

# In search for BSM physics in the beta decay of $^{45}\text{Ca}$

Physics of fundamental Symmetries and  
Interactions 2019



THE UNIVERSITY OF  
TENNESSEE  
KNOXVILLE

Noah Birge

# The Standard Model (SM)

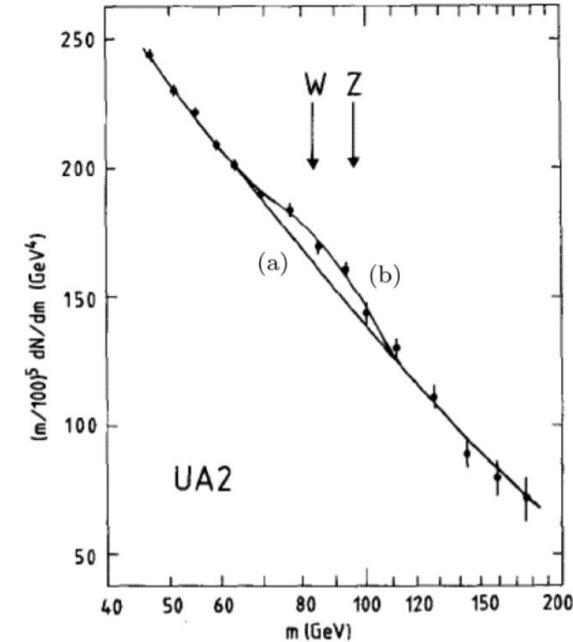
three generations of matter  
(fermions)

interactions / force carriers  
(bosons)

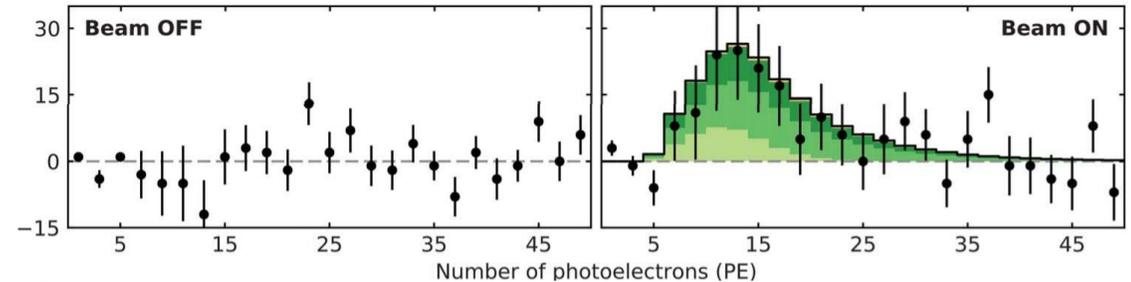
|                | I  | II   | III  |                                      |                                  |
|----------------|--|--|--|--------------------------------------|----------------------------------|
| mass           | $\approx 2.2 \text{ MeV}/c^2$                  | $\approx 1.28 \text{ GeV}/c^2$               | $\approx 173.1 \text{ GeV}/c^2$              | 0                                    | $\approx 124.97 \text{ GeV}/c^2$ |
| charge         | $\frac{2}{3}$                                  | $\frac{2}{3}$                                | $\frac{2}{3}$                                | 0                                    | 0                                |
| spin           | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                    | 0                                |
| <b>QUARKS</b>  | <b>u</b><br>up                                 | <b>c</b><br>charm                            | <b>t</b><br>top                              | <b>g</b><br>gluon                    | <b>H</b><br>higgs                |
|                | $\approx 4.7 \text{ MeV}/c^2$                  | $\approx 96 \text{ MeV}/c^2$                 | $\approx 4.18 \text{ GeV}/c^2$               | 0                                    |                                  |
|                | $-\frac{1}{3}$                                 | $-\frac{1}{3}$                               | $-\frac{1}{3}$                               | 0                                    |                                  |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                    |                                  |
|                | <b>d</b><br>down                               | <b>s</b><br>strange                          | <b>b</b><br>bottom                           | <b><math>\gamma</math></b><br>photon |                                  |
|                | $\approx 0.511 \text{ MeV}/c^2$                | $\approx 105.66 \text{ MeV}/c^2$             | $\approx 1.7768 \text{ GeV}/c^2$             | 0                                    |                                  |
|                | -1   | -1   | -1   | 0                                    |                                  |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                    |                                  |
| <b>LEPTONS</b> | <b>e</b><br>electron                           | <b><math>\mu</math></b><br>muon              | <b><math>\tau</math></b><br>tau              | <b>Z</b><br>Z boson                  |                                  |
|                | $< 2.2 \text{ eV}/c^2$                         | $< 0.17 \text{ MeV}/c^2$                     | $< 18.2 \text{ MeV}/c^2$                     | $\approx 80.39 \text{ GeV}/c^2$      |                                  |
|                | 0  | 0  | 0  | $\pm 1$                              |                                  |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                    |                                  |
|                | <b><math>\nu_e</math></b><br>electron neutrino | <b><math>\nu_\mu</math></b><br>muon neutrino | <b><math>\nu_\tau</math></b><br>tau neutrino | <b>W</b><br>W boson                  |                                  |

**GAUGE BOSONS**  
**VECTOR BOSONS**

**SCALAR BOSONS**



M. Banner et al. (UA2 Collaboration), Phys. Lett. B 122, 476 (1983)



COHERENT collaboration: Science, 357 (2017)

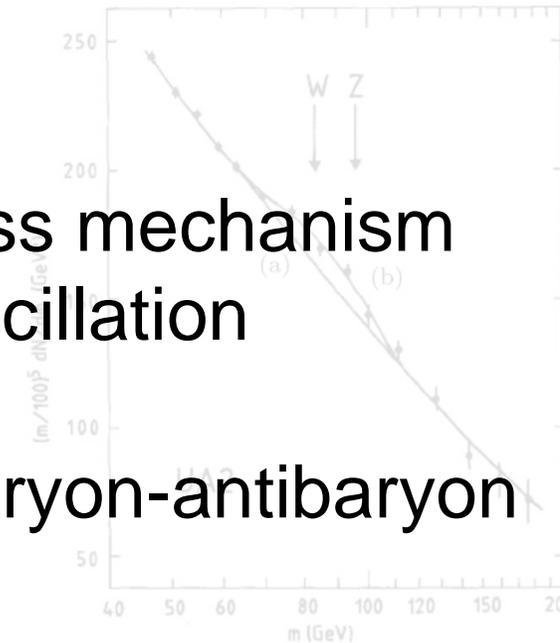
# The Standard Model (SM)

|                | three generations of matter (fermions)         |  |  | interactions / force carriers (bosons) |                     |                     |
|----------------|--|--|--|--|---------------------|---------------------|
|                | I  | II   | III  |  |                     |                     |
| mass           | $\approx 2.2 \text{ MeV}/c^2$                  | $\approx 1.28 \text{ GeV}/c^2$               | $\approx 173.1 \text{ GeV}/c^2$              | $\approx 124.97 \text{ GeV}/c^2$       |                     |                     |
| charge         | $\frac{2}{3}$                                  | $\frac{2}{3}$                                | $\frac{2}{3}$                                | 0                                      | 0                   | 0                   |
| spin           | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 0                                      | 1                   | 1                   |
| <b>QUARKS</b>  | <b>u</b><br>up                                 | <b>c</b><br>charm                            | <b>t</b><br>top                              | <b>g</b><br>gluon                      | <b>W</b><br>W boson | <b>Z</b><br>Z boson |
|                | $\approx 4.7 \text{ MeV}/c^2$                  | $\approx 96 \text{ MeV}/c^2$                 | $\approx 4.18 \text{ GeV}/c^2$               | $\approx 91.19 \text{ GeV}/c^2$        |                     |                     |
|                | $-\frac{1}{3}$                                 | $-\frac{1}{3}$                               | $-\frac{1}{3}$                               | 0                                      | 0                   | 0                   |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                      | 1                   | 1                   |
|                | <b>d</b><br>down                               | <b>s</b><br>strange                          | <b>b</b><br>bottom                           | <b>Y</b><br>photon                     |                     |                     |
| <b>LEPTONS</b> | $\approx 0.511 \text{ MeV}/c^2$                | $\approx 105.66 \text{ MeV}/c^2$             | $\approx 1.7768 \text{ GeV}/c^2$             | $\approx 80.39 \text{ GeV}/c^2$        |                     |                     |
|                | -1   | -1   | -1   | 0                                      | 0                   | 0                   |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                      | 1                   | 1                   |
|                | <b>e</b><br>electron                           | <b><math>\mu</math></b><br>muon              | <b><math>\tau</math></b><br>tau              | <b>Z</b><br>Z boson                    |                     |                     |
|                | $< 2.2 \text{ eV}/c^2$                         | $< 0.17 \text{ MeV}/c^2$                     | $< 18.2 \text{ MeV}/c^2$                     |  |                     |                     |
|                | 0  | 0  | 0  | $\pm 1$                                |                     |                     |
|                | $\frac{1}{2}$                                  | $\frac{1}{2}$                                | $\frac{1}{2}$                                | 1                                      |                     |                     |
|                | <b><math>\nu_e</math></b><br>electron neutrino | <b><math>\nu_\mu</math></b><br>muon neutrino | <b><math>\nu_\tau</math></b><br>tau neutrino | <b>W</b><br>W boson                    |                     |                     |

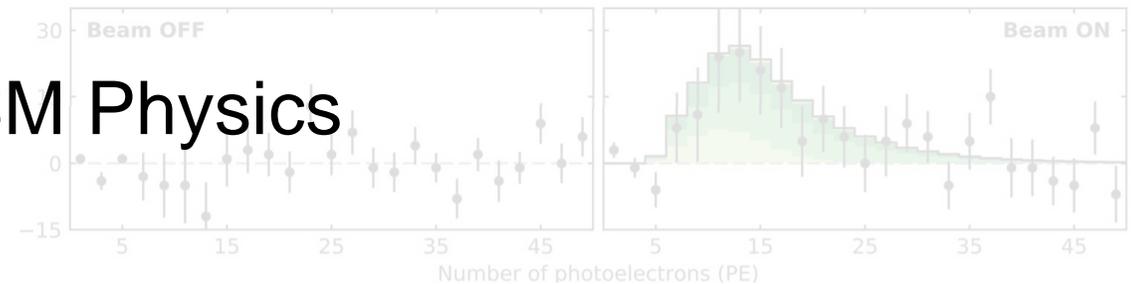
Missing:

- Gravity
- Neutrino mass mechanism and flavor oscillation
- Dark matter
- Observed baryon-antibaryon asymmetry

➔ Look for BSM Physics



M. Banner et al. (UA2 Collaboration), Phys. Lett. B 122, 476 (1983)



COHERENT collaboration: Science, 357 (2017)

