Positronium 1S-2S transition frequency measurement

Paolo Crivelli

Institute for Particle Physics, ETH Zurich

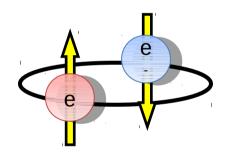
PSI2013 workshop, 12th of September, 2013

My work is supported by the Ambizione grant of the SNSF PZ00P2_132059 and ETH under the research grant ETH-47-12-1

Positronium (Ps)

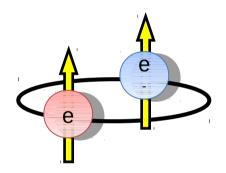
Two ground states:

Parapositronium (p-Ps) singlet spin state ¹S₀



$$|0,0
angle = (\uparrow \downarrow - \downarrow \uparrow)/\sqrt{2} \; \Big\} \quad s = 0 \quad (ext{singlet})$$

Orthopositronium (o-Ps) triplet spin state 3S₁

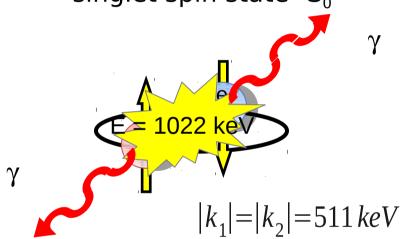


$$|0,0
angle = (\uparrow\downarrow -\downarrow\uparrow)/\sqrt{2} \; \} \quad s=0 \quad (ext{singlet}) \quad \begin{vmatrix} |1,1
angle = \uparrow\uparrow \\ |1,0
angle = (\uparrow\downarrow +\downarrow\uparrow)/\sqrt{2} \\ |1,-1
angle = \downarrow\downarrow \end{vmatrix} \quad s=1 \quad (ext{triplet})$$

Positronium (Ps)

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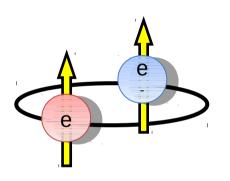


$$\Gamma_{2\gamma}^{(0)}(n^1S_0) = \sigma_{2\gamma}^1 v |\psi_n(0)|^2 = \frac{1}{2} \frac{m_e c^2}{\hbar} \frac{\alpha^5}{n^3}$$

Pirenne and Wheeler in 1946

$$\Gamma^{-1} = \tau \approx 125 \text{ ps}$$
 (in vacuum)

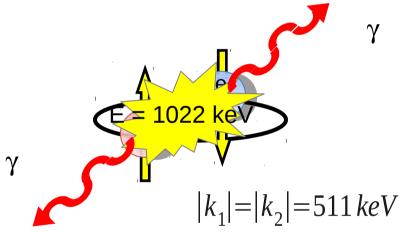
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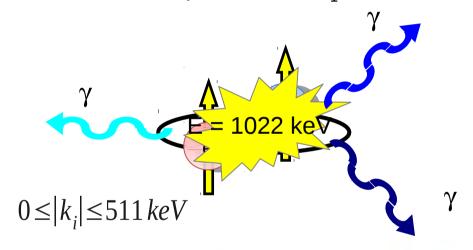


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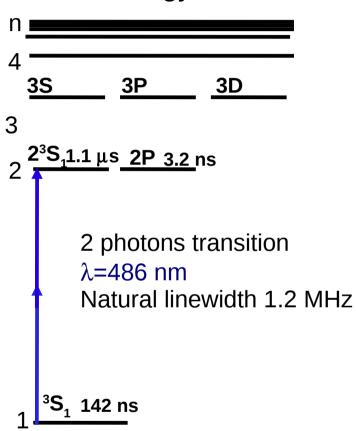
$$\Gamma_{3\gamma}^{(0)}(n^3S_1) = \frac{2}{9\pi} (\pi^2 - 9) \frac{m_e c^2}{\hbar} \frac{\alpha^6}{n^3}$$

Ore and Powell in 1949

$$\Gamma^{-1} = \tau \approx 142 \text{ ns (in vacuum)}$$

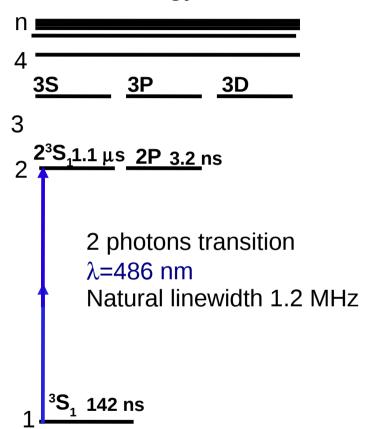
Positronium 1S-2S transition

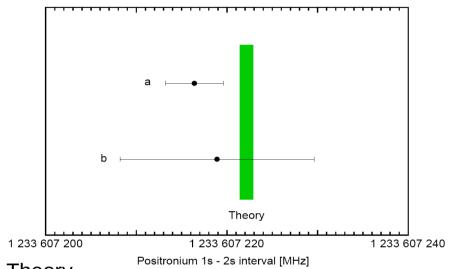
Ps Energy levels



Positronium 1S-2S transition

Ps Energy levels





Theory

$$v^{theory} = 1233607222.2(6)$$
 MHz

K. Pachucki and S. G. Karshenboim, Phys. Rev. A60, 2792 (1999), K. Melnikov and A. Yelkhovsky, Phys. Lett. B458, 143 (1999).

Experiment

$$v^a = 1233607216.4(3.2)$$
 MHz

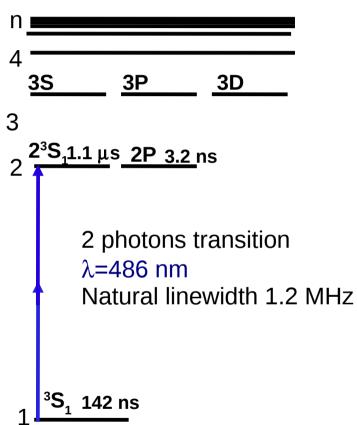
M. S. Fee et al., Phys. Rev. Lett. 70, 1397 (1993)

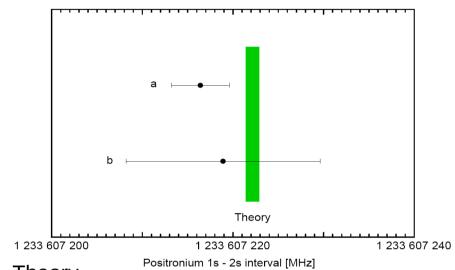
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S. Chu, A. P. Mills, Jr. and J. Hall, Phys. Rev. Lett. 52, 1689 (1984)

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Measurement of 1S-2S of Ps at a level about $5x10^{-10}$ => check QED calculations at the order α^7 m and provide best determination of m_{e^+}/m_{e^-} .

Various co	ontributions	to the	energy	levels
------------	--------------	--------	--------	--------

Contribution	Hydrogen-like electronic atom	Positronium
Schrödinger contributions		
• With $M = \infty$	1	1
• With $m_{\rm R}$ (correction)	m/M	(1)
Relativistic corrections	,	
 Dirac equation 	$(Z\alpha)^2$	α^2
• Two-body effects	$(Z\alpha)^2m/M$	α^2
Quantum electrodynamics		
• Self-energy	$\alpha(Z\alpha)^2 \ln(Z\alpha)$	$\alpha^3 \ln \alpha$
• Radiative width	$\alpha(Z\alpha)^2$	α^3
 Vacuum polarization 	$\alpha(Z\alpha)^2$	α^3
• Annihilation		
-Virtual		α^2
-Real		α^3
Nuclear effects		
• Magnetic moment (HFS)	$(Z\alpha)^2m/M$	α^2
- 2.2		•
 Charge distribution 	or $\alpha(Z\alpha)m/m_{\rm p}$ $(Z\alpha mcR_{\rm N}/\hbar)^2$	

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 Magnetic moment (HFS) 	$(Z\alpha)^2m/M$	(α^2)
	or $\alpha(Z\alpha)m/m_{\rm p}$	
 Charge distribution 	$(Z \alpha m c R_N/\hbar)^{\frac{p}{2}}$	_

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Leptonic atoms free of nuclear size effects!

Attempts with charged anti-particles were not conclusive -> use neutral objects.

