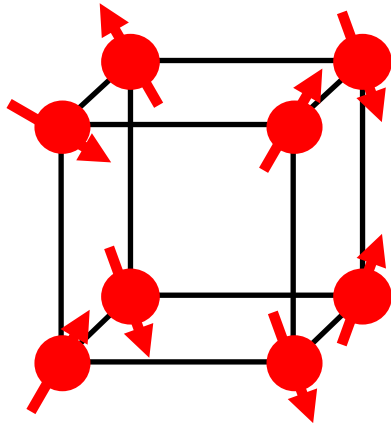
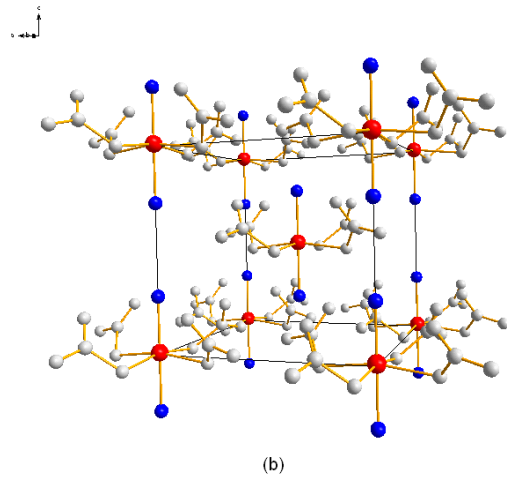


PSI Master School 2017

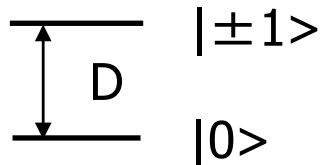
Introducing photons, neutrons and muons for materials characterization

**Lecture 14: Neutron Spectroscopy
and Magnetic Excitations**

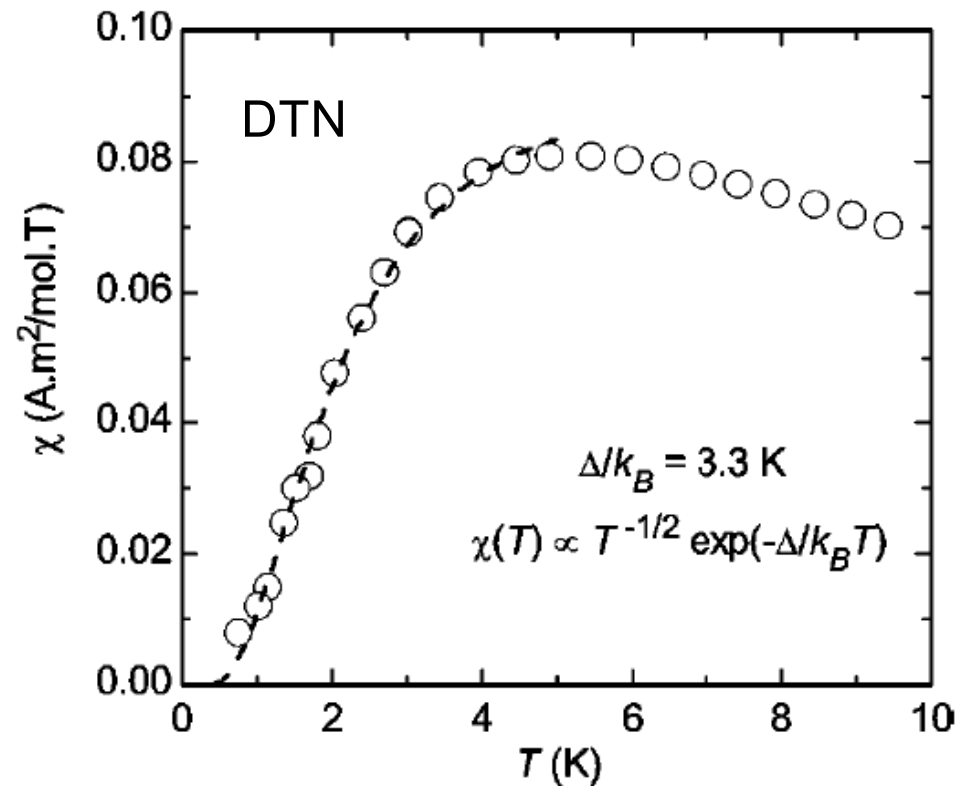
Simple example of a quantum magnet



Strong single-ion anisotropy

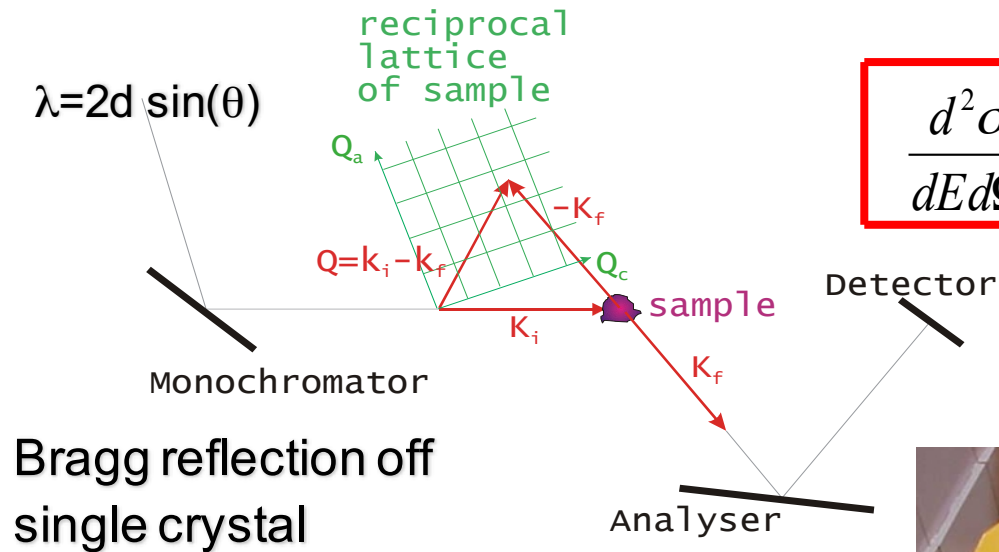


Magnetic susceptibility



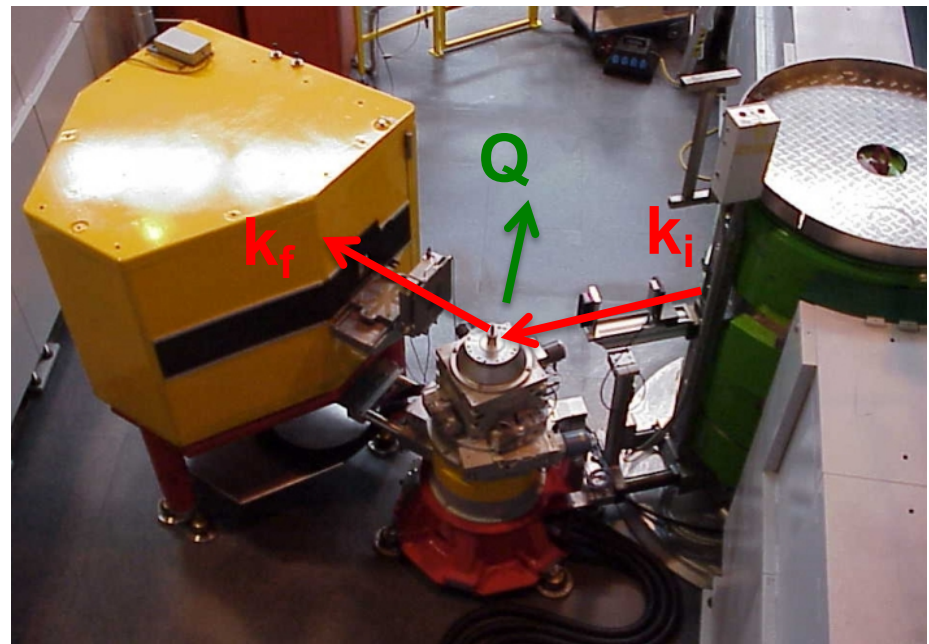
A. Paduan-Filho et al, J. Appl. Phys. **95**, 7537 (2004)

Magnetic neutron scattering



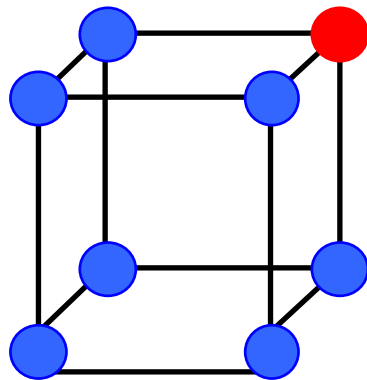
$$\frac{d^2\sigma}{dE d\Omega} \propto \sum_{\alpha\beta} (\delta_{\alpha\beta} - \hat{Q}_\alpha \hat{Q}_\beta) S^{\alpha\beta}(Q, \omega)$$

Sensitive to spin correlation functions



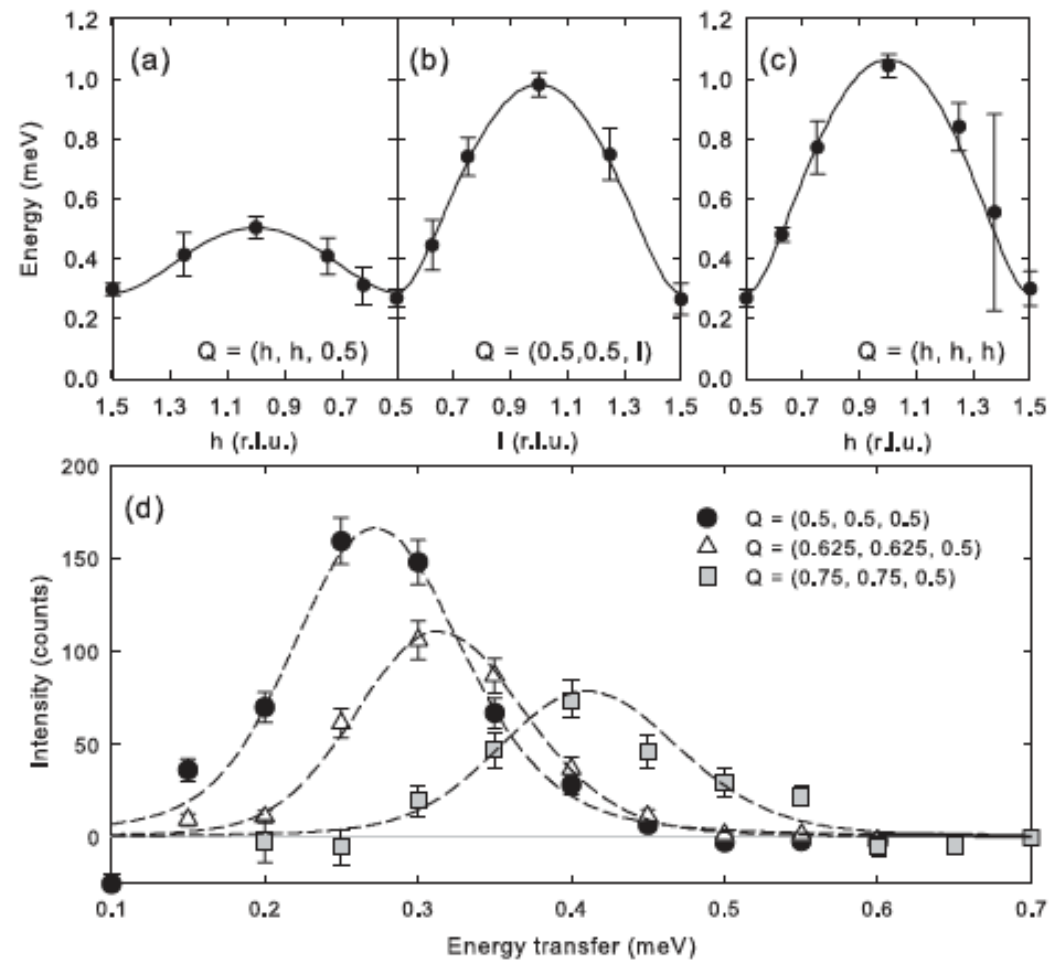
RITA spectrometer at PSI

Excitations of a quantum magnet



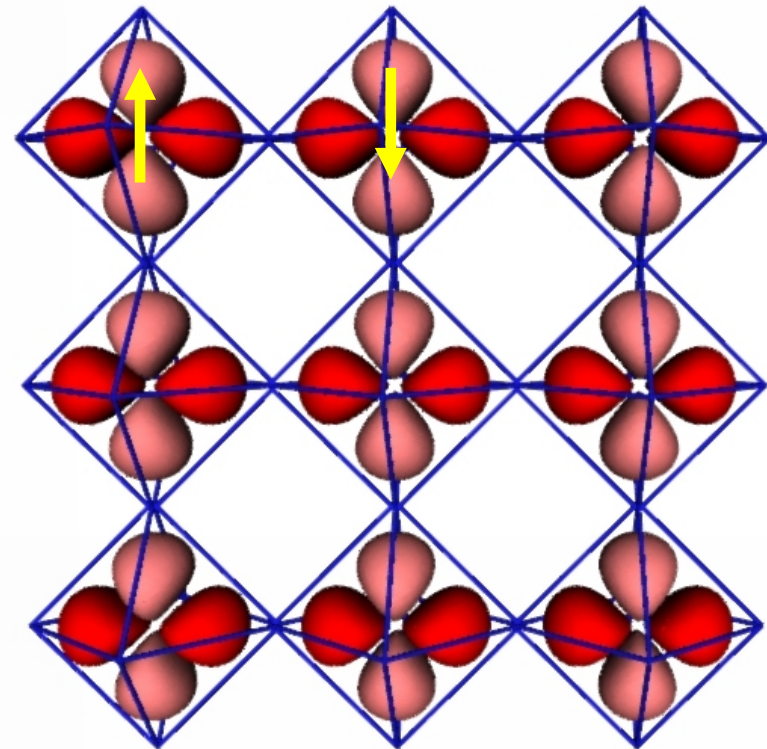
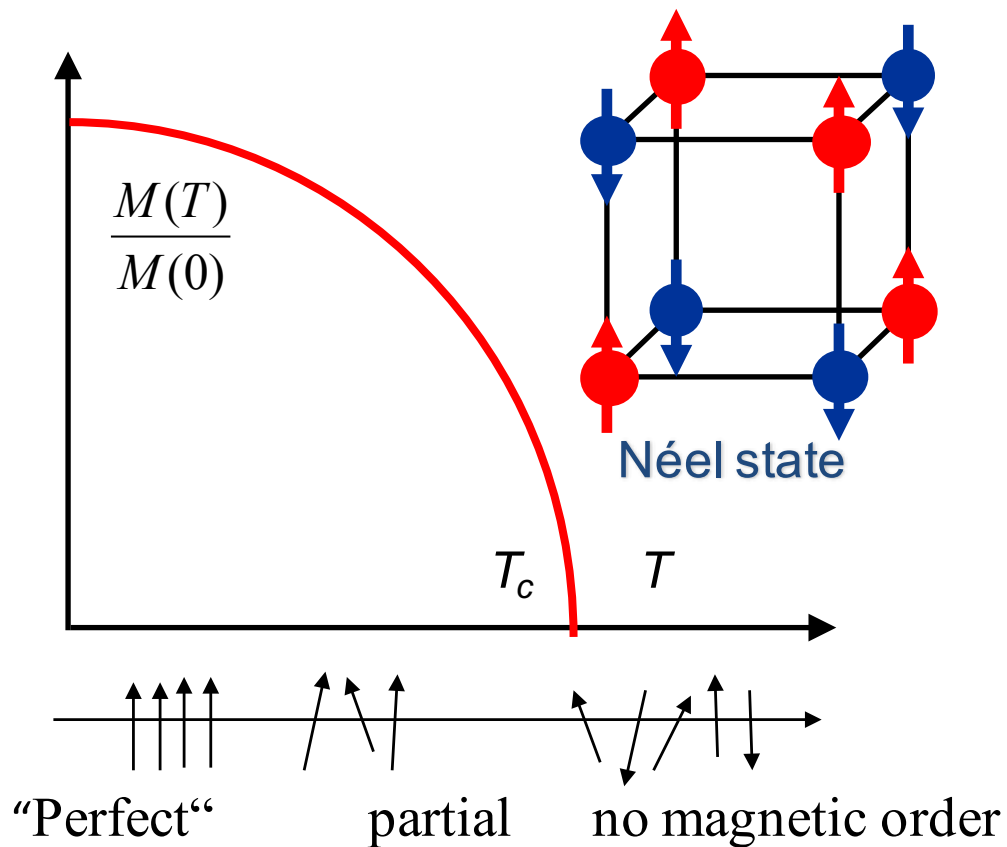
delocalization of $|\pm 1\rangle$ states
due to spin interactions

$$\omega_{\mathbf{k}\pm} = \sqrt{D^2 + 2D \sum_{\nu} J_{\nu} \cos k_{\nu}}$$

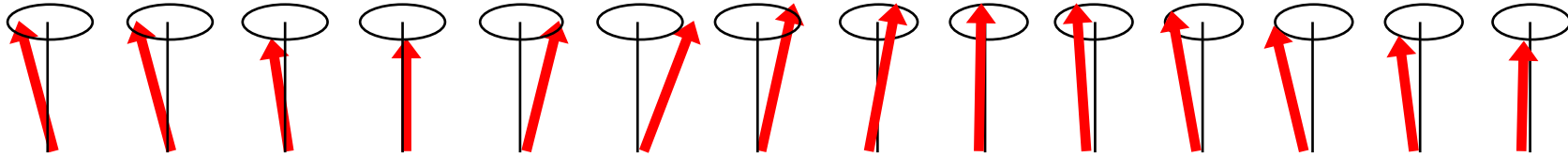


From the quantum nature of magnetism to “classical long-range order”

- ◆ $T \gg J$: spin fluctuates between up and down, but neighbours always want to point in opposite direction
- ◆ cooperative phase transition for $T < J$