# $^{45}\text{Ca}$ beta decay



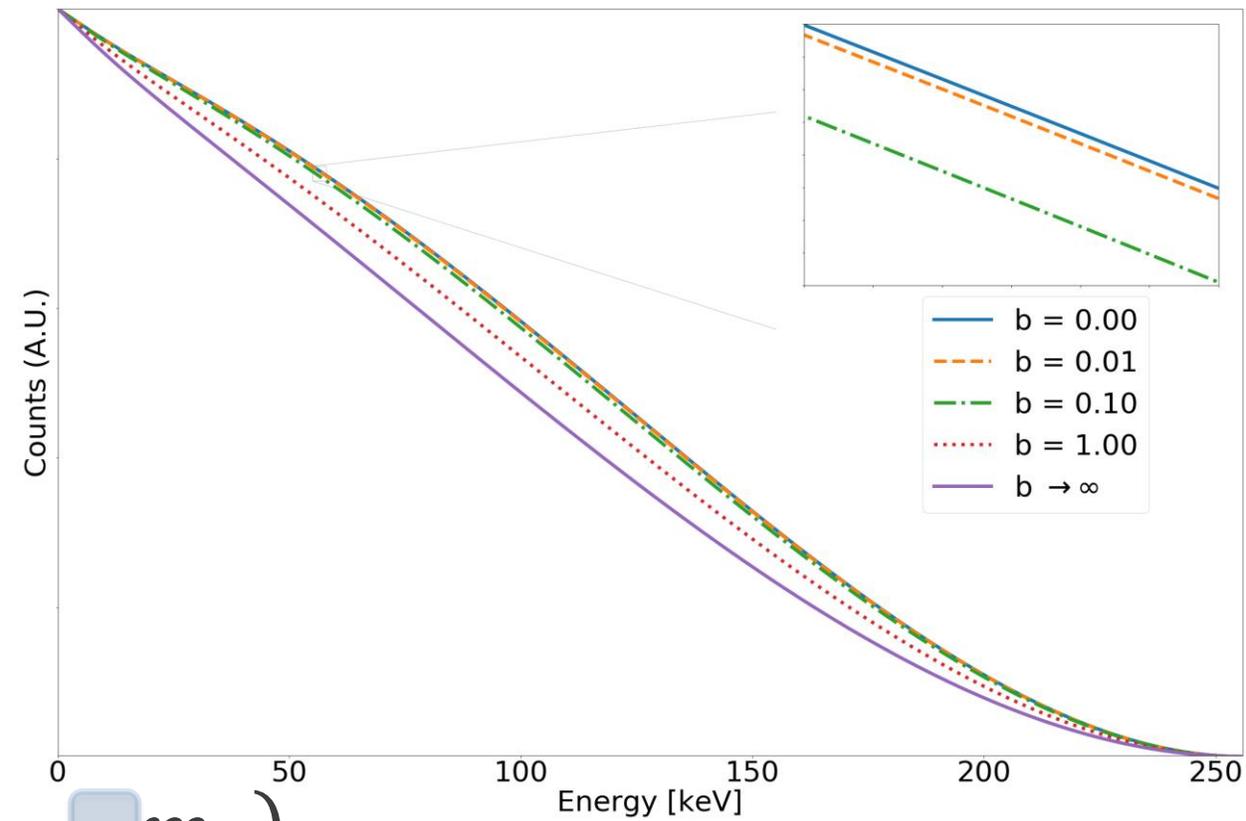
$$Q = 255 \text{ keV}$$



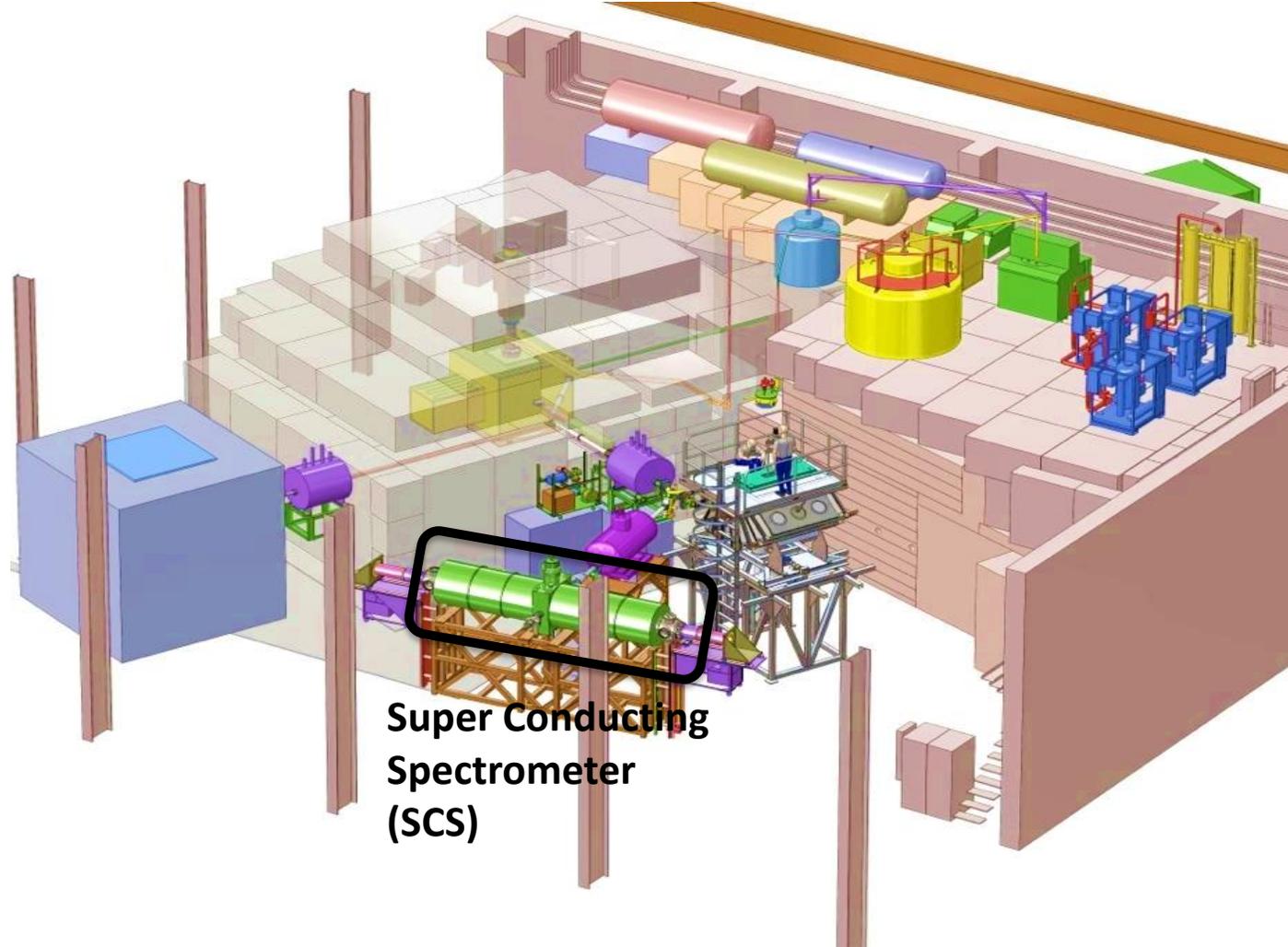
## Decay Rate:

$$\frac{d\omega}{dE_e}(E_e) \propto p_e E_e (E^0 - E_e)^2 \left\{ 1 + b \frac{m_e}{E_e} \right\}$$

$$b \propto \text{Re} \left( \frac{C_S + C'_S}{C_V + C'_V} + \frac{g_a}{g_v} \frac{C_T + C'_T}{C_A + C'_A} \right)$$

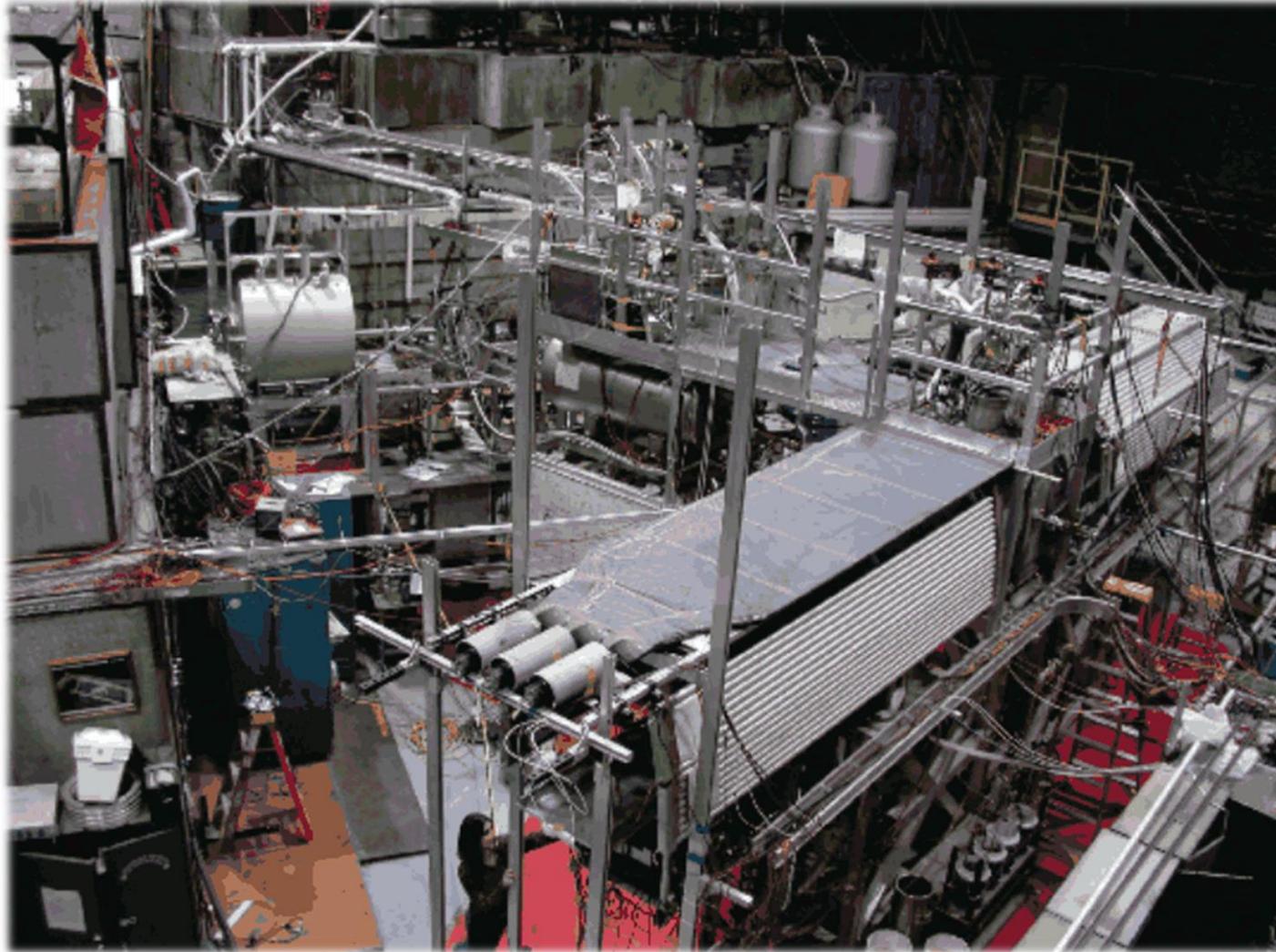


# The $^{45}\text{Ca}$ Experiment at LANSCE



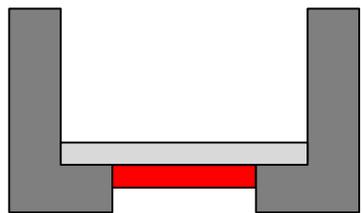
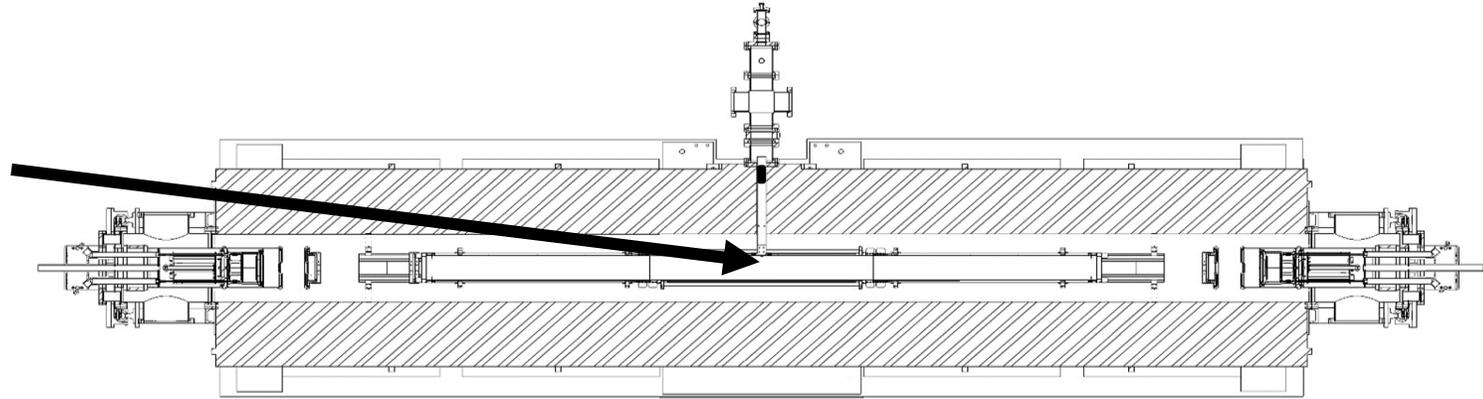
Super Conducting  
Spectrometer  
(SCS)