Recent measurement at CERN with trapped anti-H (ALPHA):

 \overline{m}_{g}/m_{g} =(+100,-65) at 5% confidence level

NATURE COMMUNICATIONS | DOI: 10.1038/ncomms2787

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Two approaches to direct measure effect of gravity on anti-matter:

- 1) Gravity fall of anti-matter (anti-hydrogen at CERN): Aegis, GBar
- 2) Use the gravitational redshift

S. G. Karshenboim, Astr. Lett. 35, 663 (2009).

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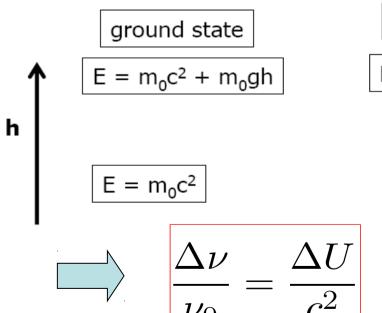
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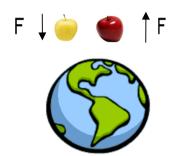
$$E = (m_0 + \Delta m) (c^2 + gh)$$

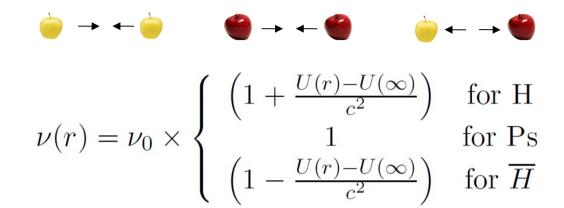
$$\mathsf{E} = (\mathsf{m}_0 {+} \Delta \mathsf{m}) \mathsf{c}^2$$

$$hv_h = \Delta m(c^2 + gh)$$

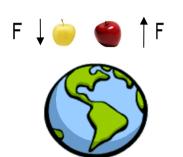
$$hv_0 = \Delta mc^2$$

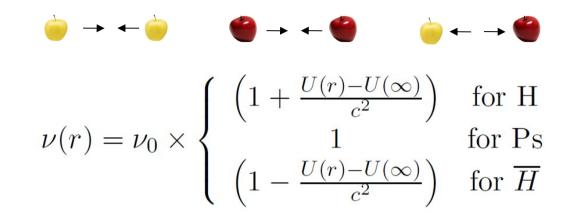
Assuming antigravity:





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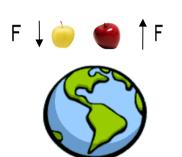


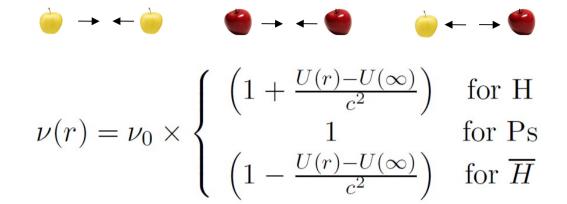


• ΔU for different altitudes in the gravitational field of the earth is too weak for Ps

dh = 5000m
$$\implies \frac{\Delta v}{v} = 5.2 \times 10^{-13}$$

Assuming antigravity:



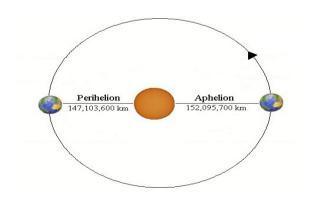


• ΔU for different altitudes in the gravitational field of the earth is too weak for Ps

dh = 5000m
$$\implies \frac{\Delta v}{v} = 5.2 \times 10^{-13}$$

• Variation in the earth orbit around the sun: 5x10⁶ km.

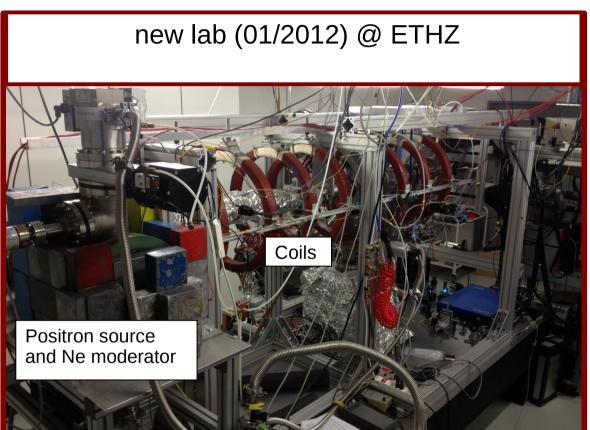
$$\frac{\Delta U(r_{\text{max}}) - \Delta U(r_{\text{min}})}{c^2} \simeq 3.2 \times 10^{-10}$$



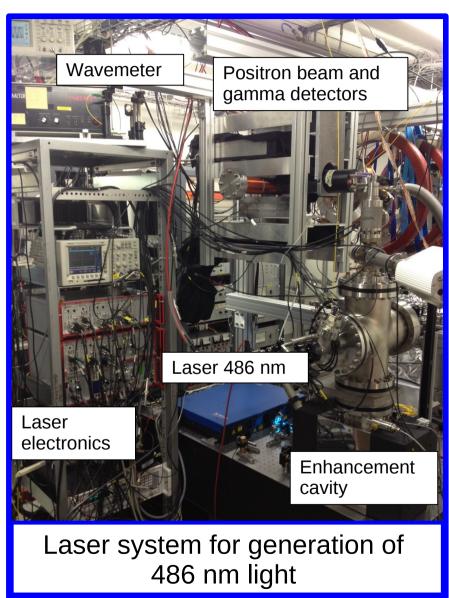
Measurement of 1S-2S Ps, Mu or HBar at a level about $1x10^{-10} =>$ sensitivity to check the shift of antigravity.

New measurement ongoing @ ETH

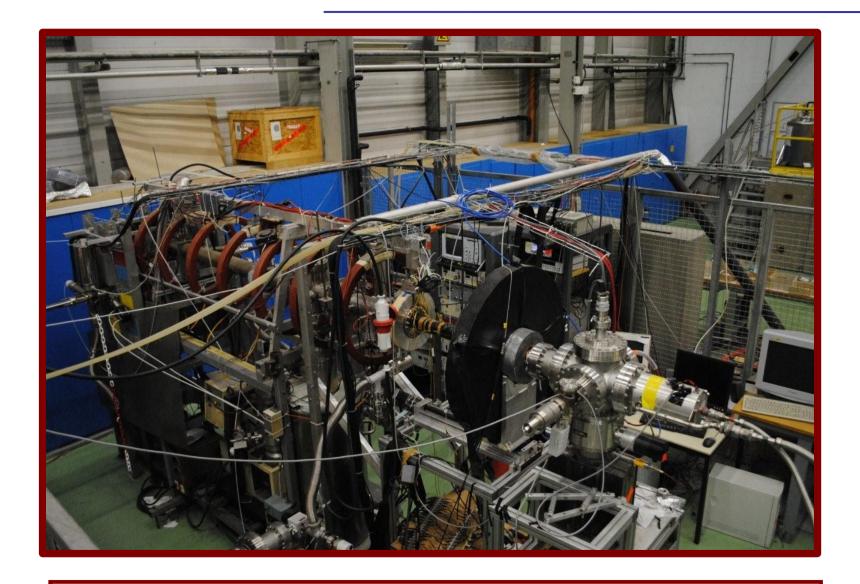
P. Crivelli (ETHZ), D. Cooke (ETHZ), S. Friedreich (ETHZ), A. Rubbia (ETHZ), A. Antognini (ETHZ), K. Kirch (ETHZ/PSI), J. Alnis (MPQ), T. W. Haensch (MPQ), B. Brown (Marquette)



Project supported by the SNSF Ambizione grant (PZ00P2_132059) and by ETH (Research Grant ETH-47 12-1)

