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Thomas Prokscha :: Low-Energy Muons Group :: Paul Scherrer Institut

# **Muon Properties and Muon Production**

Lecture at the PSI Masterschool, Sep 8<sup>th</sup> 2017, PSI



# **Outline of the Friday morning session**

- 1. Muon Properties and Muon Production (TP)
  - Discovery of the muon
  - Pion decay, muon decay, parity violation, focus on positive muons  $\mu^{\scriptscriptstyle +}$
  - Muon properties, interaction with matter, basics of application of  $\mu^{\scriptscriptstyle +}$  in condensed matter physics
  - Generation of > MeV muons and eV- keV muons («low-energy muons»)
  - Overview of PSI proton accelerator facility HIPA («High Intensity Proton Accelerator»)
  - Application of cosmic muons: radiography of large objects
- 2. Introduction to Muon Spin Rotation and Relaxation (μSR): Instrumentation and Technique (Hubertus Luetkens)
- 3. µSR on Magnetic Materials (Alex Amato)
- 4. µSR and Superconductors (Alex Amato)



The discovery of the muon

- **T. Wulf, ionization measurements with** electrometer on top of Eiffel tower
- **1911 V. Hess, balloon measurements**

Ionization increases with altitude

**R. Millikan, experiments with unmanned balloons (1925)** Discovery of cosmic radiation (1936 Nobel Price V. Hess)



- **1933 P. Kunze**, first muon track (unrecognized)
- 1936 C. D. Anderson, S. H. Neddermeyer main component of cosmic radiation: particle with 1/9 proton mass (mesotron)....

...interpreted as "Yukawa particle" (strong interaction)

- **1942 B.Rossi, N. Nereson**:  $\tau_{\mu} = 2.3(2) \ \mu s$
- 1947 M. Conversi et al. : mesotron is weakly interacting with nuclei

**C.F.** Powell et al. : discovery of the pion  $(\pi^+, \pi^-)$  (1950 Nobel Price) pion decays into muon





# The discovery of the muon



(figure 5) shows closely

together the thin trace of an electron of 37 MeV, and a much more strongly ionizing positive particle whith a much larger bending radius. The nature of this particle is unknown; for a proton it does not ionize enough and for a positive electron the ionization is too strong. The present double trace is probably a segment from a "shower" of particles as they have been observed by Blackett and Occhialini, i.e. the result of a nuclear explosion".

Kunze, P., Z. Phys. 83, (1933) 1



### **About the muon:**

### "Who ordered that?"

(...eventually I.I. Rabi won the *Nobel Prize in Physics* in 1944 for his invention of the atomic and molecular beam magnetic resonance method of observing atomic spectra).





sidor Isaac Rabi (1898-1988)



Muon as a result of pion decay

- **1956 T.D. Lee and C.N. Yang**: predicted that any process governed by the weak interaction should lead to a violation of parity.
- **1957 R. Garwin, L. Ledermann, M. Weinrich and J. Friedmann, V. Telegdi**: maximum violation of parity (spatial inversion) in weak decay of pion and muon



Two-body decay	►	muon has always the energy 4.1 MeV in the reference frame of the pion (assuming $m_v = 0$ )
Spin pion = 0		Muon has a spin 1/2 and is 100% polarized (as only left-handed neutrinos are produced)



# **Muon decay properties**





Immediate recognition of the muon's potential...



A journal of experimental and theoretical physics established by E. L. Nichols in 1893

Second Series, Vol. 105, No. 4

FEBRUARY 15, 1957

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon\*

> RICHARD L. GARWIN,<sup>†</sup> LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York (Received January 15, 1957)

It seems possible that polarized positive [...] muons will become a powerful tool for exploring magnetic fields in [...] interatomic regions.



Pion decay Muon Decay e Neutrinos have negative helicity, antineutrinos positive. An ultrarelativistic positron behaves like an antineutrino. Thus the positron tends to be emitted along the muon spin when  $V_e$  and  $\nabla_{\mu}$  go off together (highest energy  $e^+$ ). Figure from http://malct32.blogspot.ch/2010/07/proton-smaller-than-thought.html A relativistic  $e^+$  (E >>  $m_e$ ,  $m_e \sim 0.5$  MeV) "wants" to have positive helicity. The decay with opposite  $\mu^+$  and  $e^+$  spin direction is suppressed, causing the  $e^+$  emission in the direction of  $\mu^+$  spin

The decay on the right side has never been observed;  $v_{\mu}$  are "left-handed", i.e. they have **negative helicity**.