# The $^{45}\text{Ca}$ Experiment at LANSCE

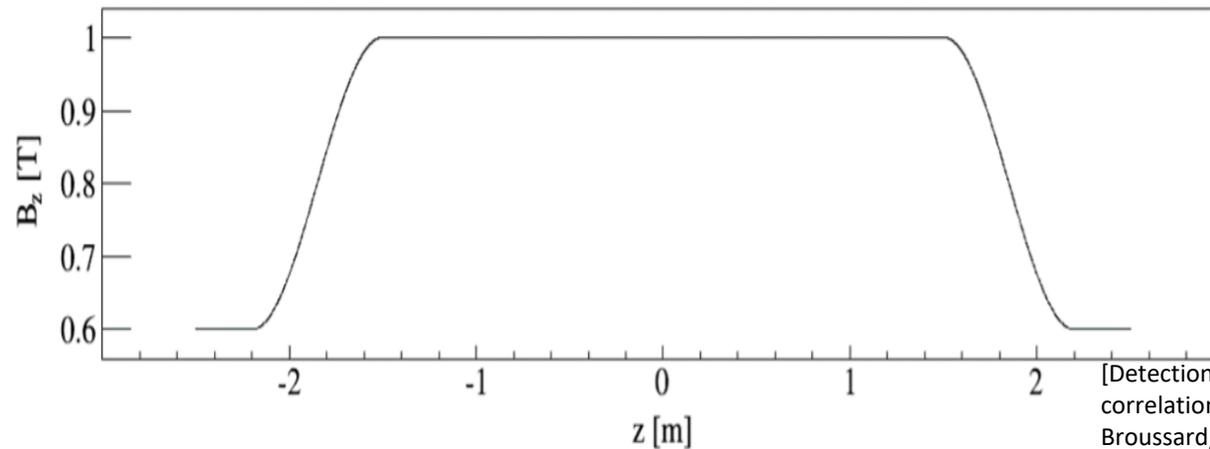


# The $^{45}\text{Ca}$ Experiment at LANL

- Prepared by IKS of KU Leuven
- $\sim 1$  kBq
- $\sim 200$  nm foil thickness



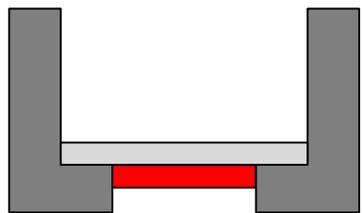
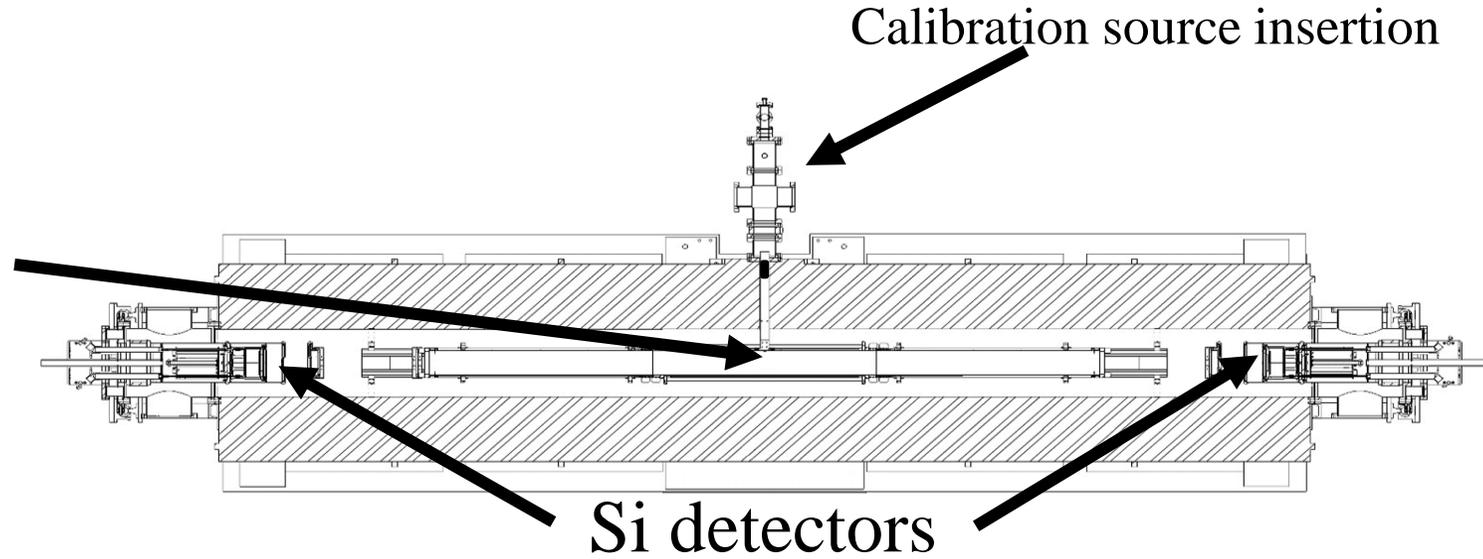
- Aluminum Frame
- Aluminum Backing
- Source



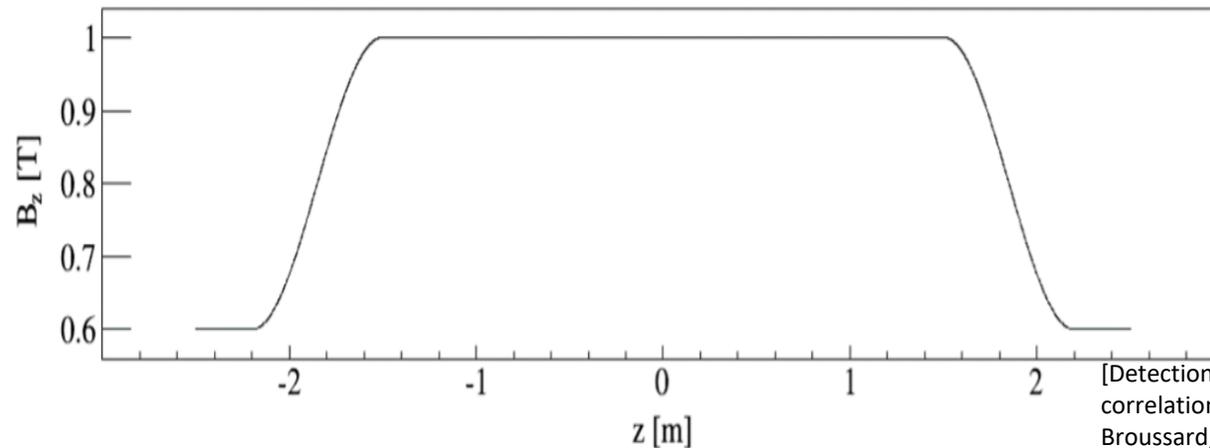
[Detection systems for neutron  $\beta$  decay correlations in the UCNB and Nab experiments, L.J. Broussard, NIM A, Vol 849, pp. 83-89]

# The $^{45}\text{Ca}$ Experiment at LANL

- Prepared by IKS of KU Leuven
- $\sim 1$  kBq
- $\sim 200$  nm foil thickness



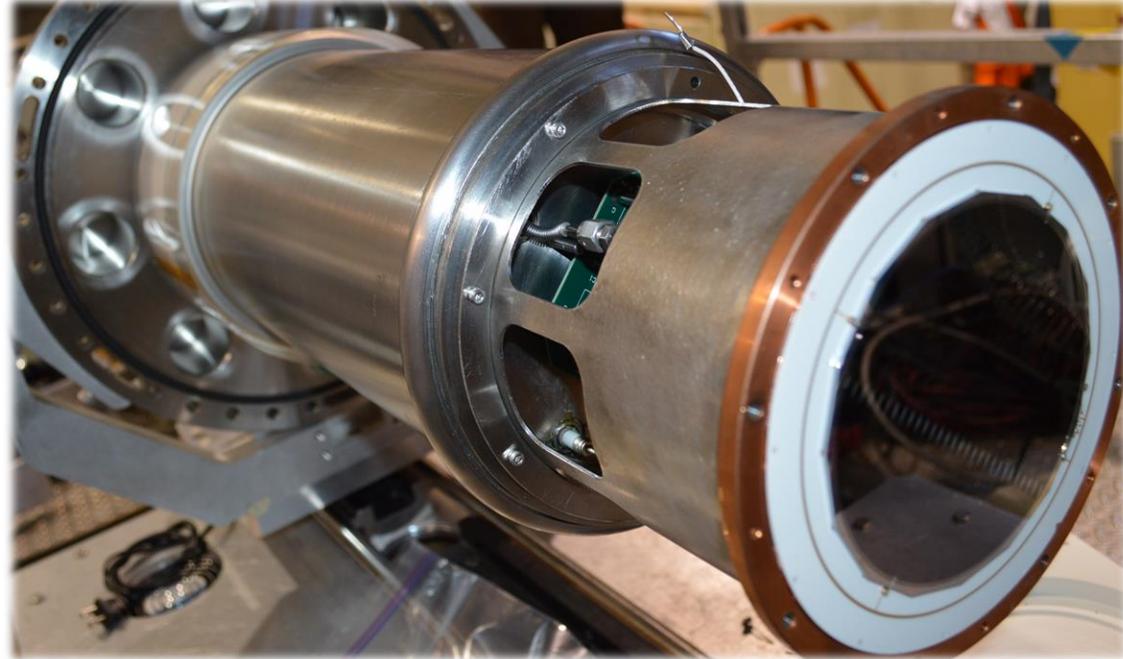
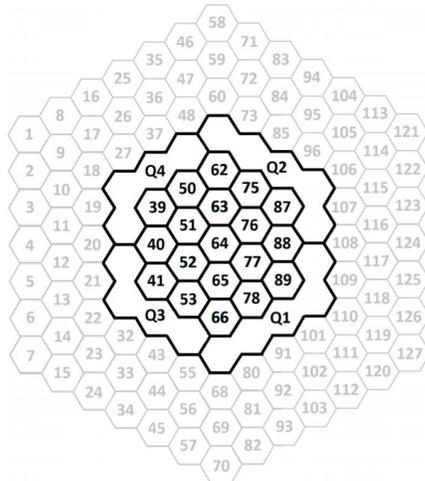
- Aluminum Frame
- Aluminum Backing
- Source



[Detection systems for neutron  $\beta$  decay correlations in the UCNB and Nab experiments, L.J. Broussard, NIM A, Vol 849, pp. 83-89]

