

Rare pion and kaon decays

---Precision measurements of rare decays---

Toshio Numao

TRIUMF

Suppressed decays

$$L = L_{\text{SM}} + L_{\text{NewPhysics}}$$

Highly suppressed
Well calculated

Helicity suppression for $V-A \rightarrow$ Pseudoscalar interactions

Branching ratio: $\Gamma(M \rightarrow e\nu)/\Gamma(M \rightarrow \mu\nu)$, $M=\pi$ or K

Clean: Hadronic contributions cancel in the ratio

NA62 and TREK talks

GIM suppression for FCNC \rightarrow 2nd order weak interactions

$K^+ \rightarrow \pi^+ \nu\bar{\nu}$ and $K_L \rightarrow \pi^0 \nu\bar{\nu}$ decays

Clean: Hadronic contributions extracted from $K-\pi e\nu$

NA62, j-PARC and Proj-X talks

SM branching ratio calculations

$$R_{e/\mu}^0 = \frac{\Gamma(\pi \rightarrow e\nu)}{\Gamma(\pi \rightarrow \mu\nu)} = \frac{g_e^2 m_e^2}{g_\mu^2 m_\mu^2} \frac{(m_\pi^2 - m_e^2)^2}{(m_\pi^2 - m_\mu^2)^2}$$

$$= 1.284 \times 10^{-4}$$

$$R_{e/\mu}^{\text{th}} = \frac{\Gamma(\pi \rightarrow e\nu + \pi \rightarrow e\nu\gamma)}{\Gamma(\pi \rightarrow \mu\nu + \pi \rightarrow \mu\nu\gamma)}$$

$$= 1.2352(1) \times 10^{-4} \quad \text{Cirigliano, Rosell 2007}$$

Experimental status:

$R_{\text{exp}} = 1.2265(34)(44) \times 10^{-4}$ (TRIUMF, 1992)

$1.2346(35)(36) \times 10^{-4}$ (PSI, 1993)

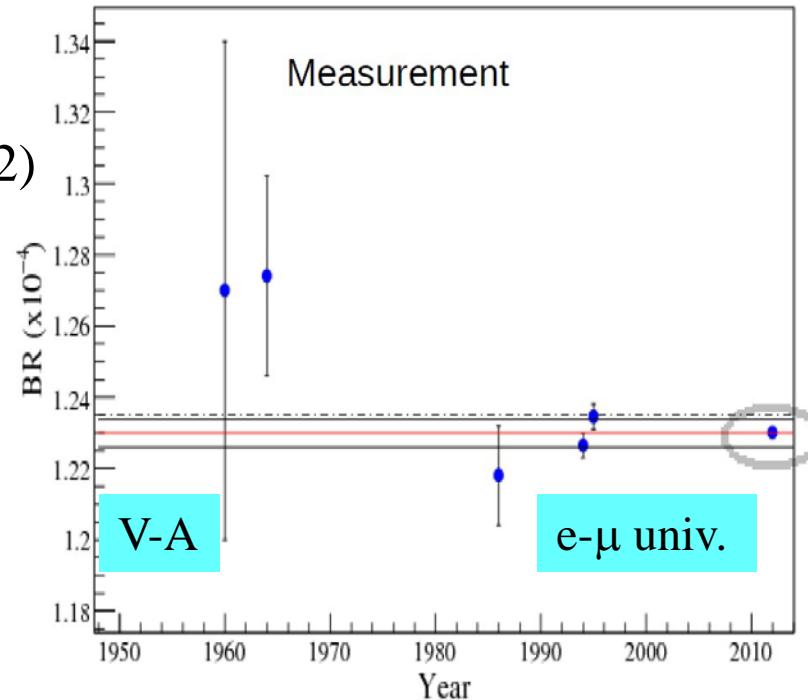
Test of $e\text{-}\mu$ universality

Beyond the SM

Mass scale up to 1000 TeV

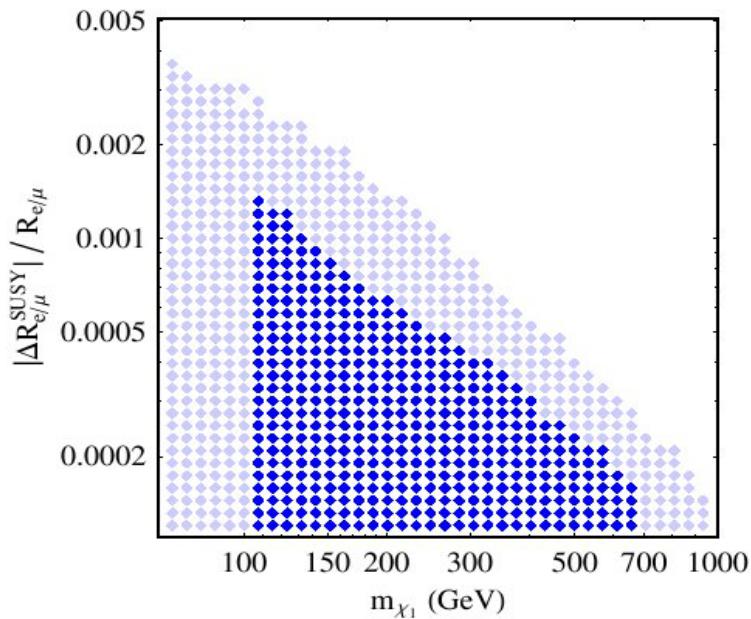
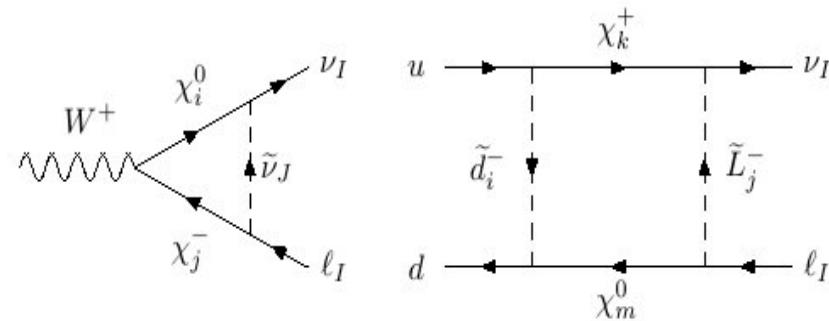
Sterile neutrino

SUSY...



Beyond the Standard Model

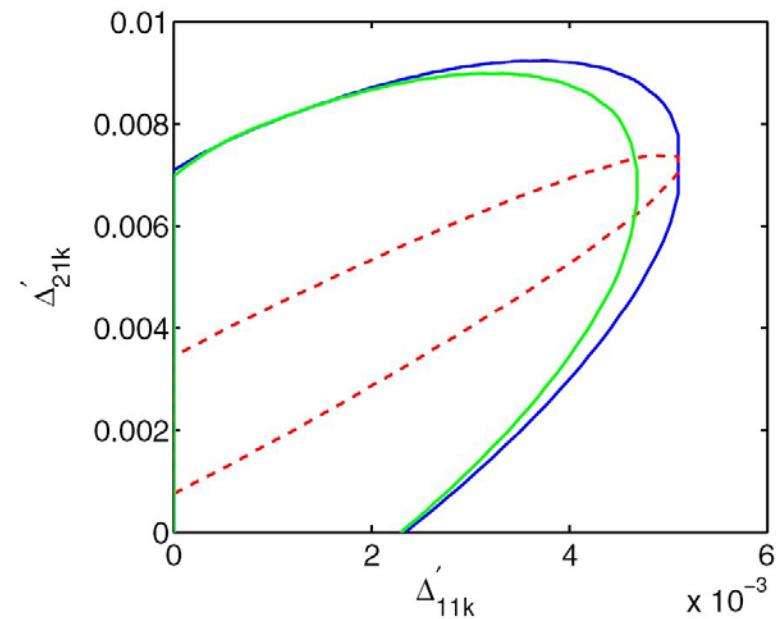
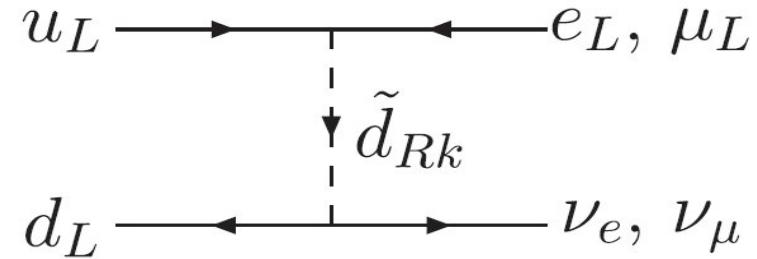
Minimal SUSY SM



Lowest chargino mass

Ramsey-Musolf... PRD76 095017 (2007)

R-Parity Violating SUSY



Pion decays---Method

$$A(\pi \rightarrow e\nu)/A(\pi \rightarrow \mu\nu)$$

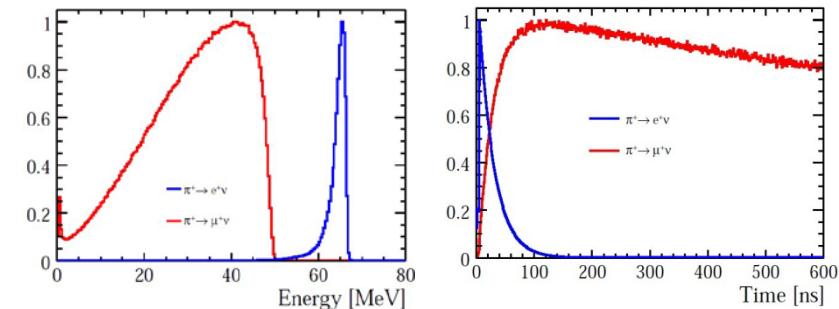
PSI 1993

- Muon range is 1.4 mm plastic.
- Acceptance difference,...

$$A(\pi \rightarrow e\nu)/A(\pi \rightarrow \mu \rightarrow e)$$

$$\begin{aligned} \pi^+ &\rightarrow \mu^+\nu \quad 26 \text{ ns} \\ &\quad \swarrow \quad \downarrow \quad \text{e}^+\nu\bar{\nu} \quad 2 \text{ }\mu\text{s} \end{aligned}$$

TRIUMF 1992



- Small energy-dependent effects for positrons
- Pion life

Unavoidable correction (uncertainty)

- Low energy tail of the $\pi \rightarrow e\nu$ peak.