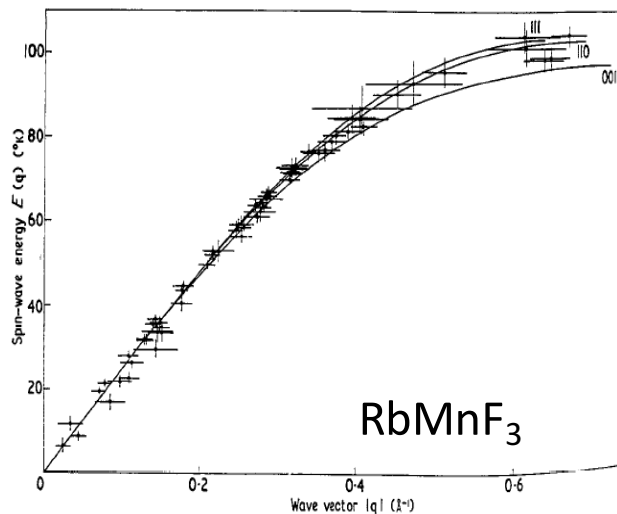


The nature of spin waves



Small deviations of the magnetic moments away from ordered direction

$$\hat{H} = \sum_{l \neq l'} J_{ll'} \hat{S}_l \hat{S}_{l'}$$



Windsor and Stevenson, Proc Phys Soc London (1966)

$$\hat{S}_l^+ = \sqrt{2S} \hat{a}_l \quad \hat{S}_l^- = \sqrt{2S} \hat{a}_l^+ \quad \hat{S}_l^z = S - \hat{a}_l^+ \hat{a}_l$$

$$\hat{a}_l = \frac{1}{\sqrt{N}} \sum_{\kappa} \exp(i\kappa l) \hat{a}_{\kappa} \quad \{\hat{a}_{\kappa}, \hat{a}_{\kappa'}^+\} = \delta_{\kappa\kappa'}$$

$$\hat{H} = \text{const} + \sum_{\kappa} \hbar\omega_{\kappa} \hat{a}_{\kappa}^+ \hat{a}_{\kappa}$$

$$\hbar\omega_{\kappa} = 2S [J(\kappa) - J(0)]$$

$$\hat{H} = \text{const} + \sum_{\kappa} \hbar\omega_{\kappa} \hat{b}_{\kappa}^+ \hat{b}_{\kappa}$$

$$\hbar\omega_{\kappa} = 2S \sqrt{[J(0)]^2 - [J(\kappa)]^2}$$

Cross-section of the inelastic magnetic neutron scattering

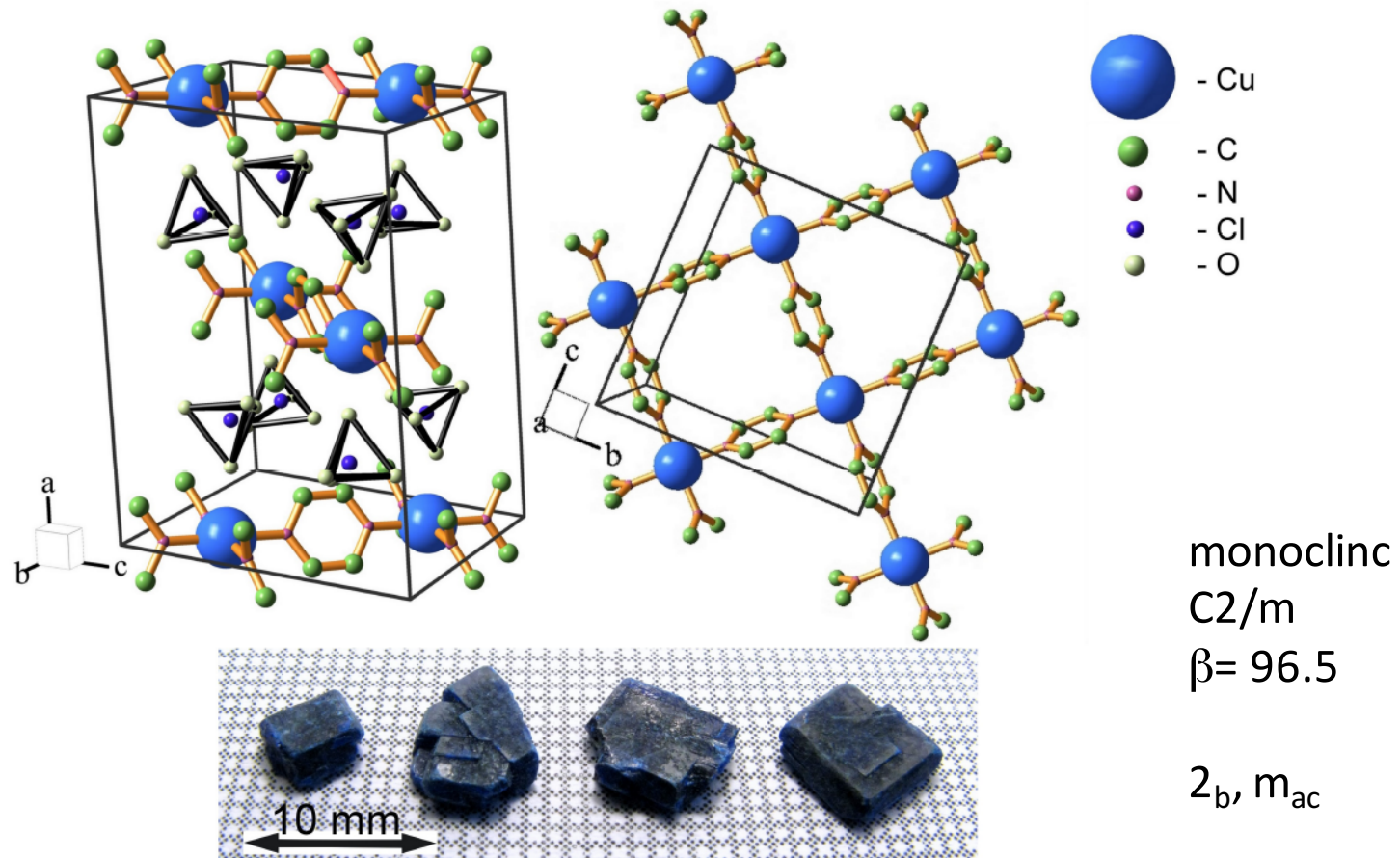
The diagram illustrates the cross-section of inelastic magnetic neutron scattering. The central equation is enclosed in a red box and is annotated with labels:

- Polarization factor**: points to the term $S(1 + \hat{q}_z^2)$.
- Form factor**: points to the term $\left| \frac{1}{2} gF(\mathbf{q}) \right|^2$.
- DW factor**: points to the term $e^{-2W_{\mathbf{q}}}$.
- Magnon creation**: points to the first term in the summation, $\delta(\boldsymbol{\kappa} - \mathbf{q} - \boldsymbol{\tau}) \delta(\hbar\omega_{\boldsymbol{\kappa}} - \hbar\omega) \langle\langle \mathbf{n}_{\boldsymbol{\kappa}} + 1 \rangle\rangle$.
- Magnon annihilation**: points to the second term in the summation, $\delta(\boldsymbol{\kappa} + \mathbf{q} - \boldsymbol{\tau}) \delta(\hbar\omega_{\boldsymbol{\kappa}} + \hbar\omega) \langle\langle \mathbf{n}_{\boldsymbol{\kappa}} \rangle\rangle$.

$$\left(\frac{d^2\sigma}{d\Omega dE'} \right) = (\gamma r_0)^2 \frac{k'}{k} \frac{(2\pi)^3}{V_0} \frac{1}{2} S(1 + \hat{q}_z^2) \left| \frac{1}{2} gF(\mathbf{q}) \right|^2 e^{-2W_{\mathbf{q}}} \times$$

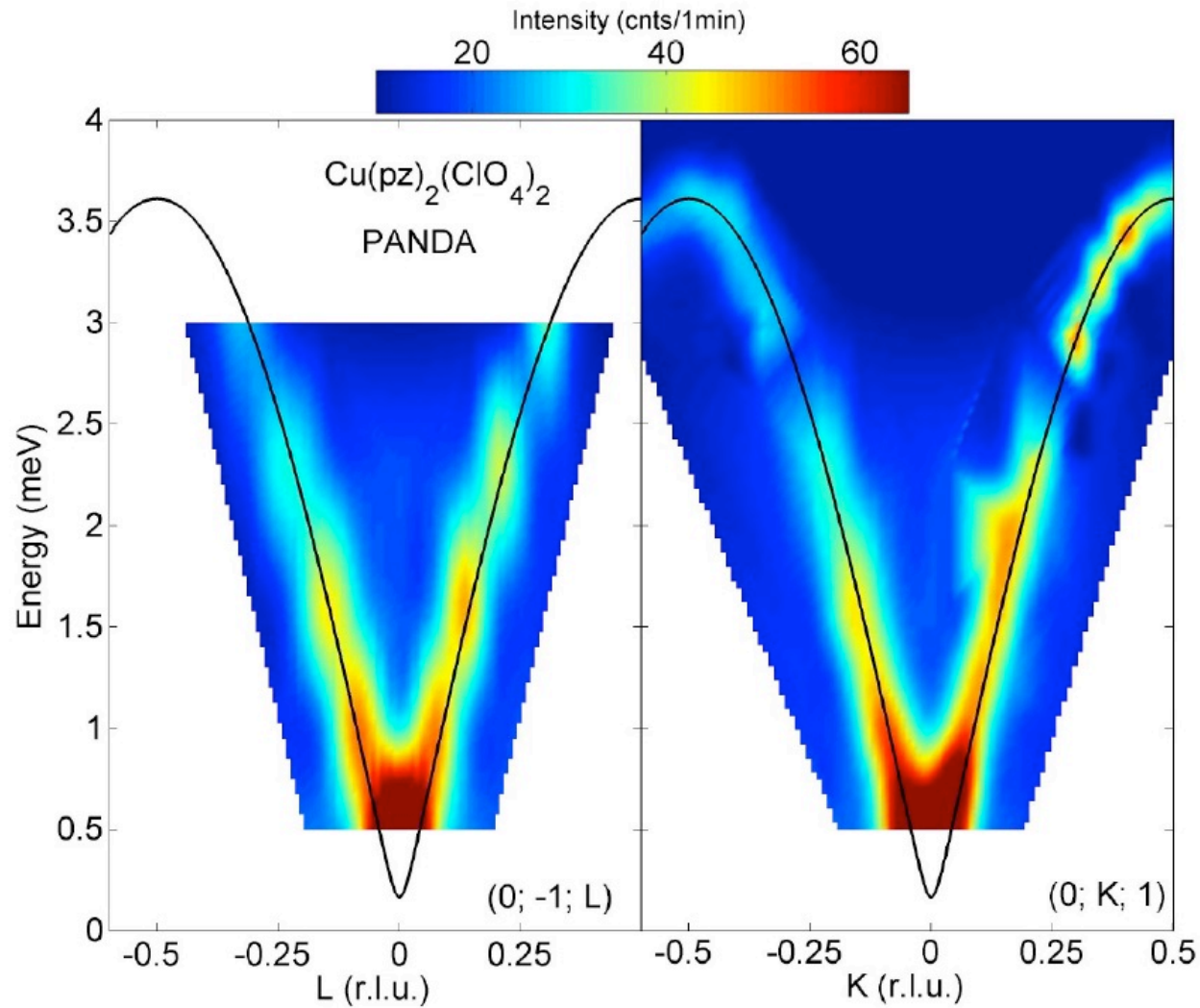
$$\times \sum_{\boldsymbol{\tau}, \boldsymbol{\kappa}} \left[\delta(\boldsymbol{\kappa} - \mathbf{q} - \boldsymbol{\tau}) \delta(\hbar\omega_{\boldsymbol{\kappa}} - \hbar\omega) \langle\langle \mathbf{n}_{\boldsymbol{\kappa}} + 1 \rangle\rangle + \delta(\boldsymbol{\kappa} + \mathbf{q} - \boldsymbol{\tau}) \delta(\hbar\omega_{\boldsymbol{\kappa}} + \hbar\omega) \langle\langle \mathbf{n}_{\boldsymbol{\kappa}} \rangle\rangle \right]$$

Simple Example: $\text{Cu}(\text{pz})_2(\text{ClO}_4)_2$



Identical exchange interactions along bc and $-bc$ directions
Absence of DM interactions due to symmetry

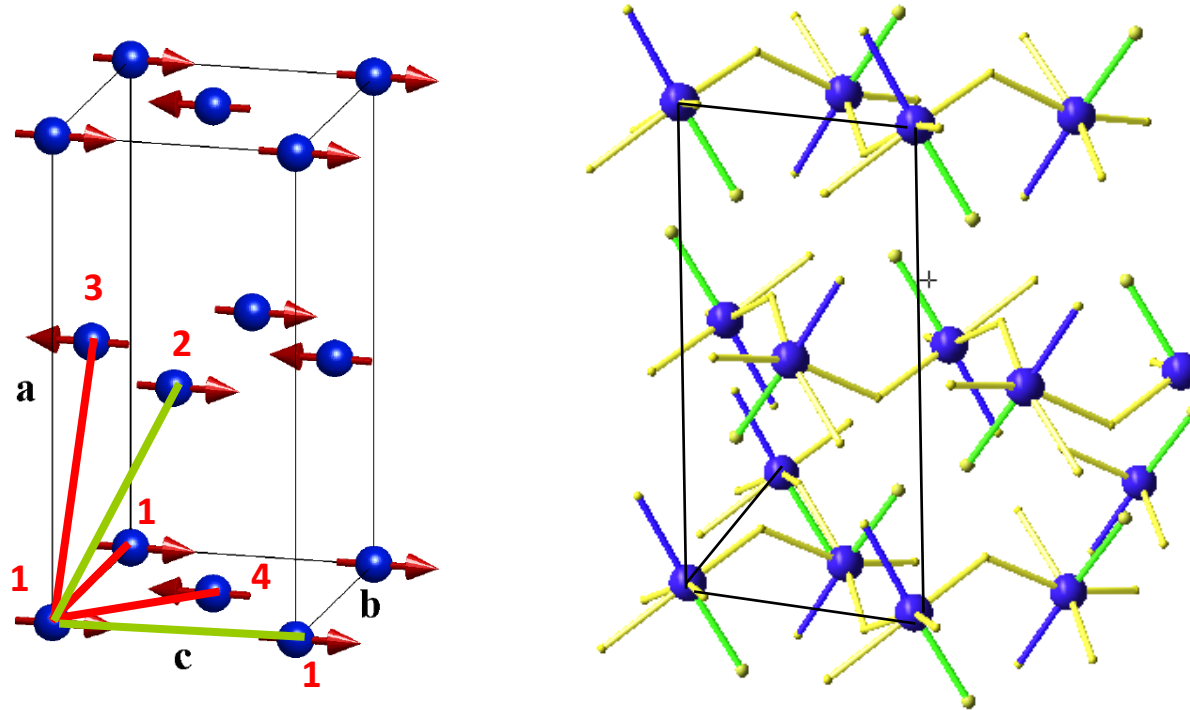
Spin-wave excitations



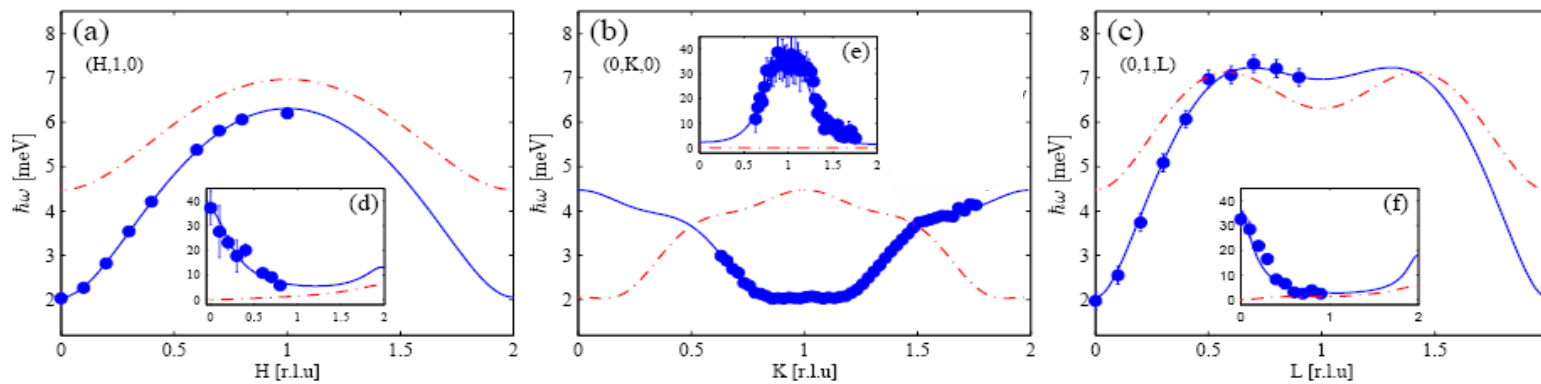
- Spin waves are best seen in reciprocal space where they occur as peaks as a function of energy
- Measured with inelastic neutron scattering instruments (types?)