Generation of 100% polarized μ<sup>+</sup> Anisotropic muon decay, preferential emission of decay e<sup>+</sup> in  $\mu^+$  spin direction



 $W(E, \theta) = 1 + a(E, \theta) \cos(\theta)$ 

Decay asymmetry a = 1/3 when integrating over all e<sup>+</sup> energies

Detecting spatial emission of e<sup>+</sup> as a function of time:

time evolution of muon spin/muon polarization P(t)

i) generation of polarized muons (parity violation)

ii) anisotropic muon decay (parity violation)

iii) precession of the muon magnetic moment *m* in a magnetic field *B*:

 $dm/dt = m \times B$  $m = \gamma_{\mu} \cdot \overline{n} \cdot S_{\mu}$ 



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 $dm/dt = m \times B$  $m = \gamma_{\mu} \cdot \bar{n} \cdot S_{\mu}$ 

 $W(E, \theta)$  is derived from the differential decay rate  $d\Gamma(x, \theta)$ ,  $x = 2E/m_{\mu}$ :

 $d\Gamma(x,\theta) \simeq \frac{1}{\tau_{\mu}} \{ (3-2x) \mp P(2x-1)\cos\theta \} x^2 \, dx \, d(\cos\theta)$ 

Integrating over all energies x:

$$\mathrm{d}\overline{\Gamma}(\theta) \simeq \frac{1}{2\tau_{\mu}} (1 \mp P_{\overline{3}}^{1} \cos \theta) \mathrm{d}(\cos \theta).$$

F. Scheck, Physics Reports 44, 187 (1978)



### **Muon properties**

#### elementary particle/antiparticle:



mass:	207x electron	mass (105.6 MeV, 1/9x proton mass)		
charge:	+ e, oder -e			
spin:	1/2			
magnetic moment : $3.18 \mu_{p}$				
$\gamma_{\mu}$ = gyromagnetic	ratio:	2π·135.5 MHz/T		
(proton:		2π·42.8MHz/T,		
electron:		2π·28.1GHz/T)		

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unstable particle:
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mean lifetime: \tau_{\mu} = 2.2 µs, N(t)=N(0)exp(-t/\tau_{\mu})
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#### muon beams can be generated with 100% polarization

parity violation in muon decay makes it useful as a microscopic spin probe to measure local magnetic fields in a sample

 $\rightarrow$  muon spin rotation technique (µSR)





### **Muon properties**

#### elementary particle/antiparticle:



mass:207x electron mass (105.6 MeV, 1/9x proton mass)charge:+e, oder -espin: $\frac{1}{2}$  $m_{\mu} >> m_{e}$ : much smaller energy loss due to Bremsstrahlung (~m-4);no strong interaction:

-----> large range of "relativistic" muons in matter, suitable for radiographic imaging of "massive" objects



Particle data group, Chin. Phys. C 38, 090001 (2014)



### Range of muons in matter



- 48C I-



### **Generation of muons**



#### **Polarized muon production:**

high energy protons generate pions ( $m_{\pi} \simeq 140$  MeV) in collisions with nuclei:



For Beam-on-Fixed-Target it needs E<sub>p</sub> > 290 MeV

"Meson factories" have  $E_p = 500 - 3000$  MeV

 $\pi^+ \rightarrow \mu^+ + \nu_{\mu}$  ( $\pi^{+/-}$  lifetime 26 ns, 100%  $\mu^+$  polarization in  $\pi^+$  rest frame)



### How to generate muons

Muons can be produced electromagnetically in e+/e- collisions:

 $e^+ + e^- \rightarrow \mu^+ + \mu^-$ .

(Standard reaction of electron-positron physics)

However, the cross section is very small compared to pion production cross sections which is up to 20 mb =  $2 \times 10^{-26}$  cm<sup>2</sup>:

 $\sigma_{\mu\mu}$  ~  $4\pi\alpha^2/3s$  ~ 2 x 10<sup>-32</sup> cm<sup>2</sup> for 1 GeV colliding beam energy (=  $\sqrt{s}$ ),

and this process does not generate polarized muons.

F. Scheck, Muon physics, Physics Reports 44, 187 (1978).



### Natural muons:

*Cosmic* muons (although the muons do NOT come from the cosmos...)







