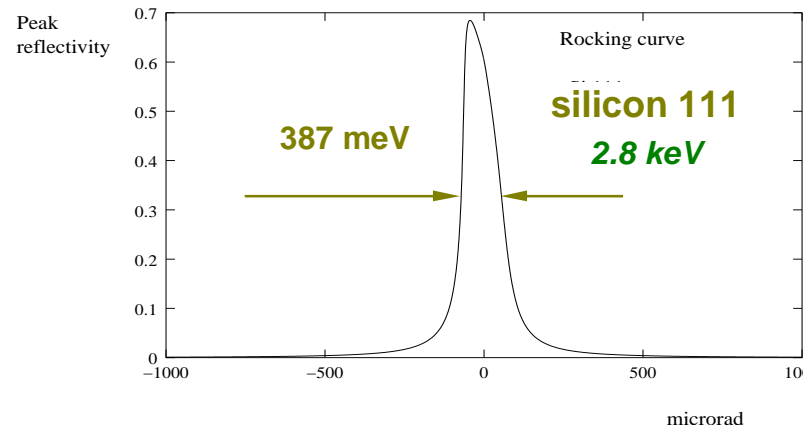


# CRYSTAL RESOLUTION

*dynamical theory  
of diffraction*

*XOP2 code  
plane crystal*

*Sanchez, del Rio, 1995*



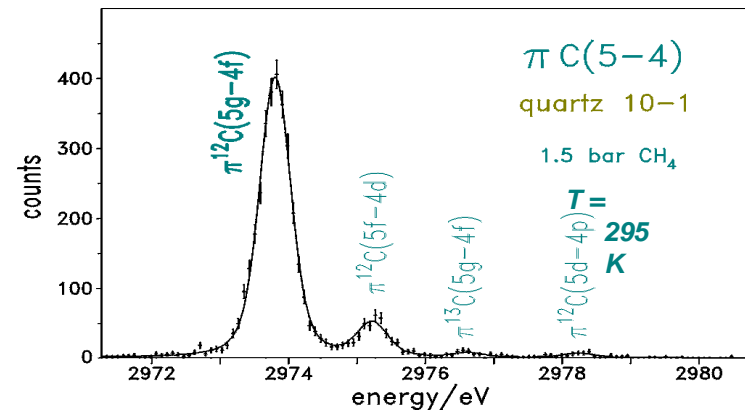
*for real crystal mounting?*



*measurement indispensable!*

*no narrow few keV  $\gamma$  lines available*

*exotic atom - pionic carbon*



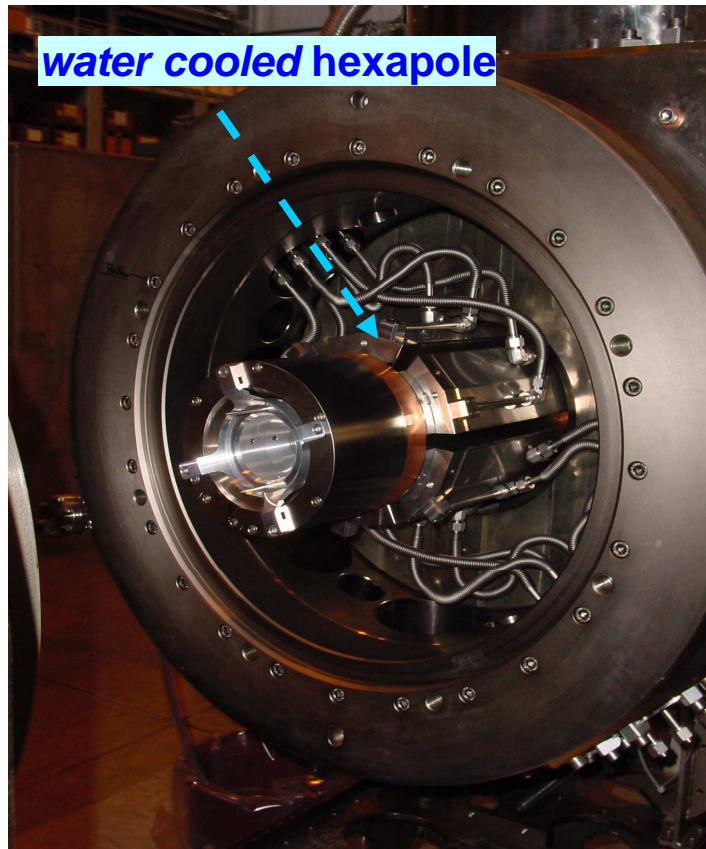
*closest to energy  
of  $\square \text{H}(4p-1s)$*

*3500 events in 70 h - needed 10 x more*

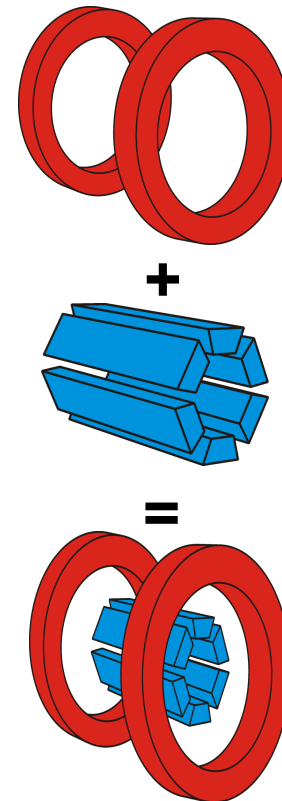
*accuracy limited by rate !*

# ECRIT = Electron Cyclotron Resonance Ion Trap

"misuse" ion source as X-ray source



water cooled hexapole



Superconducting coils

- cyclotron trap

permanent hexapole

- AECR-U type
- 1 Tesla at the hexapole wall
- open structure

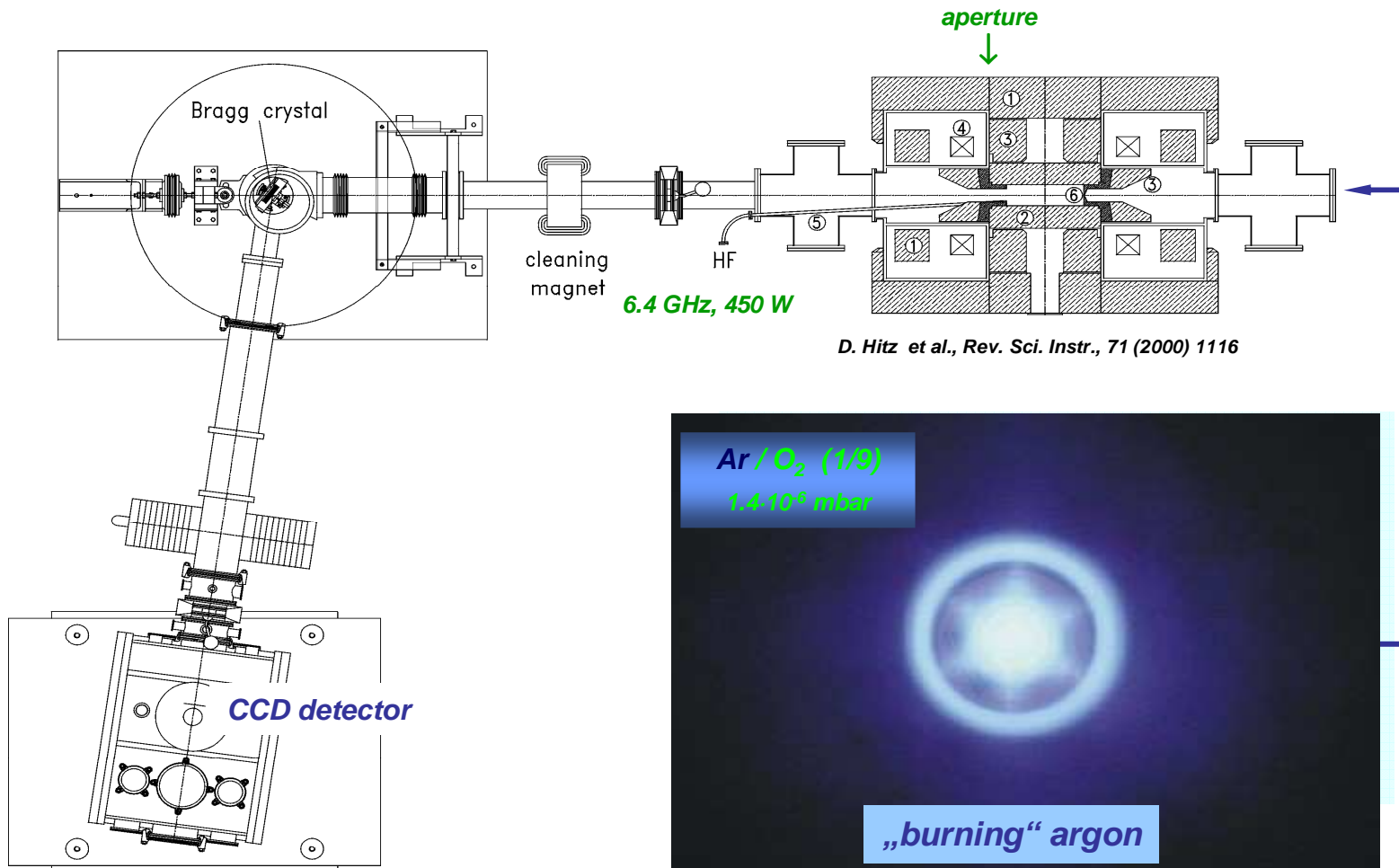
large mirror ratio = 4.3

$$B_{\max} / B_{\min} !$$

S. Biri, L. Simons, D. Hitz et al., Rev. Sci. Instr., 71 (2000) 1116  
K. Stiebing, Frankfurt – design assistance

# CRYSTAL SPECTROMETER and PSI ECRIT

Electron Cyclotron Resonance Ion Trap  
= cyclotron trap (4) + hexapole magnet (2)