LiNiPO₄: exchange interactions

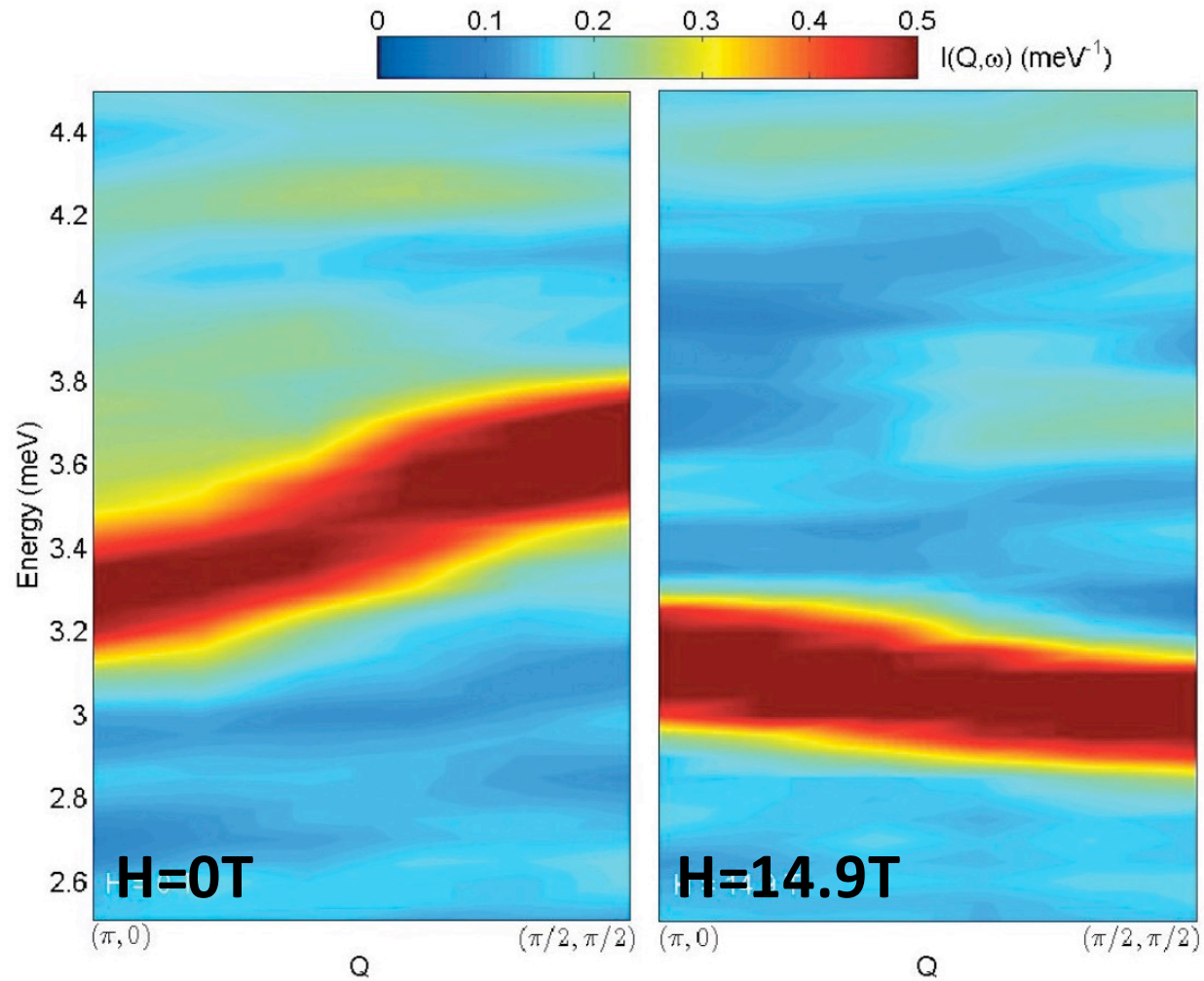
$J_{14}=1.04\text{meV}$
 $J_{11}=0.67\text{meV}$
 $J_{13}=0.3\text{meV}$
 $J_{12}=-0.11\text{meV}$
 $J_{11}=-0.05\text{meV}$
 $D_x=0.17\text{meV}$
 $D_y=0.91\text{meV}$
 $D_z=0\text{meV}$



T.B.S. Jensen et al, Phys. Rev. B 79, 092413 (2009).

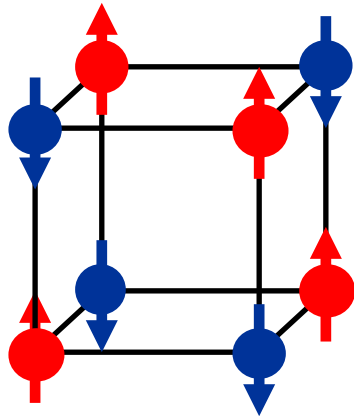


Novel excitations in $\text{Cu}(\text{pz})_2(\text{ClO}_4)_2$

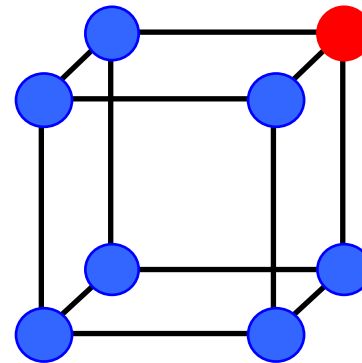


Quantum vs. “classical” magnetism

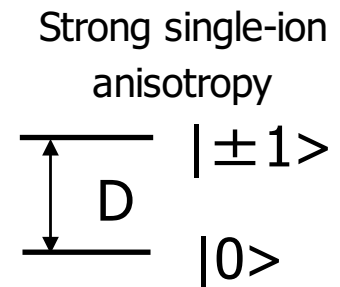
- Magnetism is of quantum nature
- Many materials behave rather classical, and the quantization of spin degrees of freedom is suppressed



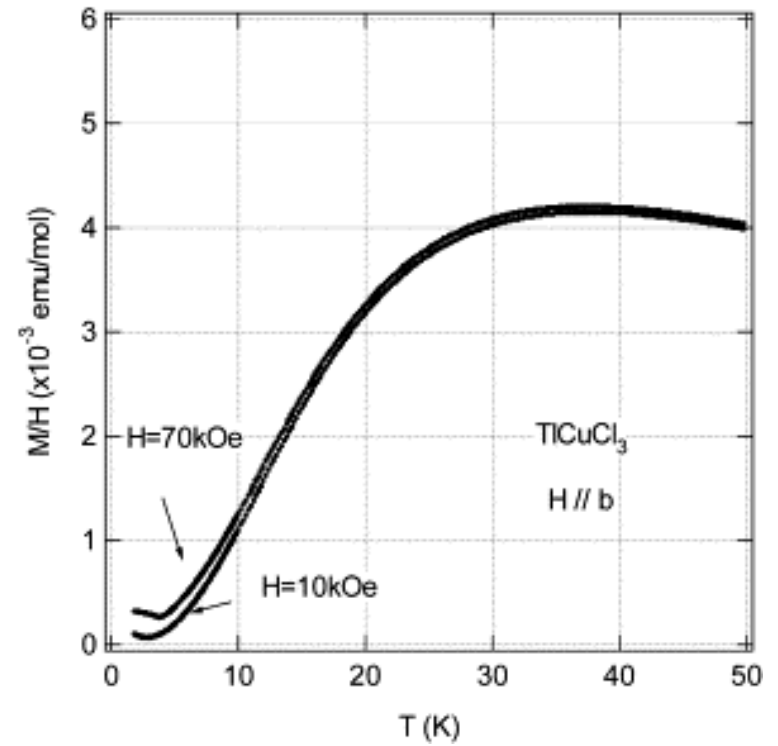
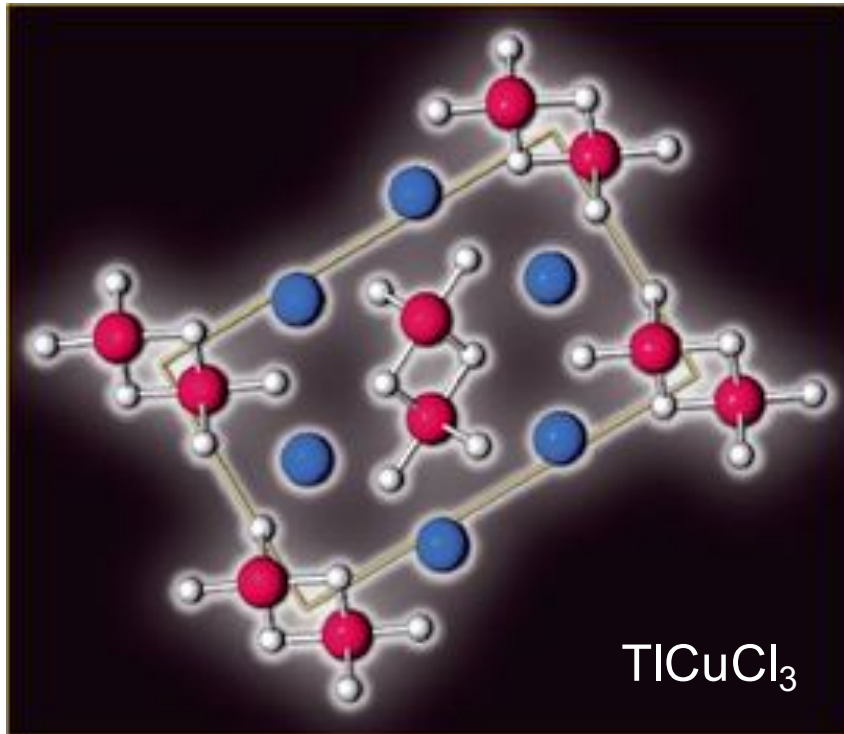
Wave-like perturbation of magnetic moments away from their ordered direction



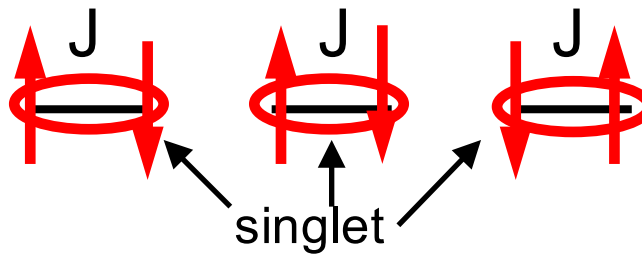
delocalization of $|\pm 1\rangle$ states due to spin interactions



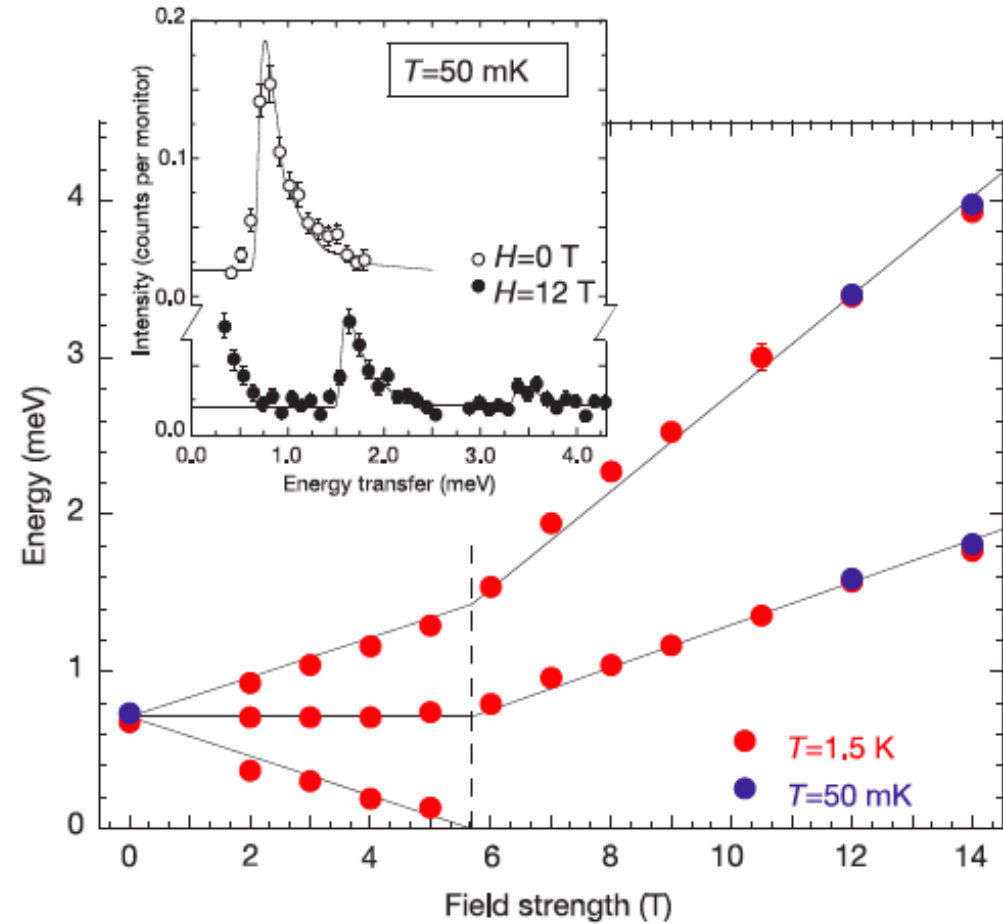
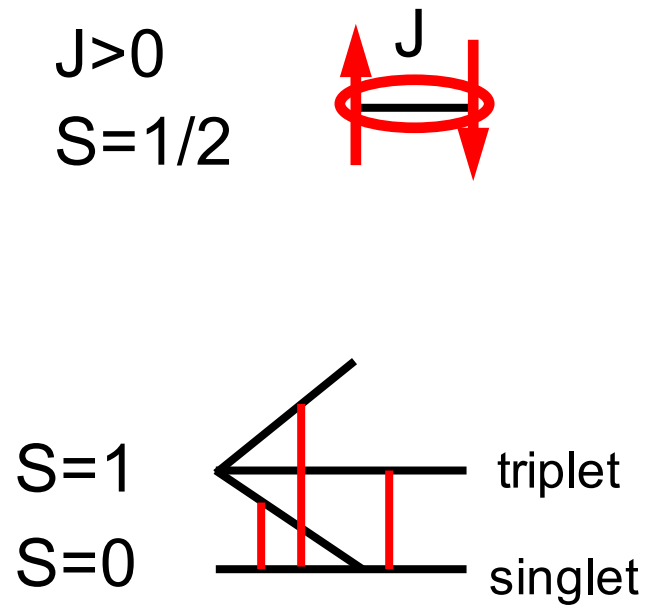
Quantum dimer material



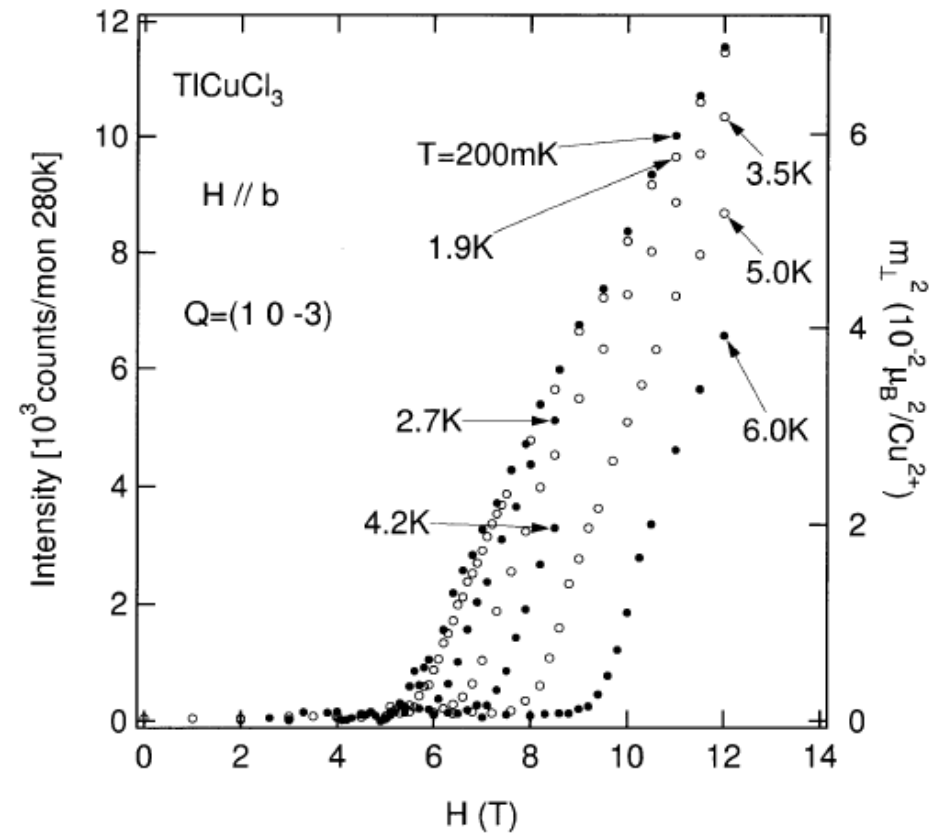
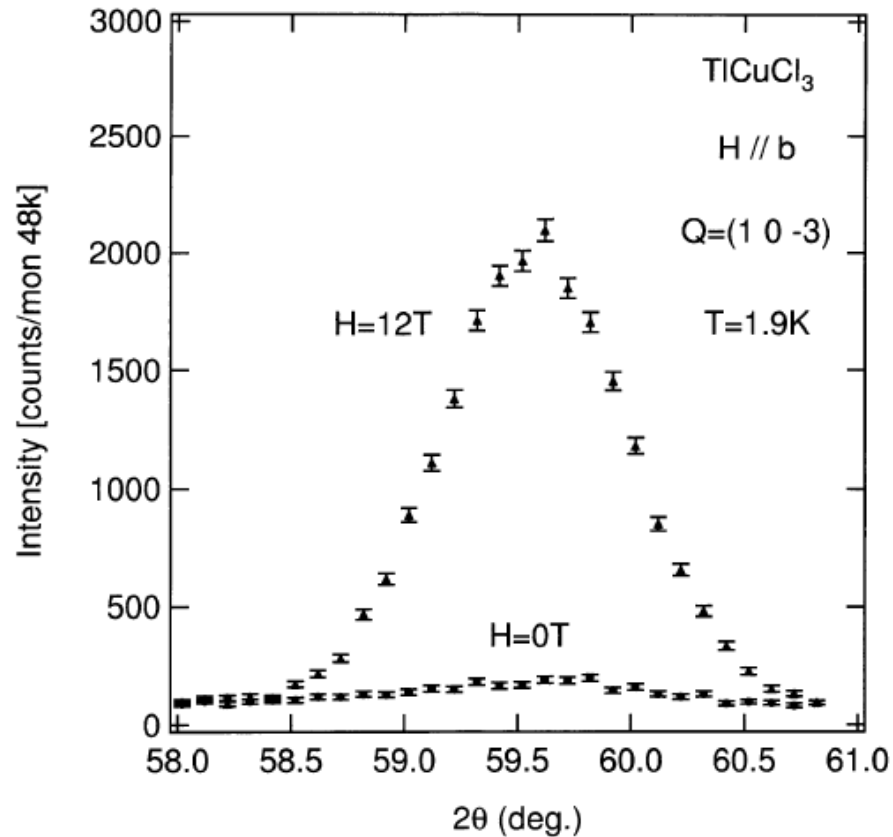
$$J > 0$$
$$S = 1/2$$