### **Accelerator muons**

Accelerator muons (keV-MeV): ~100% polarization, depth resolution few nm to mm, lateral resolution mm to cm measuring magnetic field distributions/fluctuations

intensity: 1000 Muons/second/cm<sup>2</sup> (keV) up to 10<sup>7</sup> Muons/second/cm<sup>2</sup> (MeV)

requires a proton accelerator (E  $_{\rm p}$  > 500 MeV, I  $_{\rm p}$  > 100  $\mu A$ )





### **Accelerator muons**

How to accelerate protons to energies > 300 MeV (pion production threshold) and proton beam currents  $I_p > 100 \mu A$  (to generate muon/pion beam with high intensities >  $10^7/s$ ) ?

**Isochronous Cyclotron:** compact, operated at tens of MHz RF frequency (**quasi-continuous muon beams**), constant RF frequency, constant (in time) magnetic field increasing with radius. Beam energy < 1 GeV (limited by magnetic field of magnets with saturation field of 2 T).









# Continuous versus pulsed muon beams

continuous muon beams

"Continuous Wave (CW)"

- No distinct time structure
- Each muon individually counted. "Start" signal (muon detector)
- Very small time resolution (< 100 ps possible)</p>

Detection of large magnetic fields
 Detection of fast relaxing signals

Reduction of muon rate to avoid "pileup"

Non-negligible background

pulsed (50Hz) muon beams

- Distinct time structure (pulse structure of proton beam)
- All muons coming at (almost) the same time.
   No need of muon detector.
   (Pulse width 10ns 100ns)
- Very low background (possibility to measure slow depolarization rates)
- Limited time resolution
  - Detection of large magnetic fields and/or fast relaxing signals <u>impossible</u>
- High rates requires very high detector segmentation



### Continuous versus pulsed muon beams

continuous muon beams

No need of high detector segmentation



Example: "GPS" instrument at PSI 1 backward + 1 forward detectors pulsed (50Hz) muon beams

#### High detector segmentation mandatory



Example: "MuSR" instrument at ISIS 32 backward + 32 forward detectors PAUL SCHERRER INSTITUT

### Continuous versus pulsed muon beams





# The PSI isochronous cyclotron

2.4 mA: ~1.5 x 10<sup>16</sup> protons/sec @ 590 MeV:
1.4 MW on 5x5 mm<sup>2</sup> = 50 kW/mm<sup>2</sup>, stainless steel melts in ~0.1 ms; electric power demand of 3000 households

#### A MW proton beam allows to generate 100% polarized 4-MeV $\mu^+$ beams with rates >10<sup>8</sup>/sec



Larmor frequency of protons:  $q/(2\pi m) = 15.25 \text{ MHz/T}$   $v_0 = q/(2\pi\gamma m) \cdot B$ ,  $\gamma = E_{tot}/mc^2$  $v_{rf} = n \cdot v_0$ , frequency of accelerating radio-frequency

Isochronous cyclotron:  $B_0(R) \sim \gamma(R)$ , constant  $v_{rf}$ ! PSI cyclotron:  $B_0 = 0.554$  T,  $v_0 = 8.45$  MHz, n = 6,  $\rightarrow v_{rf} = 50.7$  MHz





### PSI muon beam time structure



Pion decay time of 26 ns is "smearing" the proton beam structure in the muon beam. This results in a "continuous" muon beam.

A  $\mu^+$  rate *R* of 10<sup>5</sup>/s means: average time between two  $\mu^+$  is 1/*R* = 10  $\mu$ s. Probability *p* to have **the next**  $\mu^+$  at time *t*:

p = 1 - exp(-Rt) ("pile-up", follows from Poisson
statistics)

Single  $\mu^+$  can be detected with very good time resolution (< 0.1 ns), compared to a bunch width of 50-100 ns at pulsed beams.  $\rightarrow$  measurement of GHz frequencies and fast relaxation rates (>100  $\mu$ s<sup>-1</sup>) possible. But "accidental" background in  $\mu$ -decay histograms (can be reduced by muons-on-request).