PIENU at TRIUMF

Data taking: -2012

NaI+CsI: 2 % (FWHM) @ 70MeV

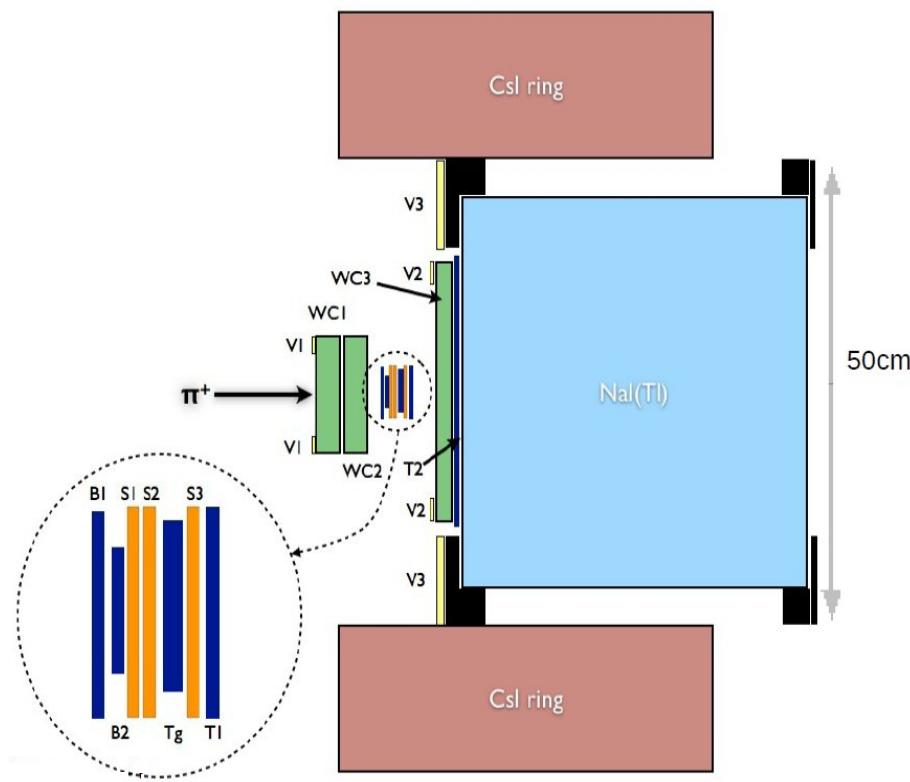
Radiation length: 20

Solid angle: 25 %

Pion stop: 50 kHz

Goal: <0.1 %

No. of pienu: 5 M (clean)



PEN at PSI

Data taking: -2010

CsI: 6 % (FWHM) @ 70 MeV

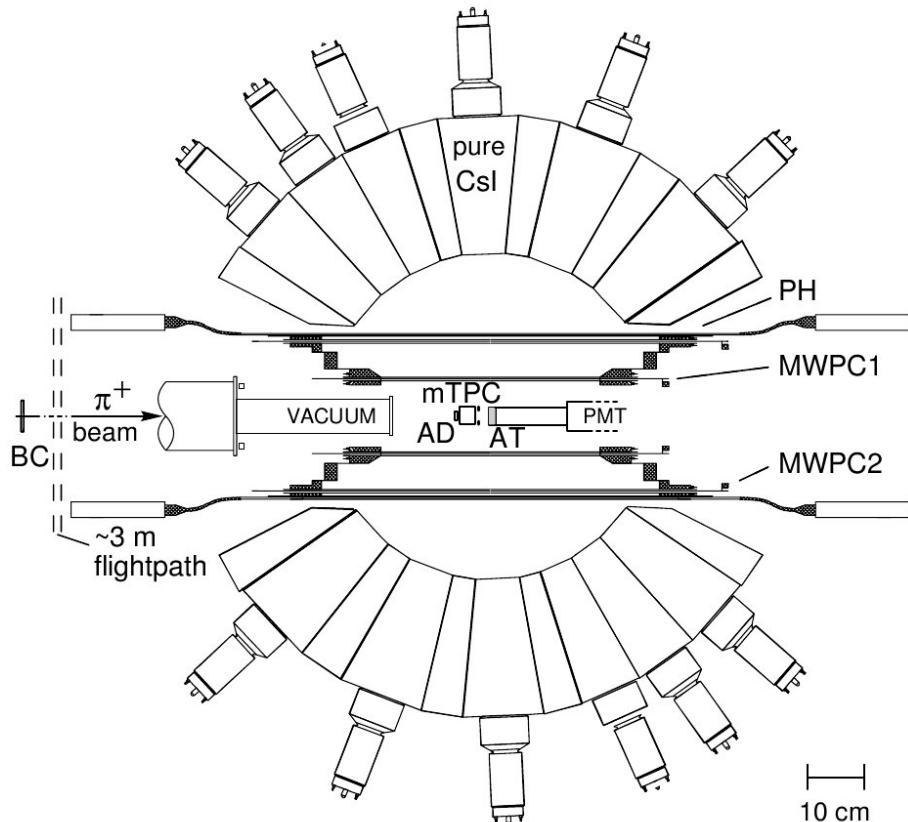
Radiation length: 12

Solid angle: 70 %

Pion Stop: 10-50 kHz

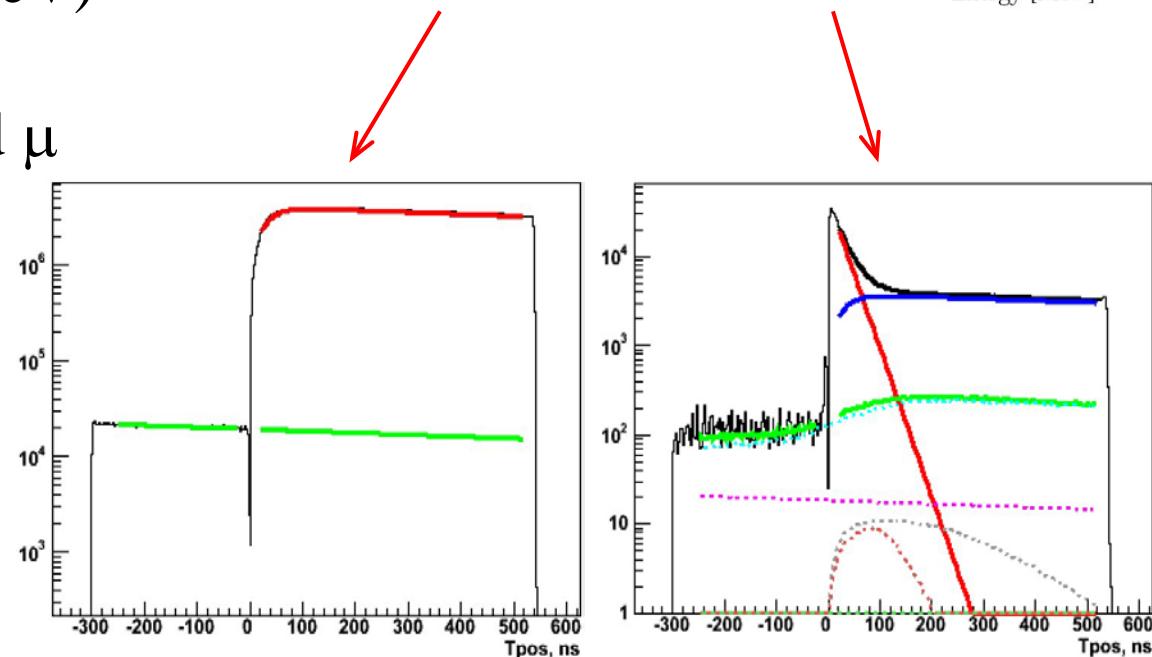
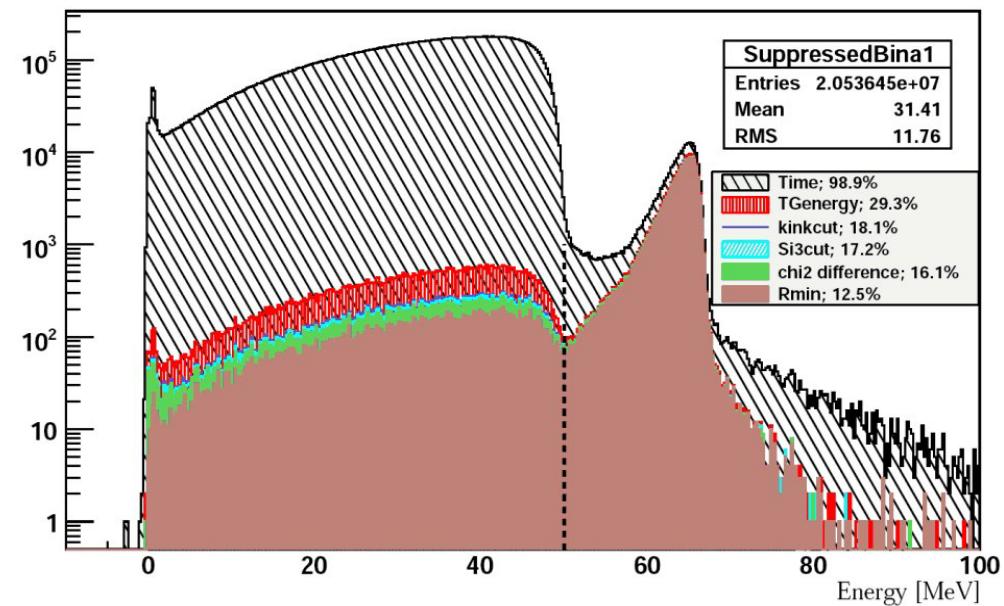
Goal: <0.1 %

No. of pienu: 22 M

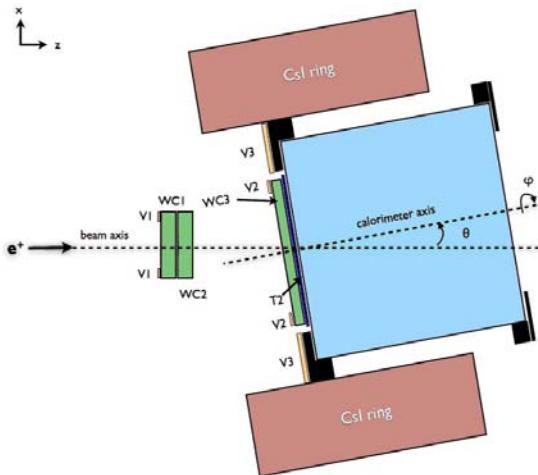


TRIUMF PIENU

- Time window -300 to 500ns
- Enhance π -ev decay @ trigger
 - Early decays (5-40ns), or
 - High energy (>45 MeV)
- Select single π stops.
- Separate time spectra (50 MeV)
- Fit simultaneously
 - π -ev, π - μ -e, (π DIF), old μ
 - radiative π decays
 - π + old μ
 - (μ DIF)
- Tail correction
- Other corrections