Field dependence of excitations



Quantum phase transition in TlCuCl_3



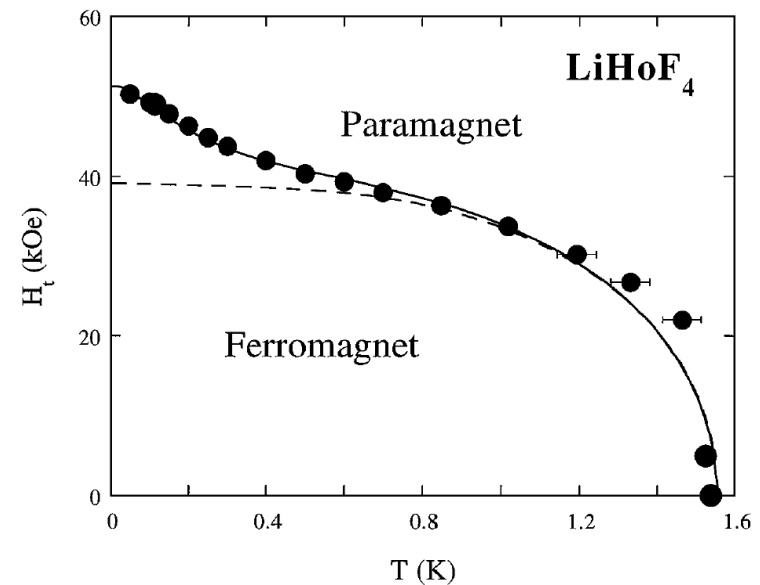
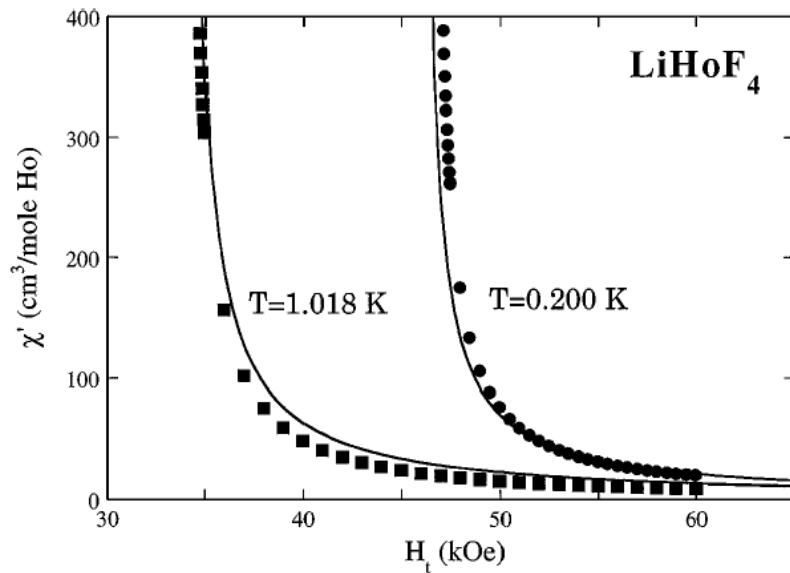
H. Tanak et al, J. Phys. Soc. Japan **4**, 939 (2001).

What are the properties of a material at the quantum critical point?

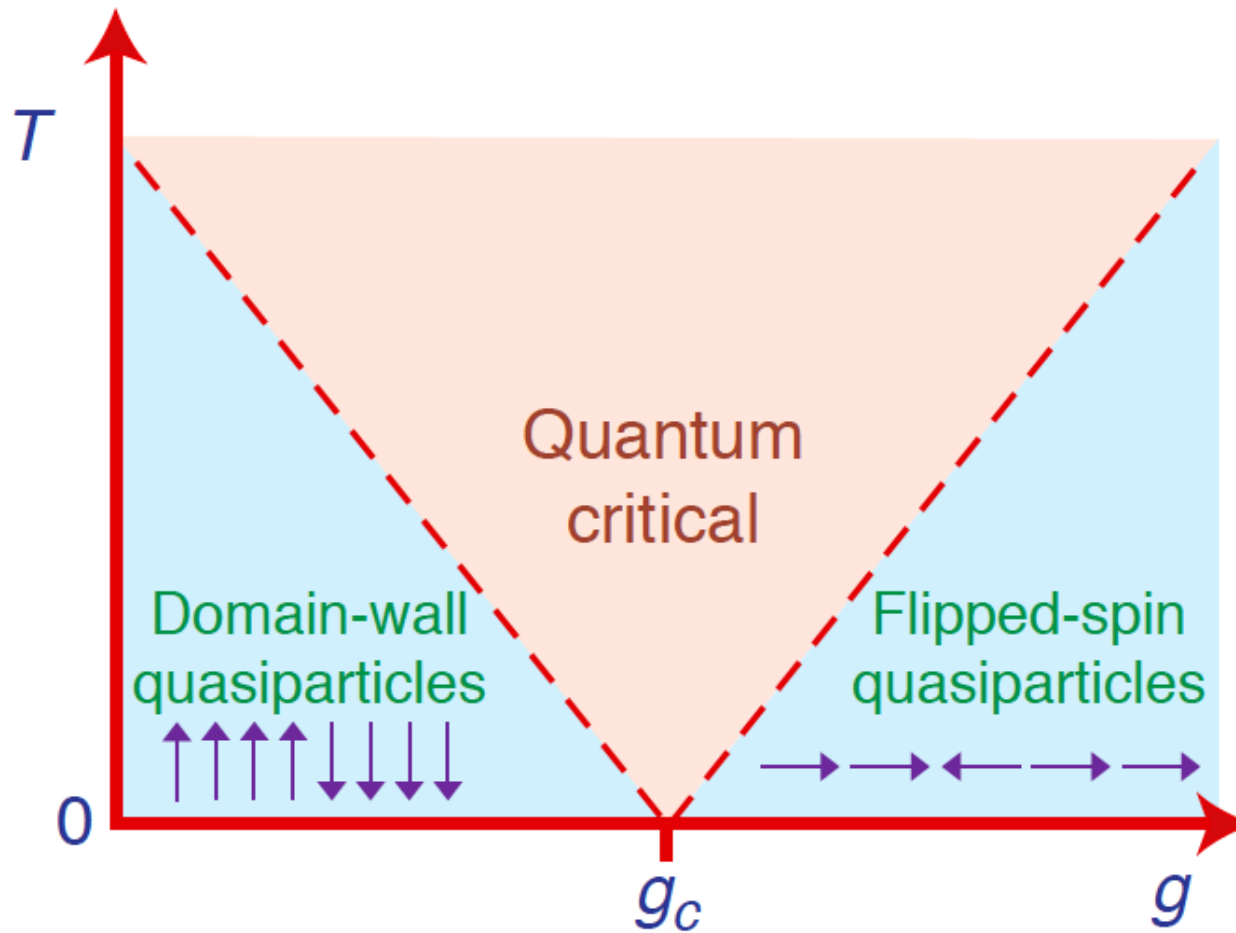
Tuning of the magnetic ground state

Quantum Phase Transition:

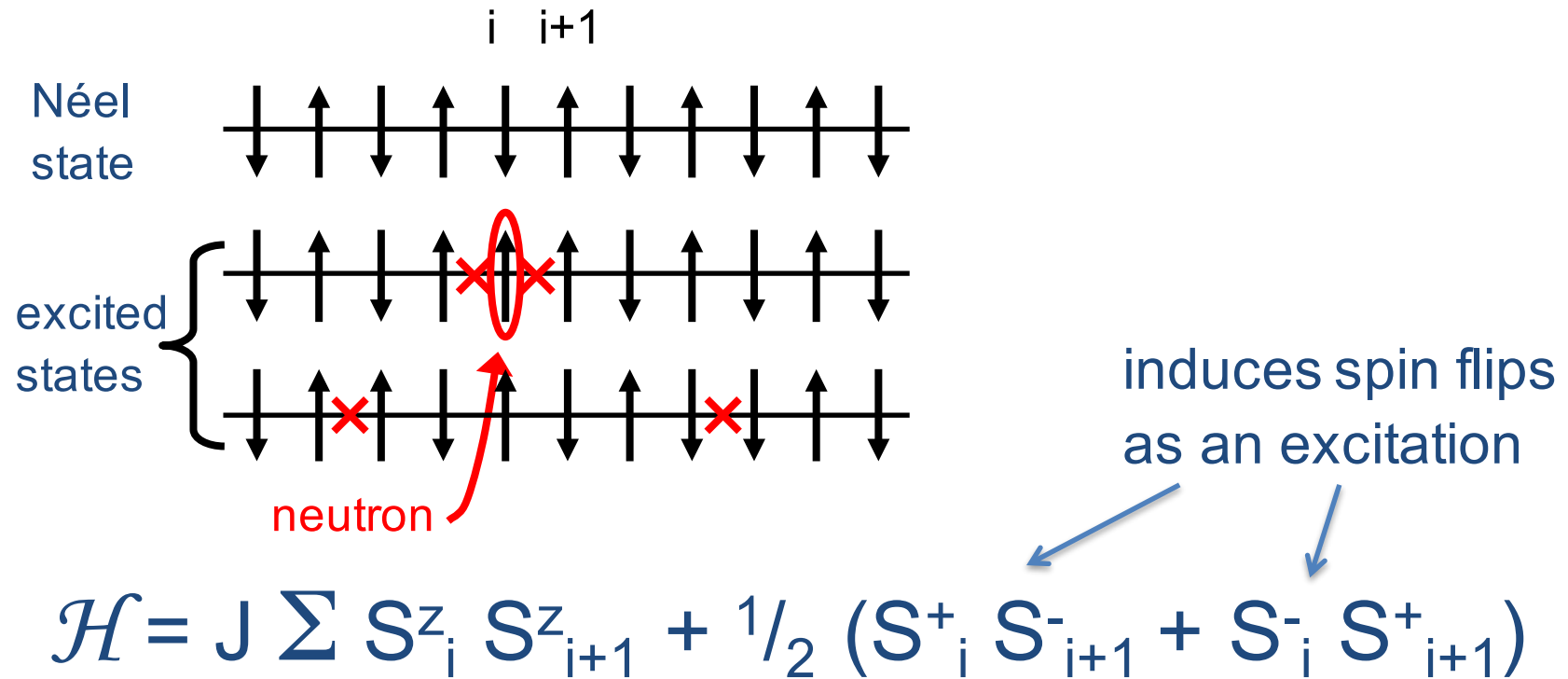
$$H = -J \sum S_i^z S_j^z - \mu_B H^x \sum S_i^x$$



No energy scale at the quantum critical point apart from T

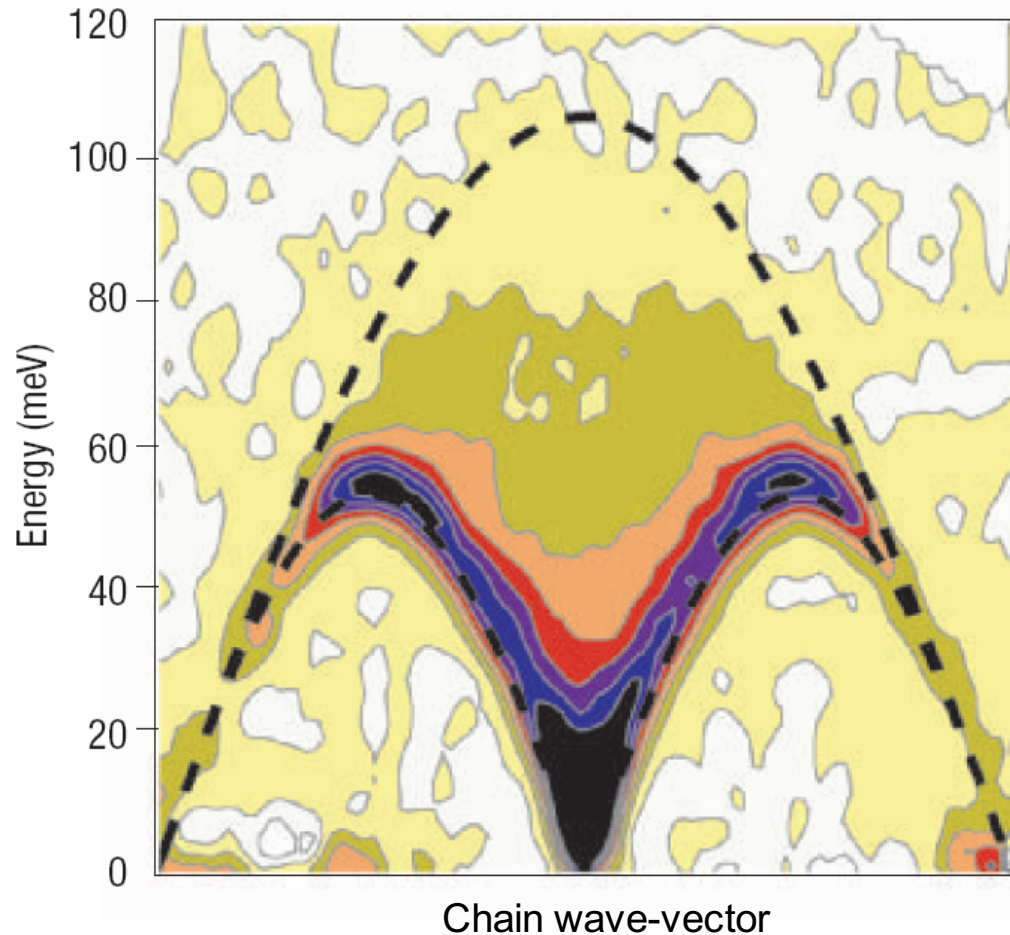


Quantum critical AF S=1/2 Heisenberg Chains



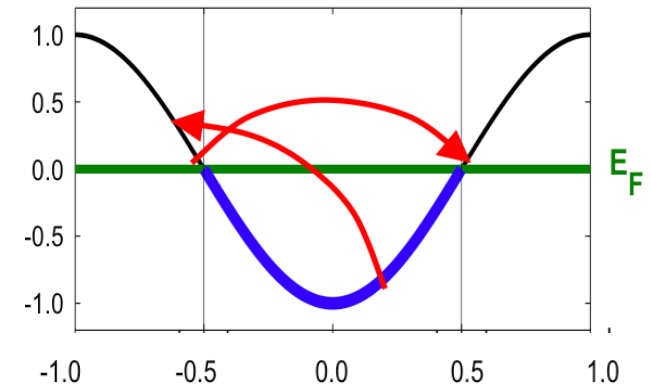
- quasi long-range order: AF correlations fall off as a power law
- new type of excitations: spinons carrying S=1/2
- pair of excitations induced by neutron scattering

AF S=1/2 Heisenberg Chains



B. Lake et al, Nature Materials

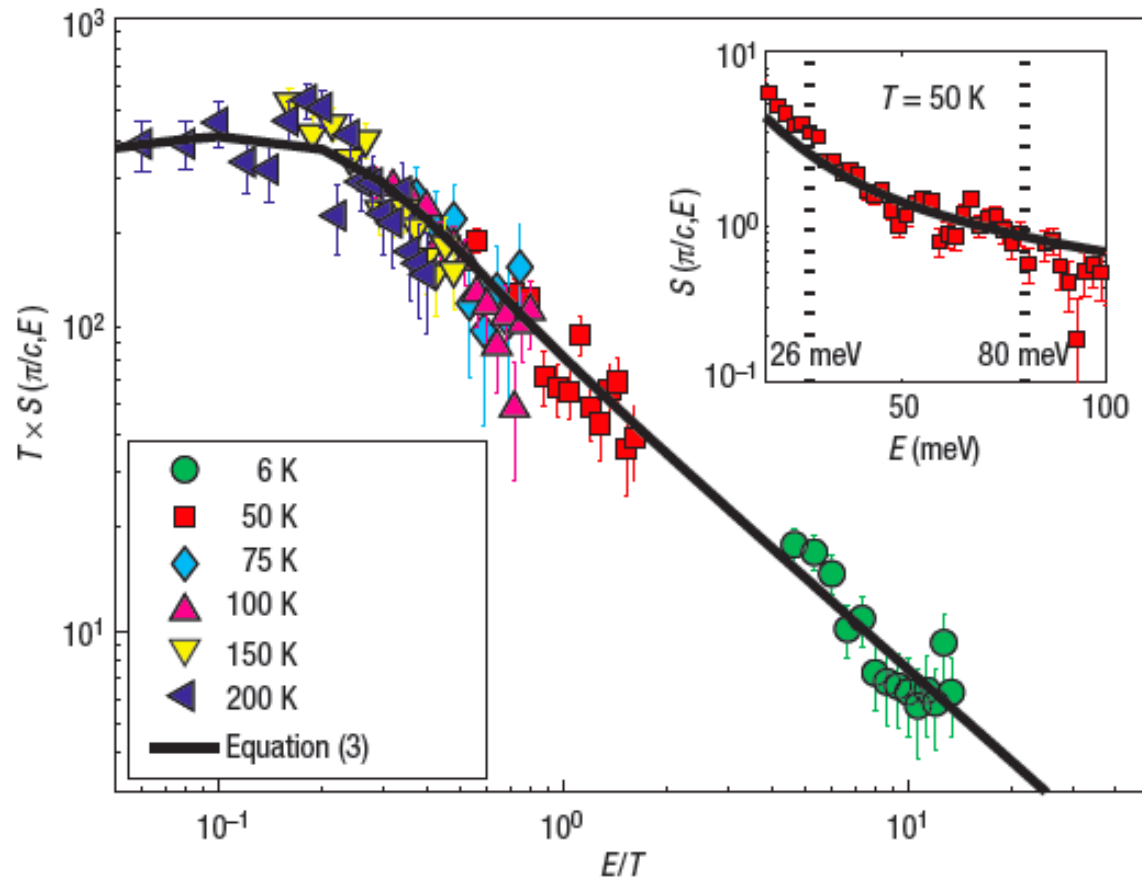
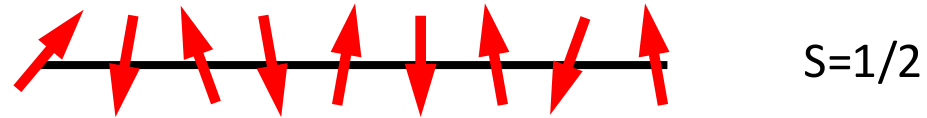
- pair of spinons are created by neutron scattering
- continuum of excitations
- can be pictures as a particle excitation