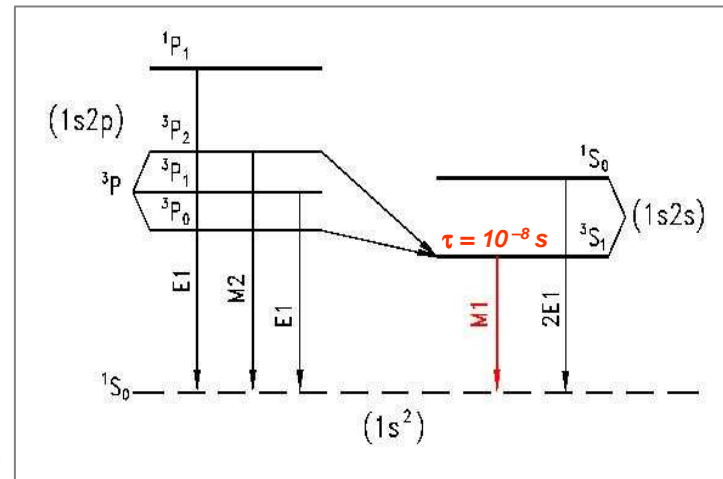
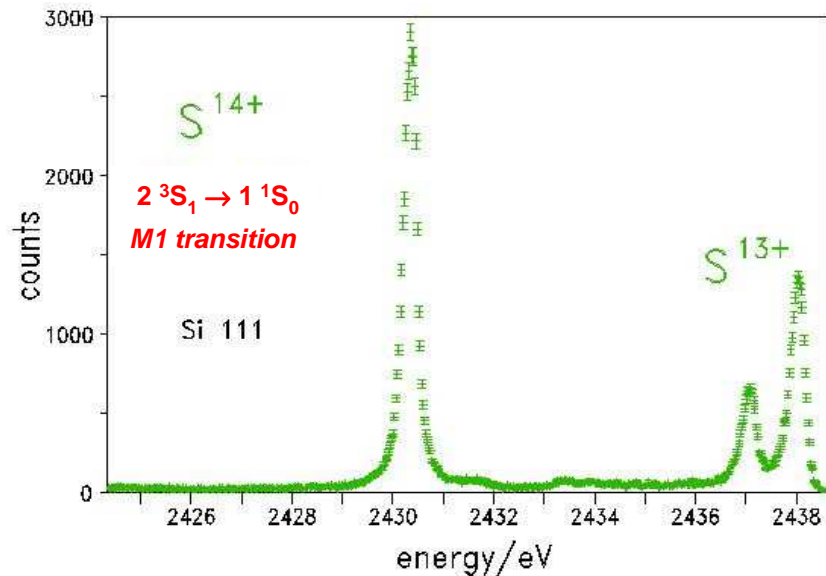


## SPECTROMETER RESPONSE at $\pi H$ Lyman ENERGIES

**M1 transitions** in He - like S  $\Leftrightarrow \pi H(2p-1s)$

Cl  $\Leftrightarrow \pi H(3p-1s)$

Ar  $\Leftrightarrow \pi H(4p-1s)$



**30000 events in line (3 h)  $\Leftrightarrow$  tails can be fixed with sufficient accuracy**

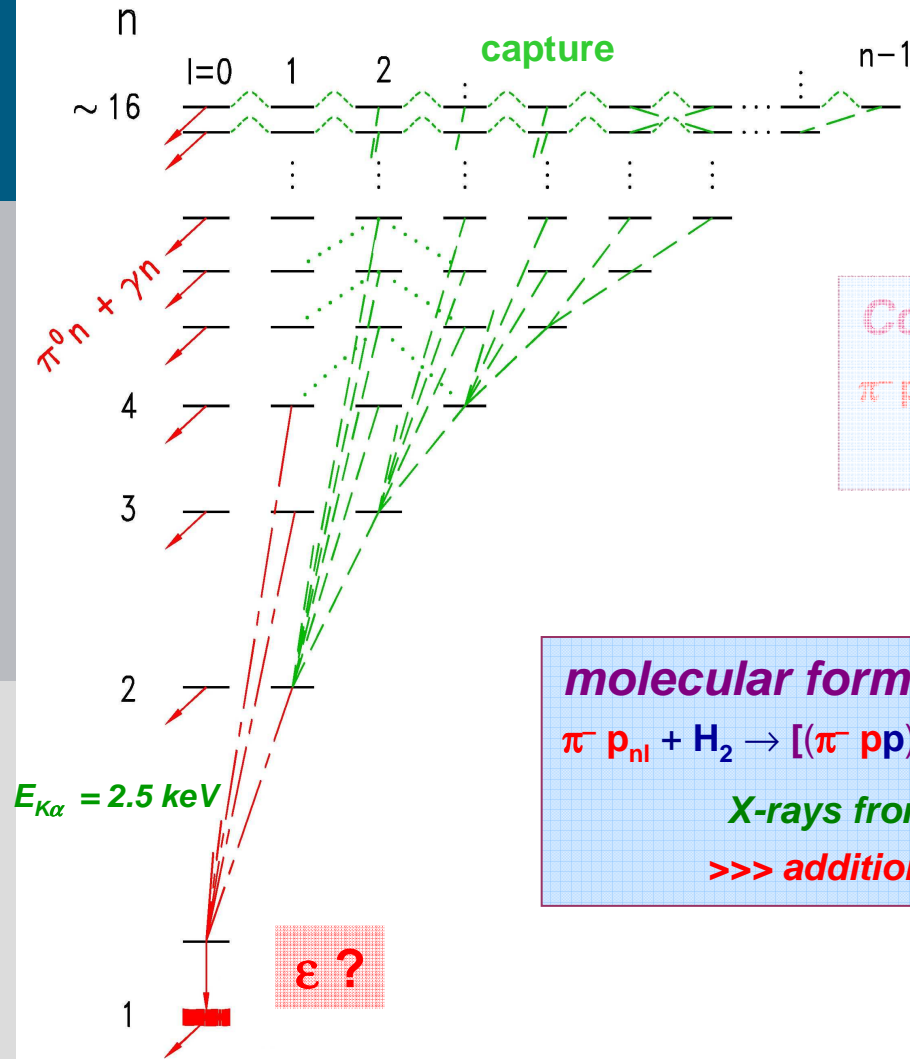
**to be compared with Monte-Carlo ray tracing folded with plane crystal response**

D.F.Anagnostopoulos et al., Nucl. Instr. Meth. B 205 (2003) 9  
D.F.Anagnostopoulos et al., Nucl. Instr. Meth. A 545 (2005) 217

# OBSTACLES

- *Molecular formation*
- *Coulomb de-exciatation*

# $\pi\text{H}$ - ATOMIC CASCADE I



**density dependent**

**Coulomb de-excitation**  
 $\pi p_{nl} + \text{H} = \text{H} \rightarrow \pi p_{n'l'} + \text{H} + \text{H} + \text{kinetic energy}$   
 $\gg \gg \text{Doppler broadening} \ll \ll$

**molecular formation**  
 $\pi p_{nl} + \text{H}_2 \rightarrow [(\pi pp)_{njv} \cdot p] ee_{kv} \text{ decay by Auger process}$   
**X-rays from molecular states ?**  
 $\gg \gg \text{additional energy shift ?} \ll \ll$