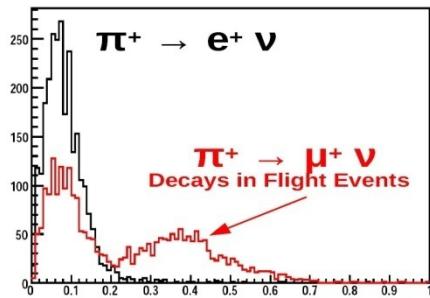
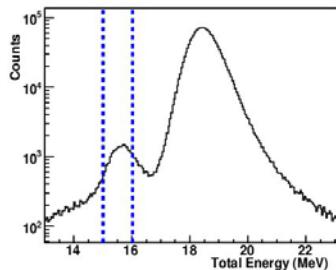


Correction for low energy π -e ν (tail)



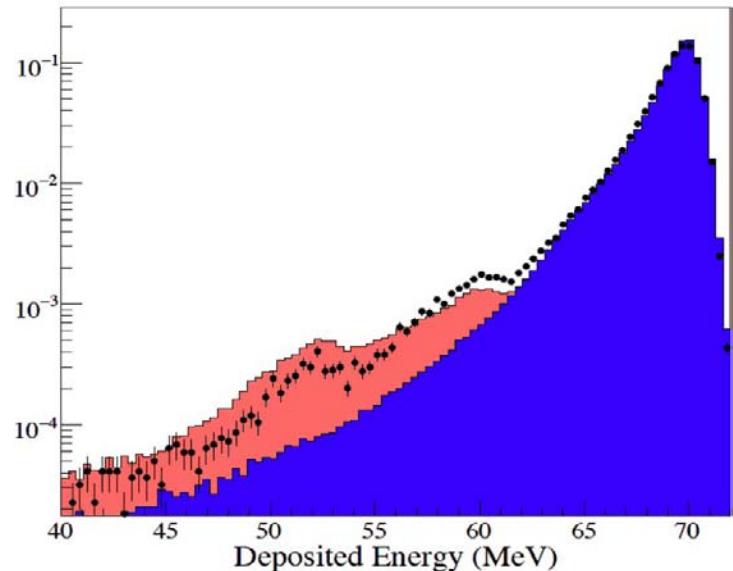
Response function measurements

Response function measurement.
Lower bound.

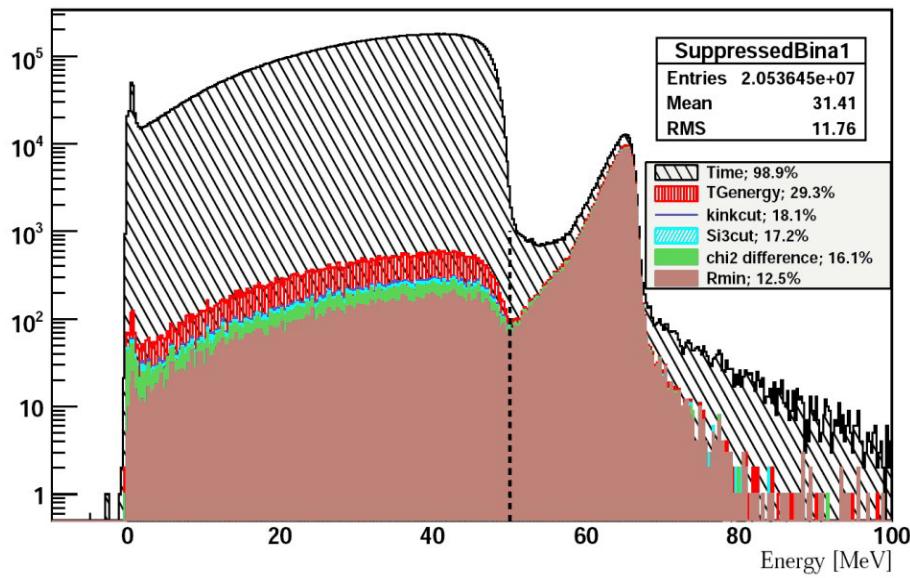


- Suppress π - μ -e background.
- Subtract π , μ DIF background.
- Correct for selection bias.

Fraction = $2 \pm 0.1\%$ (improvement expected)

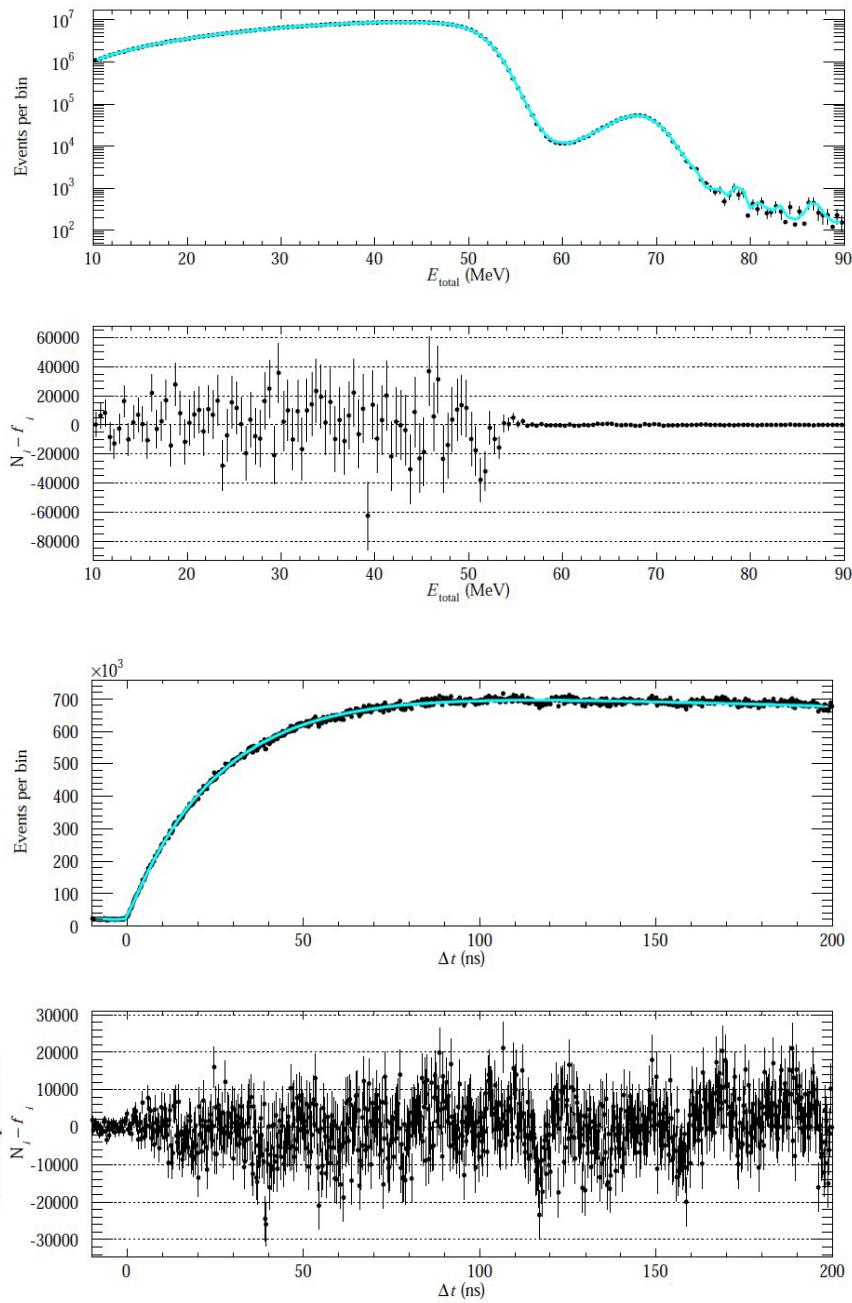
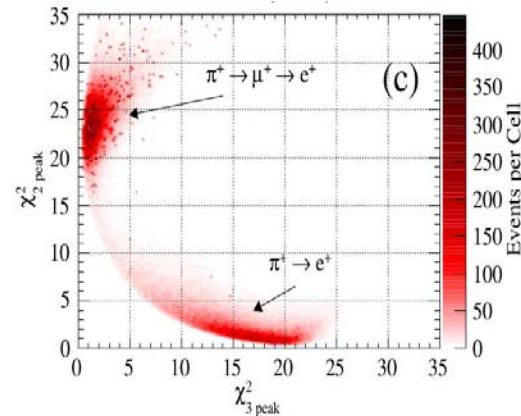
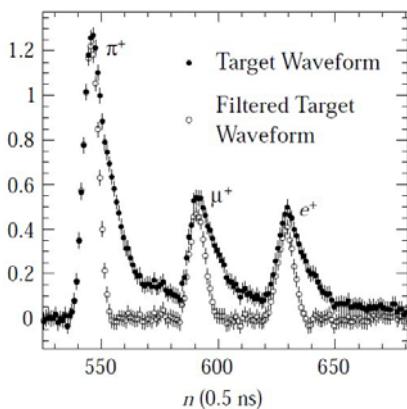