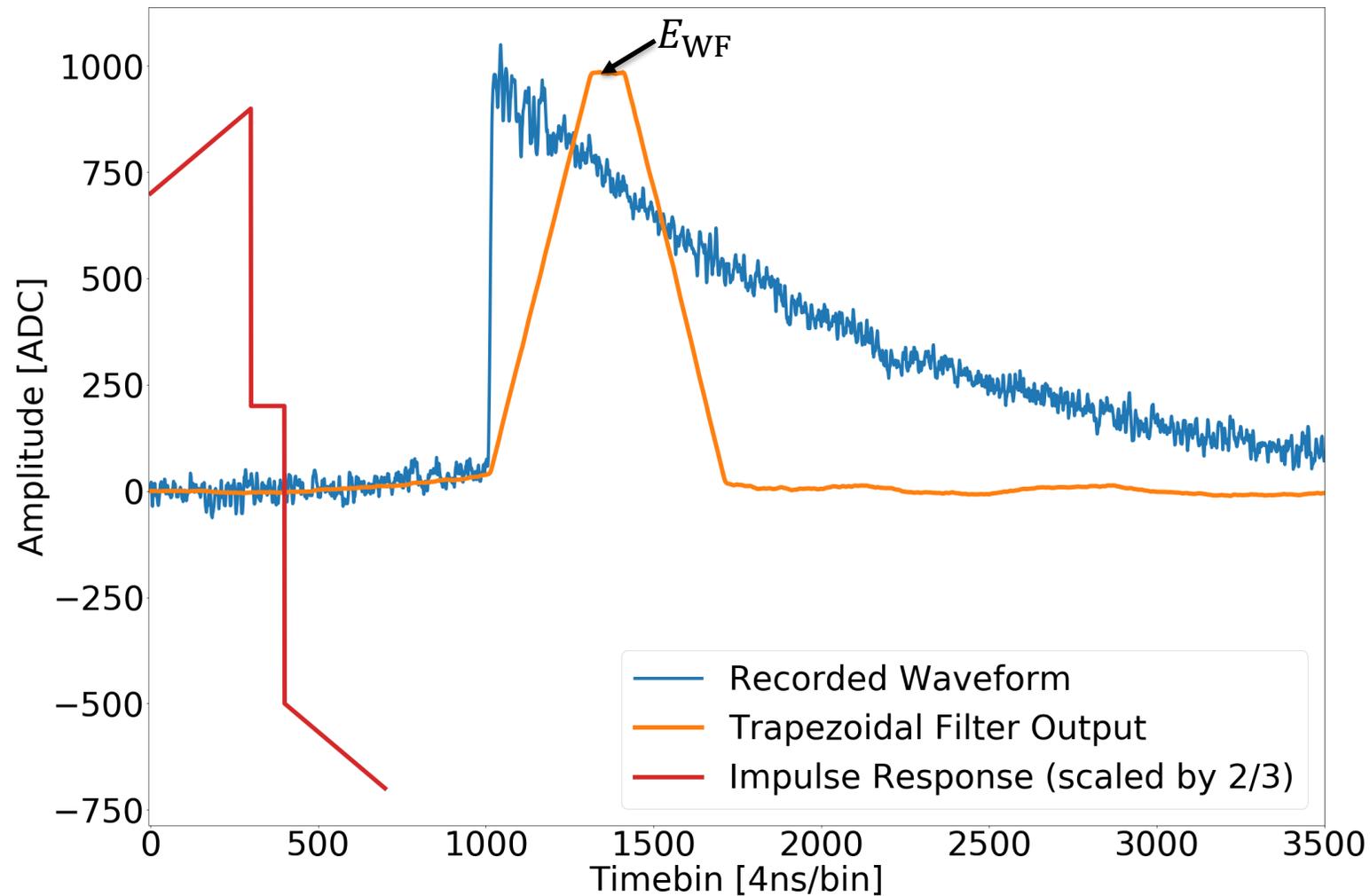
# $^{45}\text{Ca}$ Detectors

- Single crystal Si
- Large area  $\sim 11$  cm
- 100nm dead layer
- Thick  $\sim 1.5$ mm
- Pixelated



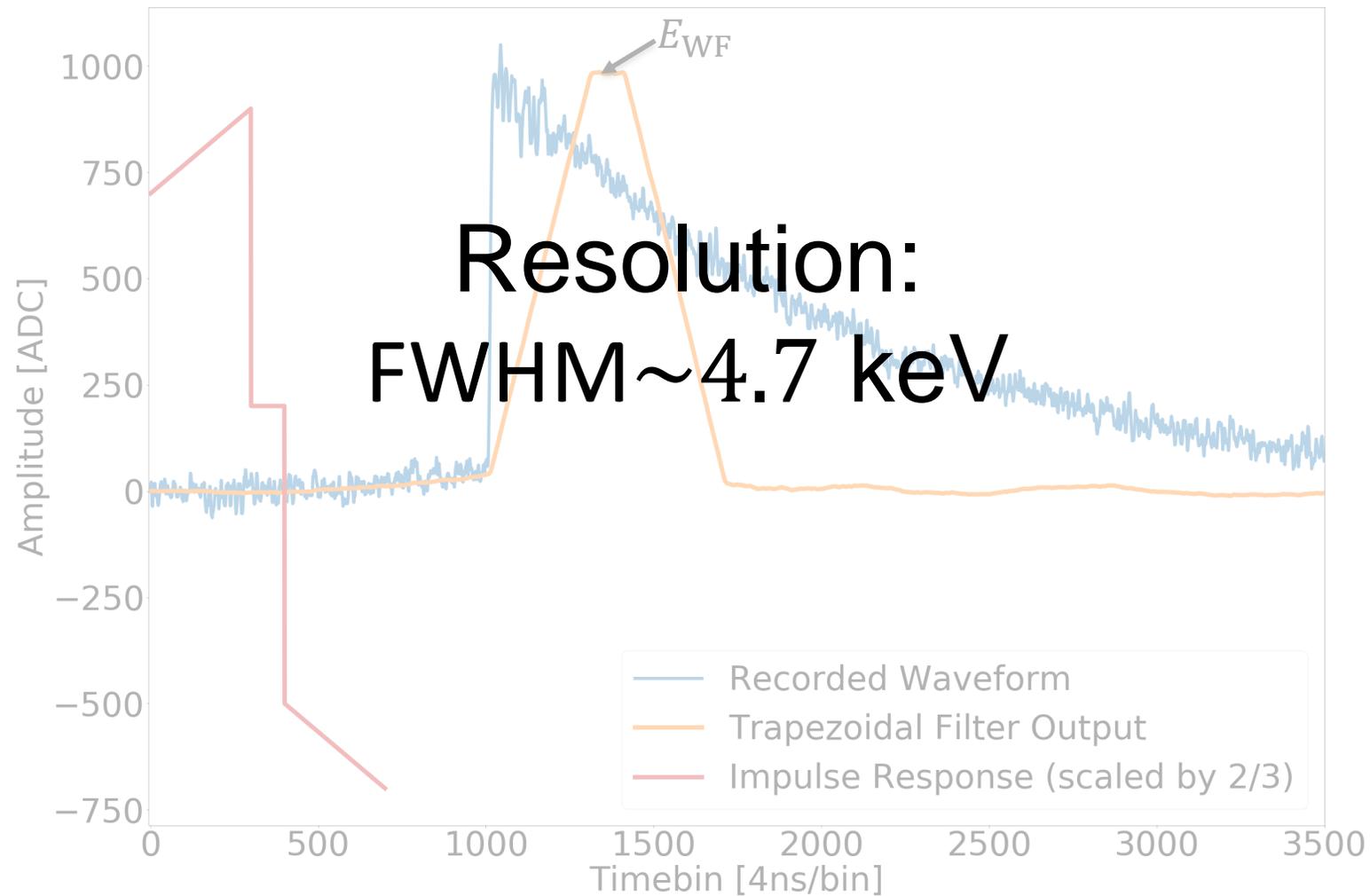
[Detection systems for neutron  $\beta$  decay correlations in the UCNB and Nab experiments, L.J. Broussard, NIM A, Vol 849, pp. 83-89]

# Energy Extraction: Long Trapezoidal Filter



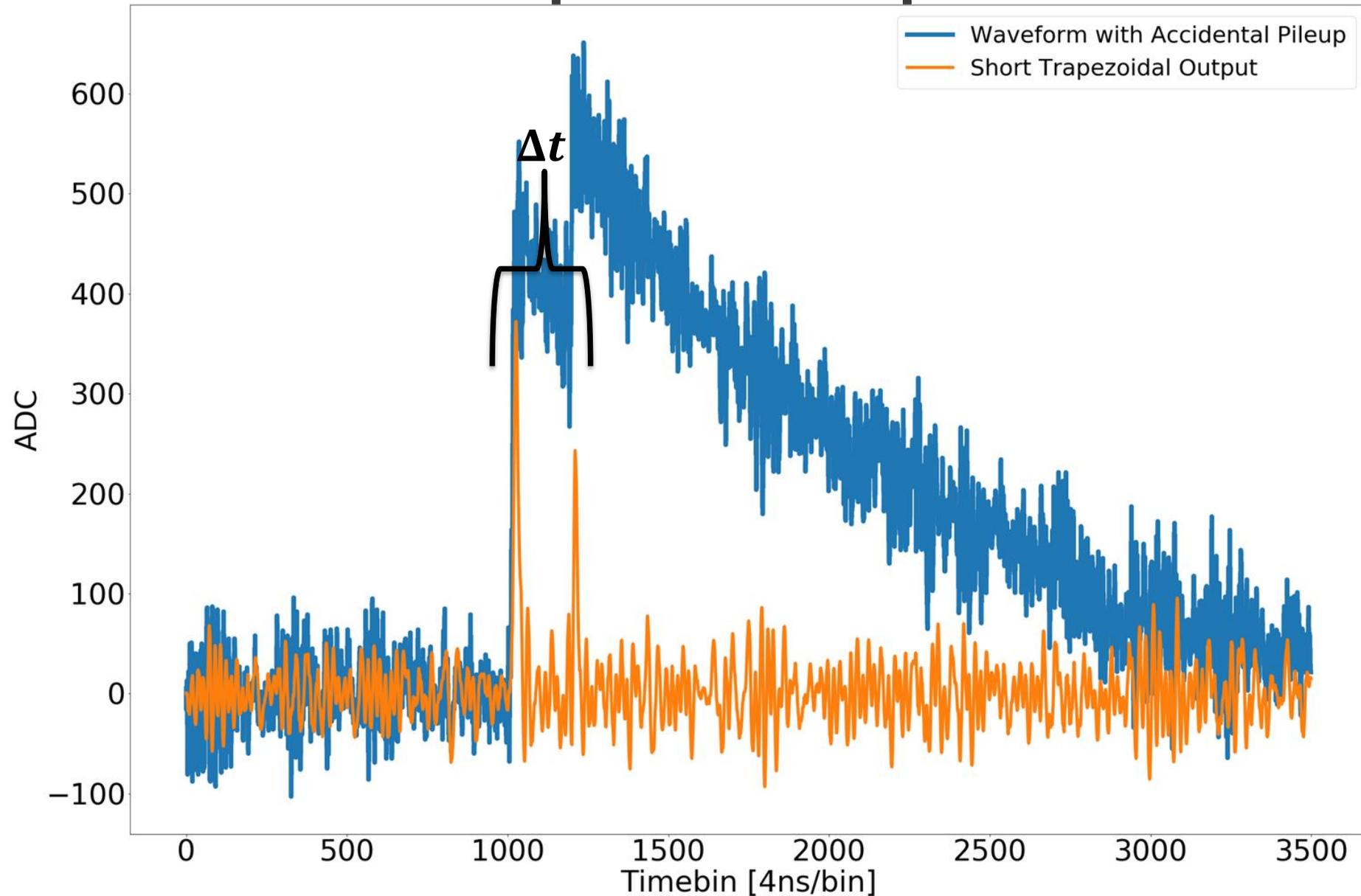
V. Jordanov, et al., *Digital synthesis of pulse shapes in real time for high resolution radiation spectroscopy*, NIMA, Vol 345