# MOLECULAR POTENTIALS

known to exist from muon-catalysed fusion,  $\mu\text{H}$

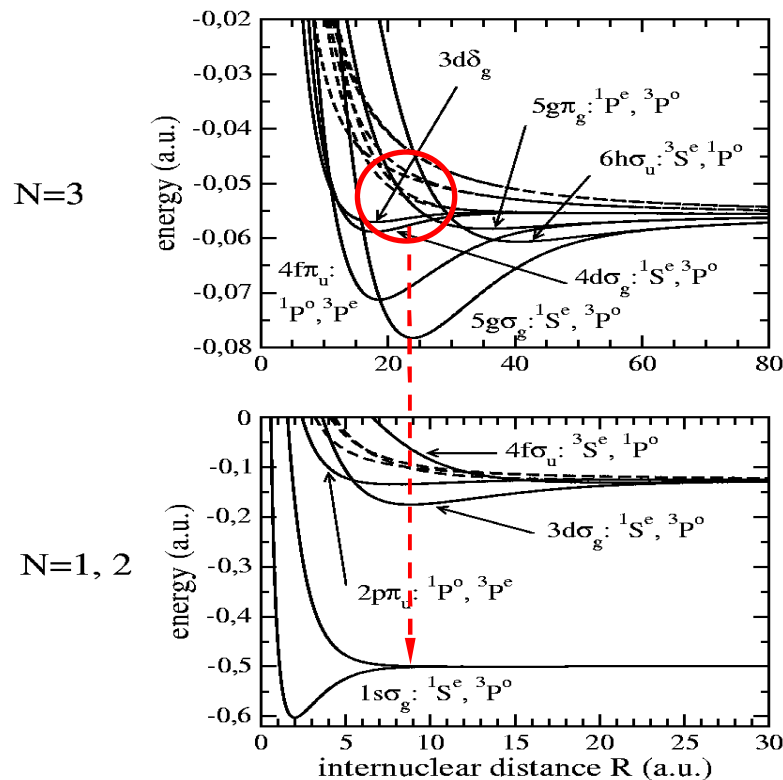


**X-ray transitions from molecular states ?**  
rate  $\leftrightarrow$  collision probability (density) !

$\mu\text{H}$  experiment

quenching of  $\mu p_{2s}$  via  $[(\mu p p)p] e e$  formation

R. Pohl et al., *Hyp. Int.* 138 (2001) 35



consequences for  $\pi\text{H}$  ( $n p \rightarrow 1s$ ) transitions

$$E_x \rightarrow E_x - \Delta E ?$$

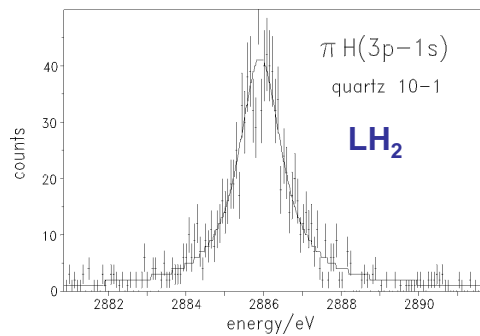
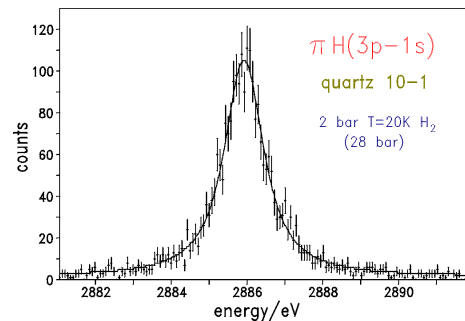
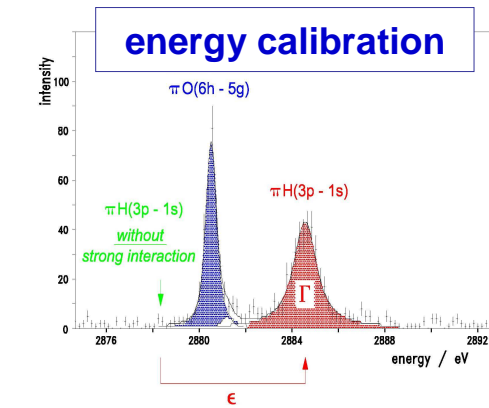
(how many) bound states below  
dissociation limit of 4.5 eV ?

Jonsell, Froelich and Wallenius for  $n=1,2,3$   
*Phys. Rev A* 59 (1999) 3440

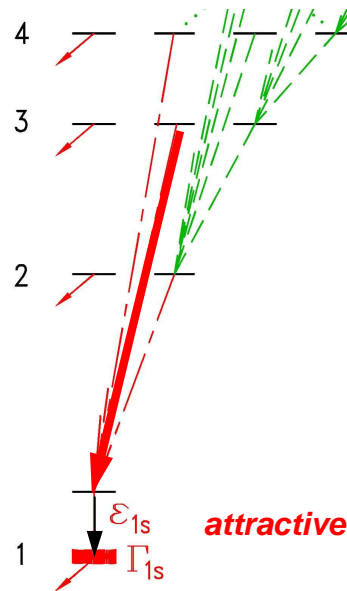
calculation	$pp\mu$	$dd\mu$
$\Gamma_{\text{X-ray}} / \Gamma_{\text{total}}$	$\approx 0.03$	$\approx 1$

Lindroth, Wallenius and Jonsell  
*Phys. Rev A* 68 (2003) 032502  
Kilic, Karr and Hilico  
*Phys. Rev. A* 70 (2004) 042506

# $\pi H(3p-1s)$ energy density dependence - measurement



**strong interaction**



$\pi H / \pi O$  mixture

(98%/2%)  
1.2 bar @  $T = 85K$

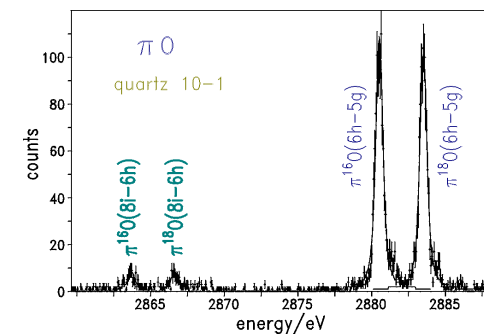
energy calibration  
simultaneously

$\pi O$

mixture  $^4He / ^{16}O_2 / ^{18}O_2$   
( $\approx 80\% / 10\% / 10\%$ )

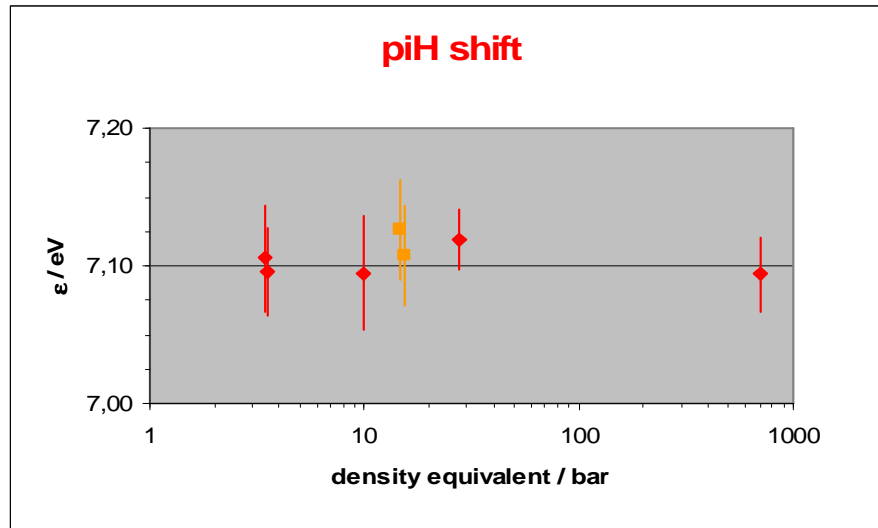
2 bar @  $T = 86K$

energy calibration/measurement  
alternating



# $\pi\text{H}(3p-1s)$ energy density dependence - result

no density dependence identified  $\Rightarrow$  "no" X-ray transitions from molecular states



R-98.01

Maik Hennebach, thesis Cologne 2003

$$\epsilon_{1s} = + 7.120 \pm 0.008 \pm 0.009 \text{ eV}$$



mainly pion mass  $\Delta E_{QED} = \pm 0.006 \text{ eV} !$   
 new calculation  $\pi\text{H} \Rightarrow \Delta E_{QED} = \pm 0.001 \text{ eV} !$   
 P. Indelicato, priv. comm.

there is another final QED value since 2010!

↙ not yet used here

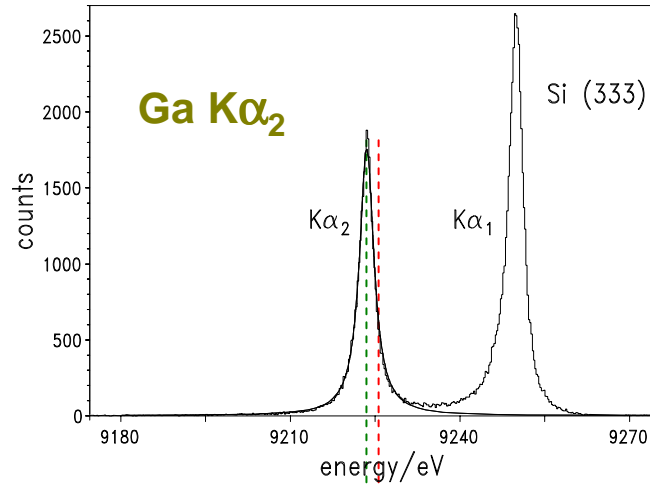
previous experiment – Ar  $K\alpha$   
 ETHZ-PSI H.-Ch.Schröder et al.  
 Eur.Phys.J.C 1(2001)473

$$\epsilon_{1s} = + 7.120 \pm 0.008 \pm 0.006 \text{ eV } (\pm 0.2\%)$$

↑  
 preliminary

# PIONIC DEUTERIUM

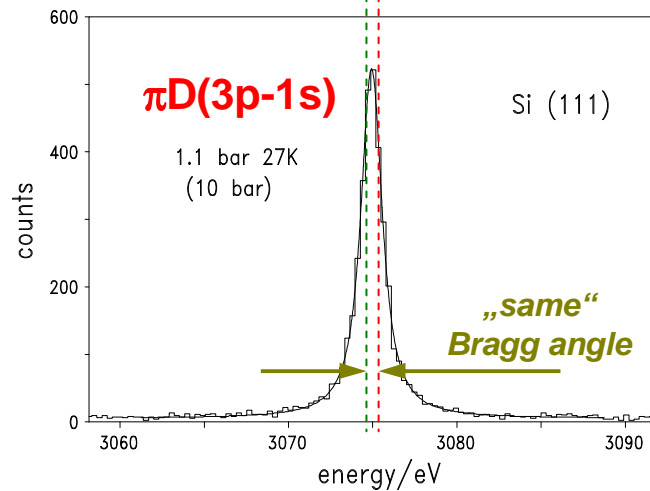
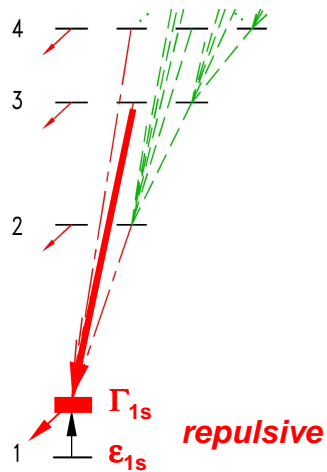
energy calibration