70 MeV e⁺ at 0°.

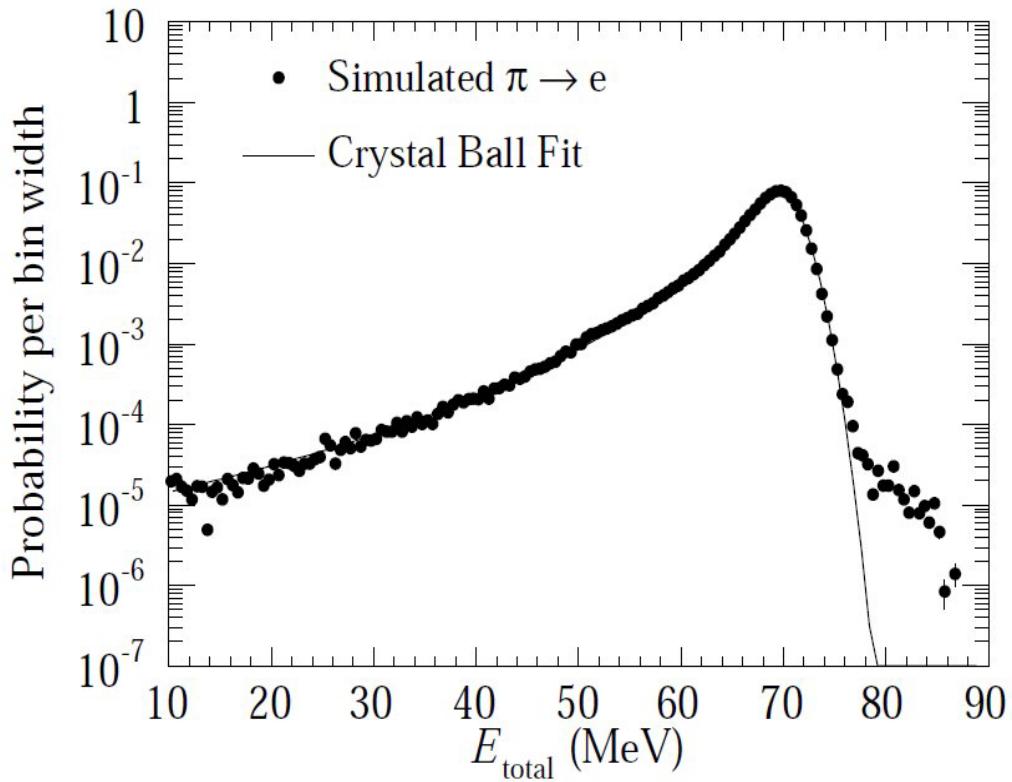


BG suppressed spectra

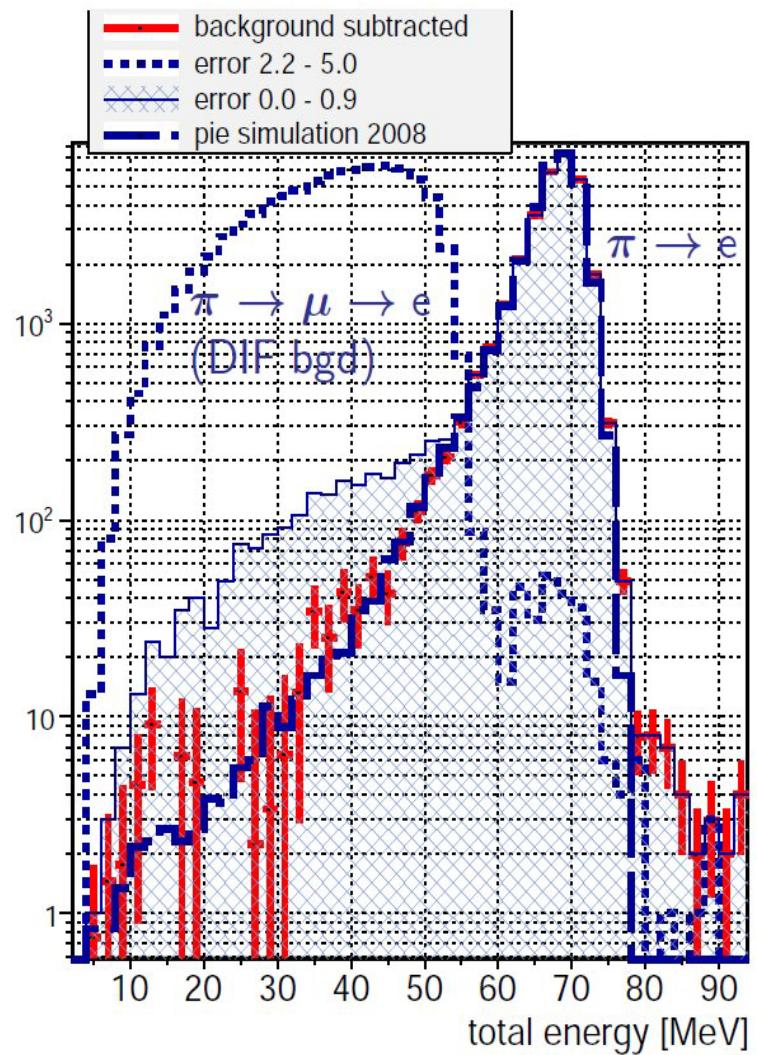
- Time window -25 to 250ns
- Enhance π -ev events @trigger
 - Above 50 MeV
 - No μ pulse
- Single π stops
- Maximum Likelihood Meth.
- 5 main components; π -ev, π - μ -e,
 π DIF, old μ , proton (prompt)...
- Inputs; Energy, time...
- Tail included in the estimates



Correction for low energy pienu (tail)



-Fit to MC generated spectrum
-Iteration



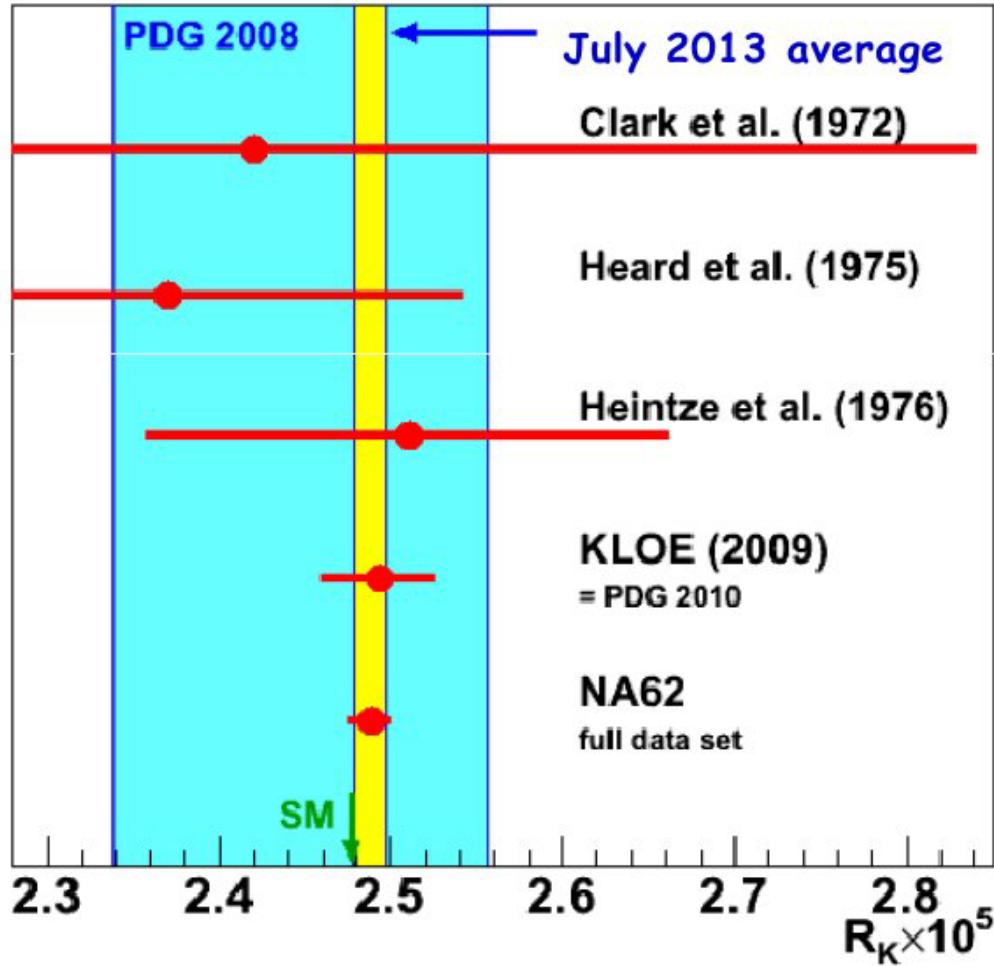
Summary of uncertainties

| Source | Old Triumf | PIENU | From proposal PEN |
|-----------------|---------------|---------------|----------------------|
| Statistical | 0.0028 | 0.0005 | 0.0002 |
| Low-energy tail | 0.0025 | 0.0003 | ? |
| Accept diff. | 0.0011 | 0.0003 | 0.0002 |
| Pion life | 0.0009 | 0.0002 | ? |
| Other | 0.0011 | 0.0003 | 0.0002 |
| Total | 0.0047 | 0.0006 | 0.0005 |

K-eν/K-μν

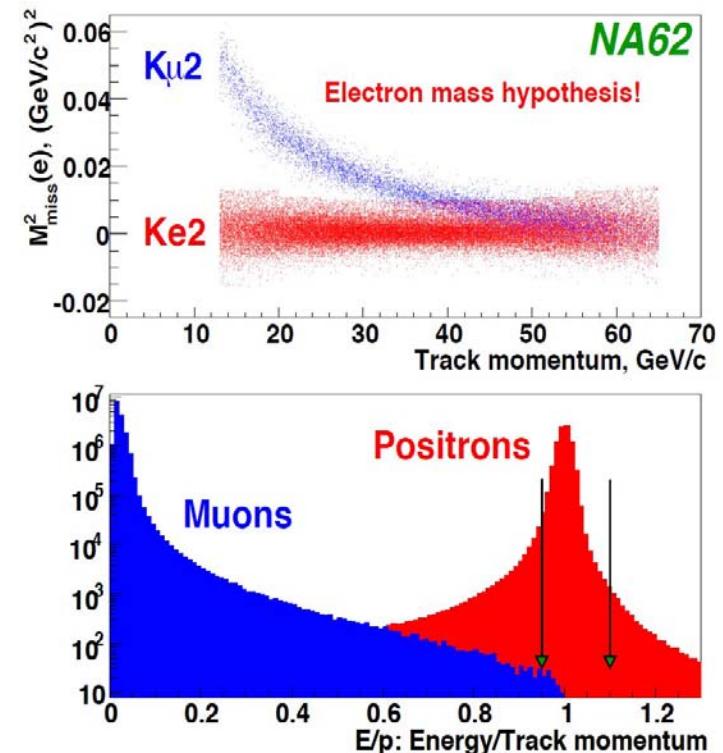
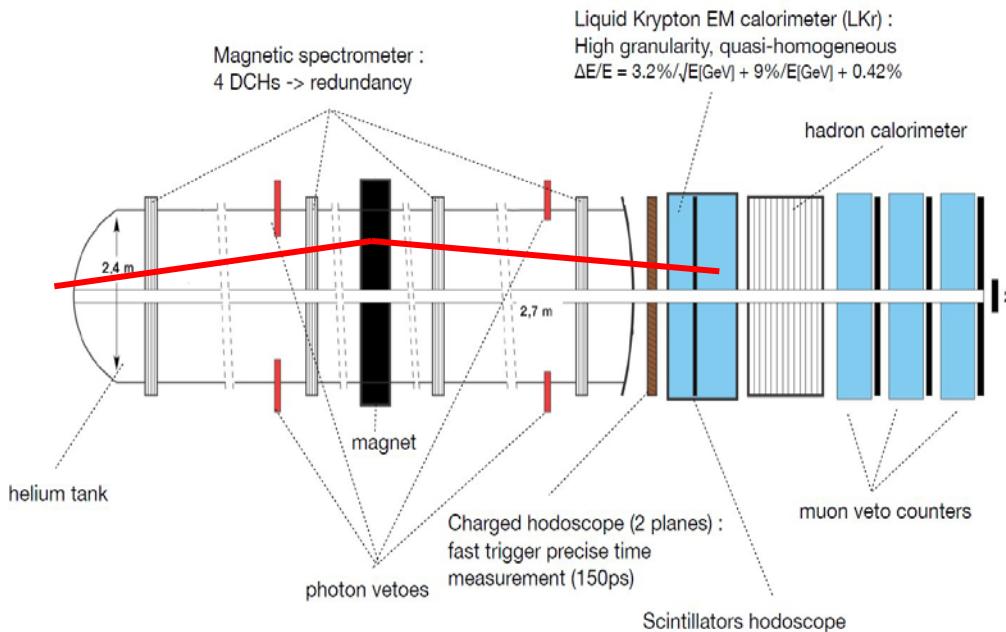
$$\begin{aligned}
 R_K &= \frac{\Gamma(K \rightarrow e\nu)}{\Gamma(K \rightarrow \mu\nu)} \\
 &= \frac{g_e^2 m_e^2 (m_K^2 - m_e^2)^2}{g_\mu^2 m_\mu^2 (m_K^2 - m_\mu^2)^2} \\
 &\quad \times (1 + \delta R_K) \\
 &= (2.477 \pm 0.001) \times 10^{-5}
 \end{aligned}$$