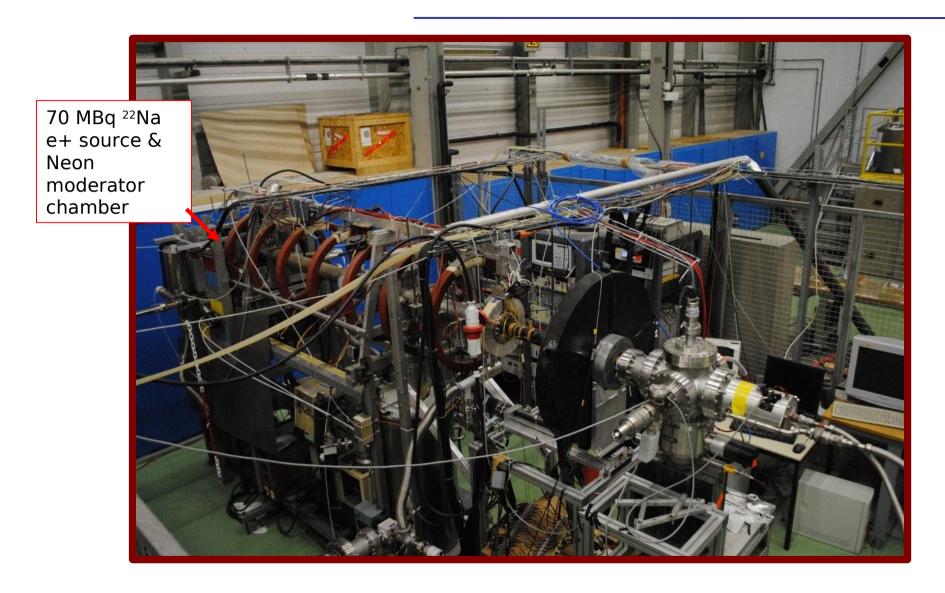


ETHZ slow positron beam

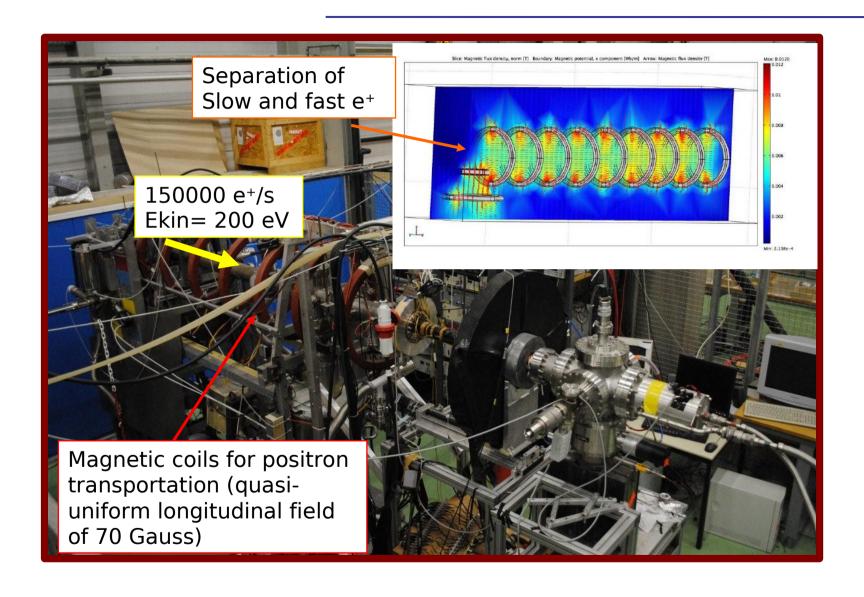


Production of positronium in vacuum requires slow positrons

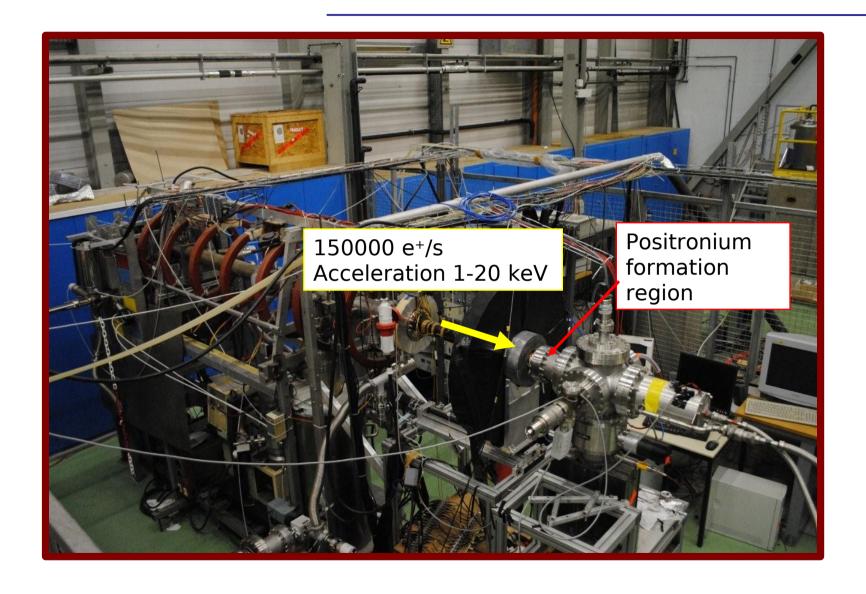
The positron source



Positron transportation

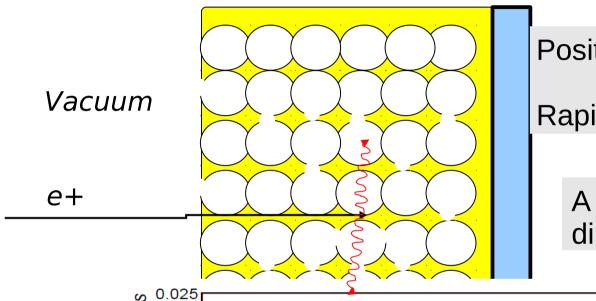


Positron-Positronium conversion target



Positron implantation

Porous Silica thin film ~1000nm 3-4 nm pore size

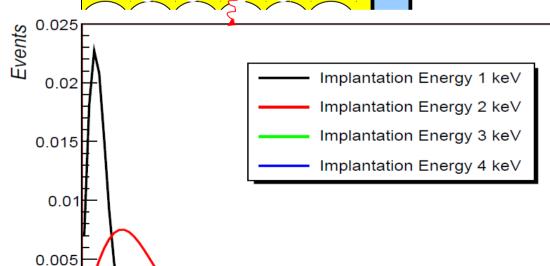


100

Positron implanted with keV energies

Rapidly thermalizes in the bulk (~ps)

A fraction undergo direct annihilation



Depth (nm)

700

800

900

300

Makhovian profile

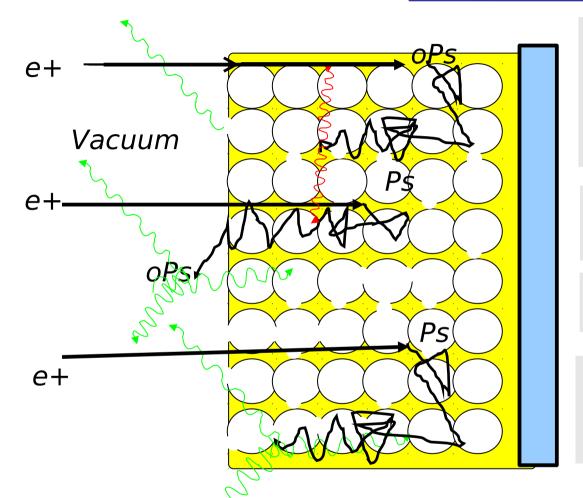
$$P(x,E) = \frac{mx^{m-1}}{x_0^m} e^{-(x/x_0)^m},$$

$$x_0 = \frac{x_m}{\Gamma((1/m) + 1)},$$

$$x_{\rm m} = \frac{40}{\rho} E^{1.6},$$

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Positronium formation



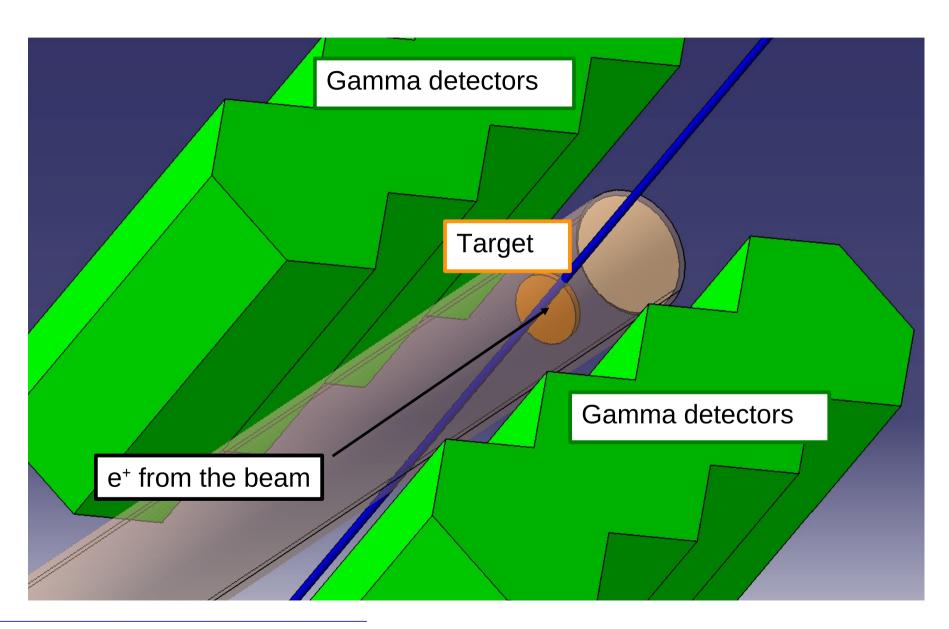
Positronium formation in SiO₂ by capturing 1 ionized electron (spur electrons) (1/4 pPs, 3/4 oPs)