# Energy Extraction: Long Trapezoidal Filter

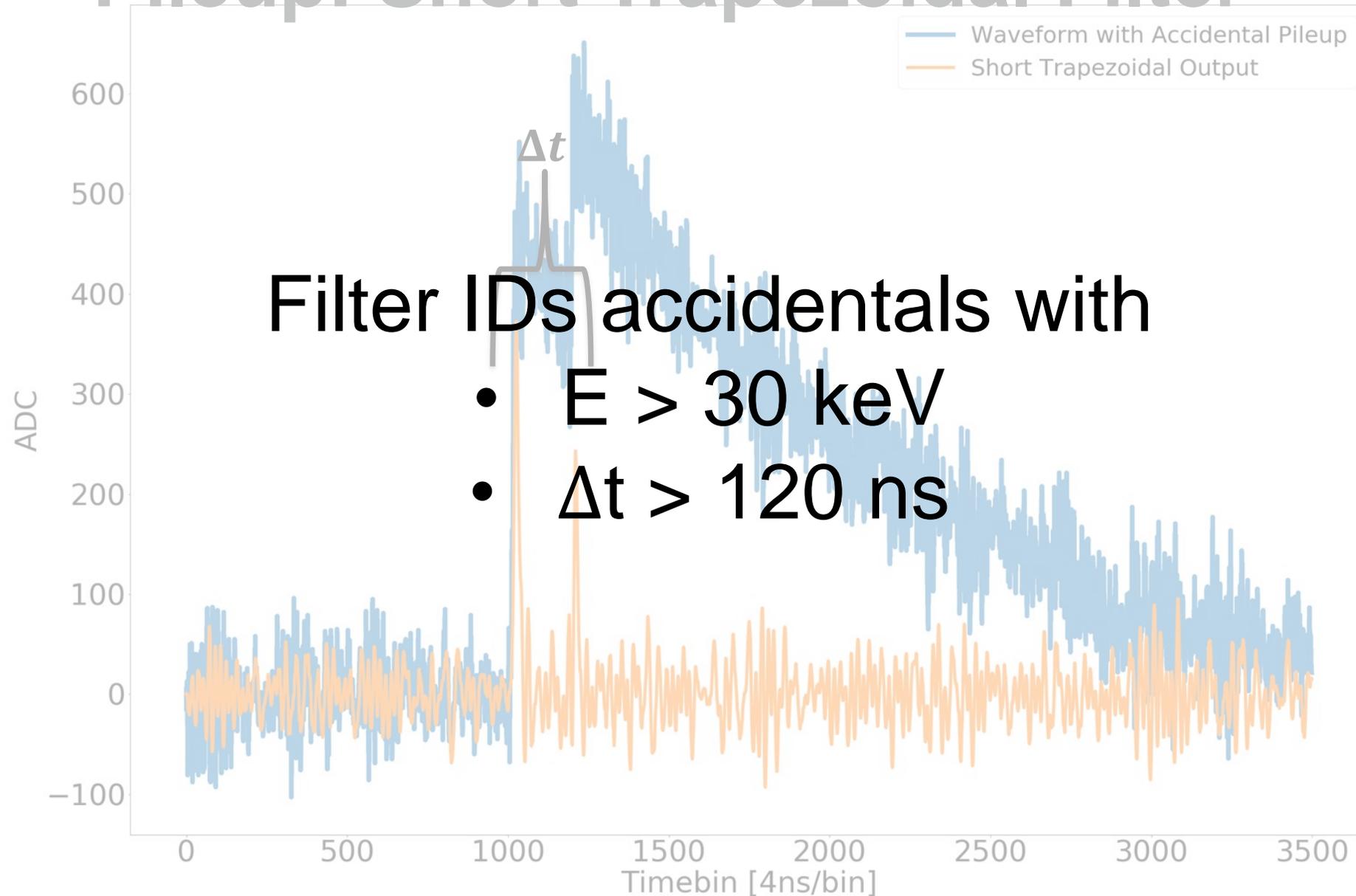


V. Jordanov, et al., *Digital synthesis of pulse shapes in real time for high resolution radiation spectroscopy*, NIMA, Vol 345

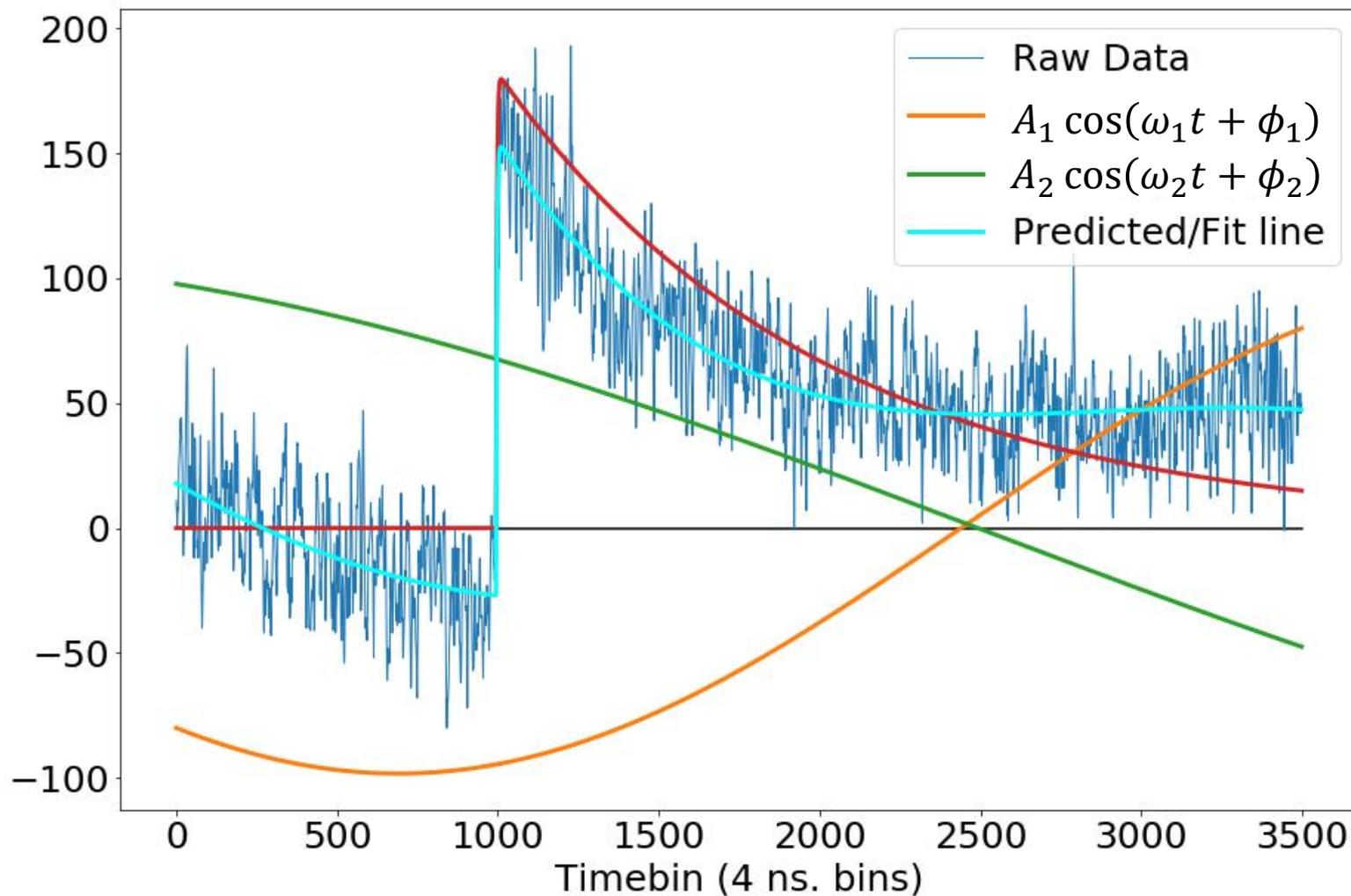
# Accidental Pileup: Short Trapezoidal Filter