Cirigliano, Rosell 2007



$$\text{Average} = (2.488 \pm 0.009) \times 10^{-5}$$

NA48-3/NA62@CERN



DIF experiment

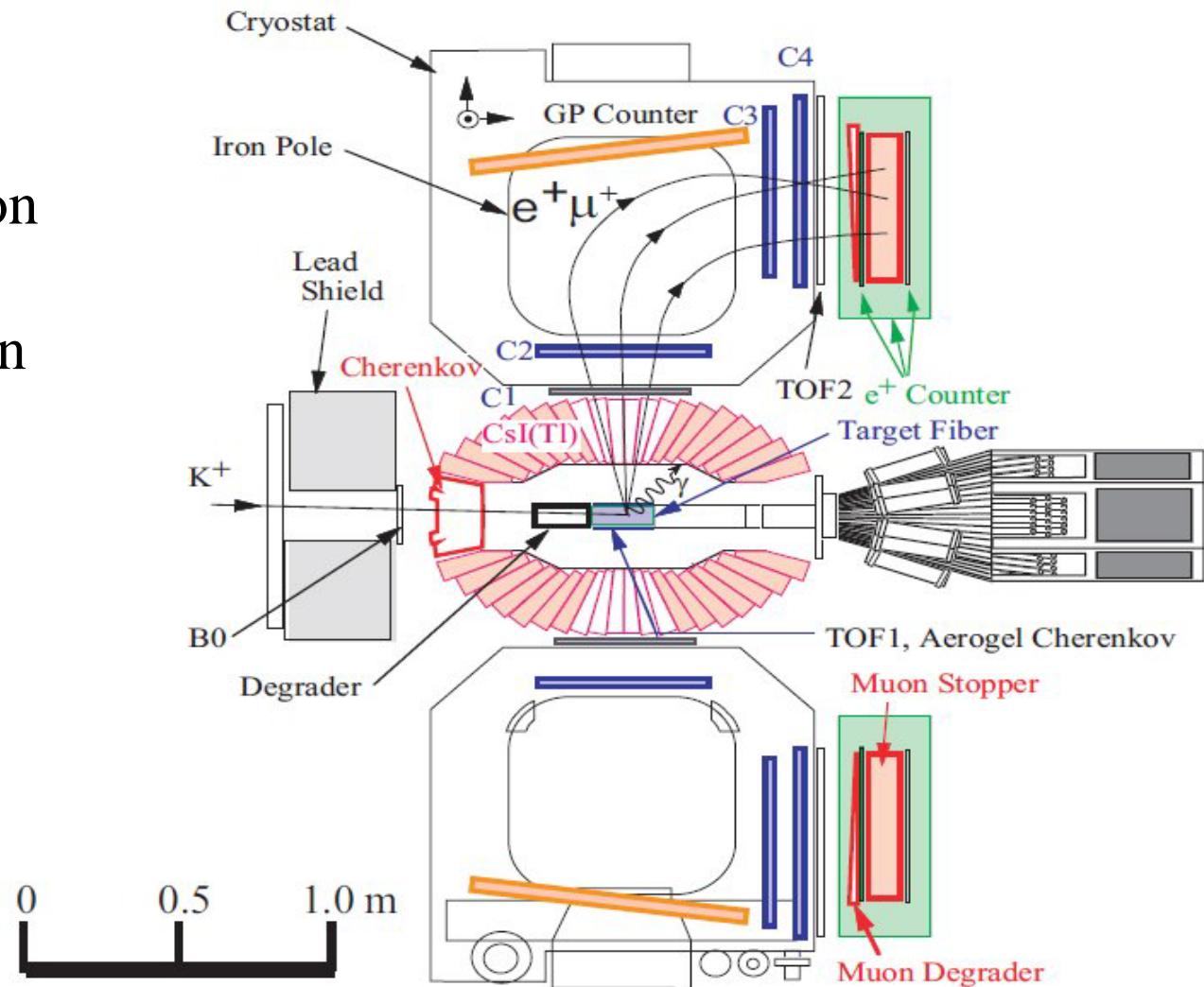
$$M_{\text{miss}}^2 = (P_K - P_{\text{lep}})^2$$

$$R_K = (2.488 \pm 0.007_{\text{stat}} \pm 0.007_{\text{syst}}) \times 10^{-5}$$

RICH for less BG in future?

TREK @J-PARC

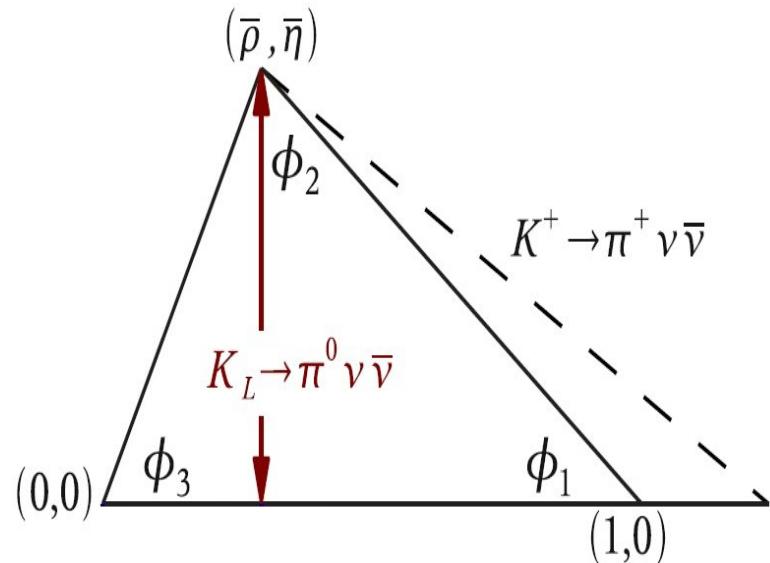
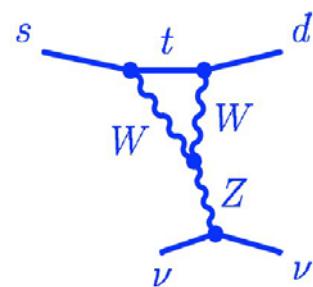
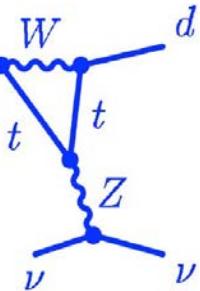
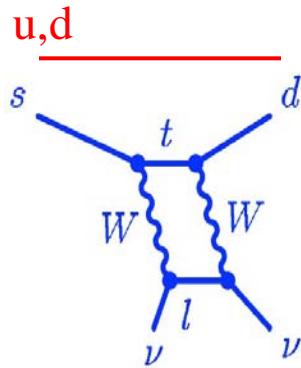
- Designed for T-violation
- Decay at rest
- Aims at 0.2 % precision



Summary of μ -e universality

| Modes | g_e/g_μ | Goals |
|---|---------------------|------------------------|
| $\pi\text{-}e\nu/\pi\text{-}\mu\nu$ | 0.9979 ± 0.0016 | $\rightarrow 0.0004 >$ |
| $K\text{-}e\nu/K\text{-}\mu\nu$ | 1.0022 ± 0.0018 | $\rightarrow 0.0010$ |
| $\tau\text{-}e\nu\bar{\nu}/\tau\text{-}\mu\nu\bar{\nu}$ | 0.9980 ± 0.0015 | |
| $W\text{-}e\nu/W\text{-}\mu\nu$ | 0.999 ± 0.011 | |
| Average | 0.9991 ± 0.0009 | |