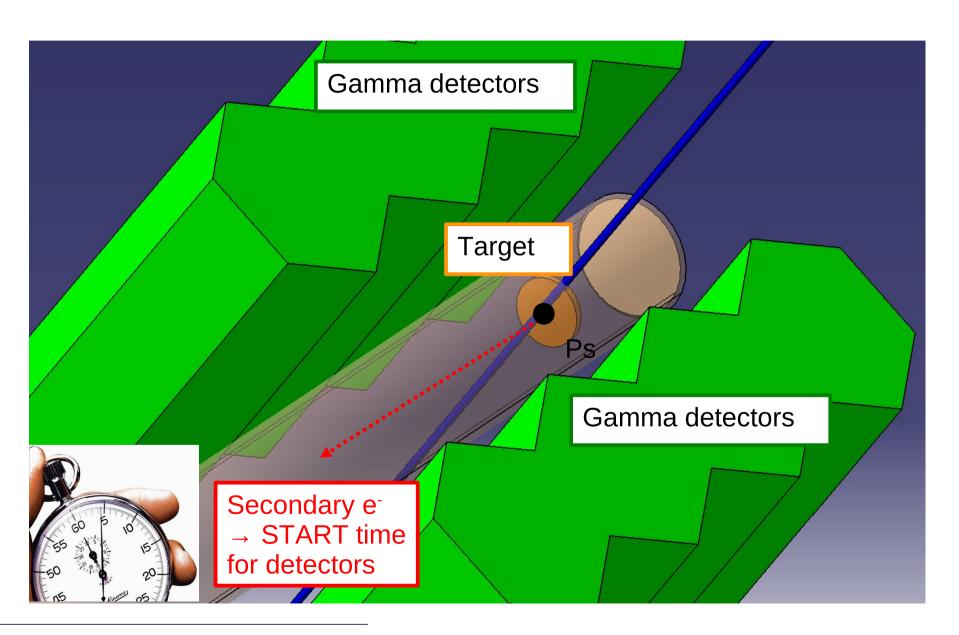
Diffusion to the pore surface and emission in the pores

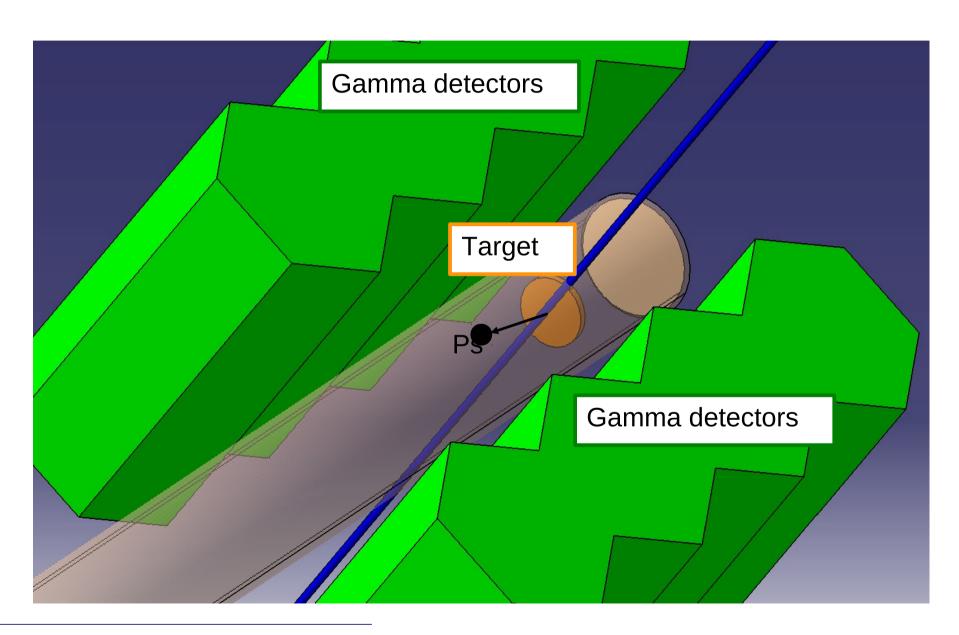
$$W_{PS} = \mu_{PS} + E_B - 6.8 \text{ eV} = -1 \text{ eV}$$

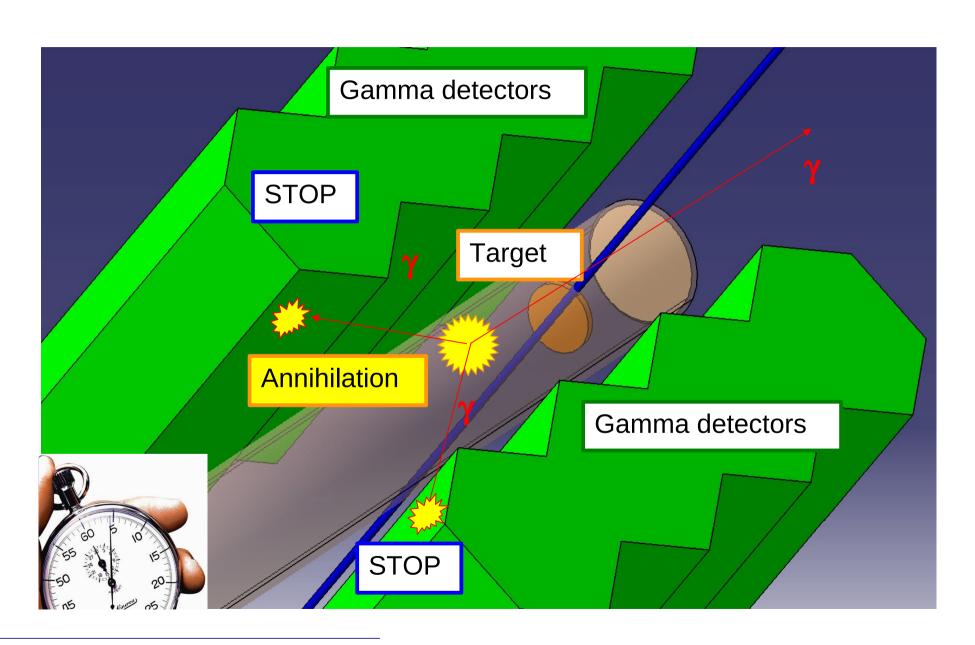
Thermalization via collisions and diffusion in the interconnected pore network

A fraction of them is emitted into vacuum.

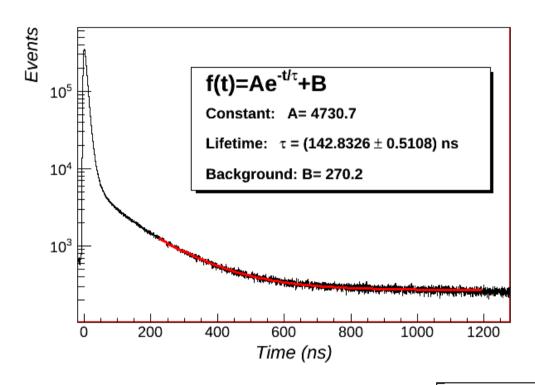


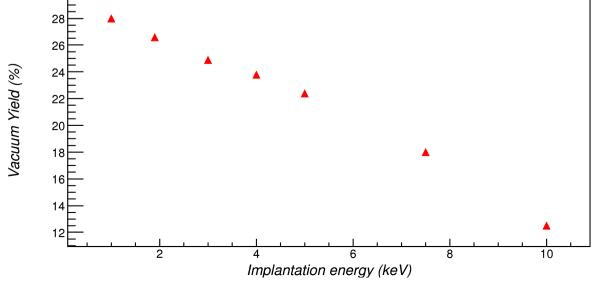




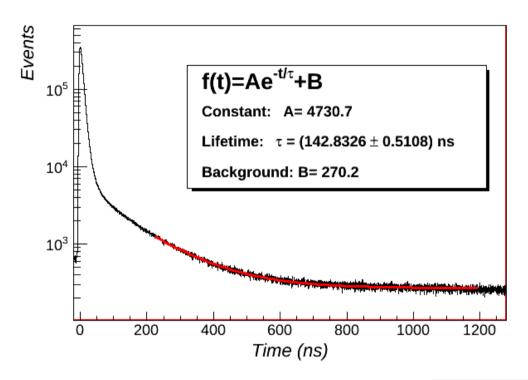


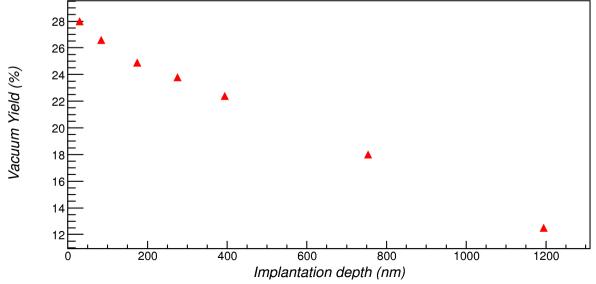
Positron annihilation lifetime spectra- PALS