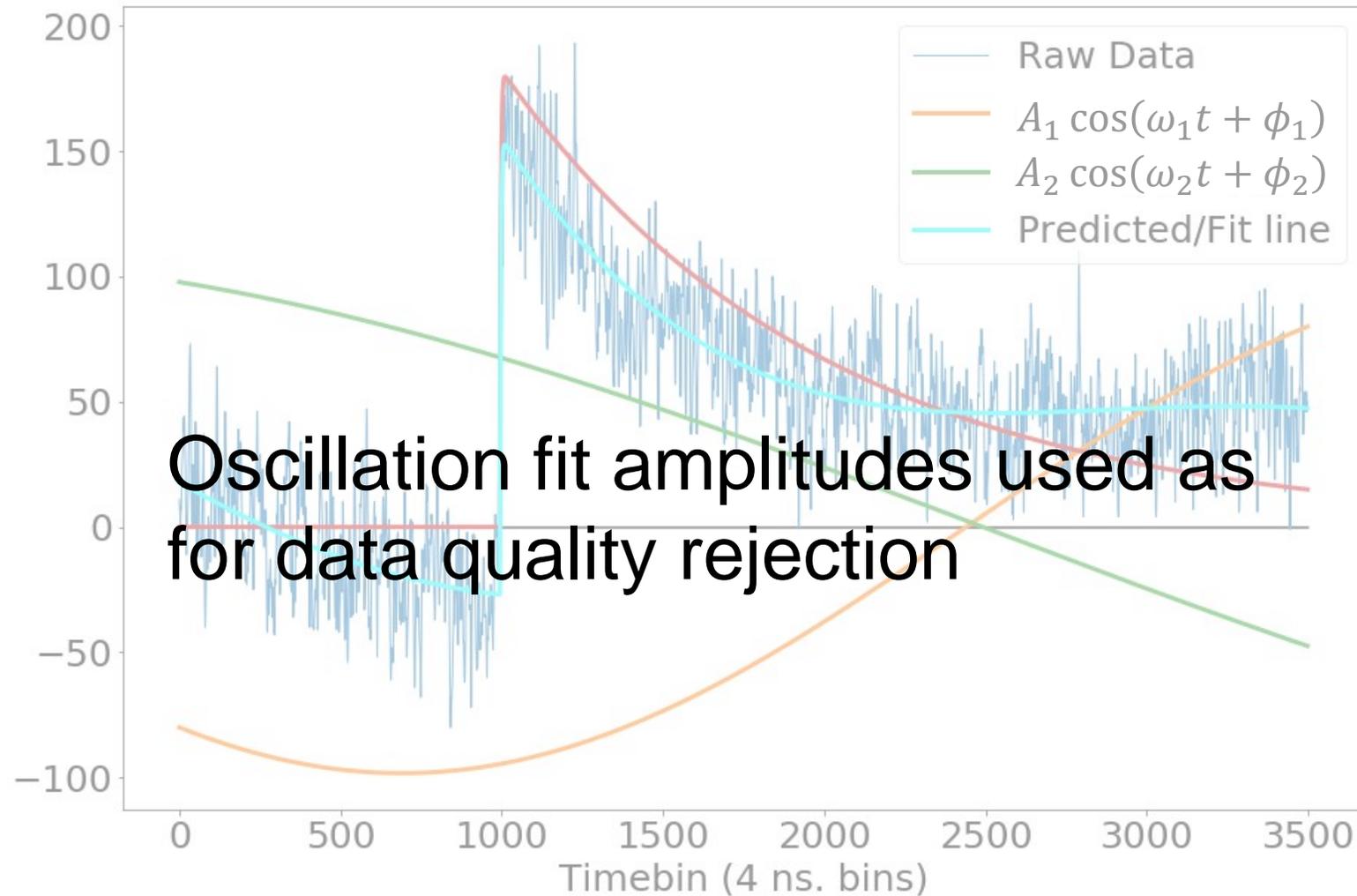
# Pileup: Short Trapezoidal Filter



# Baseline Oscillation: Linear Least Squares Fit



# Baseline Oscillation: Linear Least Squares Fit

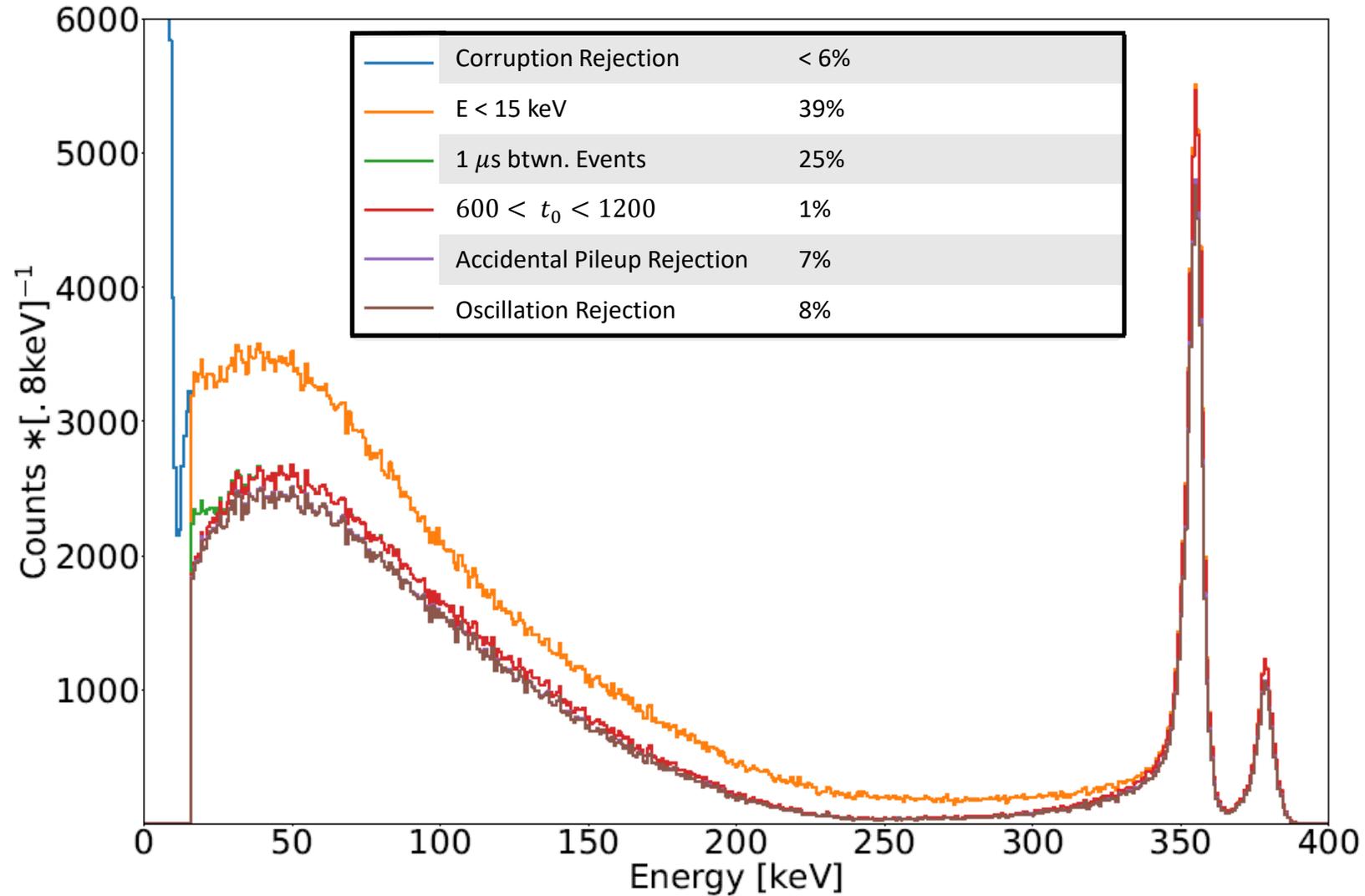


# Towards a 'b' extraction

- Bin energies
- Build Spectra
  - Single Pixel Spectra
- Calibration Source Spectra+ MC Simulation
  - Calibration & Linearity
  - Electronic Response Function (ERF)
- Build Calibrated  $^{45}\text{Ca}$  spectra
  - Extract 'b'
  - Quantify dominant uncertainties

# Single-Pixel Spectra

- Single pixel spectra
  - Events isolated to a single pixel and well separated in time ( $1 \mu\text{s}$ )

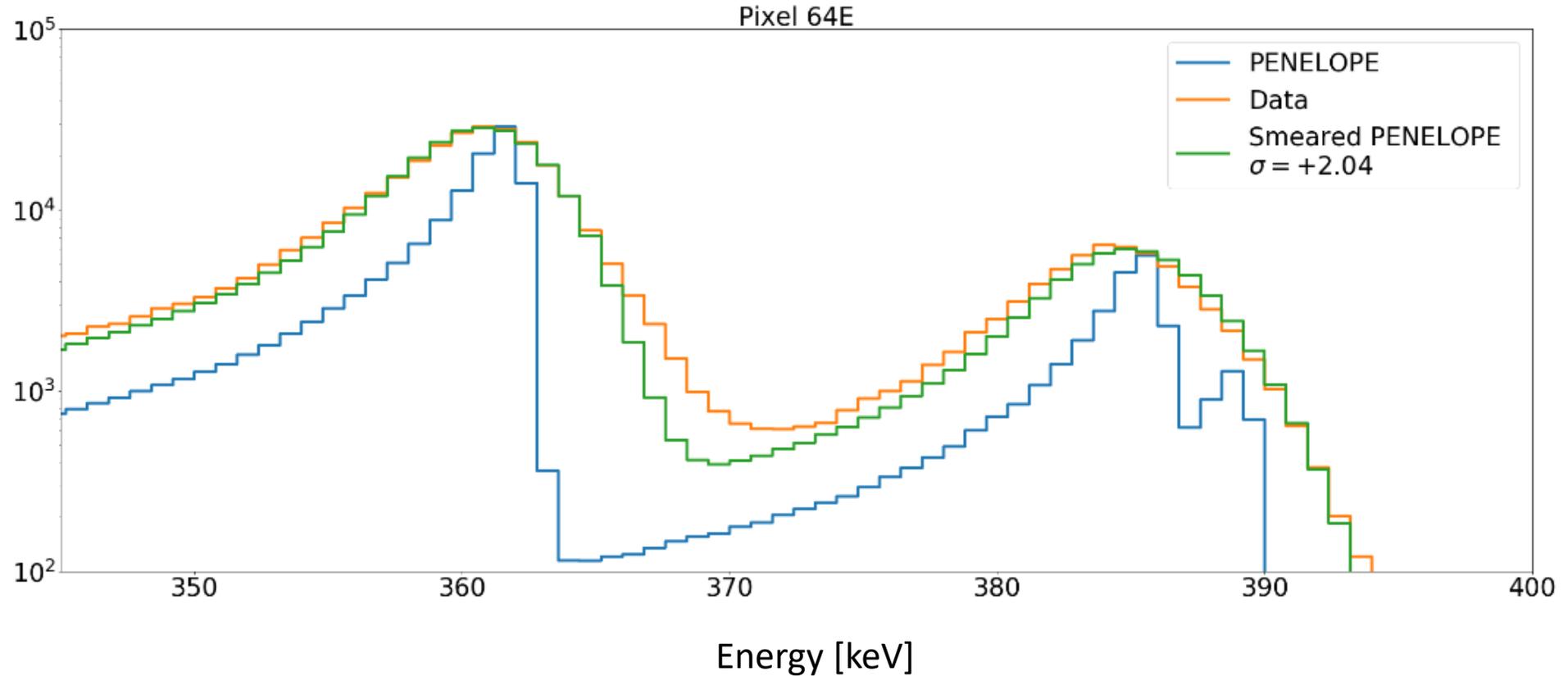


# Monte Carlo Simulation

- Monte Carlo (MC) simulations (PENELOPE)
  - Developed by collaborator B. Zeck\*
  - Includes foil losses, dead layer losses, bremsstrahlung losses & accounts for physical and field geometries.
  
- Charge collection and electronic response function (ERF) modeled as gaussian smearing of PENELOPE energies

\*Angular Correlation and Spectroscopy Measurements of the  $\beta$ -Decay of Neutrons and  $^{45}\text{Ca}$  Nuclei, NCSU Thesis  
<http://www.lib.ncsu.edu/resolver/1840.20/36693>