K $\rightarrow\pi\nu\bar{\nu}$ decays

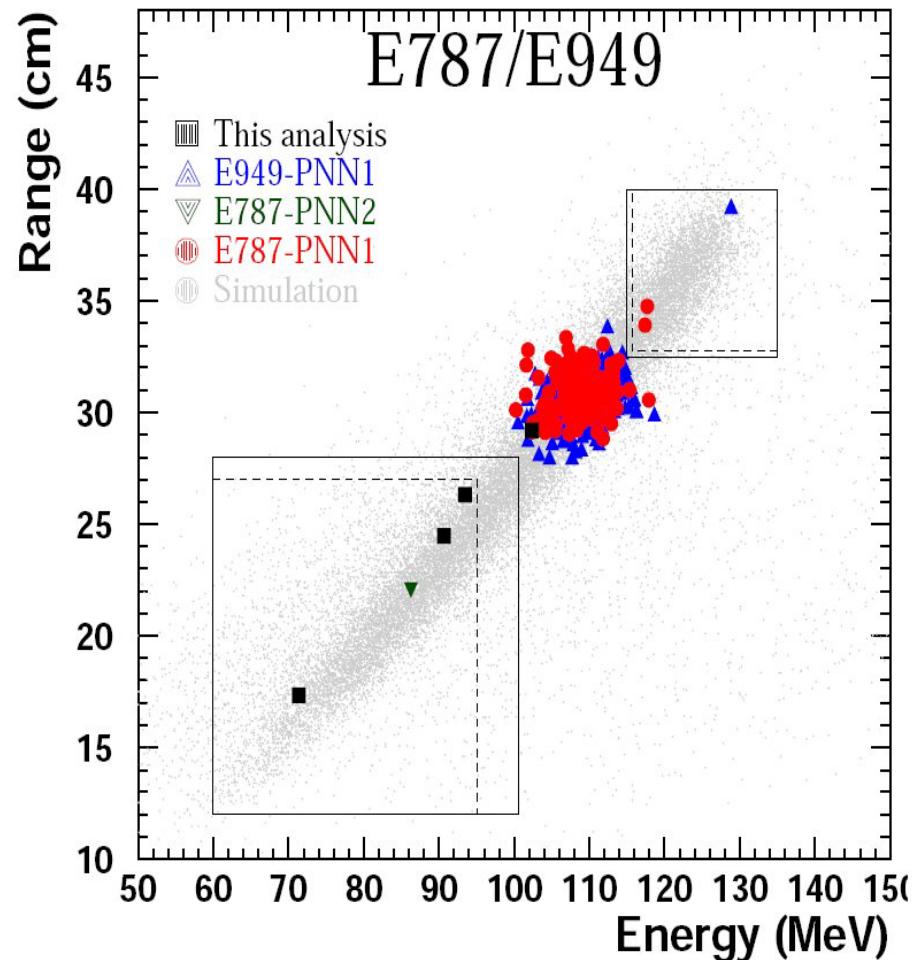
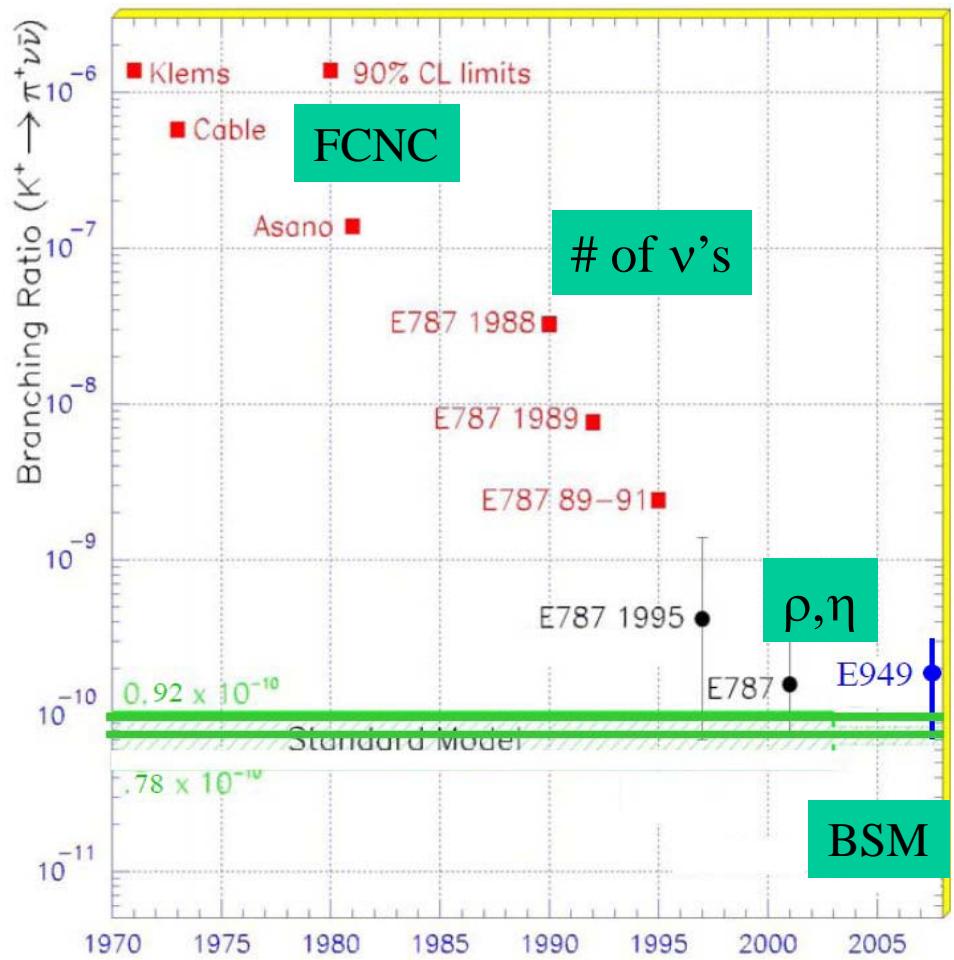


- K- $\pi\nu\bar{\nu}$ decay provides hadronic form factors.
- Calculated including the full 2-loop EW corrections.
- Uncertainties come from that of the CKM matrix.
- Uncertainty in the charm contribution in K^+ decay is 5 %.
- K_L decay is CP violating with very small uncertainty (1 %).

$$\text{Br}(K^+) = (7.81 \pm 0.75 \pm 0.29) \times 10^{-11}$$

$$\text{Br}(K_L) = (2.43 \pm 0.39 \pm 0.06) \times 10^{-11} \quad \text{J.Brod et.al., 2011}$$

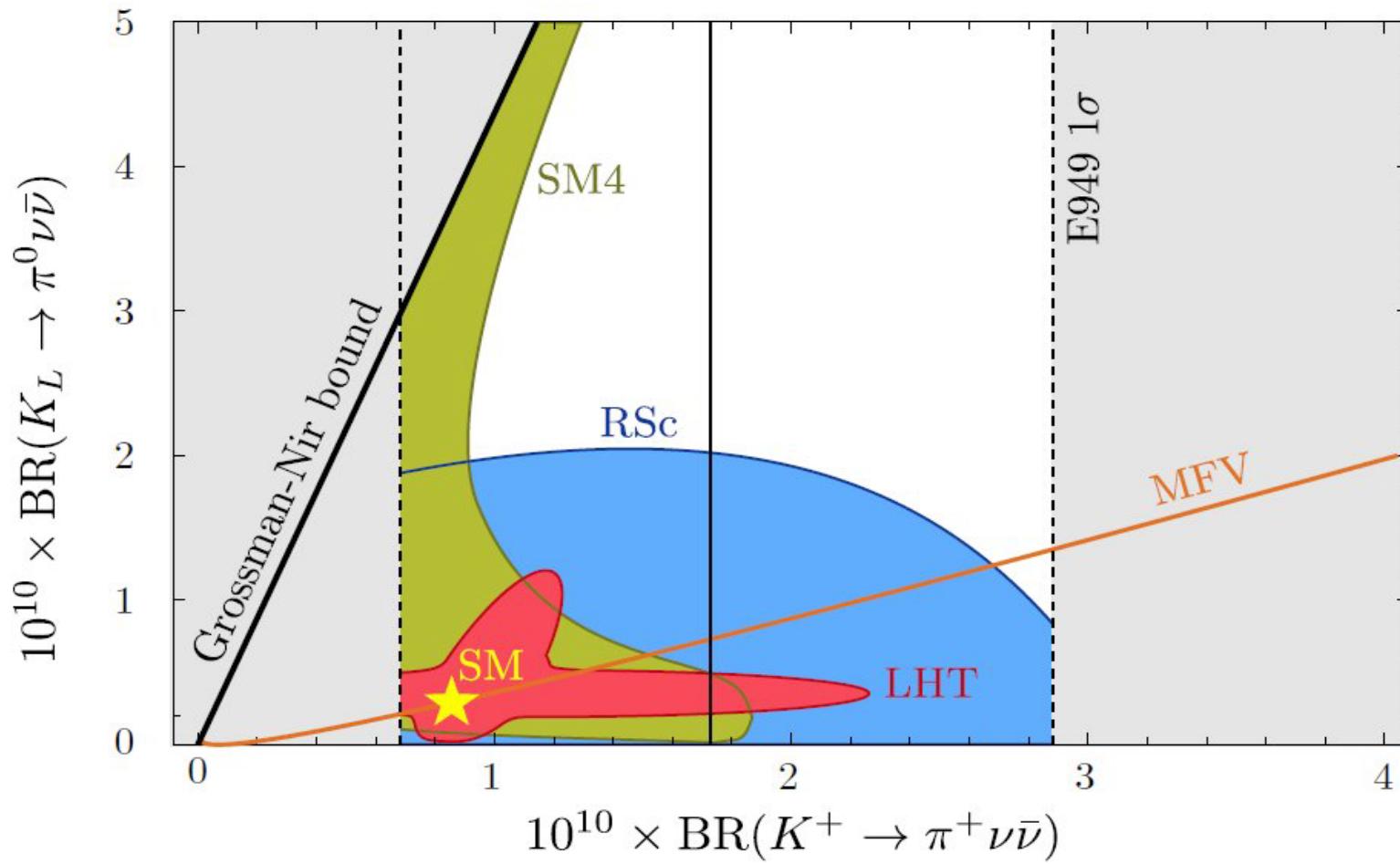
K^+ decays



Present = $(1.73 + 1.15 - 1.05) \times 10^{-10}$

BNL E949

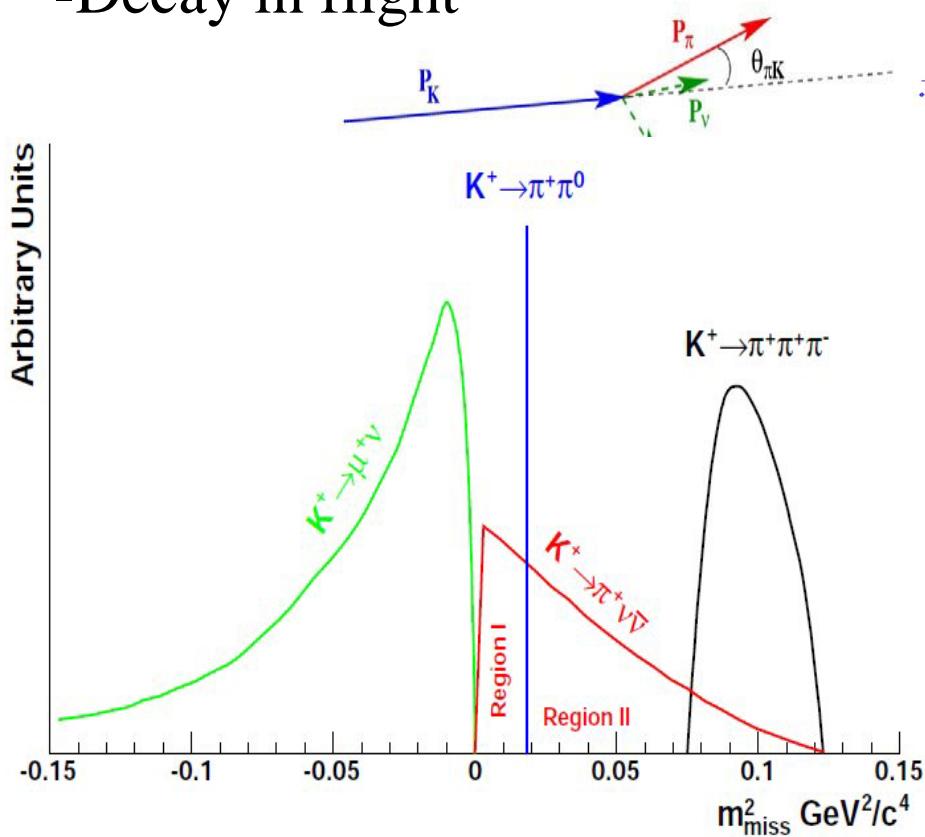
$K\pi\nu\bar{\nu}$ beyond the Standard Model