target material: GaAs

by chance: tabulated energy  
also from GaAs  
⇒ no chemical shift

strong interaction



3 bar } no molecule formation seen  
10 bar }  
22 bar }

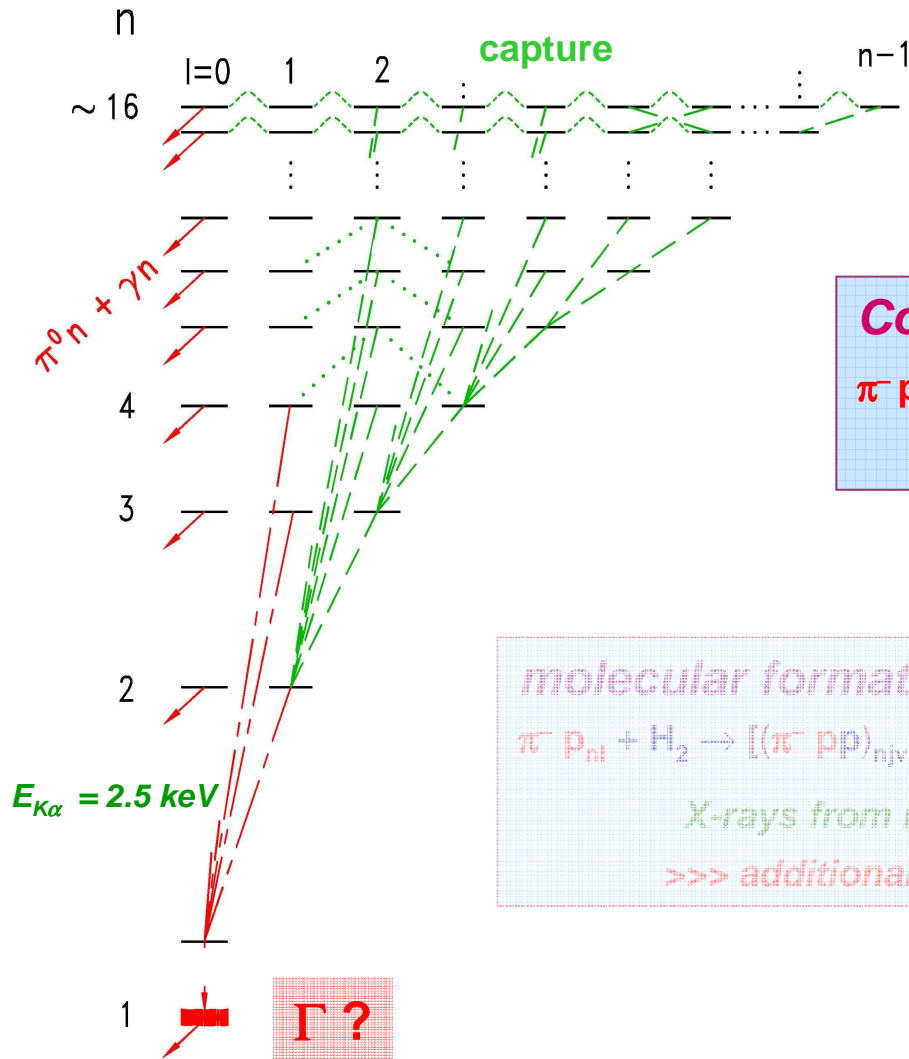
$$\epsilon_{1s} = -2.356 \pm 0.031 (\pm 1.3\%)$$

uncertainties

- 27 meV Ga  $K\alpha_2$
- 10 meV statistics
- 8 meV pion mass
- 5 meV systematics
- 2 meV QED

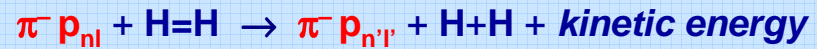
T. Strauch, PhD thesis 2009 Univ. Cologne  
T. Strauch et al., to be published

# $\pi\text{H}$ - ATOMIC CASCADE II



*density dependent*

## Coulomb de-excitation



*>>> Doppler broadening ! <<<*

## molecular formation



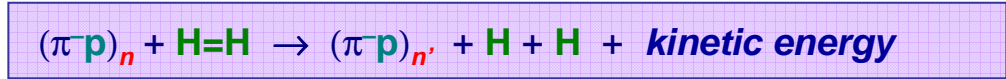
*X-rays from molecular states ?*

*>>> additional energy shift ? <<<*

$E_{K\alpha} = 2.5 \text{ keV}$

# COULOMB DE-EXCITATION

# NEUTRON - TOF



$$(\pi^- p)_{ns} \rightarrow \pi^0 n$$

↑  
moving neutron source

analogue

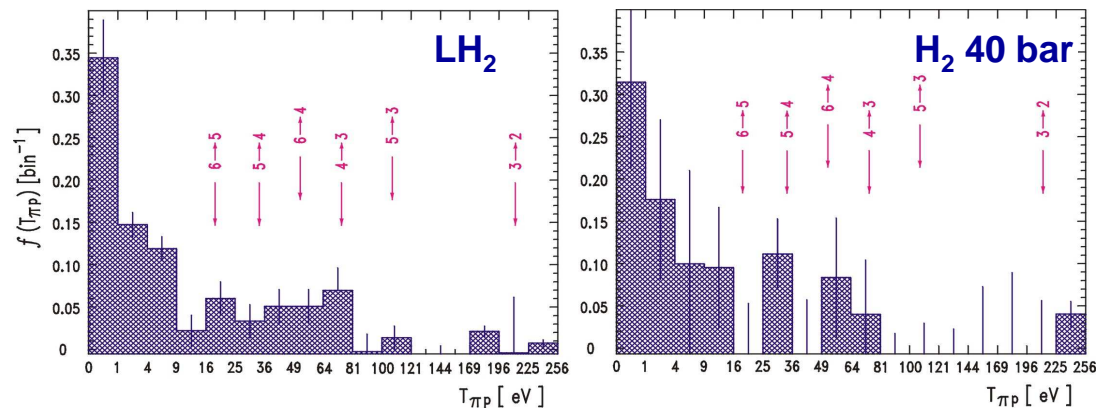
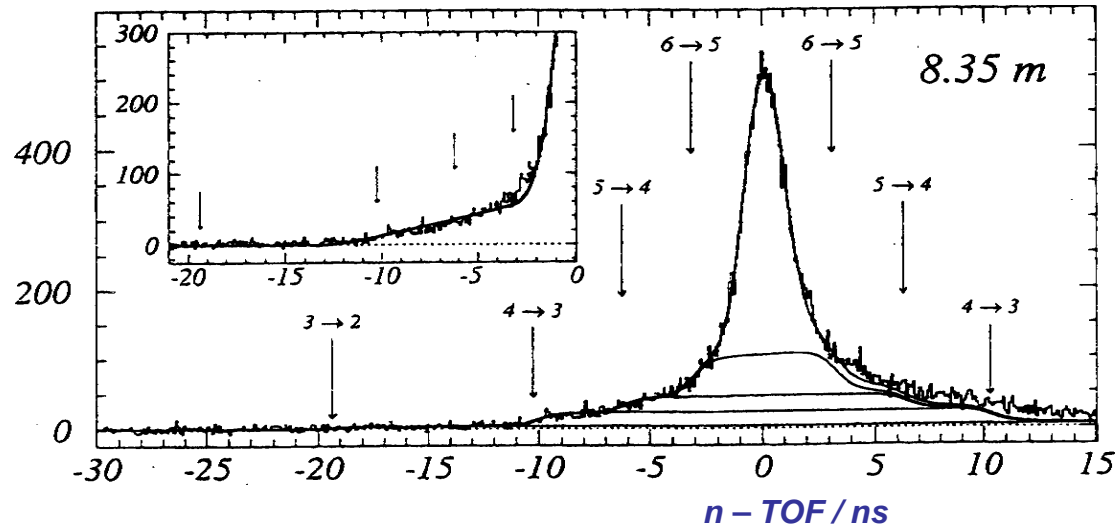
$$(\pi^- p)_{np} \rightarrow (\pi^- p)_{1s} + X\text{-ray}$$