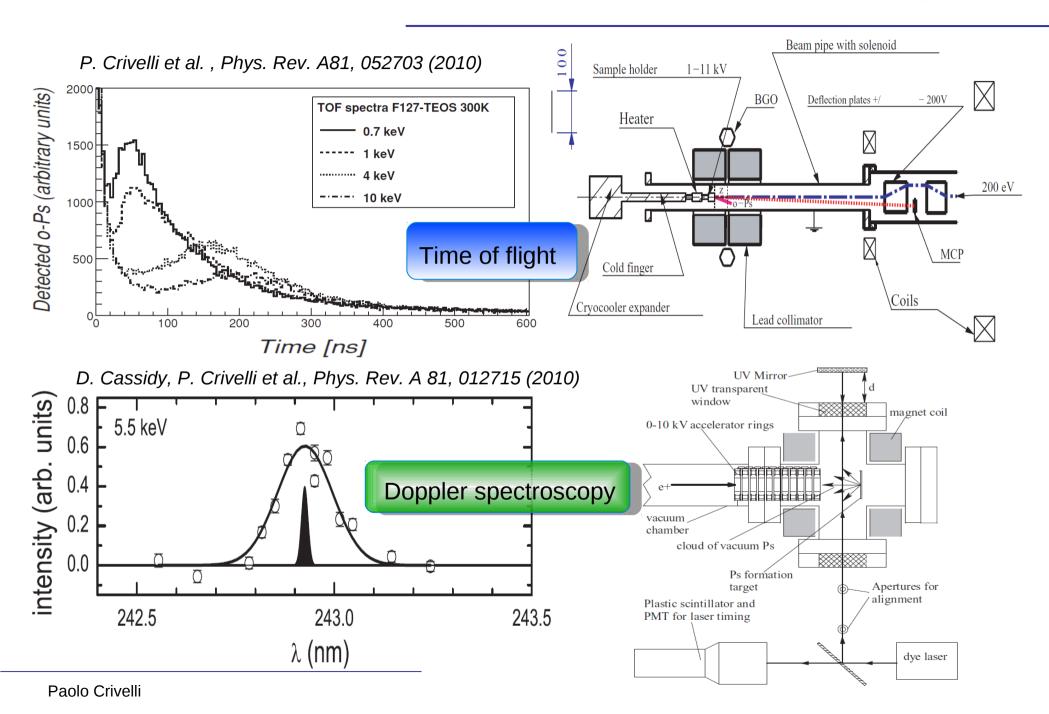


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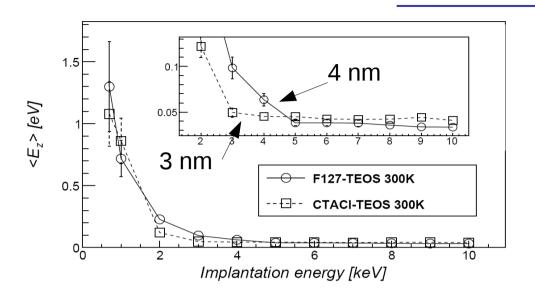


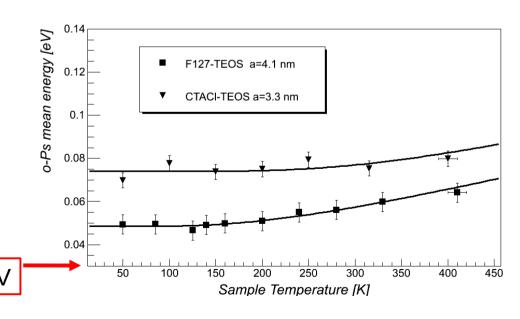


Measurement of Ps energy



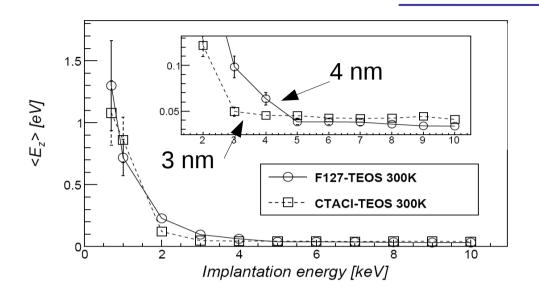
Measurement of Ps energy





Thermal energy 30 meV

Measurement of Ps energy



Ps de Broglie wavelength comparable to pore size -> Ps in the pores as to be treated QM

Ground state energy

$$E_{\mathrm{Ps}} = \frac{h^2}{2m \, d^2} \approx 0.8 \, \mathrm{eV} (1 \, \mathrm{nm}/d)^2$$

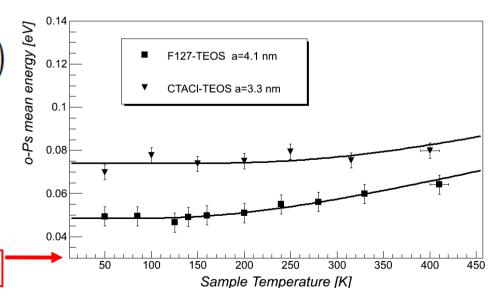
Ps as a particle in a box

$$\langle H \rangle = kT^2 \left(\frac{1}{Z(a)} \frac{dZ(a)}{dT} + \frac{1}{Z(b)} \frac{dZ(b)}{dT} + \frac{1}{Z(c)} \frac{dZ(c)}{dT} \right)$$

Z is the partition function defined as

$$Z(a) = \sum_{n=1}^{\infty} e^{-\frac{h^2 n^2}{8ma^2}/kT},$$

Thermal energy 30 meV



Colder Ps from silica films?

In principle it should be easy: use larger pores of 8-10 nm confinement energy ~50-100K (for muonium we could reach 100 K with 4 nm since de Broglie wavelength much smaller)

A. Antognini et al., PRL 108, 143401 (2010)

Recently: aluminum oxide nano-channels 5-8 nm -> 7% of Ps at 150 K

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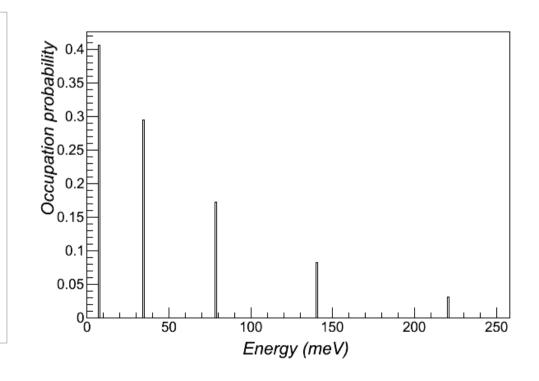
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Even at room temperature Ps is very fast $\sim 7 \times 10^4$ m/s

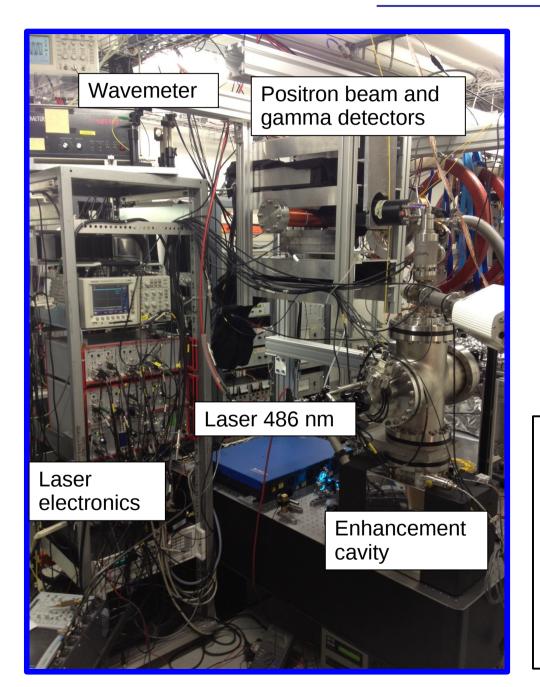
-> Second order Doppler shift ~ 30 MHz is expected to be the main systematic in our measurement.