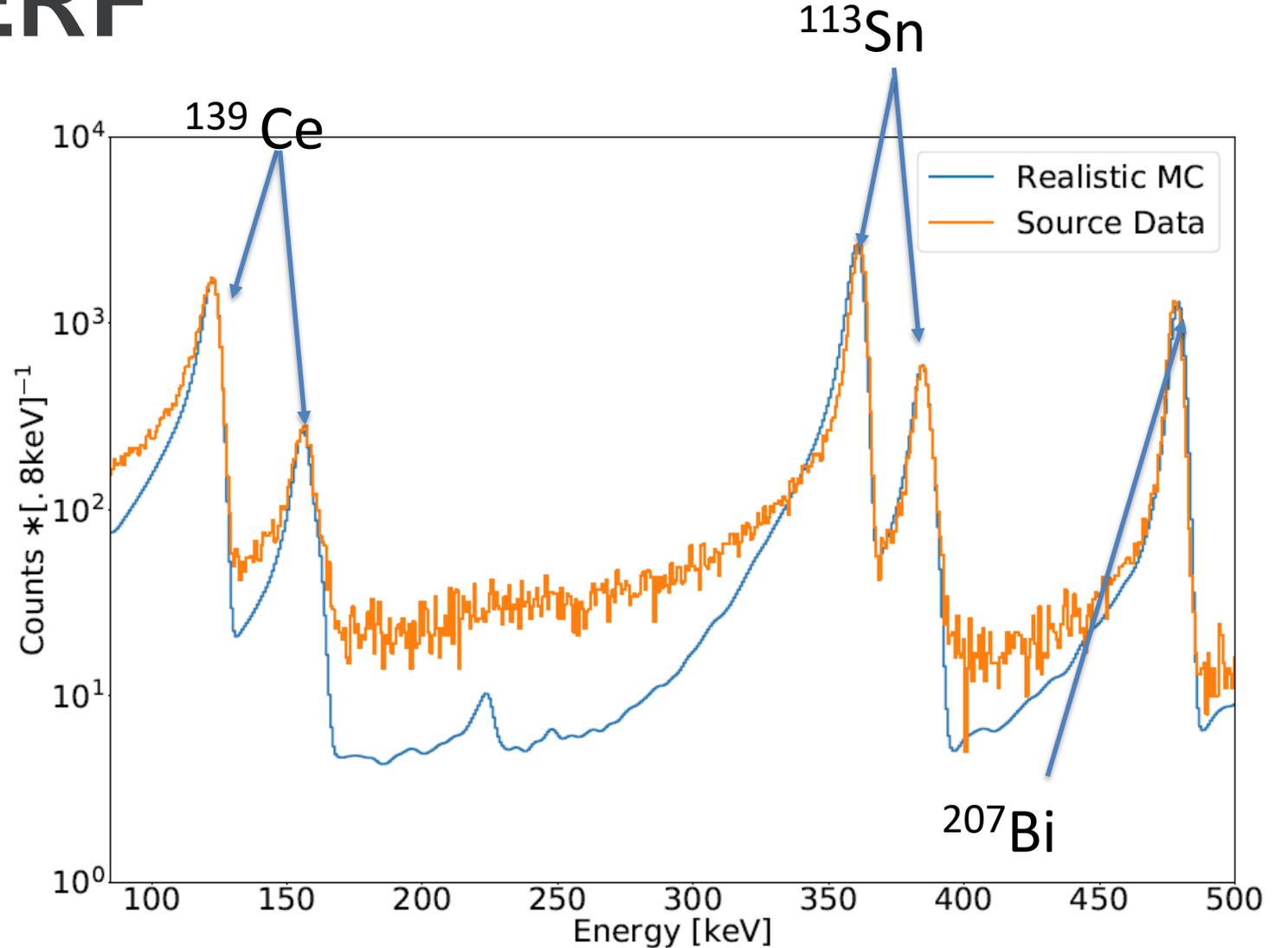
# Producing Realistic MC Spectra



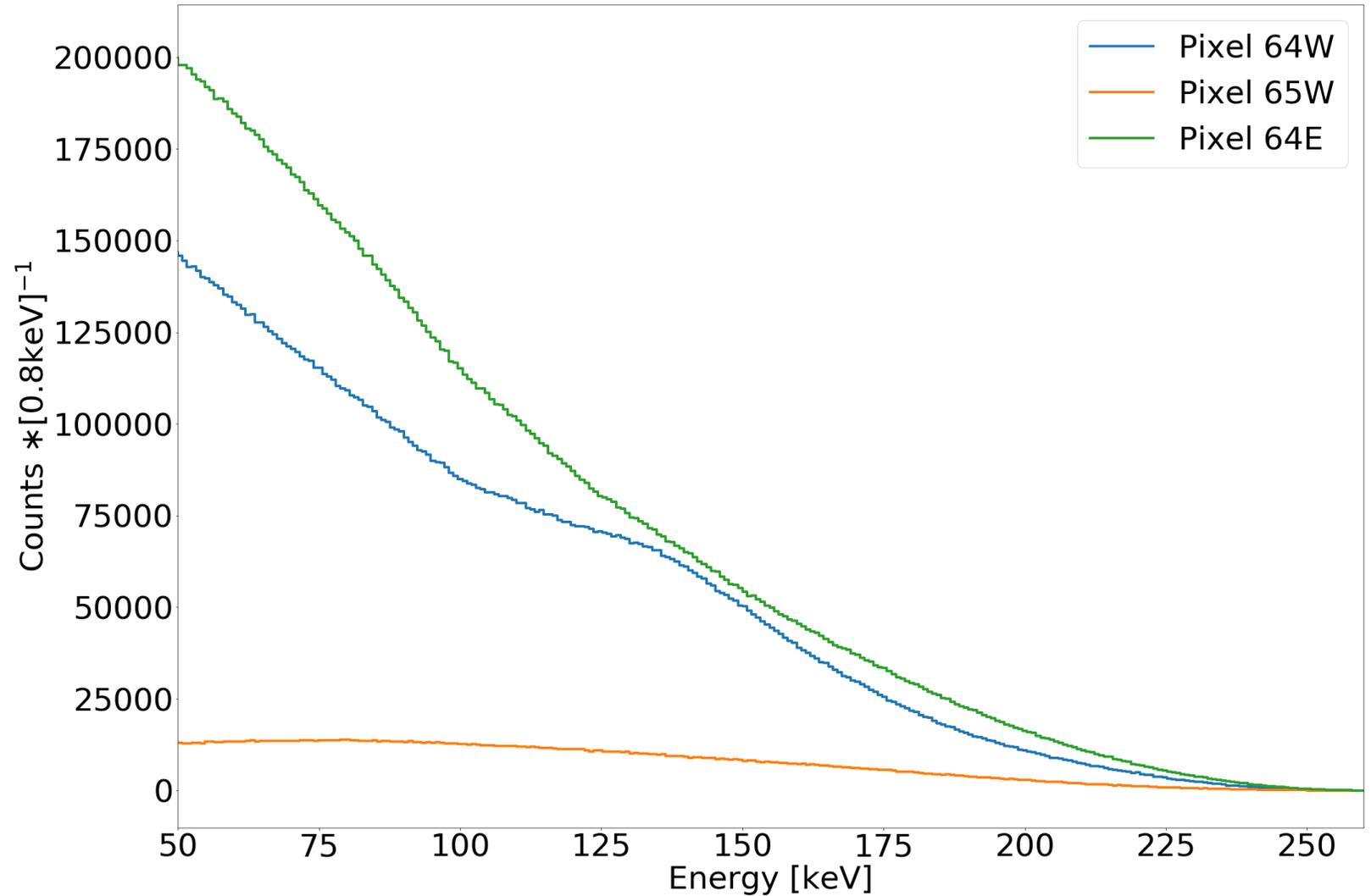
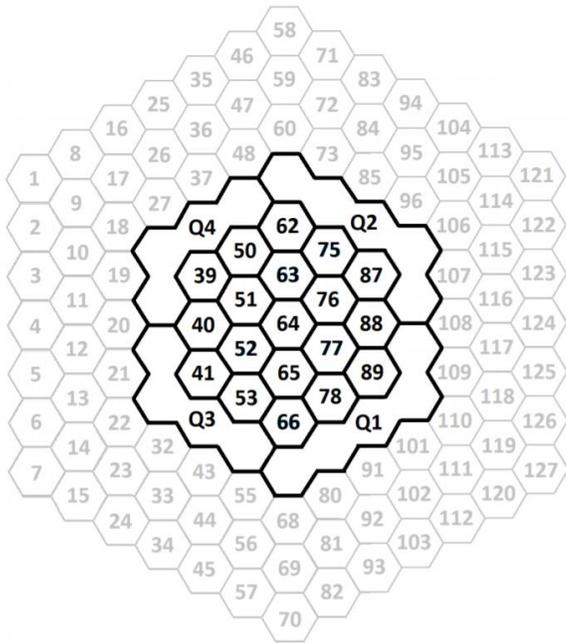
# Calibration & ERF

- Calibration Source Data:

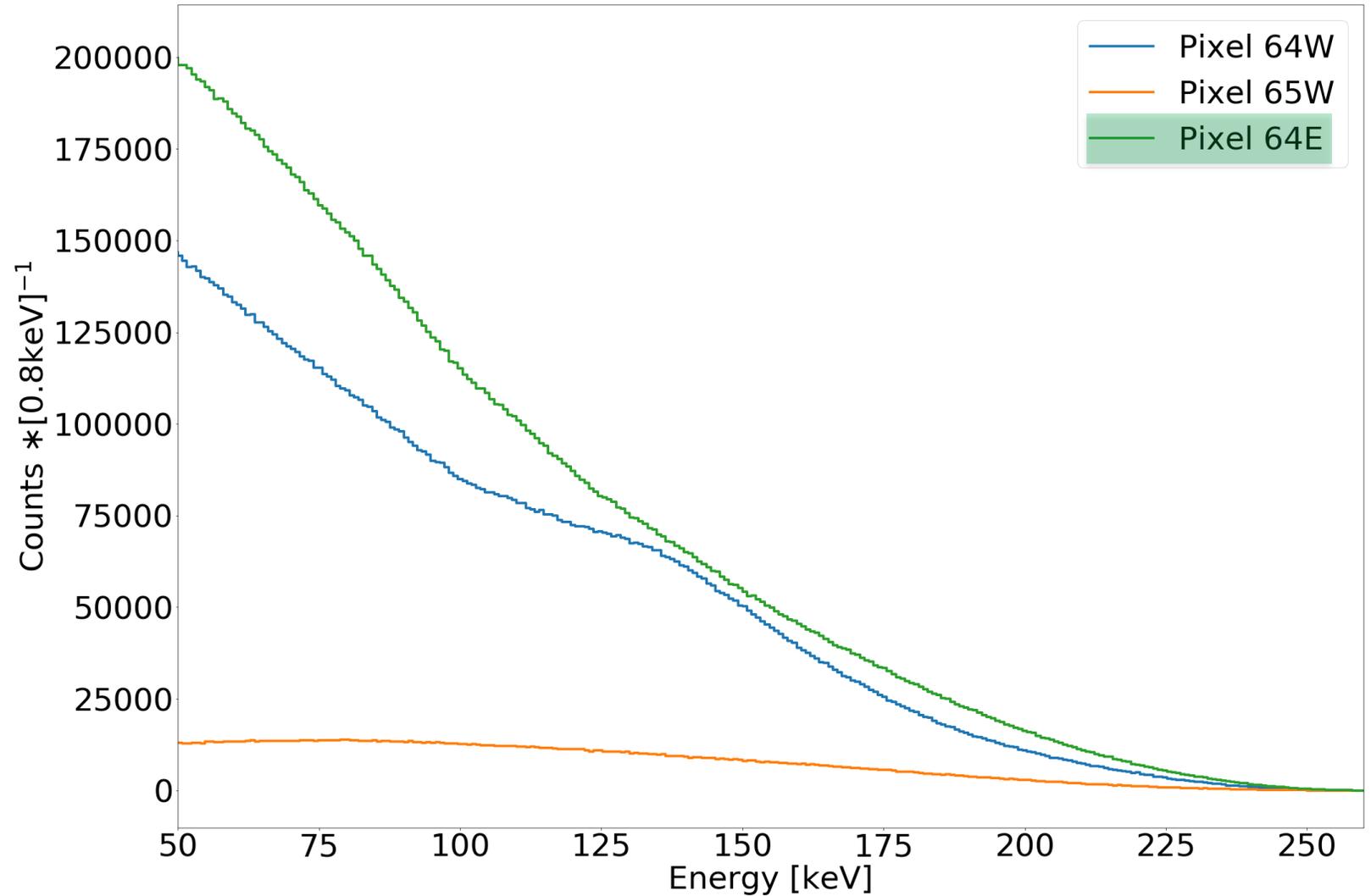
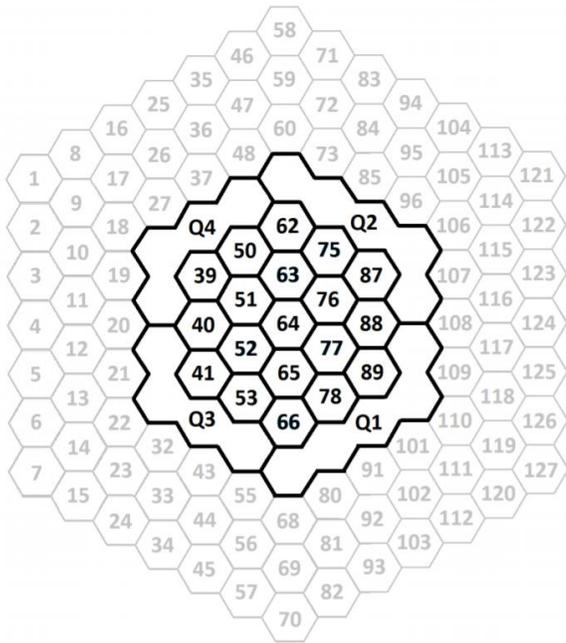
- $^{113}\text{Sn}$ ,  $^{207}\text{Bi}$ , &  $^{139}\text{Ce}$



# Single-pixel $^{45}\text{Ca}$ spectra



# Single-pixel $^{45}\text{Ca}$ spectra



# Extracting the Fierz Term

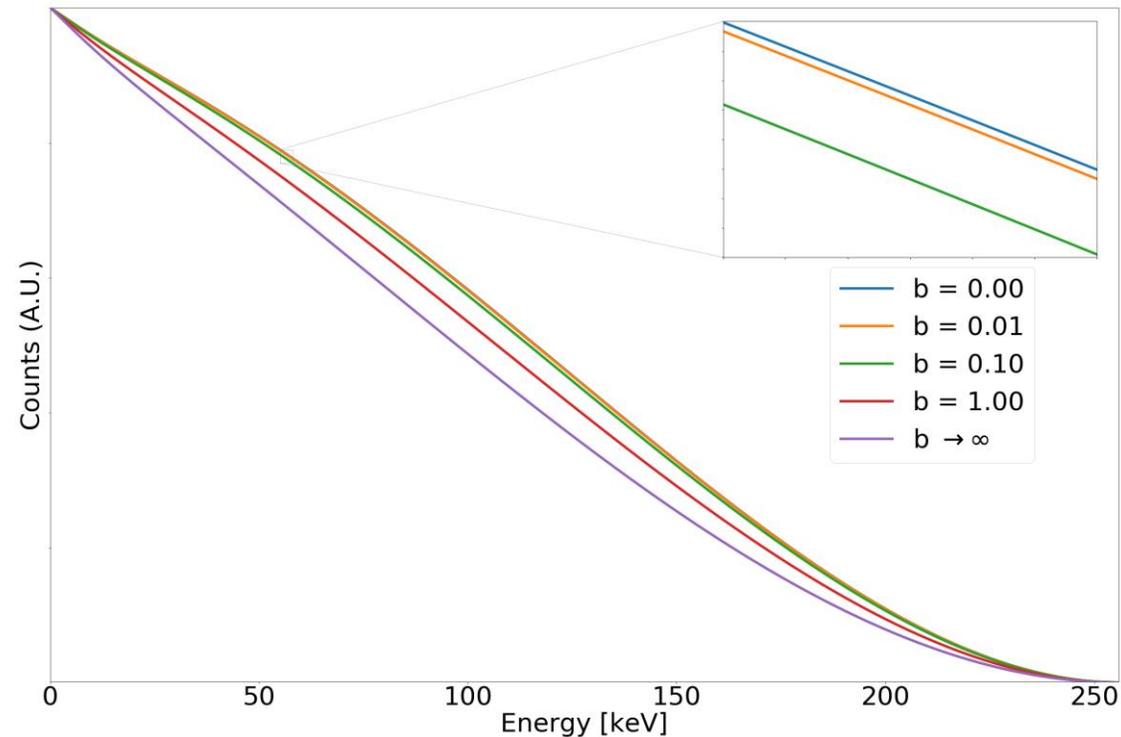
$$w(b) = PS \left\{ 1 + b \frac{m_e}{E_e} \right\}$$