↑  
moving X-ray source

non-radiative transitions

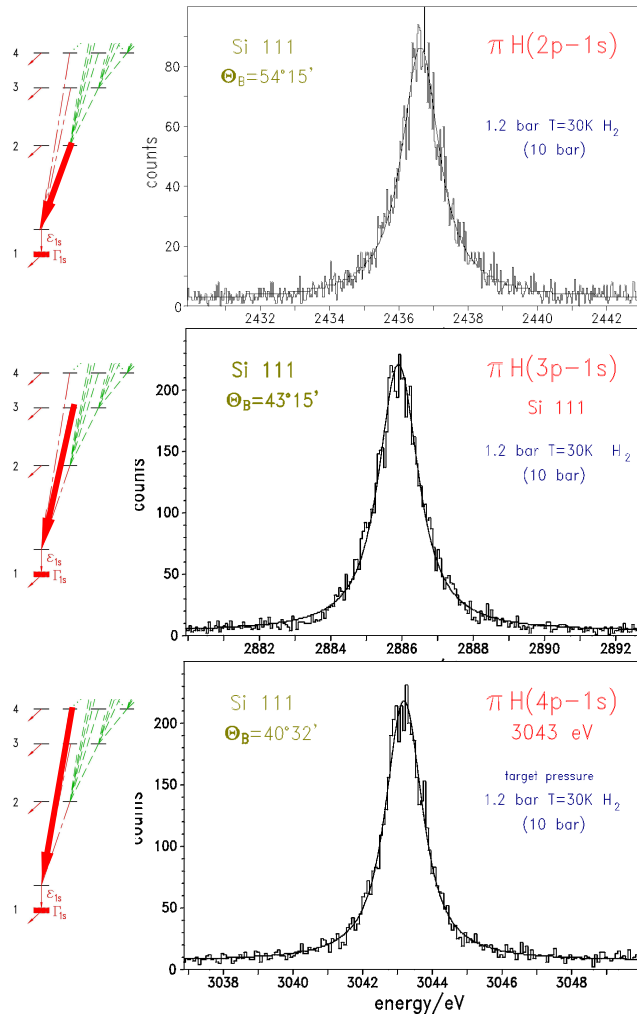
↓  
quasi-discrete velocity profile

**Doppler broadening**



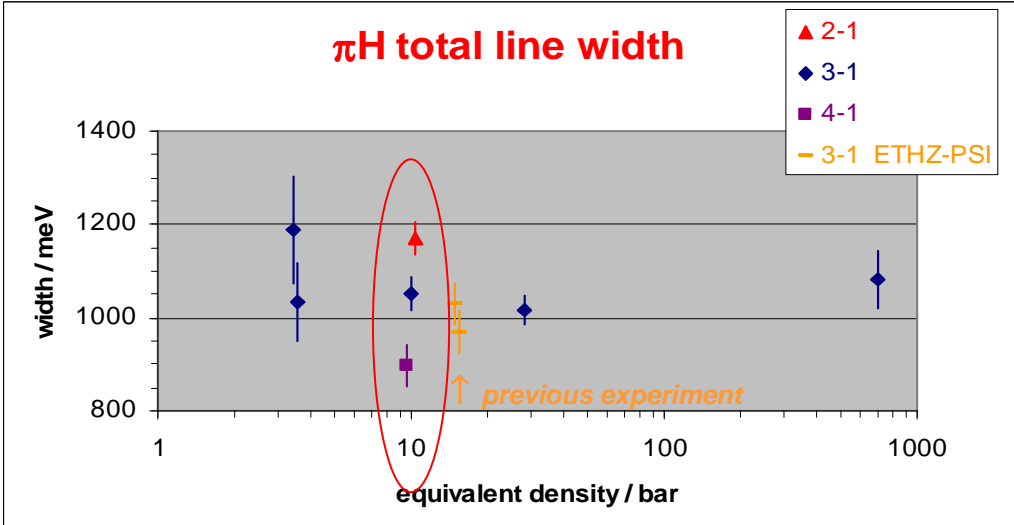
A. Badertscher et al., Eur. Phys. Lett. 54 (2001) 313

# LINE WIDTH and INITIAL STATE



*not corrected*  
for  
*Coulomb de-excitation*

*crystal resolution*  
from  $\pi C$  / ECRIT  
*subtracted*



remove  $\Gamma_{1s}$

**LINE SHAPE**

=

**R**

⊗

~~**L**~~

⊗

**Σ D**

crystal  
response

~~Lorentzian  
 $\Gamma_{1s}$~~

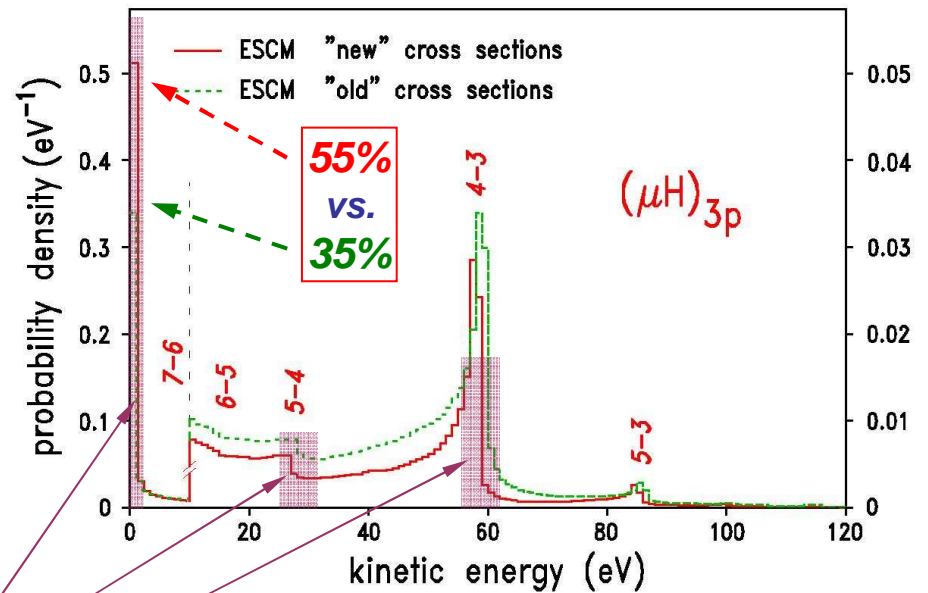
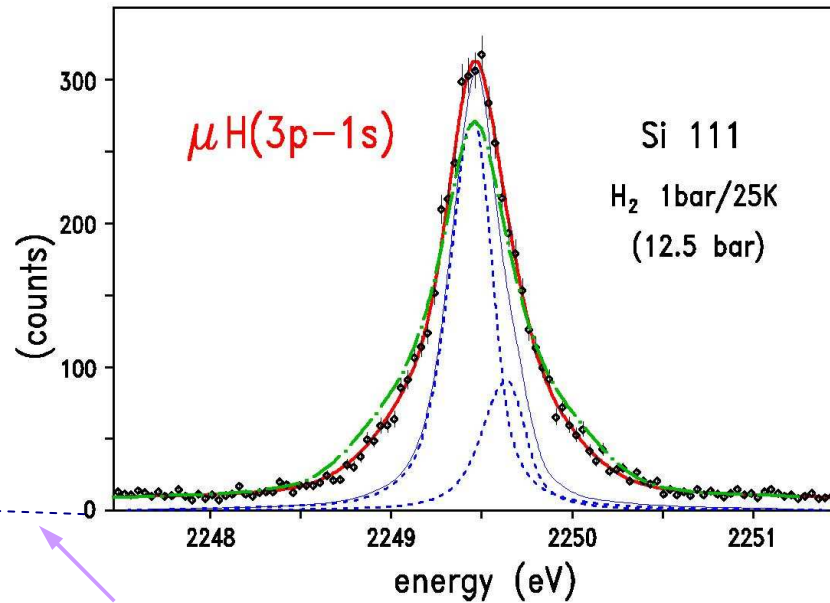
Doppler broadening  
Coulomb de-excitation  
depends on initial state

**ECRIT**

**MUONIC HYDROGEN**

**CONSTRAINT from  
CASCADE CALCULATION ?**

# MUONIC HYDROGEN



no satellites from molecular formation identified

low-Tkin:  $61 \pm 2$  %  
 medium-Tkin  $25 \pm 3$  %  
 high-Tkin  $14 \pm 4$  %

box fits = model free fit

triplet / singlet =  $3.0 \pm 0.3$

$\Delta E = 183$  meV (theory)

recalculation of cross sections

thesis: D. Civita, (Coimbra)  
 D.S. Covita et al., Phys. Rev. Lett. 102 (2009) 023401

ESCM: extended standard cascade calculation and cross sections  
 T.S.Jensen and V.E.Markushin, Eur. Phys. J. D 19,165 (2002); ibid.D 21,261 (2002); ibid.D 21,271 (2002)  
 cross sections  
 G.Ya. Koreman, V.N. Pomerantsev and V.P. Popov, JETP. Lett. 81, 543 (2005)  
 V.N. Pomerantsev and V.P. Popov, Phys. Rev 130, 341 (2006)  
 V.P. Popov and V.N. Pomerantsev, arXiv:0712.3111v1[nucl-th] (2007)