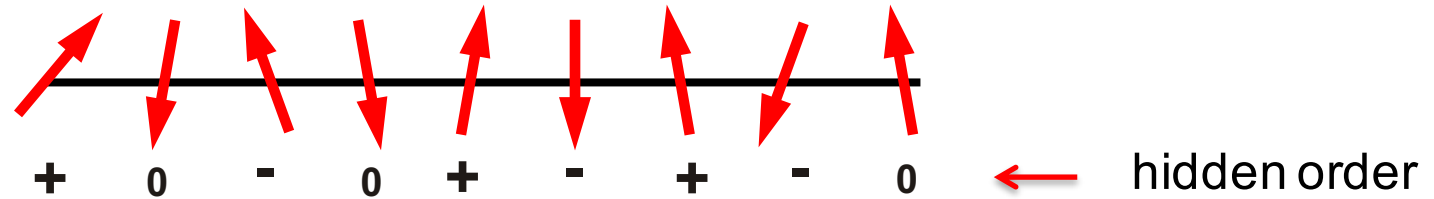
KCuF₃ at T=50K > T_N

$$\mathcal{H} = J \sum S_i^z S_{i+1}^z + \frac{1}{2} (S_i^+ S_{i+1}^- + S_i^- S_{i+1}^+)$$

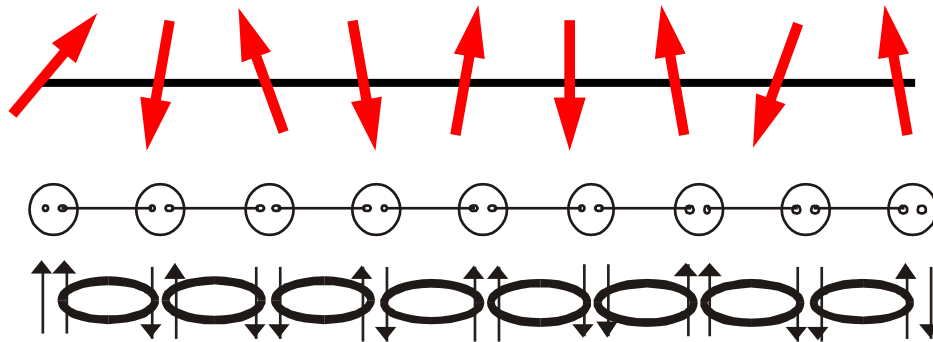
Quantum critical scaling of AF S=1/2 chain



Quantum Spin liquid: antiferromagnetic $S=1$ chain



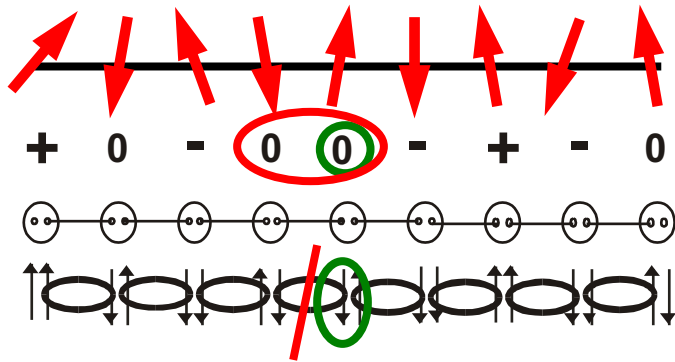
coupled $S=1$ model with string order



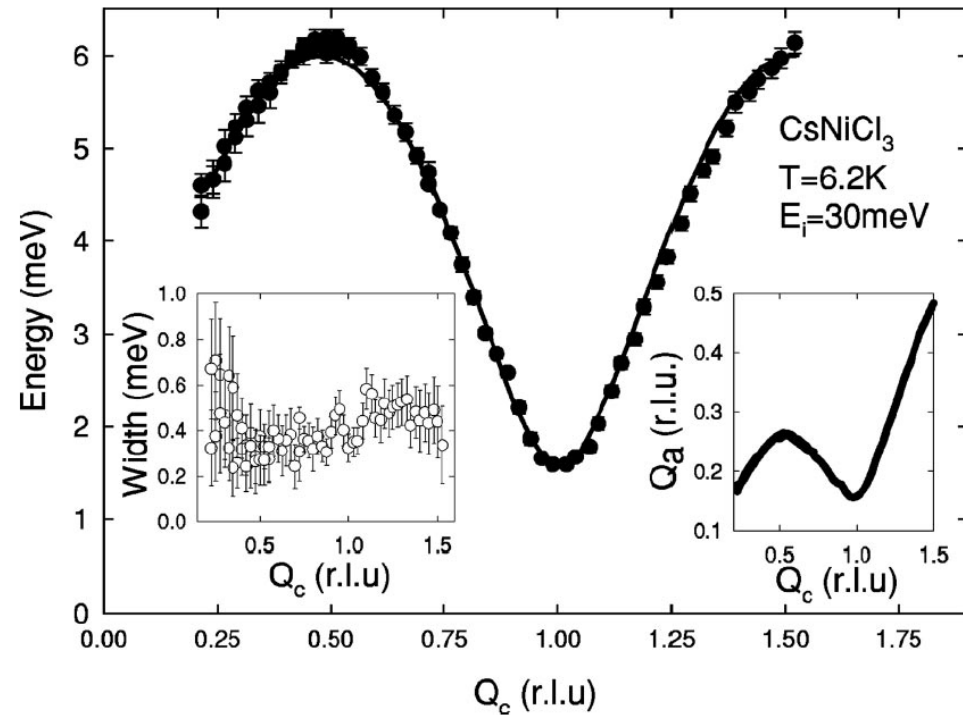
valence-bond solid model
symmetrized pair of $S=1/2$

Quantum spin liquid state in AF S=1 chains

The gapped excitation spectrum is dominated by S=1 triplet excitations with hidden spin order

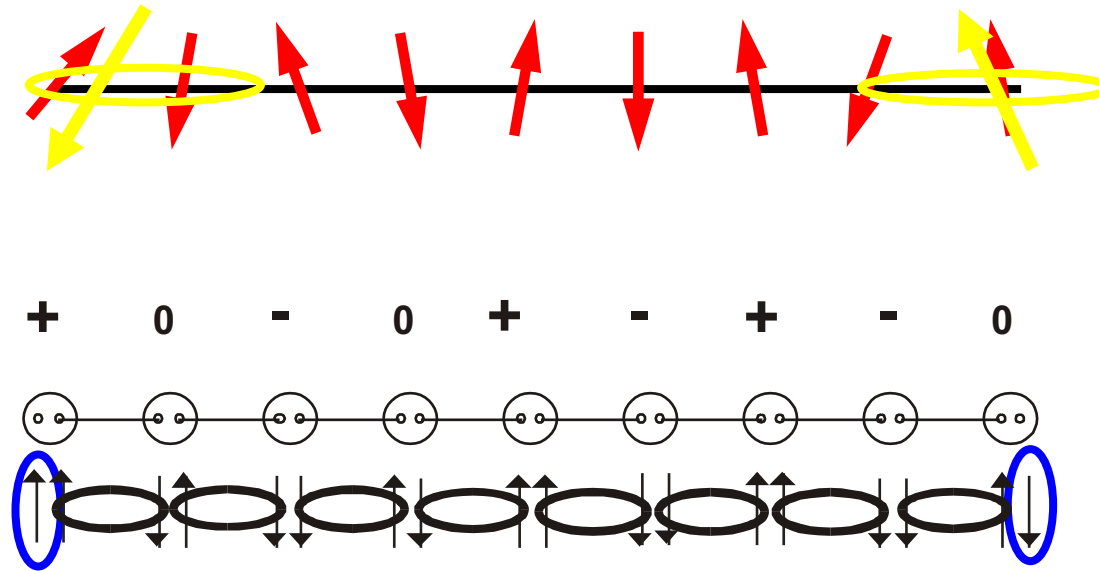


excitations are moving hidden domain walls



M. Kenzelmann et al, Phys. Rev B **66**, 024407 (2002)

Role of defects in spin liquids?



valence-bond model predicts chain-end $S=1/2$

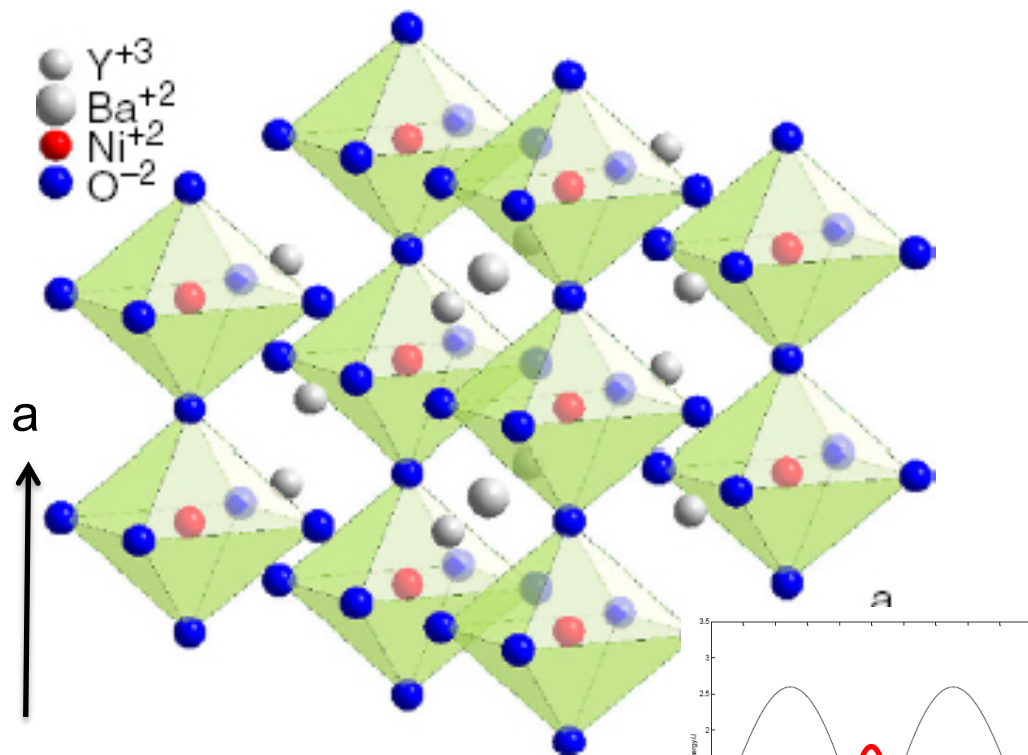
$S=1/2$ degree of freedoms are coupled (either ferromagnetically or antiferromagnetically)

I. Affleck et al. *Phys. Rev. Lett.* **1987**

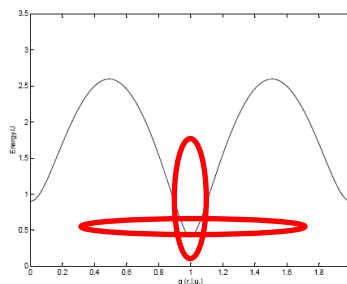
M. Hagiwara et al. *Phys. Rev. Lett.* **1990**

Sensitivity of a quantum spin liquid to impurities

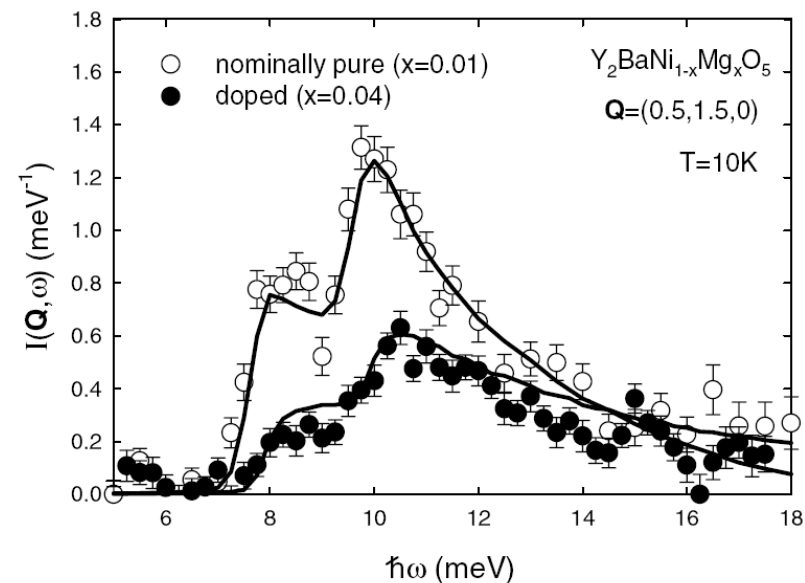
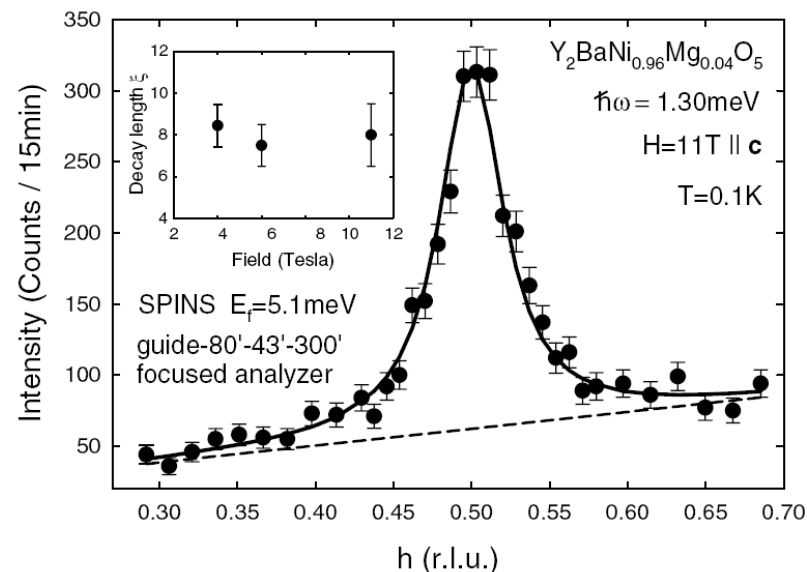
Replace a small amount of Ni ions with non-magnetic Mg



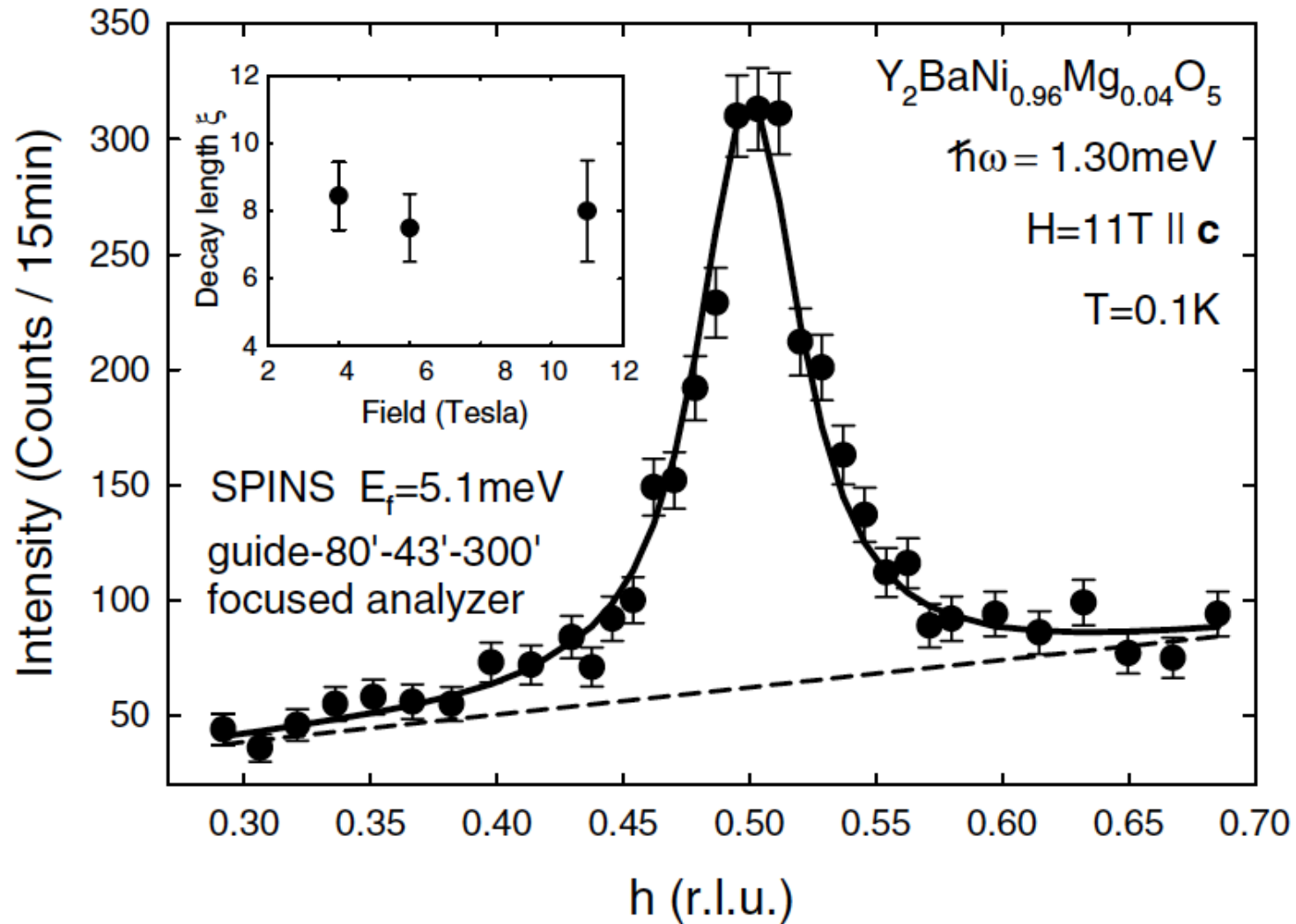
Upward renormalization of quantum gap with decreasing chain length