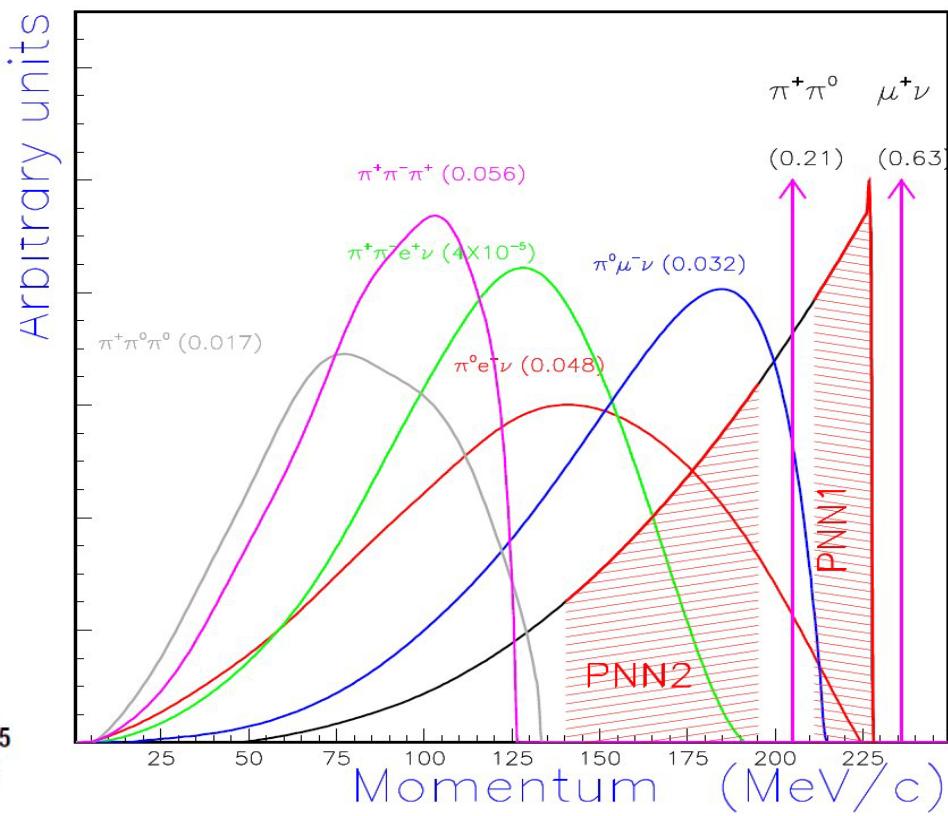
$K^+ - \pi^+ \nu\bar{\nu}$ experiments

Signature: a single π^+

NA62
-Decay in flight

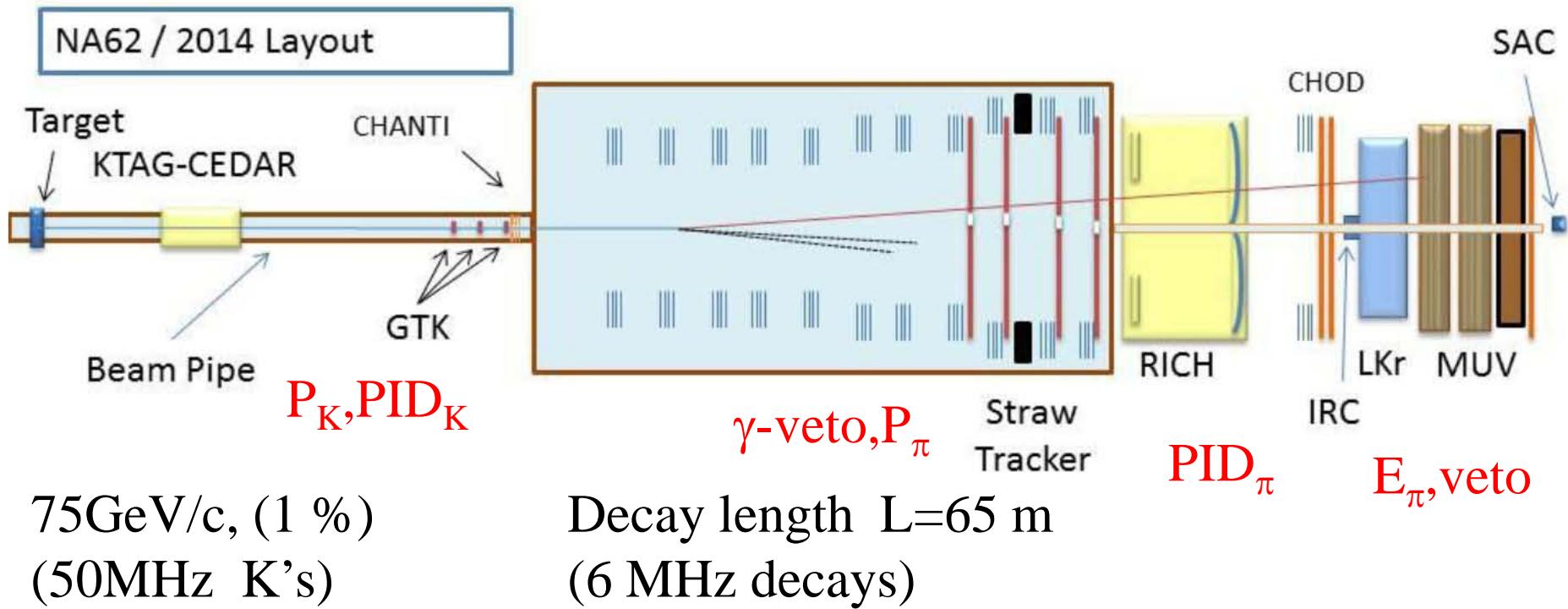


ORKA
-Decay at rest



Kinematics, particle ID, Photon veto

NA62@CERN

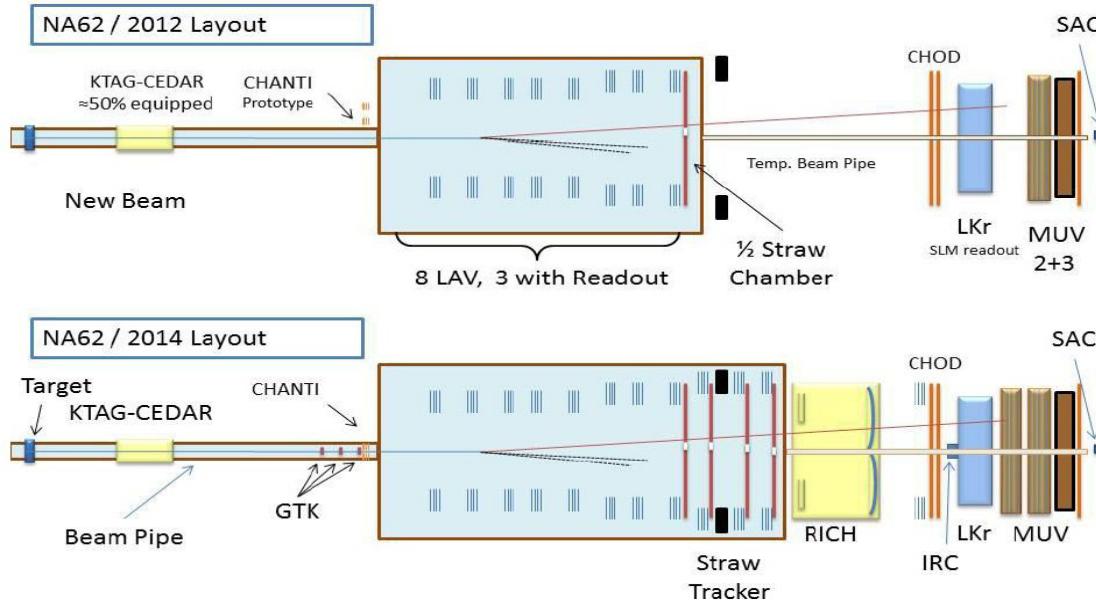


Kin. Rejection: 2×10^{-4} ($K_{\pi 2}$), 7×10^{-5} ($K_{\mu 2}$)
 PID: 10^{-7} (μ/π)
 PV: 10^{-8} for $\pi^0 \rightarrow \gamma\gamma$