> 20100 time (ns)



**Generation of muon beams** 

### "Arizona" or "Surface Muon Beam" (only μ<sup>+</sup>), ~100% polarization





**Generation of muon beams** 

(Traditional) "Decay Muon Beam" (µ<sup>+</sup> or µ<sup>-</sup>), ~80% polarization



to select beam momentum p: magnetic dipole magnets (bending magnets)

to focus beam: magnetic quadrupole dublets or triplets, solenoids (for «surface muons»)

to vary beam intensity, momentum width *Ap/p*: slits

to remove positrons from beam, to rotate muon spin (for «surface muons» only): ExB velocity filter (separator, spin-rotator)



# How to generate a low-energy $\mu^{\!\!+}$ beam with tunable energies between 1 and 30 keV?

Muons are born energetically in pion decay (~4 MeV)

Need a special moderation technique to slow down energetic muons from the MeV to keV energies



Generation of thermal  $\mu^+$  at a pulsed accelerator

VOLUME 74, NUMBER 24 PHYSICAL REVIEW LETTERS

12 JUNE 1995

#### Ultraslow Positive-Muon Generation by Laser Ionization of Thermal Muonium from Hot Tungsten at Primary Proton Beam

K. Nagamine,<sup>1,2</sup> Y. Miyake,<sup>1</sup> K. Shimomura,<sup>1</sup> P. Birrer,<sup>1</sup> J. P. Marangos,<sup>1,3</sup> M. Iwasaki,<sup>1</sup> P. Strasser,<sup>2,4</sup> and T. Kuga<sup>5</sup>



P. Bakule,Y.Matsuda,Y.Miyake, K. Nagamine, M. Iwasaki, Y. Ikedo, K. Shimomura, P. Strasser, S. Makimura, Nucl. Instr Meth. B **266**, 335 (2008).

**Intensity:** ~15 LE- $\mu^+$ /sec (>10<sup>3</sup>/s at J-PARC expected) **Polarization**: ~ 50% (1/2 of polarization lost in muonium)



# Generation of polarized epithermal (~eV) $\mu^{\scriptscriptstyle +}$





# Generation of polarized epithermal (~eV) $\mu^{\scriptscriptstyle +}$



E. Morenzoni et al., J. Appl. Phys. **81**, 3340 (1997).

D. Harshmann et al., Phys. Rev. B36, 8850 (1987).



### Characteristics of epithermal (~eV) $\mu^+$



E. Morenzoni, T. Prokscha, A. Suter, H. Luetkens, R. Khasanov, J.Phys.: Cond. Matt. **16**, S4583 (2004).



E. Morenzoni, F. Kottmann, D. Maden, B. Matthias, M. Meyberg, T. Prokscha, T. Wutzke, U. Zimmermann, PRL **72**, 2793 (1994).

 $\rightarrow$  suppression of electronic energy loss for E > E<sub>g</sub>, large band gap E<sub>g</sub> (10-20 eV) "soft, perfect" insulators

→ large escape depth L (10-100 nm), no loss of polarization during moderation (~10 ps)

 $\rightarrow$  moderation efficiency is low (requires highest intensities  $\mu^+$  beams, > 10<sup>8</sup>  $\mu^+$ /s, i.e. MW proton beam):

$$\varepsilon_{u+} = N_{epith}/N_{4MeV} \approx \Delta \Omega (1-F_{Mu}) L/\Delta R \approx 0.25 L/\Delta R \approx 10^{-4} - 10^{-5}$$

 $\Delta\Omega$ : probability to escape into vacuum (~50% for isotropic angular distribution)  $F_{Mu}$ : muonium formation probability



# Low-energy (keV) µ<sup>+</sup> facility at PSI

Rates are for 6-cm target E and 1.8 mA proton current (2017)





# The PSI Experimental Hall



# The proton accelerators, muon and neutron beams





# **Application of cosmic muons:**

# **Radiography of large objects**



# Radiography with cosmic muons

Cosmic muons (GeV energy) imaging: objects of dimension meters very low intensity: 1 Muon / minute / cm<sup>2</sup>

### Cosmic Rays

- Very high energy "primary" cosmic rays - typically protons - interact in upper atmosphere
- Shower of unstable subnuclear particles created: typically pions, kaons
- Muons and neutrinos are decay products of pions and kaons



### Imaging Maya Pyramids with Cosmic Ray Muons



An Application of the Tools of High Energy Physics

### What is the internal structure?

Measure Spatial Distribution of Material Inside by Muon Tomography



First attempts with pyramids in the 1960's by Luis Alavarez in the Pyramid of Chephren, Giza.



#### Cosmic-ray muon imaging of magma in a volcano (Satsuma-lojima, Japan):

H.K.M. Tanaka et al., Geophysical Research Letters 36, L01304, 2009.



Figure 1. (a) Map of Satsuma-Iojima volcano showing the location of the cosmic-ray muon detector (Mu). (b) Portable assembly type cosmic-ray muon telescope system. The detector matrix counts  $12 \times 12$  square pixels of 8 cm.