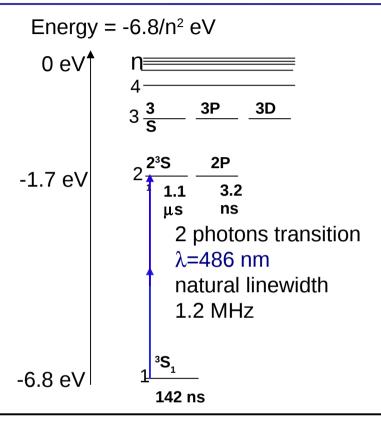
BUT for porous silica one would expect to see at least 3 peaks in the resonance curve

-> correction of the 2nd order Doppler shift



The laser system for Ps 1S-2S

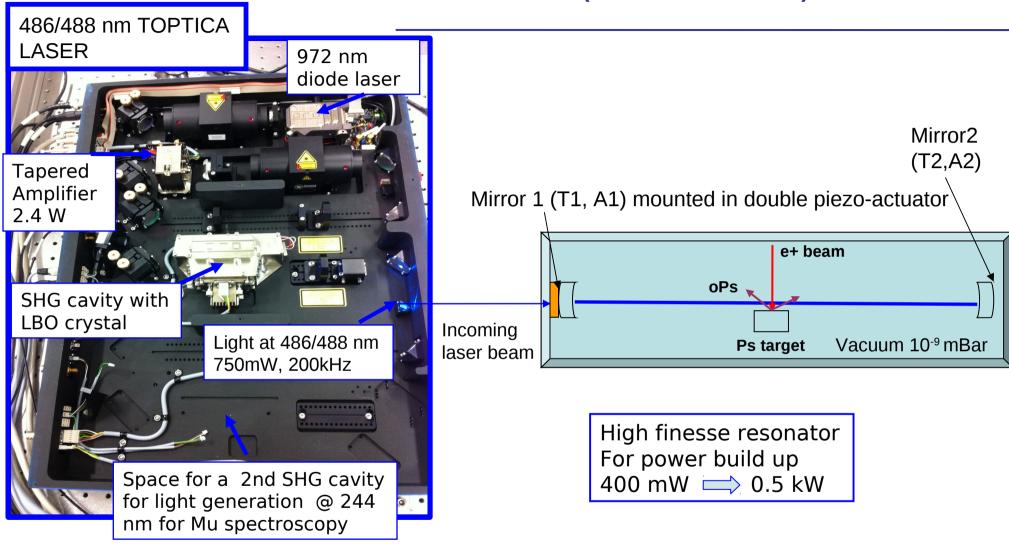




Requirements:

- -> High power (~kW) at 486 nm to get a detectable signal
- -> Long term stability (continuous data taking ~days)
- -> Scanning of the laser ± 100 MHz

The laser (Ps and Mu)



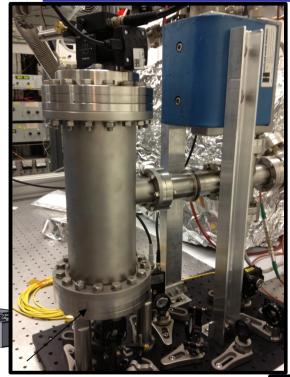


Cavity linewidth few kHz -> laser need to be stabilized to the same level.

Stabilization - the 972 nm FP

MPQ design

mirror
ULE spacer
Thermal shields
Peltier elements



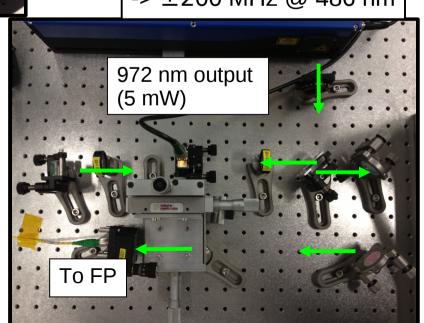
R 99.99% (Layertec) F = 31000 FSR = 1.5 GHz Linewidth 48 kHz

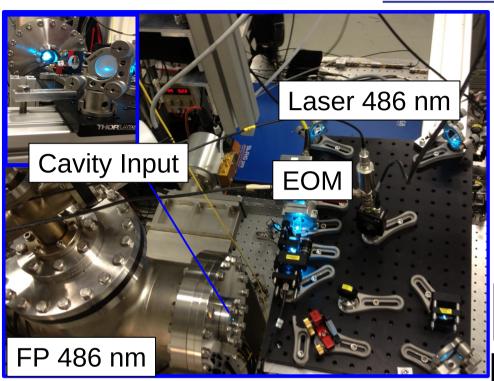
> Double pass AOM -> ±200 MHz @ 486 nm

Vacuum flange

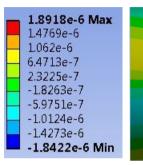
Charachterization:

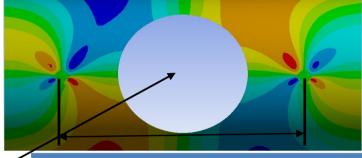
- Long term drift against Te2 (T not yet optimized) <1 MHz/day
- Short term ~ kHz (efficient incoupling to FP 486 nm)





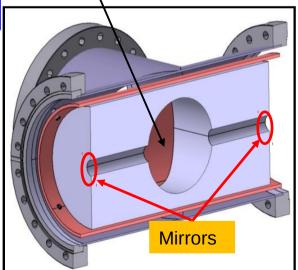
T1 = 49 ppm, T2 = 7 ppm A1 = 12 ppm, A2=7ppm FSR= 0.55 GHz Linewidth = 7 kHz Finesse ~ 80000 Incoupling 40% Static structural directional deformation analysis (ANSYS) along the X axis (units: mm)



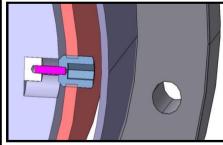


Hole for positron beam

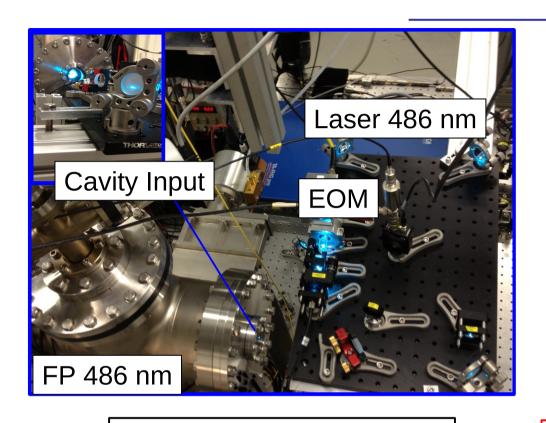
Optimized distance 186.7mm for suspending the resonator -> deformation due to gravity does not change mirror separation

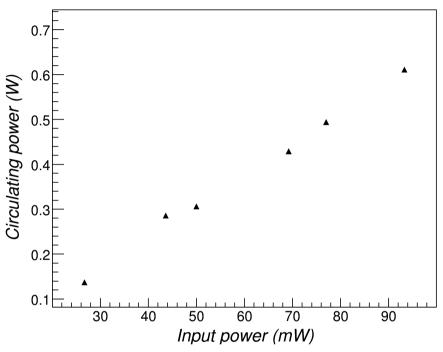


Suspension System



^{*}Ultra-low-loss mirrors from ATFilms (https://www.atflims.com)