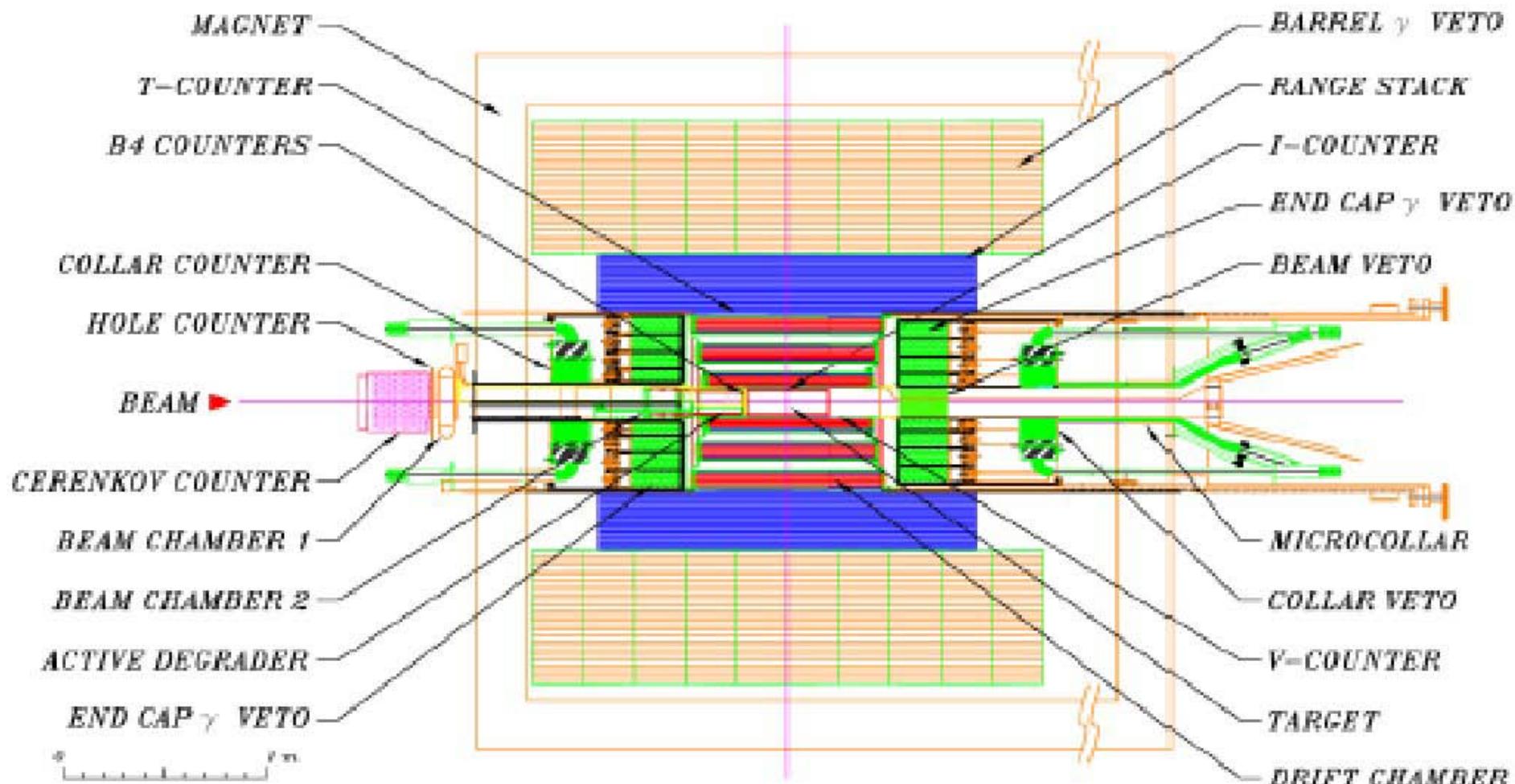
NA62

- Decay in flight
- 100 events
- Data taking, 2014-

| Decay | evt/year |
|---|------------|
| $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ [SM] (flux 4.5×10^{12}) | 45 |
| $K^+ \rightarrow \pi^+ \pi^0$ | 5 |
| $K^+ \rightarrow \mu^+ \nu$ | 1 |
| $K^+ \rightarrow \pi^+ \pi^+ \pi^-$ | < 1 |
| $K^+ \rightarrow \pi^+ \pi^- e^+ \nu + \text{other 3 tracks decays}$ | < 1 |
| $K^+ \rightarrow \pi^+ \pi^0 \gamma$ (IB) | 1.5 |
| $K^+ \rightarrow \mu^+ \nu \gamma$ (IB) | 0.5 |
| $K^+ \rightarrow \pi^0 e^+(\mu^+) \nu, \text{others}$ | negligible |
| Total background | < 10 |



ORKA@FNAL



Improved Kin.

PID: P/E/R, π - μ -e chain

Veto: Hermetic detector

ORKA

- Decay at rest
- Based on E949 experience
- Improved res. and granul.
- 500 events
- 2018?

| Component | Acceptance factor |
|-------------------------------------|-------------------------|
| $\pi \rightarrow \mu \rightarrow e$ | 2.24 ± 0.07 |
| Deadtimeless DAQ | 1.35 |
| Larger solid angle | 1.38 |
| 1.25-T B field | 1.12 ± 0.05 |
| Range stack segmentation | 1.12 ± 0.06 |
| Photon veto | $1.65^{+0.39}_{-0.18}$ |
| Improved target | 1.06 ± 0.06 |
| Macro-efficiency | 1.11 ± 0.07 |
| Delayed coincidence | 1.11 ± 0.05 |
| Product (R_{acc}) | $11.28^{+3.25}_{-2.22}$ |

Improvement factors over E949 acceptance

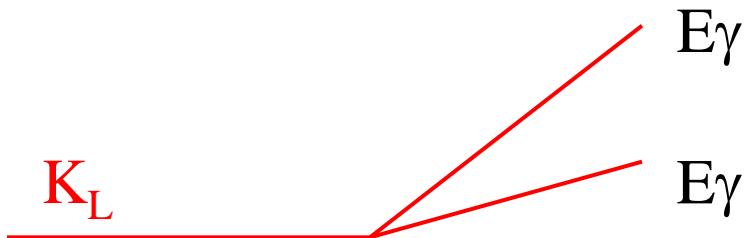
| Background | Standard | Extended |
|------------------------|-------------------|-------------------|
| $K_{\pi 2}$ | 0.019 ± 0.004 | 0.216 ± 0.023 |
| $K_{\mu 2}$ range tail | 0.010 ± 0.001 | 0.044 ± 0.005 |
| Muon band | 0.005 ± 0.002 | 0.024 ± 0.010 |
| Single beam | 0.004 ± 0.002 | 0.006 ± 0.002 |
| Double beam | 0.003 ± 0.002 | 0.003 ± 0.002 |
| CEX | 0.004 ± 0.001 | 0.005 ± 0.001 |
| Total | 0.05 ± 0.01 | 0.30 ± 0.03 |

Expected backgrounds

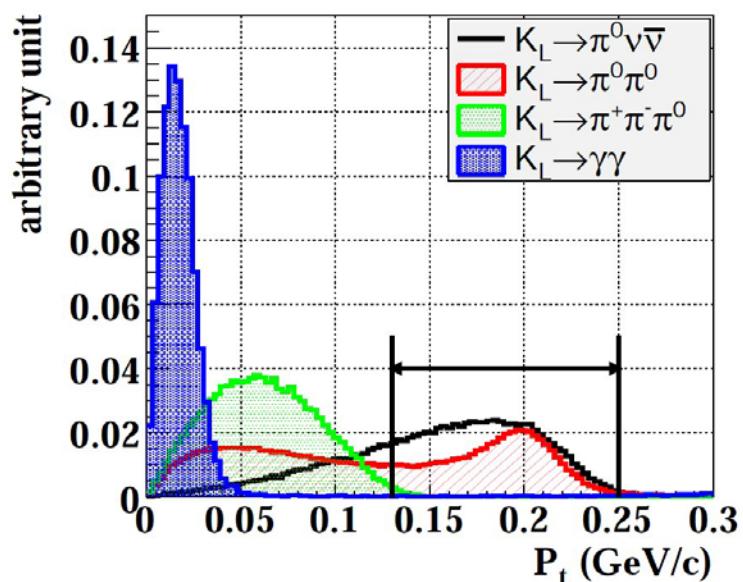
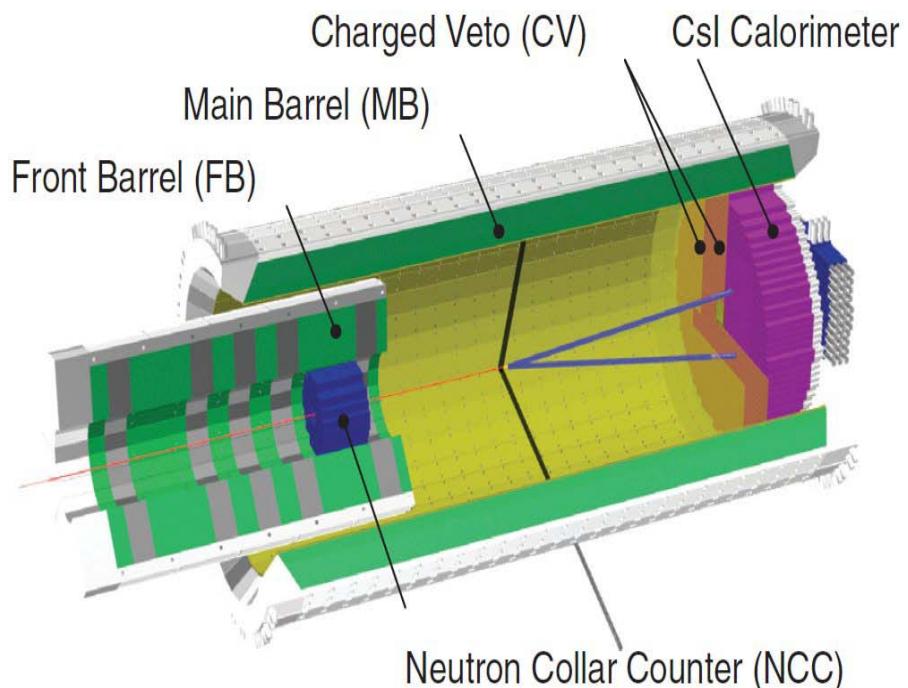
$K_L - \pi^0 \nu \bar{\nu}$

Present limit = 2.6×10^{-8} @ 90 % c.l.

PRD 81 072004(2009)



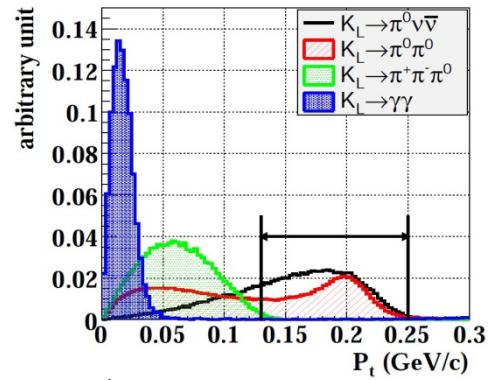
- E391a → KOTO@JPARC
- Pencil beam
- Assumes π^0 mass for 2 γ 's
→ vertex, P_T
- Large P_T
- No other activity
- Use KTEV CsI's (better res.)



$K_L - \pi^0 \bar{\nu} \nu$

From original proposal

| Background source | #Background events |
|-------------------------------------|--------------------|
| Other K_L decays | |
| $K_L \rightarrow \pi^0 \pi^0$ | 3.65 |
| $K_L \rightarrow \pi^+ \pi^- \pi^0$ | 0.93 |
| $K_L \rightarrow \pi^- e^+ \nu$ | 0.01 |
| $K_L \rightarrow \gamma\gamma$ | negligible |
| $K_L \rightarrow \pi^0 \pi^0 \pi^0$ | negligible |
| Neutron Interaction | |
| With Residual gas | 0.07 |
| At the CC02 | 0.26 |
| At the C.V. | negligible |
| Accidental Coincidence | 0.20 |



Expect 3.5 SM events with s/n=1.4.

Searches NP for 3 orders of magnitude.

Next generation experiment?

- KOTO Stage-2; 100 SM events.

- Project-X?

Conclusion

There are many world-wide efforts for precision measurements of rare pion and kaon decays, which are significantly suppressed in the standard model and therefore sensitive to new physics.

$M_{\text{ev}}/M_{\mu\nu}$ branching ratio measurements are extremely sensitive to a presence of PS interactions. The ratio also provides the best test of $e-\mu$ universality. A factor of 3-5 improvement is expected in a few years, but there will be a room for improvement by another factor of 5.

There are several challenging $K\pi v\bar{v}$ experiments, either running or planned to run soon. Results are expected in the next few years.