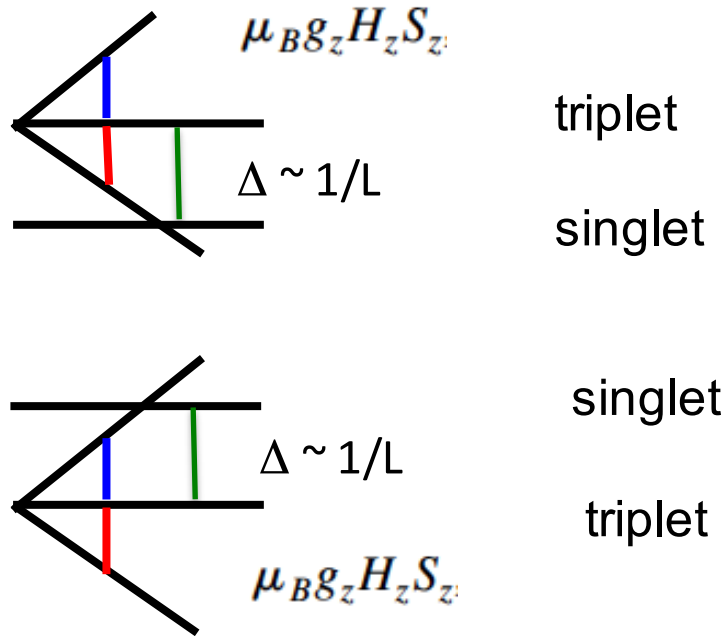
$$\Delta \sim 1/\xi$$



Cooperative chain-end degree of freedoms

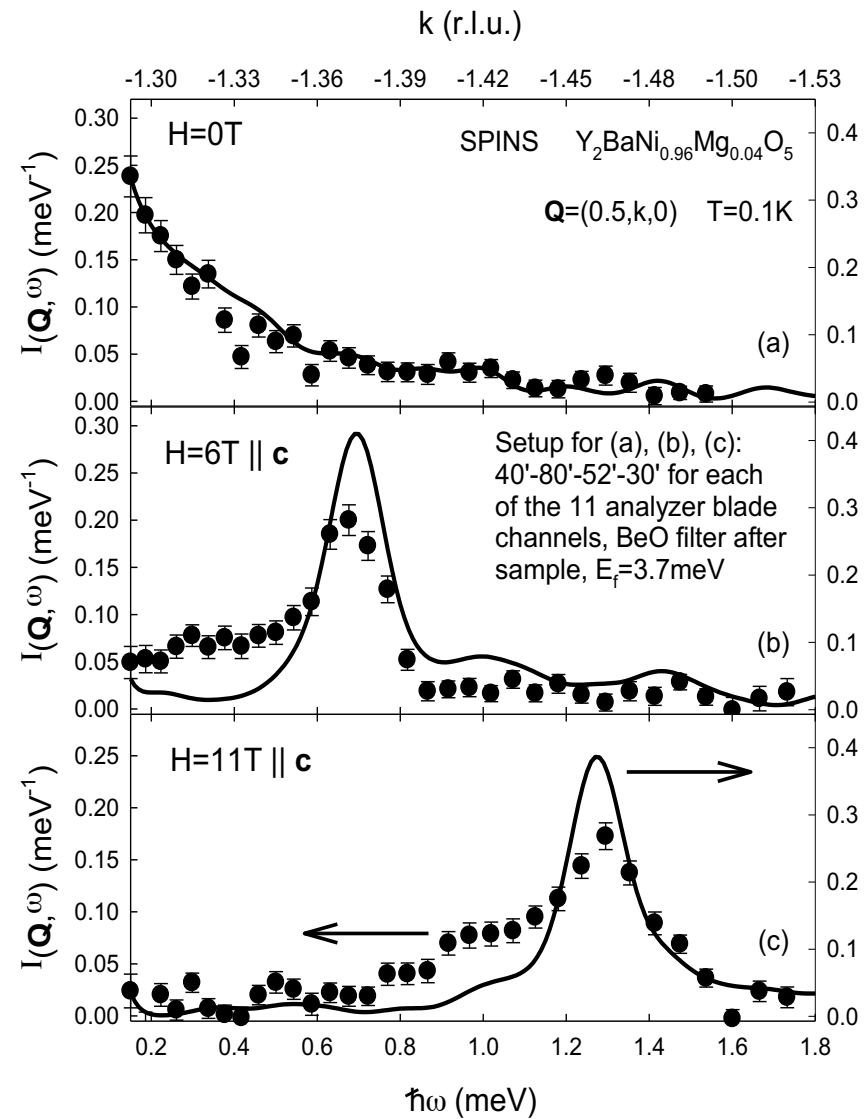


End-chain cooperative degrees of freedom



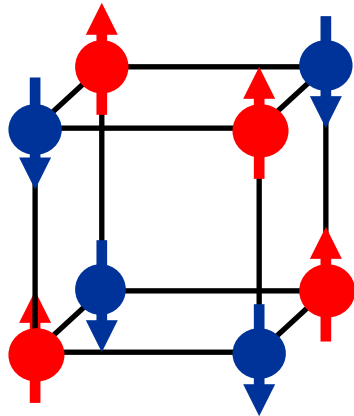
Presence of $S=1/2$ degrees of freedom at the end of $S=1$ chains in doped Y_2BaNiO_5

Quantum liquids are sensitive to impurities

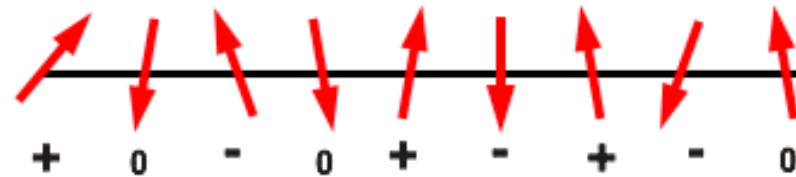


Quantum vs. “classical” magnetism

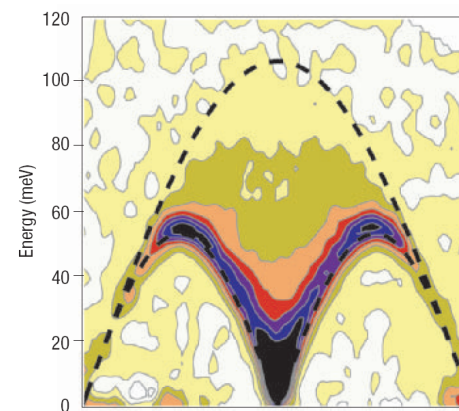
- Magnetism is of quantum nature
- Many materials behave rather classical, and the quantization of spin degrees of freedom is suppressed



Wave-like perturbation of magnetic moments away from their ordered direction

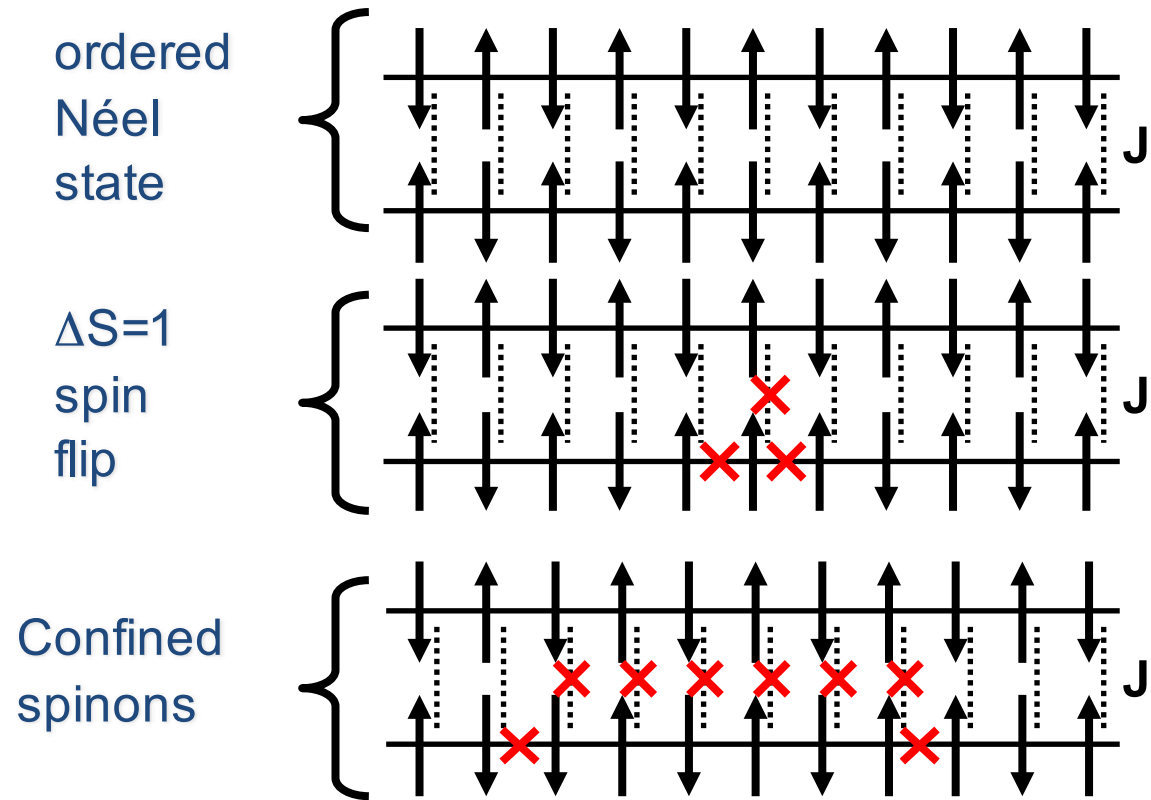


Hidden order in $S=1$ chains

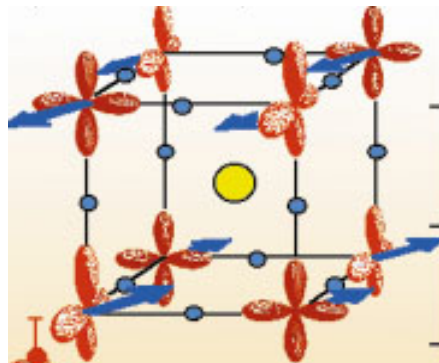
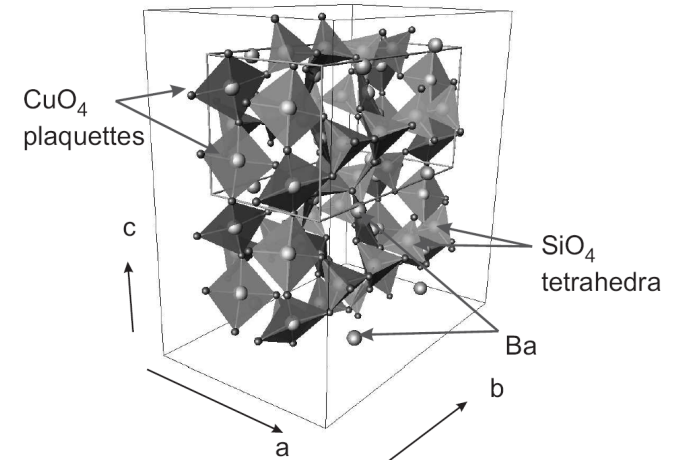


Spinons in $S=1/2$ chains

Spinon confinement in coupled S=1/2 Chains



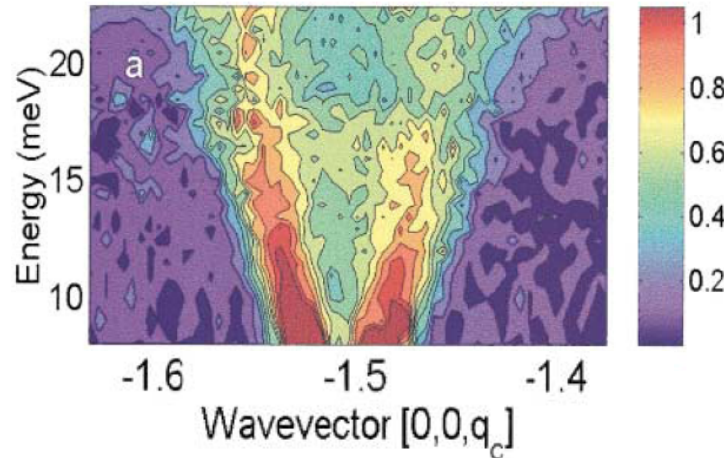
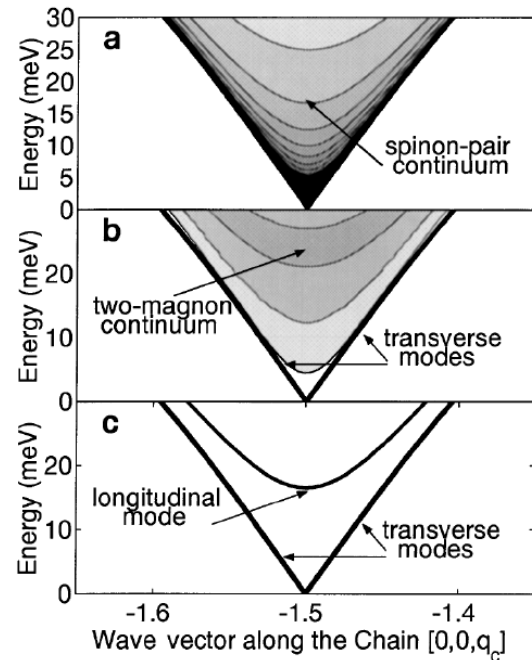
AF S=1/2 chain $\text{BaCu}_2\text{Si}_2\text{O}_7$



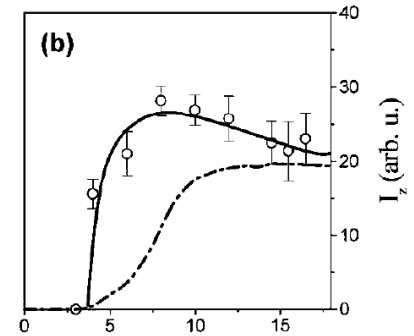
AF S=1/2 chain KCuF_3

- ✗ Long-range magnetic order
- ✗ Low-energy spectrum consists of spin waves carrying spin-1
- ✗ at higher energies two-spinon continuum

Binding of spinons and longitudinal spin-wave

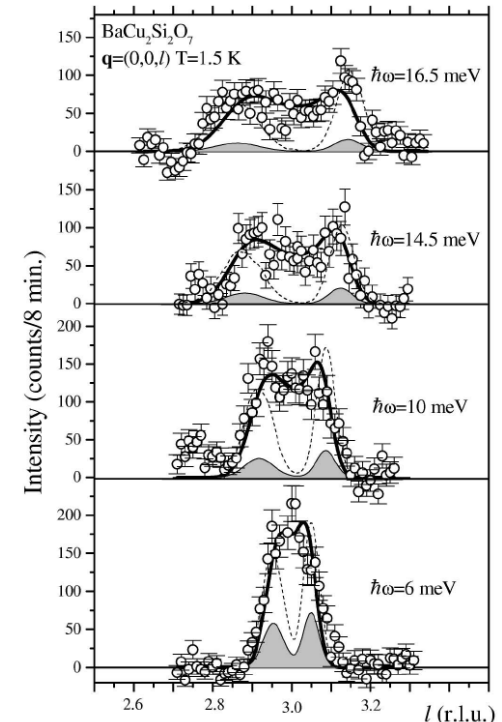


B. Lake et al, Phys. Rev. Lett. 85, 834 (2000)

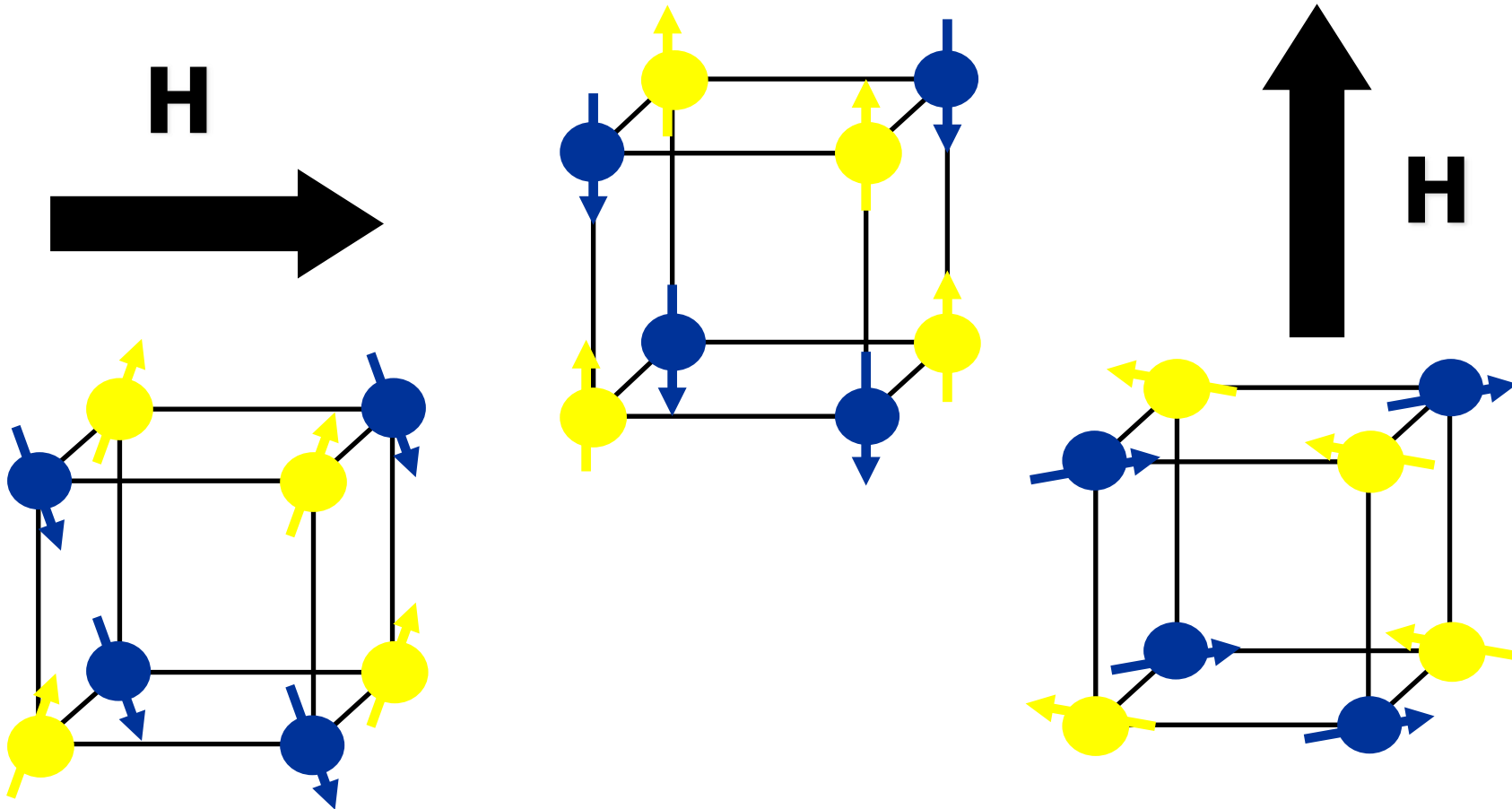


A. Zheludev et al, Phys. Rev. Lett. 85, 4801 (2000)

- ✗ Longitudinal fluctuations of ordered moment possible
- ✗ Low-energy spectrum consists of spin waves carrying spin-1
- ✗ at higher energies two-spinon continuum