$$\Gamma_{1s}$$

$$\text{LINE SHAPE} = R \otimes L \otimes \Sigma D$$

crystal  
response

Lorentzian

$$\Gamma_{1s}$$



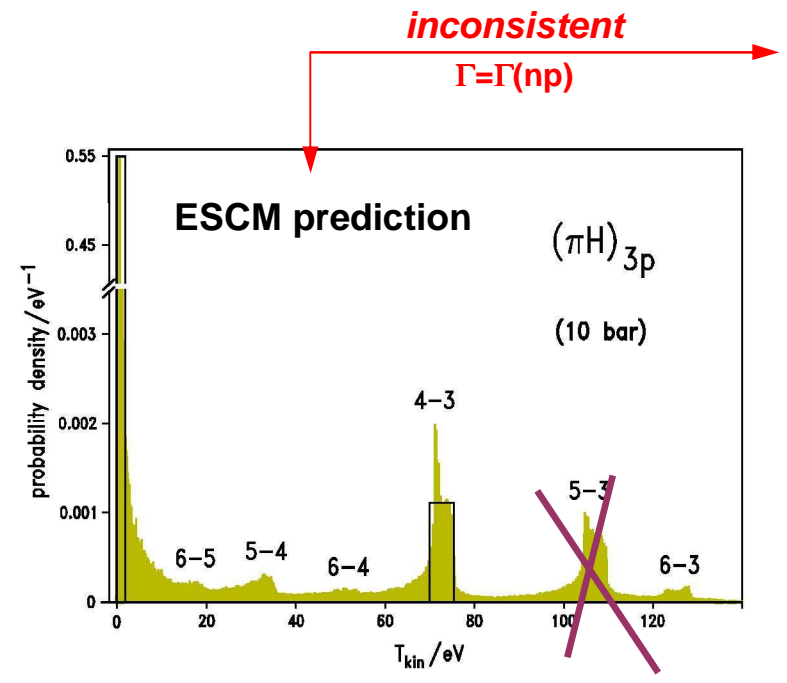
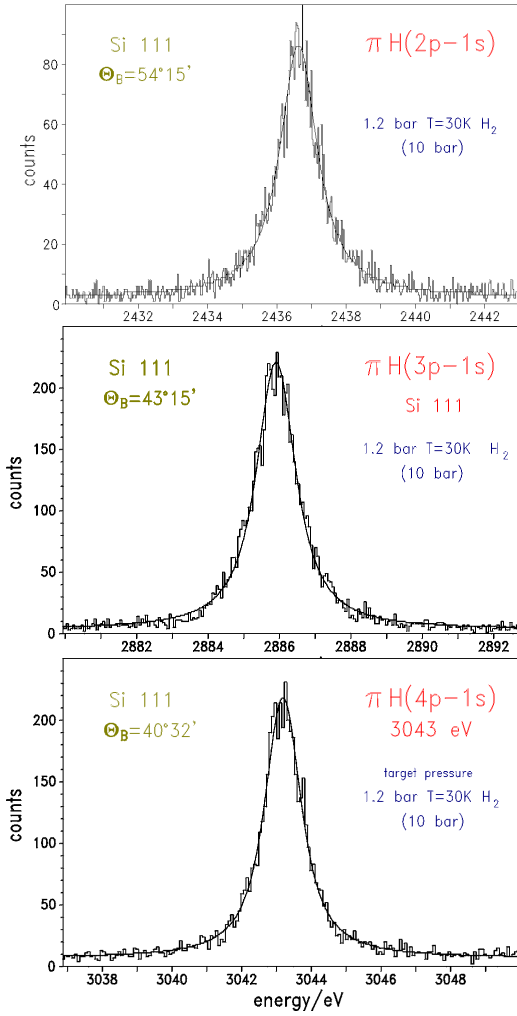
Doppler broadening

*Coulomb de-excitation*

*depends on initial state*

*model free approach*

# "BOX" FITS



*upper limit from 4p-1s*  
 $\Gamma_{1s} \approx 800 \pm 40 \text{ meV (5\%)}$

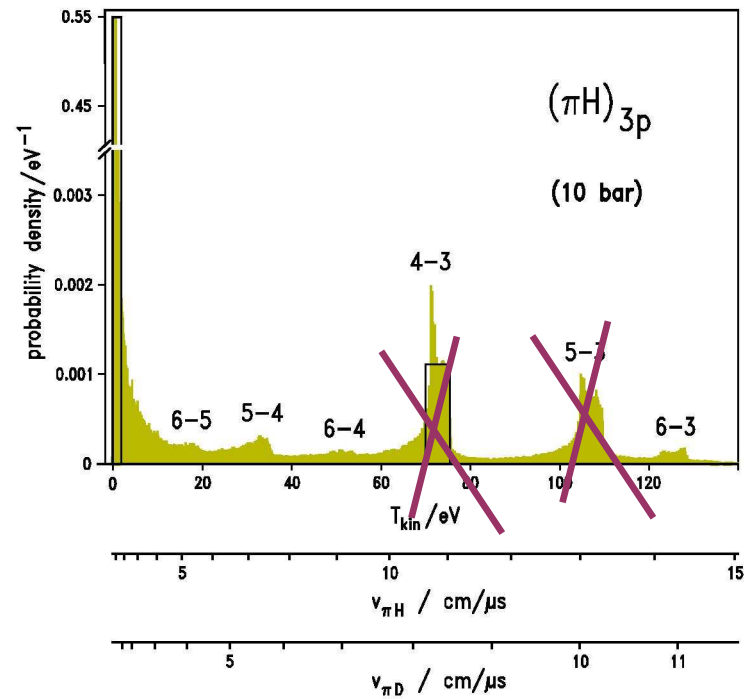
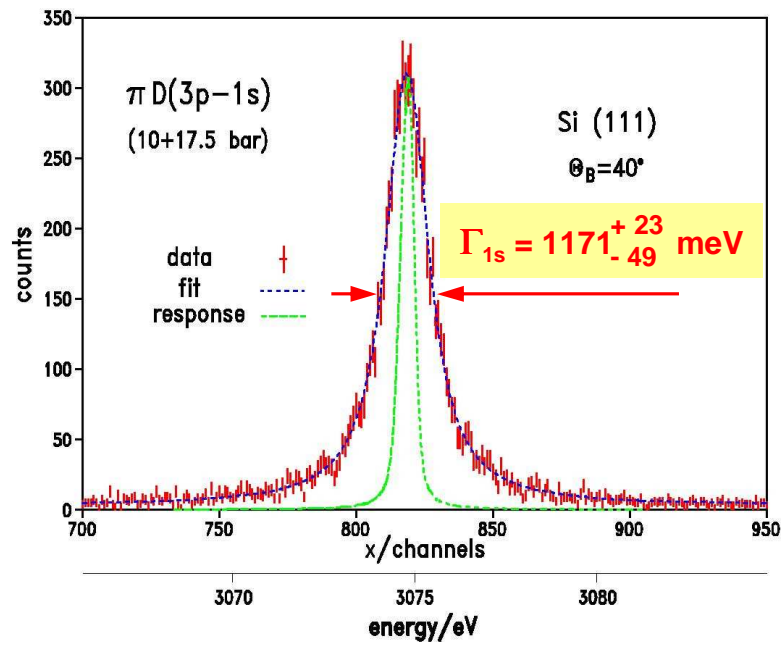
## Coulomb transition

low-energy	$\pm 50\%$
5-4	---
6-4	---
4-3	$\pm 50\%$
3-2	?
low-energy	$\pm 55\%$
5-4	---
6-4	---
4-3	$\pm 45\%$
5-3	---
low-energy	$\pm 50\%$
6-5	---
5-4	$\pm 50\%$
6-4	---

*limit without cascade theory*

*so far weighted average R-98.01*  $\Gamma_{1s} \approx 823 \pm \approx 19 \text{ meV } (\approx 2.3\%)$  preliminary

# $\pi D \Gamma_{1s}$



< 10%

High-energy components ?