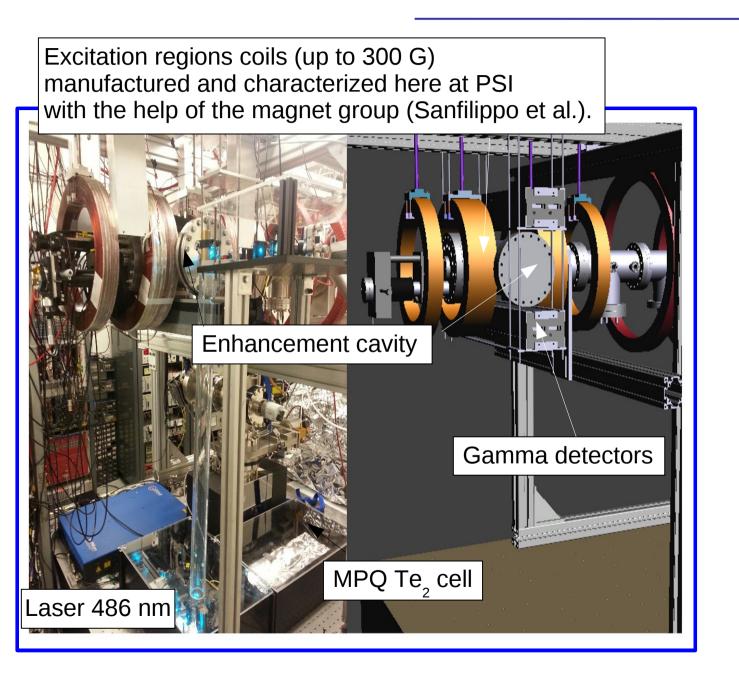
T1 = 49 ppm, T2 = 7 ppm A1 = 12 ppm, A2=7ppm FSR= 0.55 GHz Linewidth = 7 kHz Finesse ~ 80000 Incoupling 40%

At 0.4 MW/cm² (0.7 kW circulating power) mirror degradation observed.

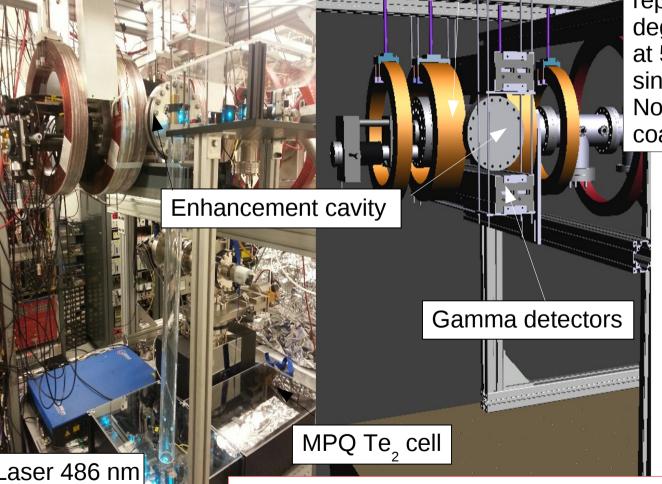
Run @ 0.5 kW:

- -> Excitation prob $\sim 4x10^{-4}$
- -> Resonant 3γ PI ~ $4x10^{-5}$

^{*}Ultra-low-loss mirrors from ATFilms (https://www.atflims.com)



Excitation regions coils (up to 300 G) manufactured and characterized here at PSI with the help of the magnet group (Sanfilippo et al.).



Problem: after mounting the cavity on beam line could not reproduce the same results, degradation occurred already at 500W ...Suspected input mirror since its transmission changed. Now both mirrors from the same coating run.

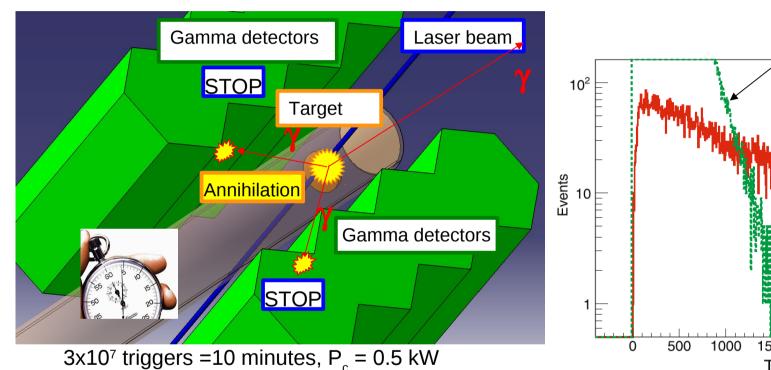
T1 = T2 = 7 ppm
A1 = A2 = 7 ppm
FSR= 0.55 GHz
Linewidth = 2.5 kHz
Finesse ~ 225000
Incoupling 24%

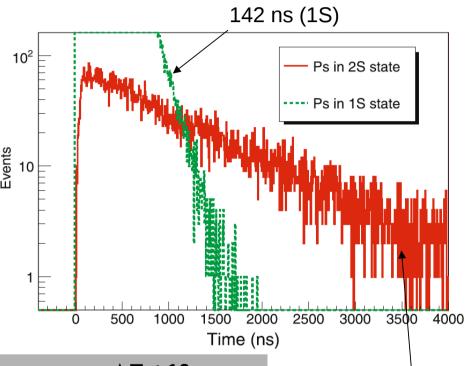
Stable generation of 500 W, no degradation over hours of continuous operation.

1) Detection of Ps 1S-2S - Lifetime method

Detection of annihilation photons. Lifetime of excited S states $\sim n^3$

 $\tau_{2S} / \tau_{1S} = 8$



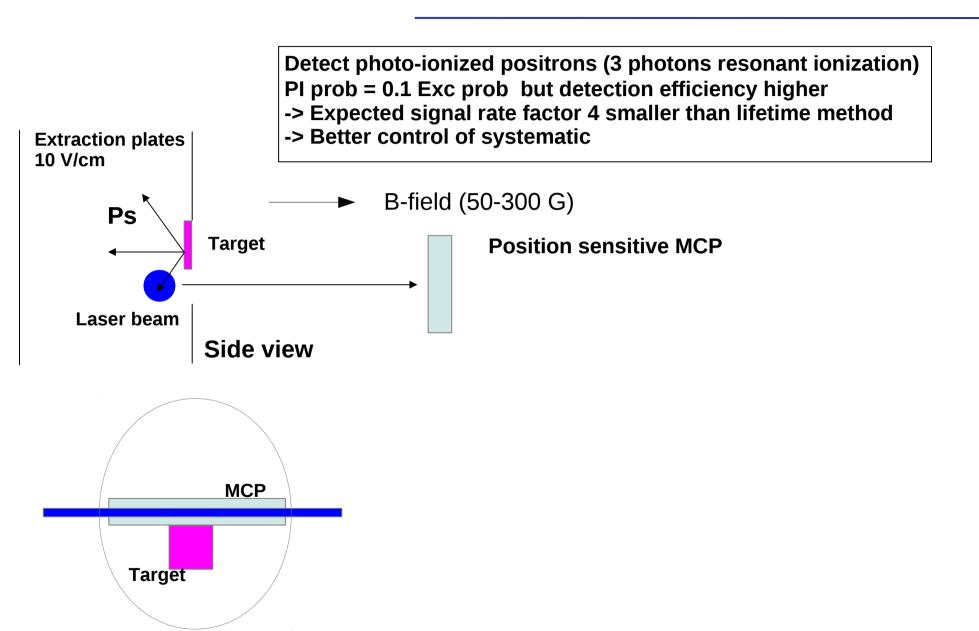


	Events	1 BGO (2-4μs)	2 BGO (2-4μs)	ΔT ±10 ns
2S Ps	4 x 10 ³	342	129	127
1S	9.8 x 10 ⁶	4	2	2
Accidentals	-	4950	42	4

1136 ns (2S)

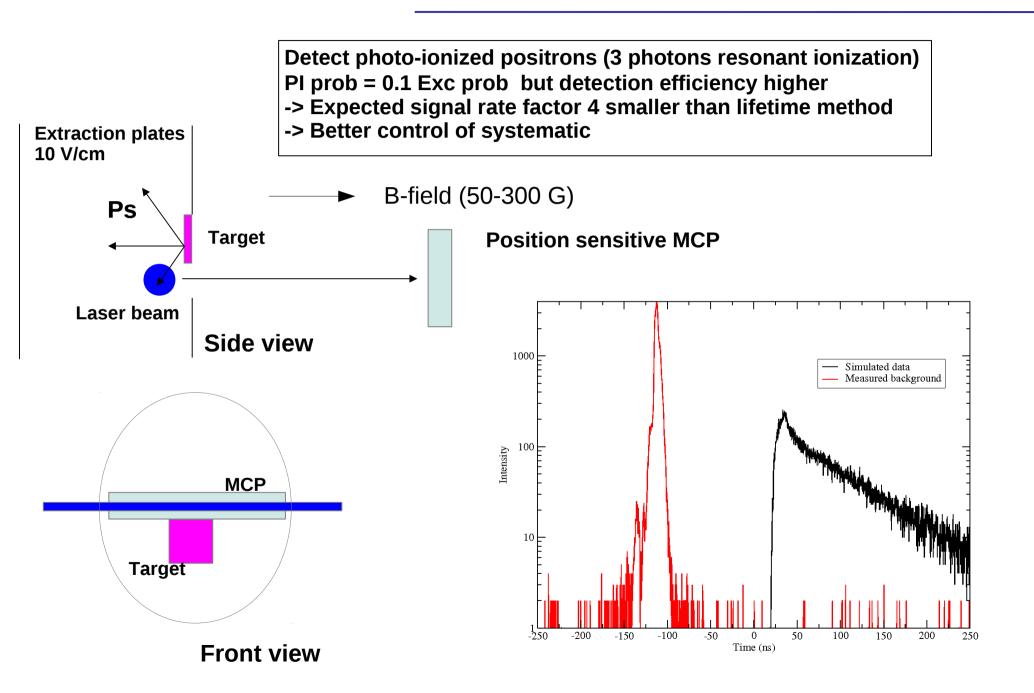
On resonance: 1250 events in 2 hours run