Ordered Magnet in Magnetic Field



Canting of spins results in small net magnetization

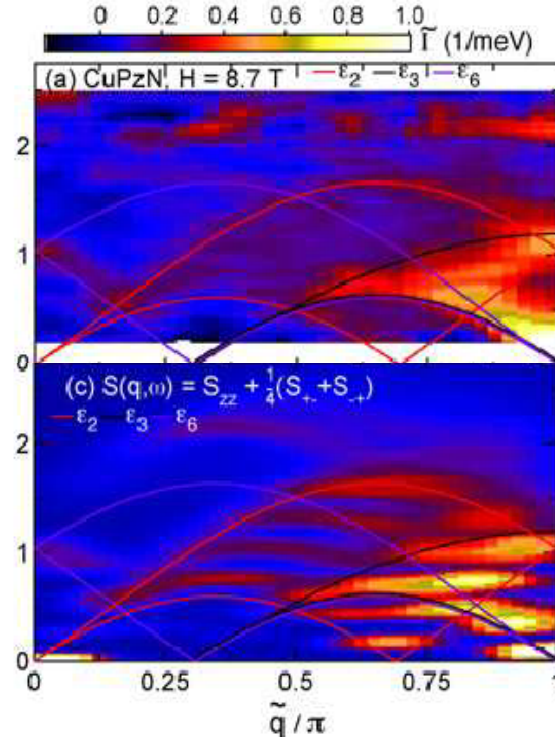
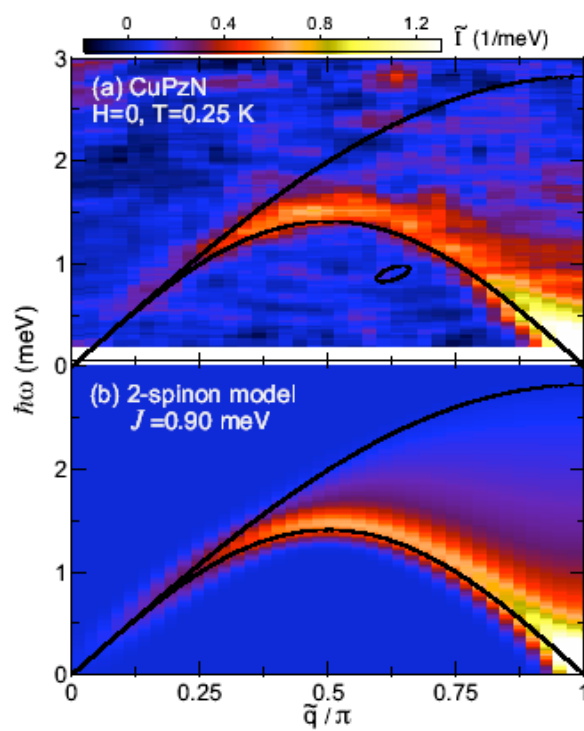
Spin undergo reorientation (spin-flop transition)

S=1/2 Chain in a Magnetic Field

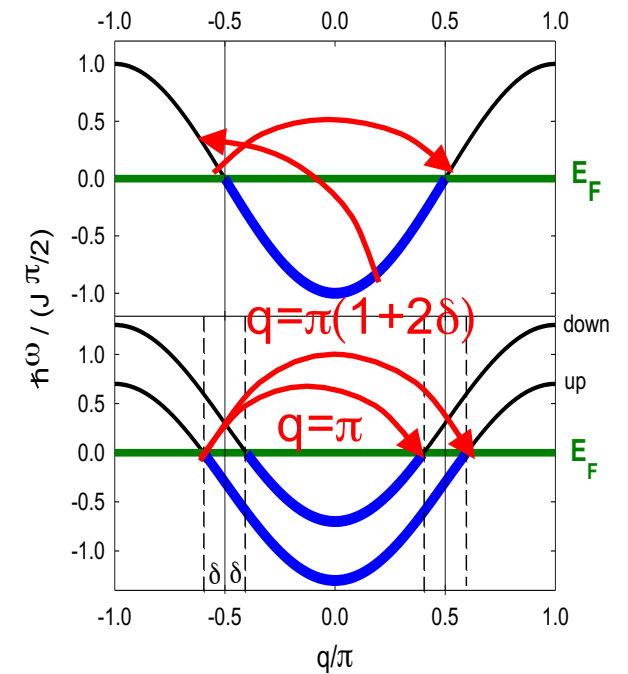
$$\mathcal{H} = \sum_i J \mathbf{S}_i \cdot \mathbf{S}_{i+1} - g_u \mu_B H S^z_i$$

spinon excitations

incommensurate with lattice



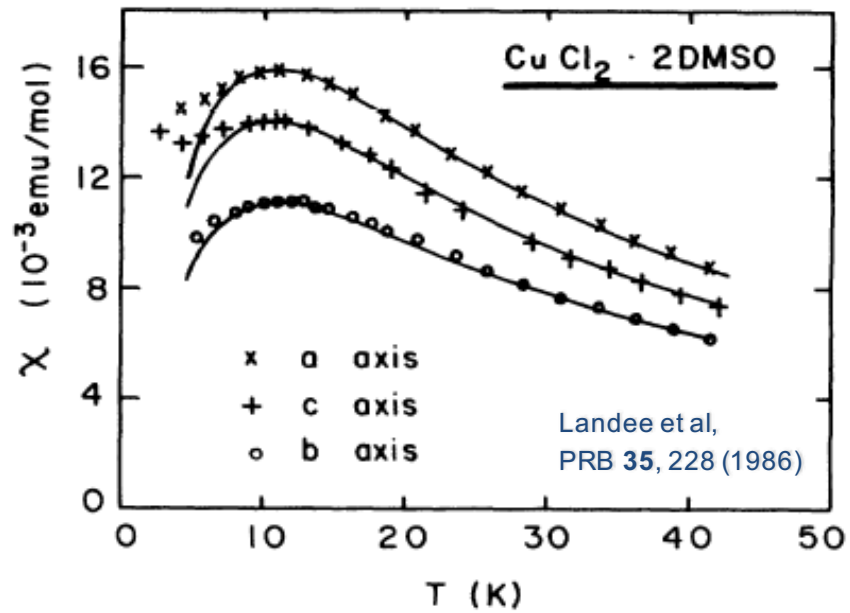
Particle-hole excitations



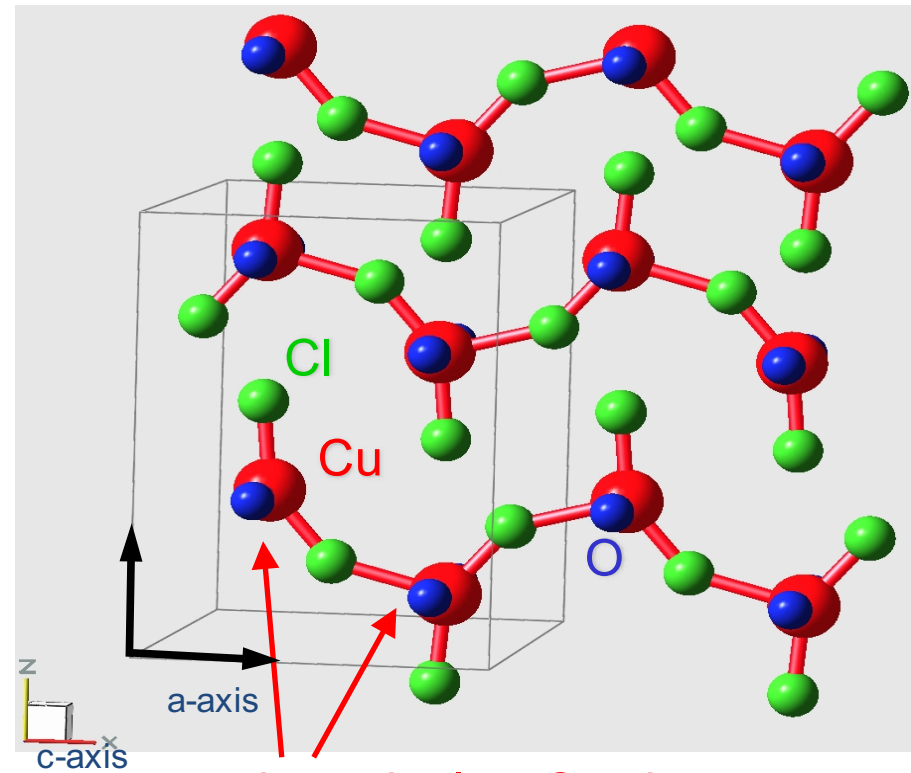
Excitation spectrum of CuPzN

M.B. Stone et al, Phys. Rev. Lett 2003

CDC S=1/2 chain

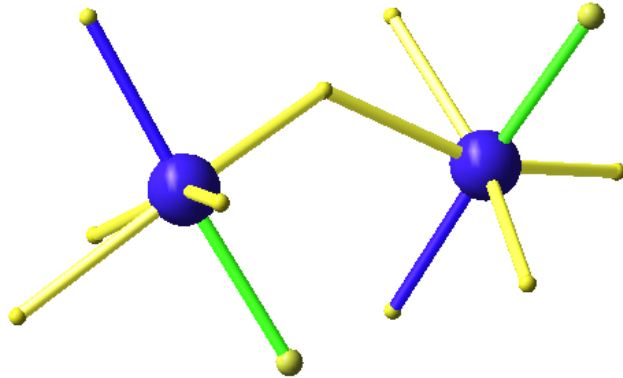


Broad maximum in magn. susceptibility



two inequivalent Cu sites

Magneto-electric quantum magnet CDC



$$D/J = 0.0102(5) \quad g^s = 0.068(3)$$

Y. Chen et al, Phys. Rev. B **75**, 214409 (2007)

1) Staggered gyromagnetic factor

$$g = \begin{pmatrix} 2.28 & 0 & \pm g_s \\ 0 & 1.97 & 0 \\ \pm g_s & 0 & 2.12 \end{pmatrix} = g^u \pm g^s,$$

2) Staggered Dzyaloshinskii-Moriya interactions

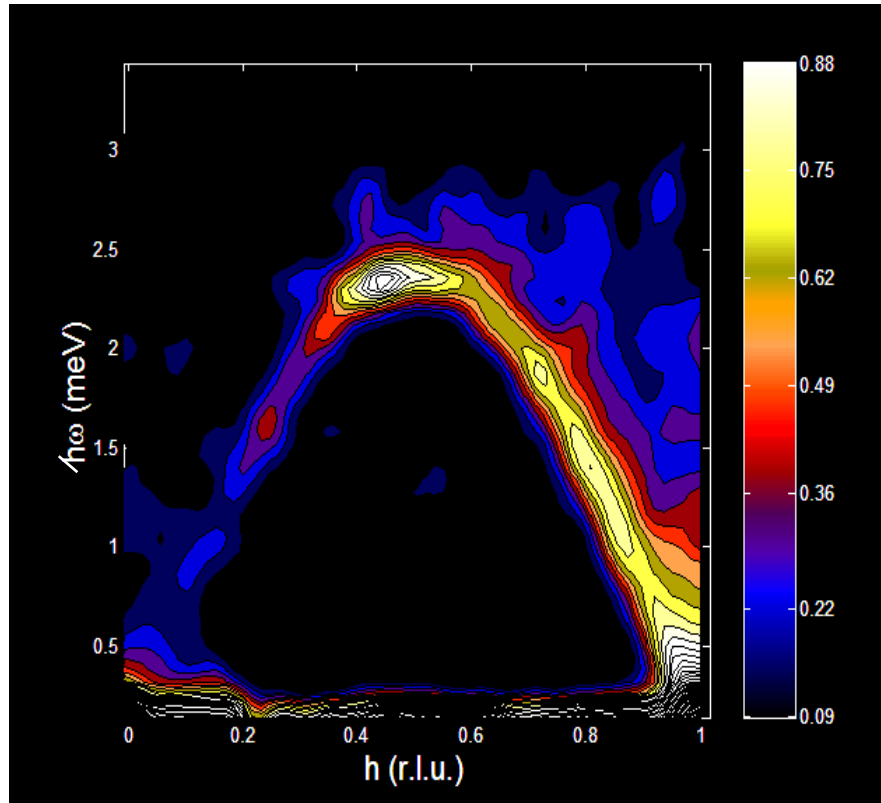
$$H_{DM} = \sum_i (-1)^i \mathbf{D} \cdot (\mathbf{S}_{i-1} \times \mathbf{S}_i)$$

$$\mathbf{h} = \frac{1}{2J} \mathbf{D} \times g^u \mathbf{H} + g^s \mathbf{H},$$

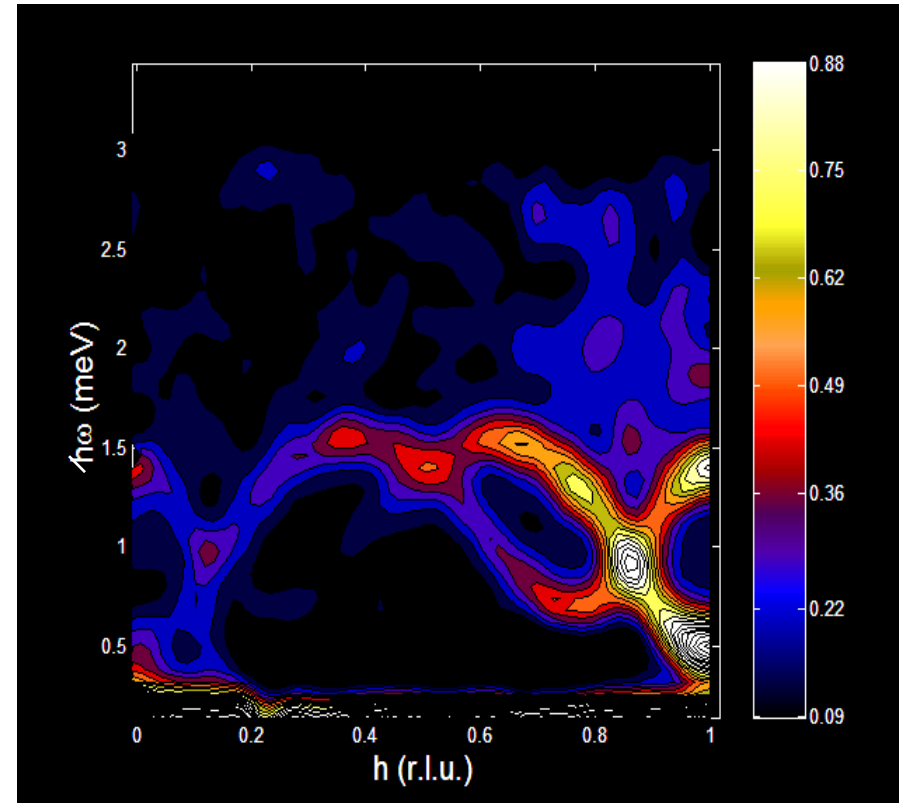
$$\mathcal{H} = J \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+1} - \sum_{j,a,b} H^a [g^u_{ab} + (-1)^j g^s_{ab}] S^b_j + \sum_j (-1)^j \mathbf{D} \cdot (\mathbf{S}_{j-1} \times \mathbf{S}_j)$$