# SUMMARY

# $\pi N$ scattering lengths $a^+$ and $\tilde{a}$

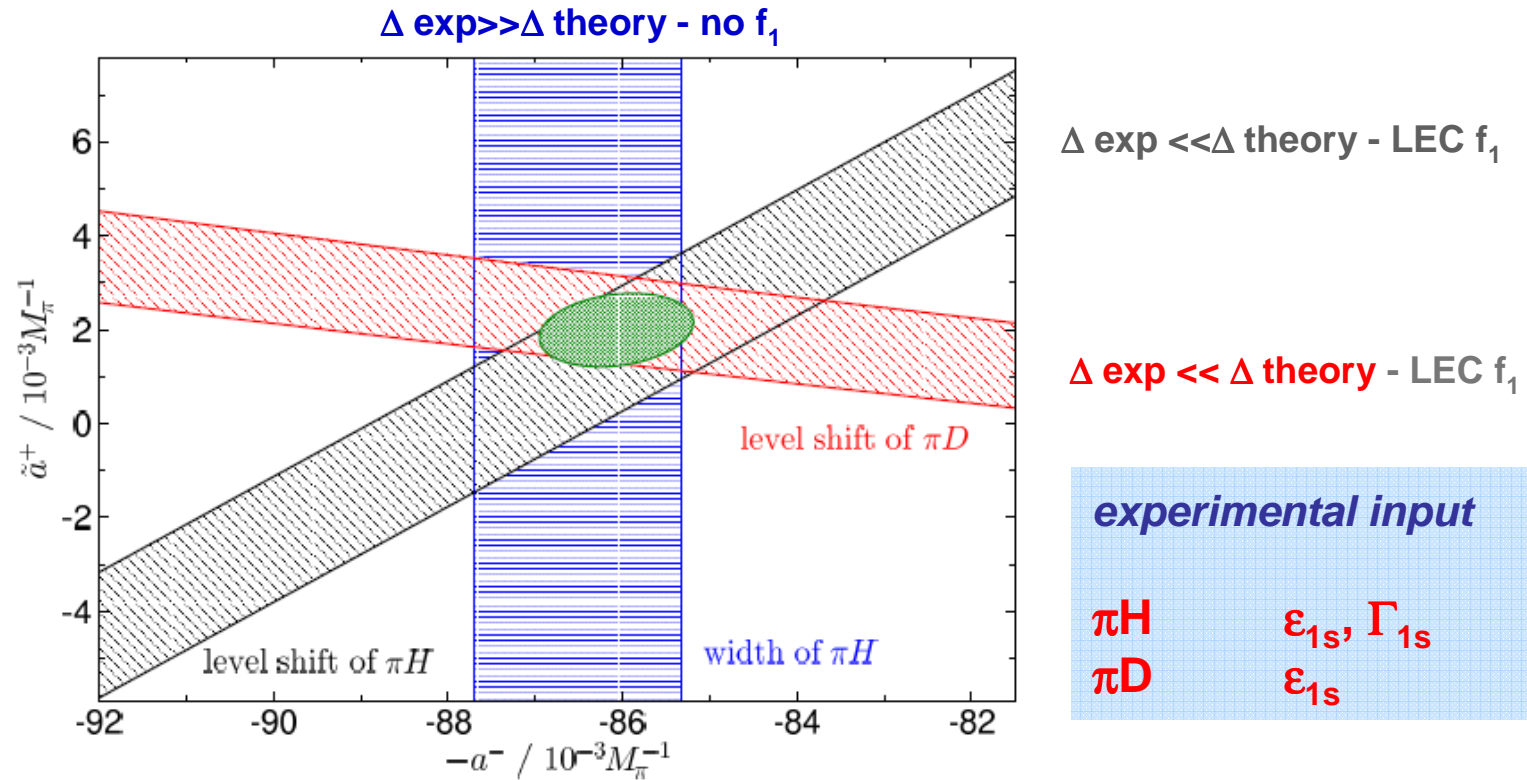


FIG. 2: Combined constraints in the  $\tilde{a}^+ - a^-$  plane from data on the width and energy shift of  $\pi H$ , as well as the  $\pi D$  energy shift.

*cPT: V. Baru, C. Hanhart, M. Hoferichter, B. Kubis, A. Nogga, and D. R. Phillips, to be published*  
*data: R-98.01 (preliminary) and R-06.03 (final)*

# NN $\Leftrightarrow$ $\pi$ NN threshold parameter $\alpha$

charge symmetry  $\Leftrightarrow$   $\sigma_{\pi^+d \rightarrow pp}$   $\Leftrightarrow$  detailed balance  $\sigma_{pp \rightarrow \pi^+d}$

$\sigma_{\pi^-d \rightarrow nn}$

$NN \quad {}^3S_1(I=0) \rightarrow {}^3P_1(I=1)$

**$\pi D$**

$\Im a_{\pi D} \propto \Gamma_{\pi^-d \rightarrow nn} + \Gamma_{\pi^-d \rightarrow nn\gamma} \propto \alpha$

direct from G

**$\pi$  production experiments**

$\sigma_{pp \rightarrow \pi^+d} \rightarrow \alpha C_0^2 \eta + \beta C_1^2 \eta^3$

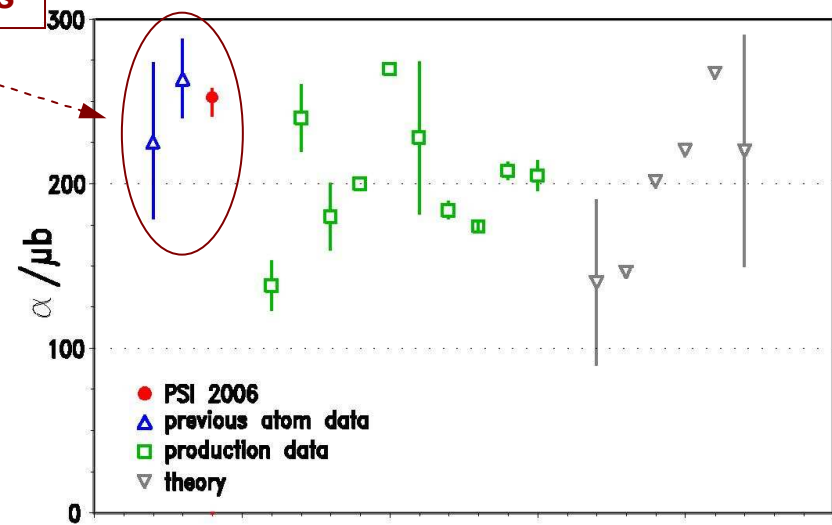
extrapolation to threshold

$\eta = k_\pi / m_\pi$

exotic-atom results

$\pi D$   
 Th. Strauch,  
 PhD thesis, Cologne 2009

Th. Strauch et al.,  
 Phys.Rev.Lett.104 (2010)142503



$\chi$ PT NLO

$\chi$ PT LO

$\chi$ PT

at present

$\Delta\alpha/\alpha \approx 30\%$

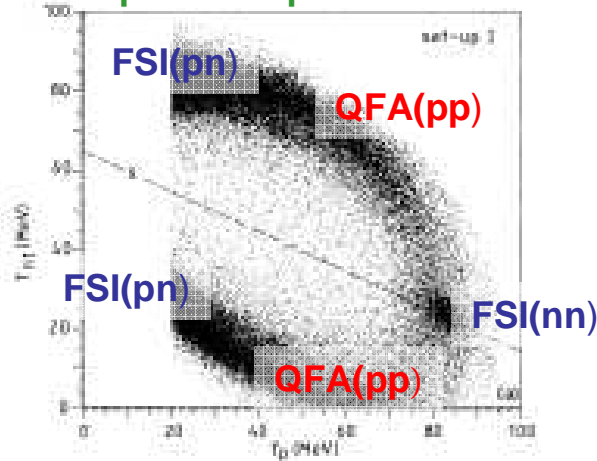
→ few %

V. Lensky et al.,  
 Eur. Phys. J. A 27 (2006) 37

# Dalitzplot $\pi^-^3\text{He} \rightarrow pnn$

PSI R-73.07

experiment pn coincidences

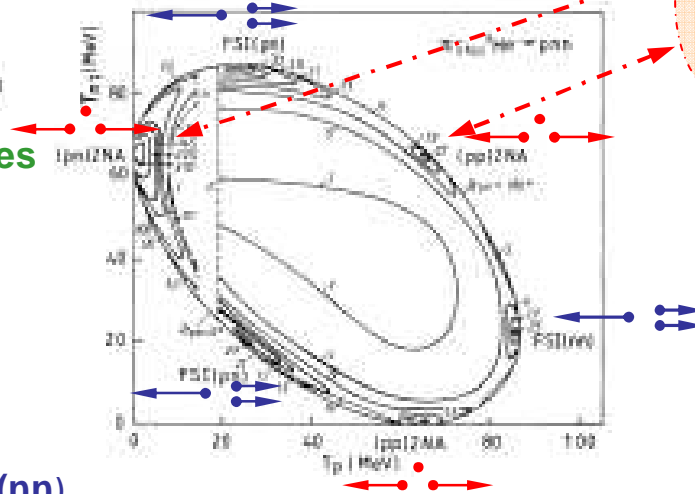


QFA quasi free reaction



FSI final state interaction

pn + nn coincidences combined



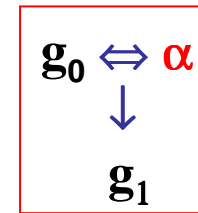
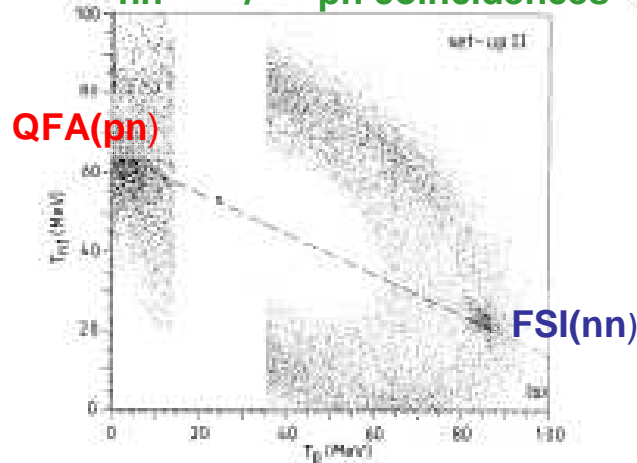
nn transitions