Muon image of magma chamber and model of magma convection

very low intensity: 1 Muon / minute / cm<sup>2</sup>



### Homeland security with cosmic muons

#### Aim: detection of hidden special nuclear material (high-Z material)

C.L. Morris et al, Science and Global Security 16, 37-53 (2008)

#### Example: muon image of a car engine, and a car engine with a 10x10x10 cm<sup>3</sup> lead cube

42 Morris et al.



Figure 3: Mean scattering angle for a slice through the scene 50 cm above the base plate. The left panel shows the engine, the middle panel the engine plus the 10  $\times$  10  $\times$  10 cm<sup>3</sup> lead sample, and the right panel the difference.

Suggestion for a counting station for muon radiography and simultaneous neutron and  $\gamma$  counting to detect fissile nuclear material

Decision Sciences International Corp. is offering such muon tomography systems

#### Tomographic Imaging with Cosmic Ray Muons 51



Figure 13: A schematic view of how a counting station might look. Vehicles would be stopped within the area covered by the counting station for a counting period  ${\sim}20~s.$ 



PRL 109. 152501 (2012)

### Imaging the core of Fukushima reactors

PHYSICAL REVIEW LETTERS

week ending 12 OCTOBER 2012

r.

#### Cosmic Ray Radiography of the Damaged Cores of the Fukushima Reactors

Konstantin Borozdin,<sup>1</sup> Steven Greene,<sup>1</sup> Zarija Lukić,<sup>2</sup> Edward Milner,<sup>1</sup> Haruo Miyadera,<sup>1</sup> Christopher Morris,<sup>1,\*</sup> and John Perry<sup>1</sup>

<sup>1</sup>Los Alamos National Laboratory, Los Alamos, New Mexico 87544, USA <sup>2</sup>Computational Cosmology Center, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA (Received 9 August 2012; published 11 October 2012)

#### 7x7 m<sup>2</sup> drift tube detectors





FIG. 1 (color). Cutaway view of a boiling water reactor and a schematic of the detector placement for the Monte Carlo calculation. In the case of attenuation radiography, only trajectory information from the lower detector was used. The location of the 1 m diameter void in the core and its placement in the bottom of the pressure vessel are indicated by arrows.

FIG. 3 (color online). Reactor reconstructions at different exposure times. In scattering radiography, the reactor core can be detected after about 10 hours of exposure. After four days, a 1 m diameter (1%) void can be detected when compared to an intact core. After 6 weeks, the void is clear and the missing material can be observed. With the attenuation method, the core can be observed when compared to an empty scene in four days. The void is undetectable even after 6 weeks of exposure.

Transmission tomography scan of unit 1 indicates complete reactor meltdown (March 2015) https://www.extremetech.com

#### Installed at Fukushima Daiichi reactor unit 2 end of 2015 http://www.lanl.gov/org/padste/adeps/physics/\_assets/docs/muon-tomography.pdf

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scattering. The many small interactions add up to yield an angular deviation that Imaging the core of Fukus roughly follows a gaussian distribution,

PHYSICAL REVIEW LETTERS PRL 109, 152501 (2012)

Cosmic Ray Radiography of the Damaged Cores of the Fukushima React

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with the width,  $\theta_0$ , related to the scattering material through its radiation length,  $L_0$ , as follows:

$$\theta_0 = \frac{13.6}{\beta c p} \sqrt{\frac{L}{L_0}} [1 + 0.038 \ln(L/L_0)]$$

where *p* is the particle's momentum in MeV c<sup>-1</sup> and  $\beta c$  is its velocity<sup>2</sup>. The radiation length decreases rapidly as the atomic number of a material increases, and  $\theta_0$ increases accordingly: in a layer 10 cm thick, a 3-GeV muon will scatter with an angle of 2.3 milliradians in water, 11 milliradians in iron and 20 milliradians in lead. By tracking the scattering angles of individual particles, the scattering material can be mapped.

K. Borozdin et al, Nature 422, 277 (2003)

#### Installed at Fukushima Daiichi reactor unit 2 end of 2015 http://www.lanl.gov/org/padste/adeps/physics/ assets/docs/muon-tomography.pdf



# Wir schaffen Wissen – heute für morgen

#### Next:

Introduction to Muon Spin Rotation and Relaxation (µSR):

> Instrumentation and Technique