$S(Q,\omega)$ measured using neutron scattering

Zero field and $T=40\text{mK}$



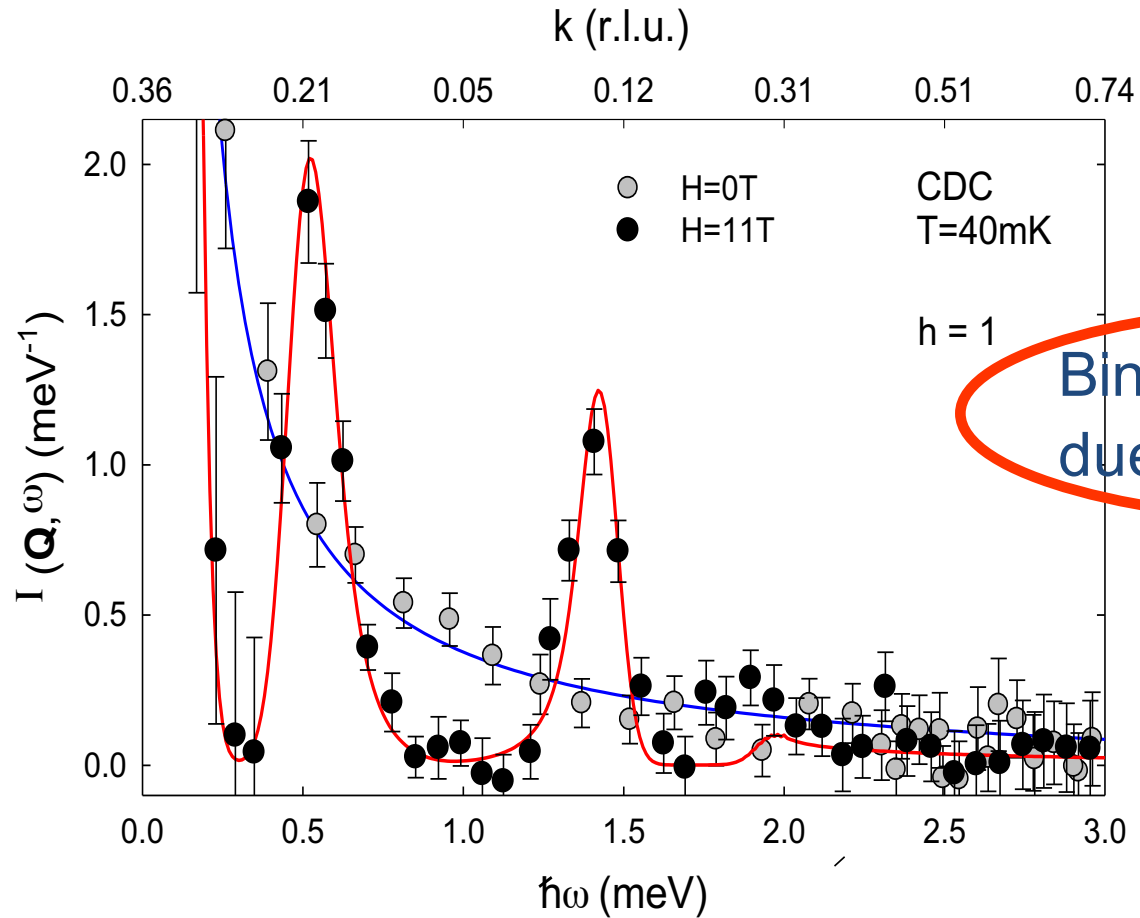
$H=11\text{T} \approx 0.8J$ and $T=40\text{mK}$



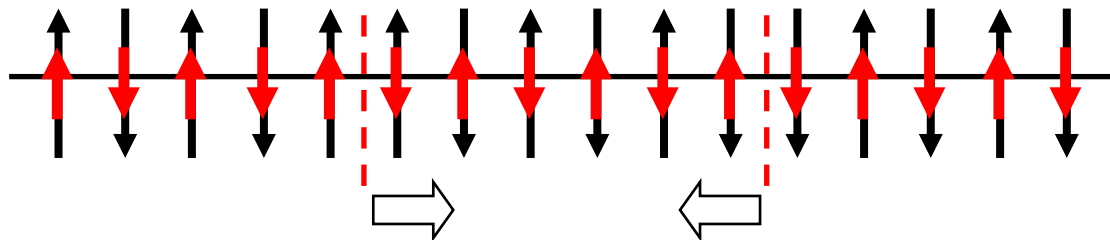
Two-spinon continuum of AF spin-1/2
Heisenberg chain with $J=1.5\text{meV}$
Intense lower bound $\hbar\omega = \pi/2 J |\sin(\pi h)|$

Spectrum at high field consists of
well-defined excitations

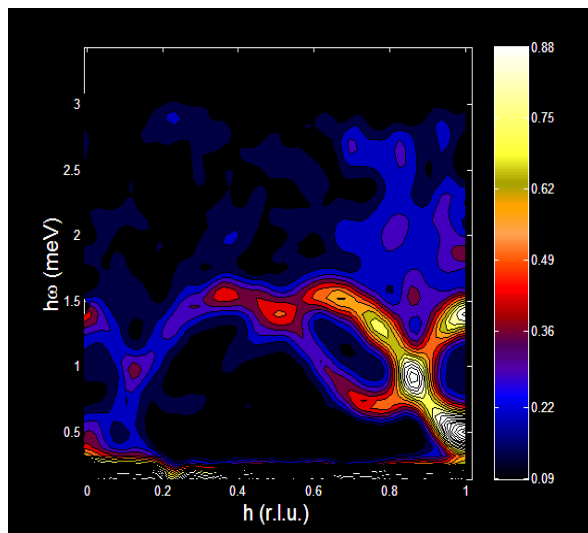
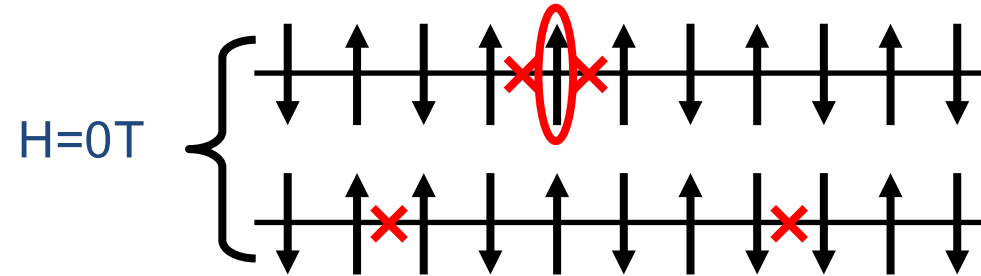
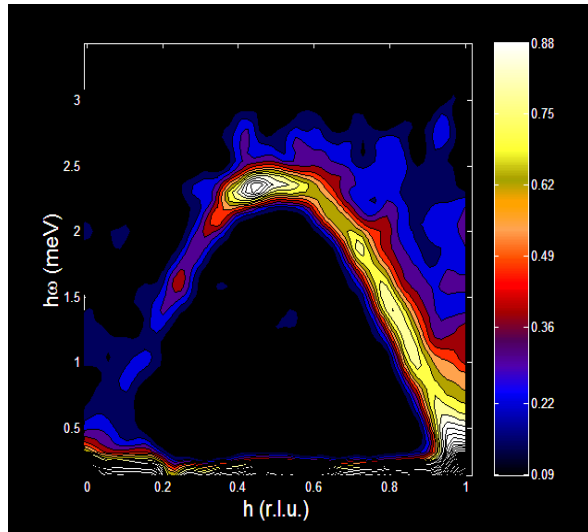
Bound spinons in staggered fields



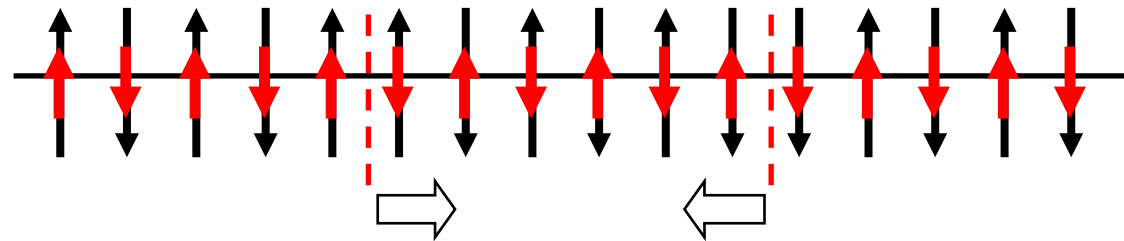
Binding of Spinons
due to staggered field



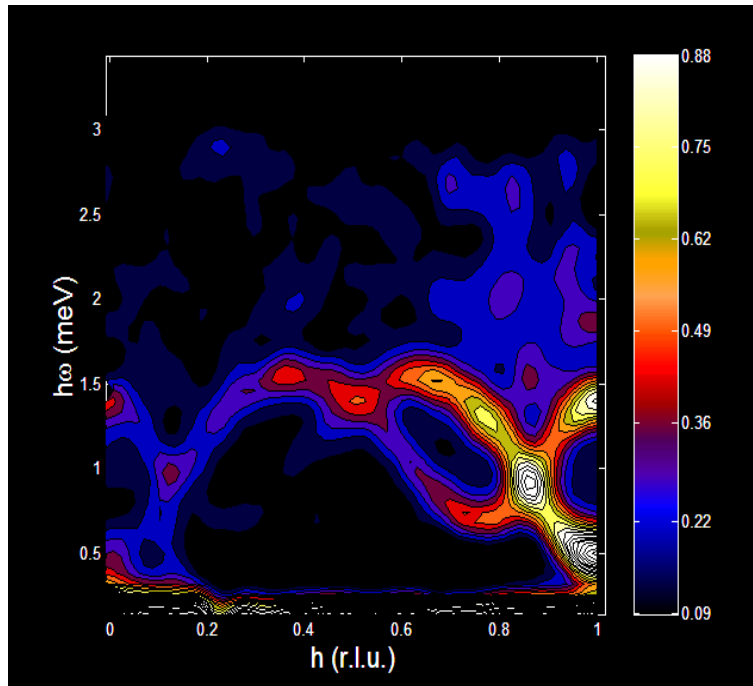
Spinons and Spinon binding in staggered fields



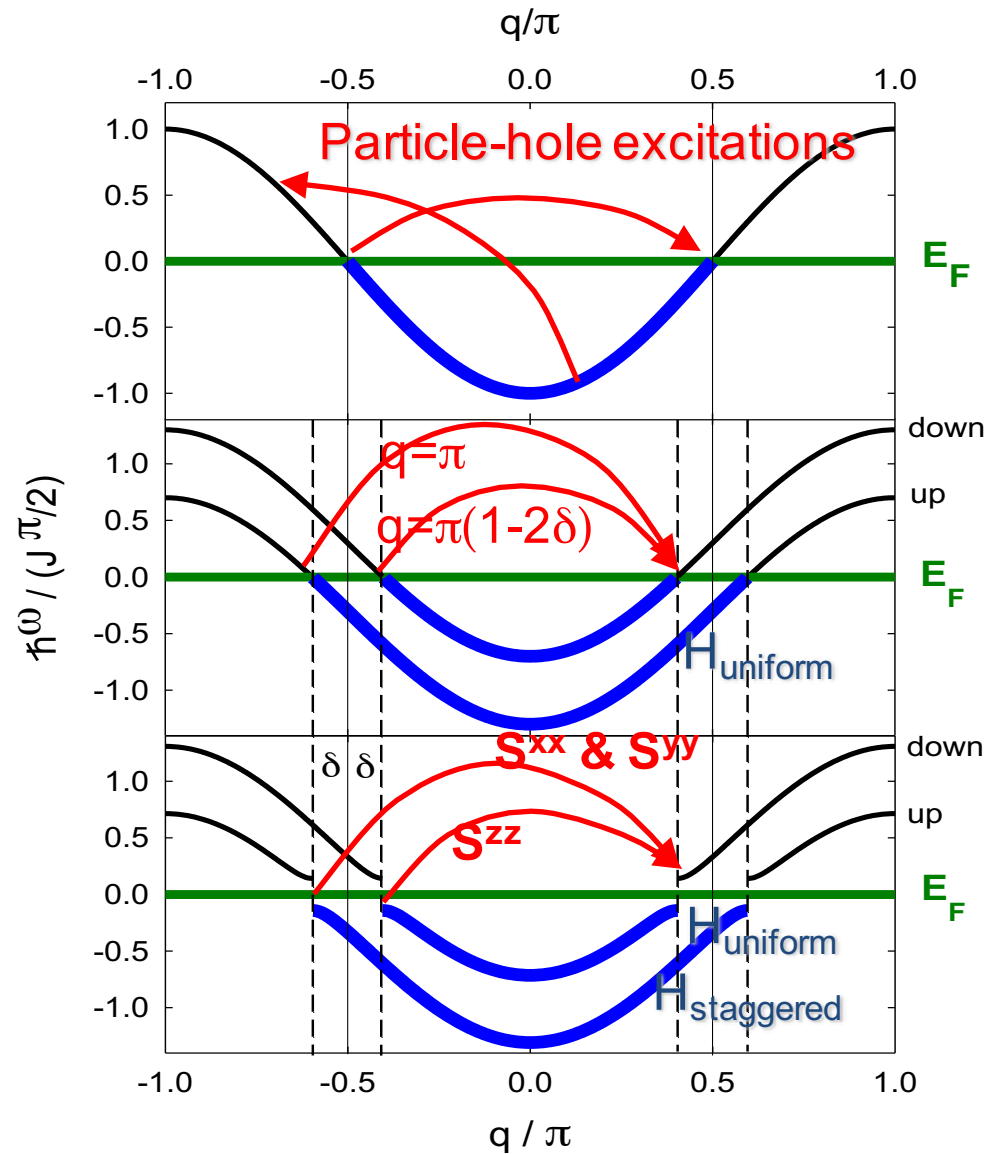
$H > 0T$ & staggered (AF) fields



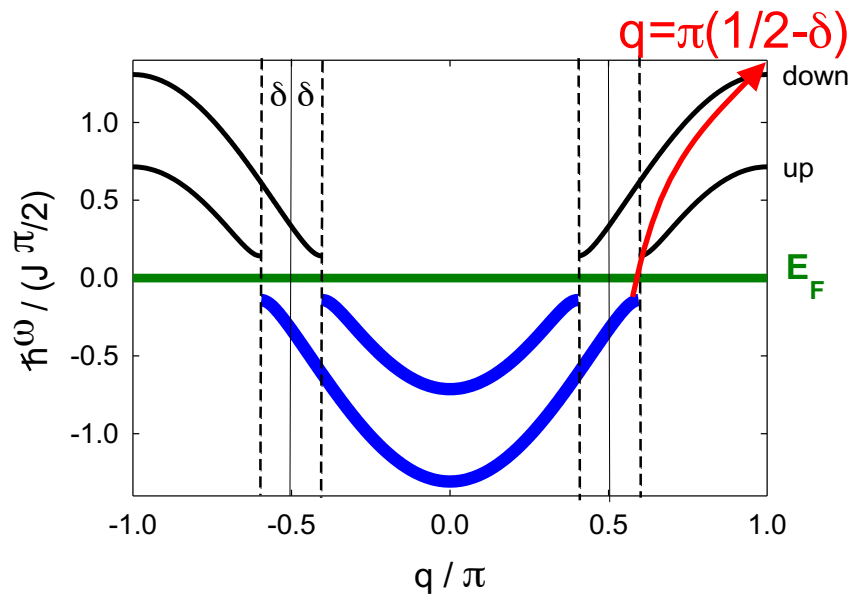
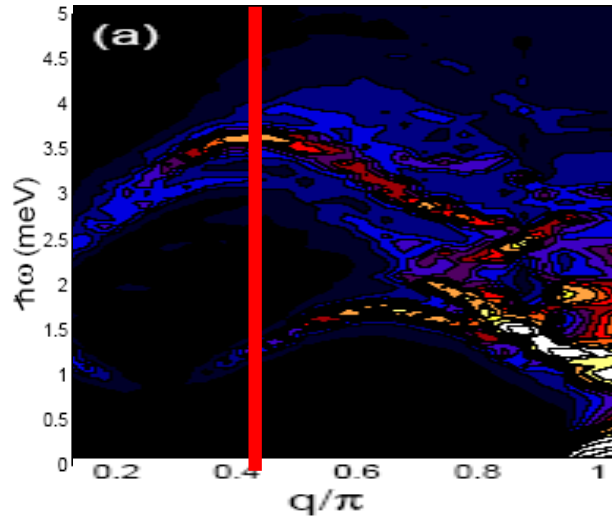
Bound spinons in the Spin fermion model



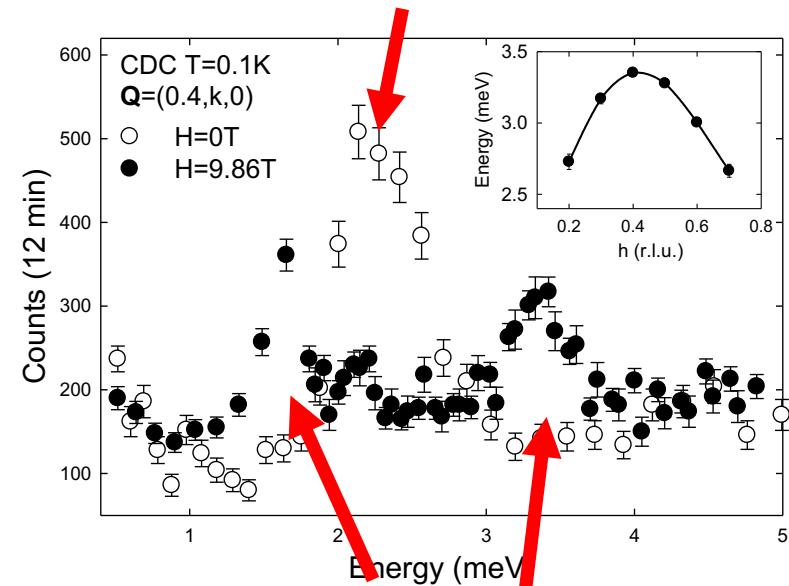
diverging density of states leads to increase of scattering at states close to Fermi surface



Small energy scales can have an effect at much higher energies



- $H=0T$: lower bound of two-spinon continuum



- $H \sim 10T$: lower-energy branch at $\sim 1.5\text{meV}$
- $H \sim 10T$: novel excitation at $\sim 3.4\text{meV}$