2) Detection of Ps 1S-2S - Pl positrons

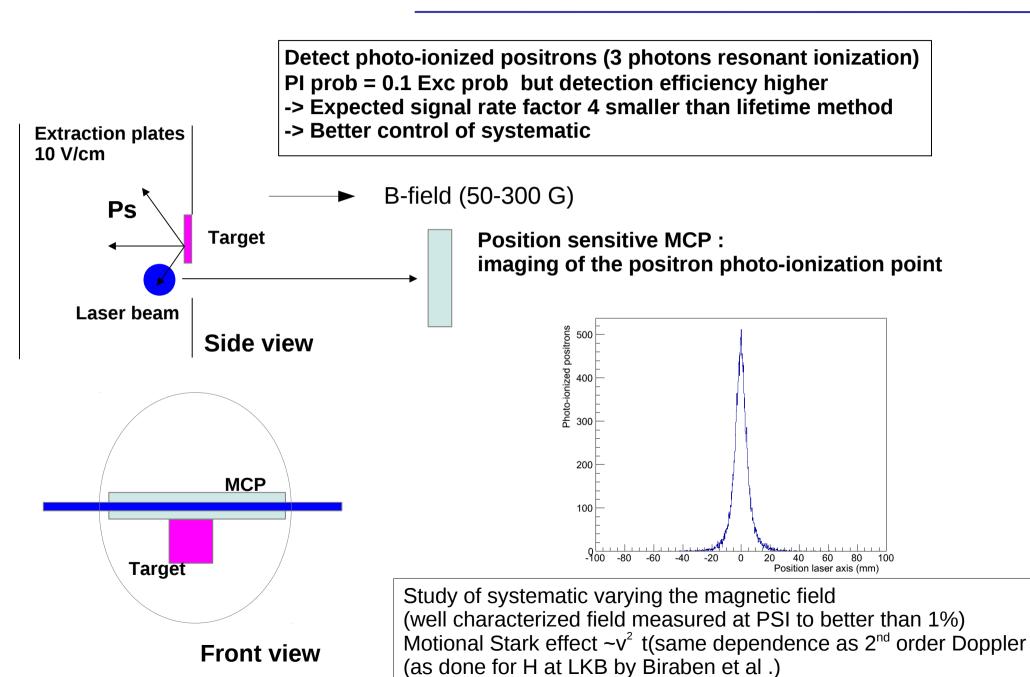


Front view

2) Detection of Ps 1S-2S - PI positrons



2) Detection of Ps 1S-2S - PI positrons



Expected accuracy

With available source of Ps:

- Porous silica films: 30% @ 40 meV mono-energetic, isotropic emission
- 1) Uncertainty from statistics 1.8 MHz -> 0.35 MHz.
- Better positron beam (1 mm), higher detection efficiency, no restriction of beam time (careful systematic study), stable Ps formation

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Measurement of 1S-2S of Ps at a level about $5x10^{-10}$ seems feasible => check QED

Outlook

- Laser system and positron beam are combined



- In July: problems with enhancemement cavity and arcing now solved
- -> stable generation of 500 W and new desing for the electrodes in the excitation chamber



- Last week cryocooler to grow Ne moderator started to have problems. The temperature of 7K cannot be kept constant...some maintenance needed

(involve handling the radioactive source)...

Use Ar instead that is providing 30% of Ne efficiency...we will go ahead with that for the moment...

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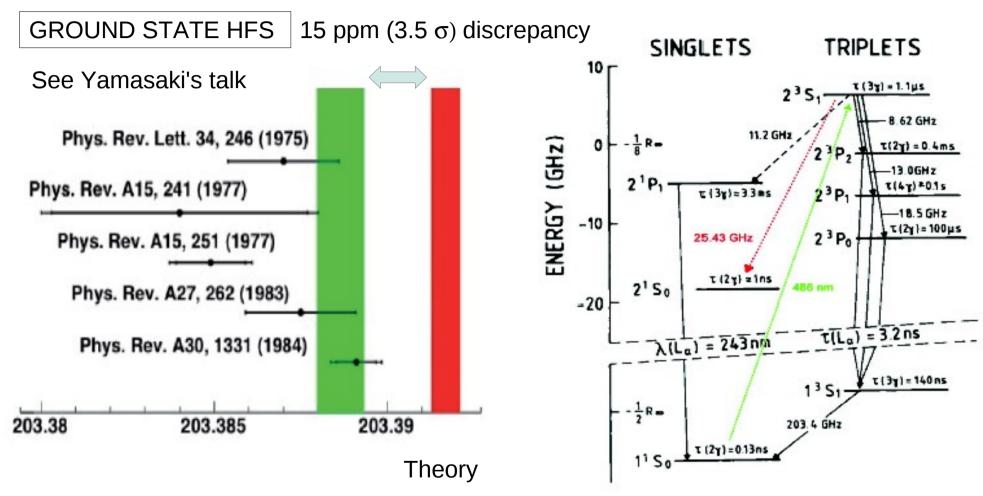
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Efforts to reduce the Ps velocity (~100 K should be achievable with porous films): -> new porous films being tested (in collaboration with CEA Saclay) and hierarchical zeolites (in collaboration with Prof. J. Perez, ETHZ Chemistry department).

2S hyperfine splitting



K. Melnikov, A. Yelkhovsky, Phys. Rev. Lett. 86, p. 1498 (1501 (2001).

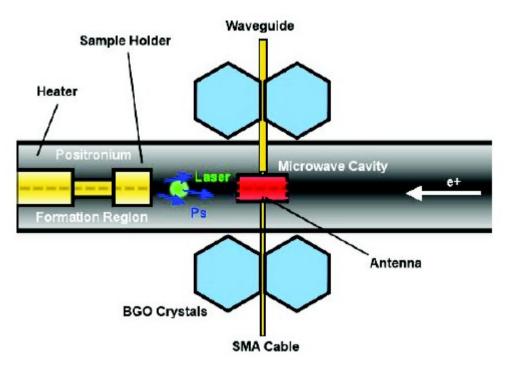
R. J. Phys. Rev. Lett. 86, p. 3280 (2001).

K. Pachucki, Phys. Rev. A 56, 297 (1997).

A. Czarnecki, K. Melnikov, A. Yelkhovsky, Phys. Rev. Lett. 82, p. 311{314 (1999).

Origin? Experimental problem (linear extrapolation to zero density), theory, new physics?

2S hyperfine splitting

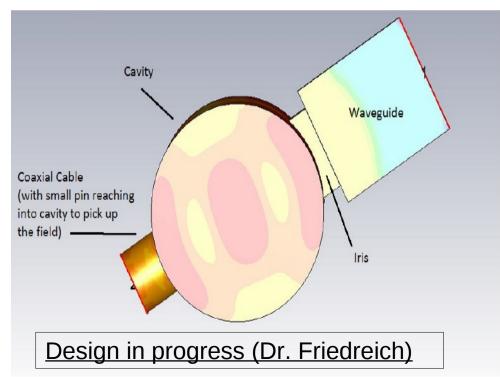


<u>Advantages</u>: Different experimental method than measurements in ground state

- no need for extrapolation to zero density since Ps in vacuum
- no need for challenging level control on magnetic field.
- Required power at 25.43 GHz is commercially available.

Goal:

- observe this transition for the first time (a level of 50 ppm seems feasible)
- long term reach accuracy comparable with the one of the ground state, using high granularity detector for background suppression and 10 times stronger positron Source. Colder Ps would be of great help.



Thank you for your attention ©