$$^3S_1(I=0) \rightarrow ^3P_1(I=1)$$

$$^1S_0(I=1) \rightarrow ^3P_0(I=1)$$

$$|g_0 / g_1| = 2.48 \pm 0.24$$

nn / pn coincidences



$\chi PT?!$

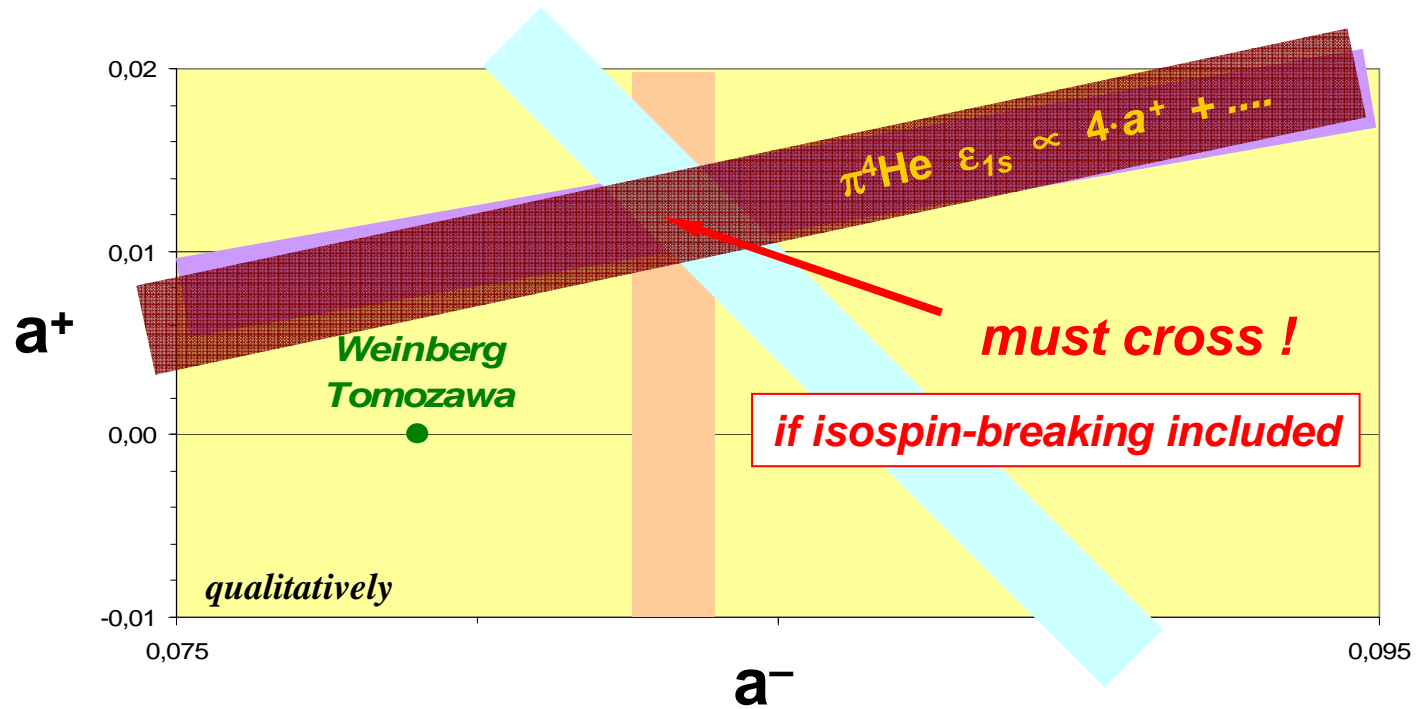
D. Gotta et al., Phys. Lett. 112B (1982) 129  
 D. Gotta et al., Phys. Rev. C 51 (1995) 469  
 E. Daum et al., Nucl. Phys. A 539 (1995) 553



**PERSPECTIVES**

**NEW QUESTIONS**

# $\pi A$ INTERACTION + ADDITIONAL ACCESS TO $a^\pm$



comparison  $I=1/2$  nuclei  ${}^3\text{He} / T$

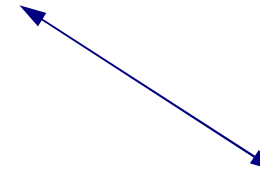
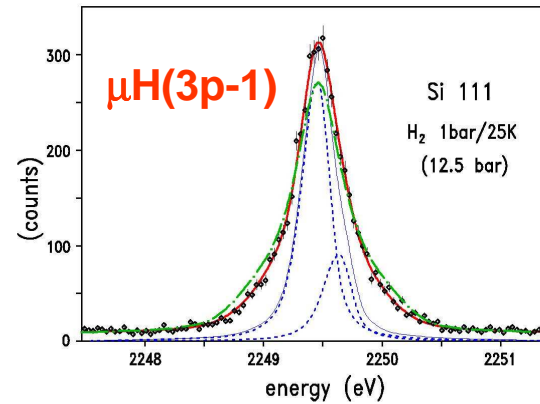
Theory

C. Werntz and H. S. Valk, *Phys. Rev. C* 37, 724 (1988).  $G(pT)$  predicted from radiative capture  $pT \rightarrow nnn$   
 Baru, Haidenbauer, Hanhart, Niskanen, *Eur. Phys. J. A* 16 (2003) 437,  $T/{}^3\text{He}$  comparison:  
 .... more coming

# CASCADE or IS SOMETHING MISSING ?

?

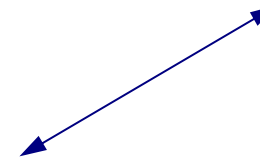
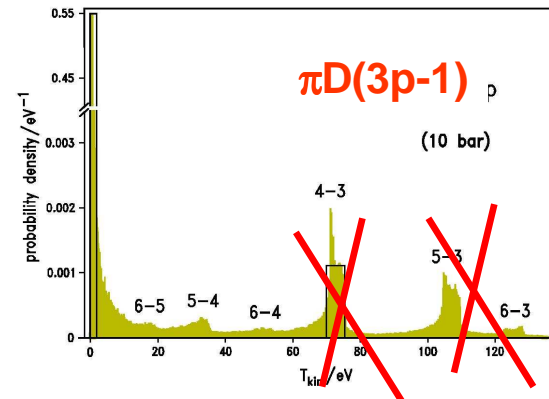
*X-ray satellites from molecular formation*



$\mu D$

?

*high-energy components*

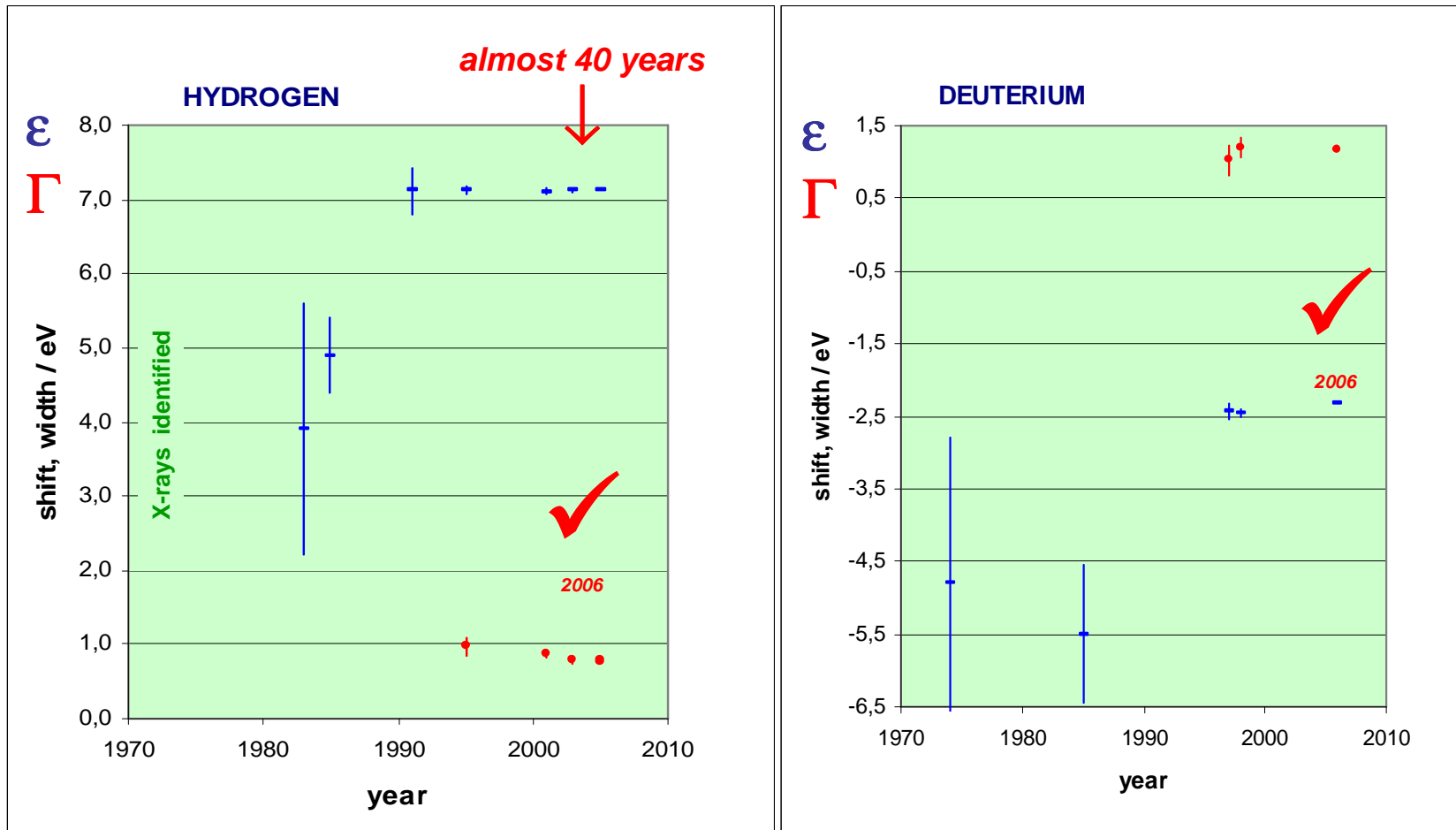


?

*does cascade theory improve for  $\pi H$  as for  $\mu H$  - if yes:  $\Delta\Gamma \rightarrow \Delta\Gamma/2$*

**cross sections**

# PIONIC HYDROGEN STORY





**THANK YOU**

## **PIONIC HYDROGEN collaboration**

*PSI experiments R-98.01 and R-06.03*

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**Cascade theory**

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**→ Diploma and PhD thesis ←**