$$w(0) = PS ; w(1) = PS \left\{ 1 + \frac{m_e}{E_e} \right\}$$

$$b[w(1) - w(0)] = PS \cdot b \frac{m_e}{E_e}$$

$$\rightarrow w(b) = w(0) + b[w(1) - w(0)]$$

$$PS := p_e E_e (E_0 - E_e)^2$$



# Extracting the Fierz Term

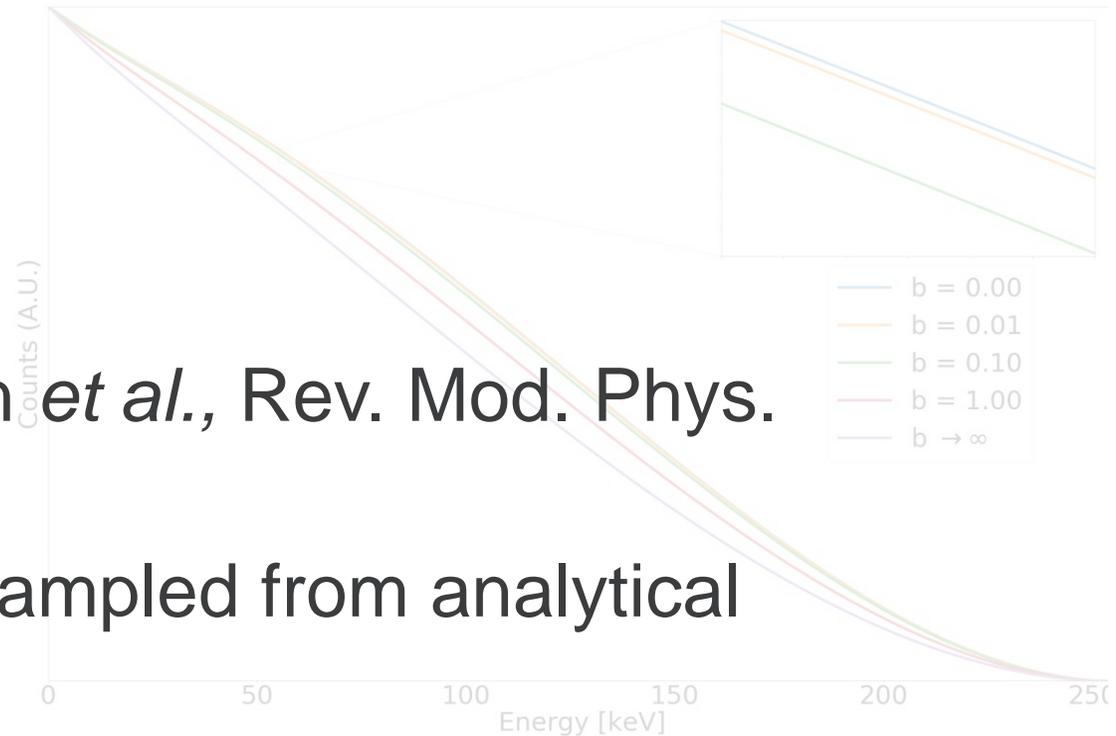
$$w(b) = PS \left\{ 1 + b \frac{m_e}{E_e} \right\}$$

Producing  $w(0)$  &  $w(1)$  spectra

– Analytical  $^{45}\text{Ca}$  spectrum: L. Hayen *et al.*, Rev. Mod. Phys. (2018)

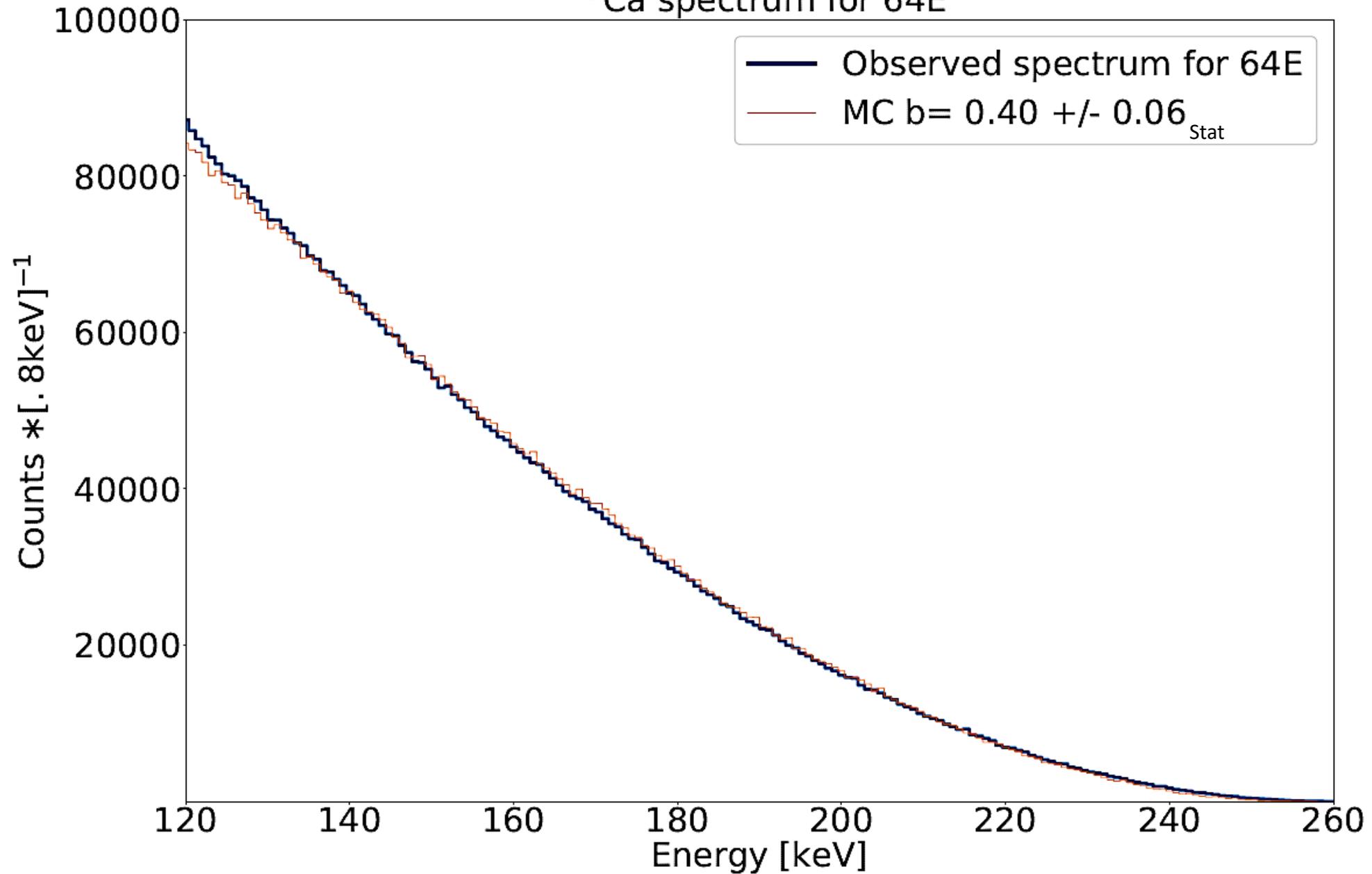
– PENELOPE treatment of events sampled from analytical spectrum

→  $w(b) = w(0) + b[w(1) - w(0)]$   
 – ERF to model detector physics



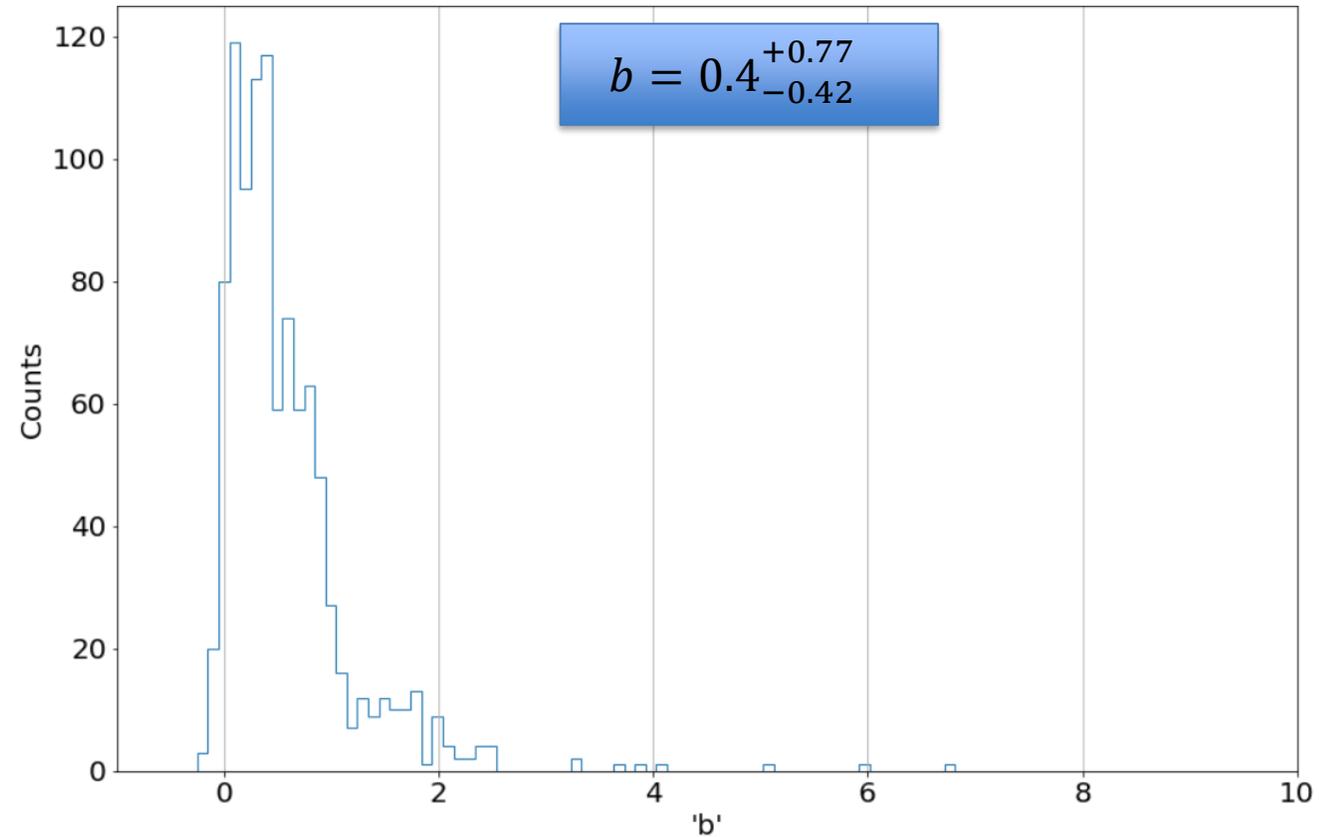
$$\text{Data} = \eta(w(0) + b[w(1) - w(0)])$$

# $^{45}\text{Ca}$ spectrum for 64E



# Calibration Systematic Uncertainty

- **Bootstrapping**
  - Resample mean of source peaks according to width of source peak
  - Recalibrate with resampled means
  - Repeat this process 1E3 times and extract 'b' for each calibration



# Systematics & Preliminary Value

| Systematic                           | Uncertainty in 'b' |
|--------------------------------------|--------------------|
| Calibration Uncertainty              | +0.77<br>-0.45     |
| Trapezoidal Filter Energy Extraction | 0.02               |
| Electronic Response Modeling         | 0.05               |
| Baseline Oscillation                 | 0.06               |
| MC Source Positioning                | +0.01<br>-0.07     |
| Detector Efficiency                  | 0.003              |
| MC Statistics                        | 0.04               |
| Fit Range Variation                  | +0.03<br>-0.04     |

$$b = 0.40 \pm 0.06_{stat.} \begin{matrix} +0.78 \\ -0.47 \end{matrix}_{sys.}$$

# Past Fierz Searches

- $^{20}\text{F} \rightarrow b = 0.0021 \pm 0.0051_{\text{stat}} \pm 0.0084_{\text{sys.}}$

- Preliminary Result

- Calorimetric Technique

*Precision Measurements in  $^{20}\text{F}$  Beta Decay*, Hughes, M. 2019, Ph.D Thesis: University of Michigan State

- $\text{UCN} \rightarrow b = 0.067 \pm 0.005_{\text{stat}} \begin{matrix} +0.090 \\ -0.061_{\text{sys.}} \end{matrix}$

- Measurement using UCNA spectrometer & UCN source

*First direct constraints on Fierz interference in free-neutron  $\beta$  decay* K. P. Hickerson *et al.* (UCNA Collaboration) Phys. Rev. C **96**, 042501(R)

- $ft$  values  $\rightarrow |b| < 0.0045$

- Super allowed transitions

*J. C. Hardy and I. S. Towner, Phys. Rev. C 91, 025501 (2015)*

# Ongoing Searches

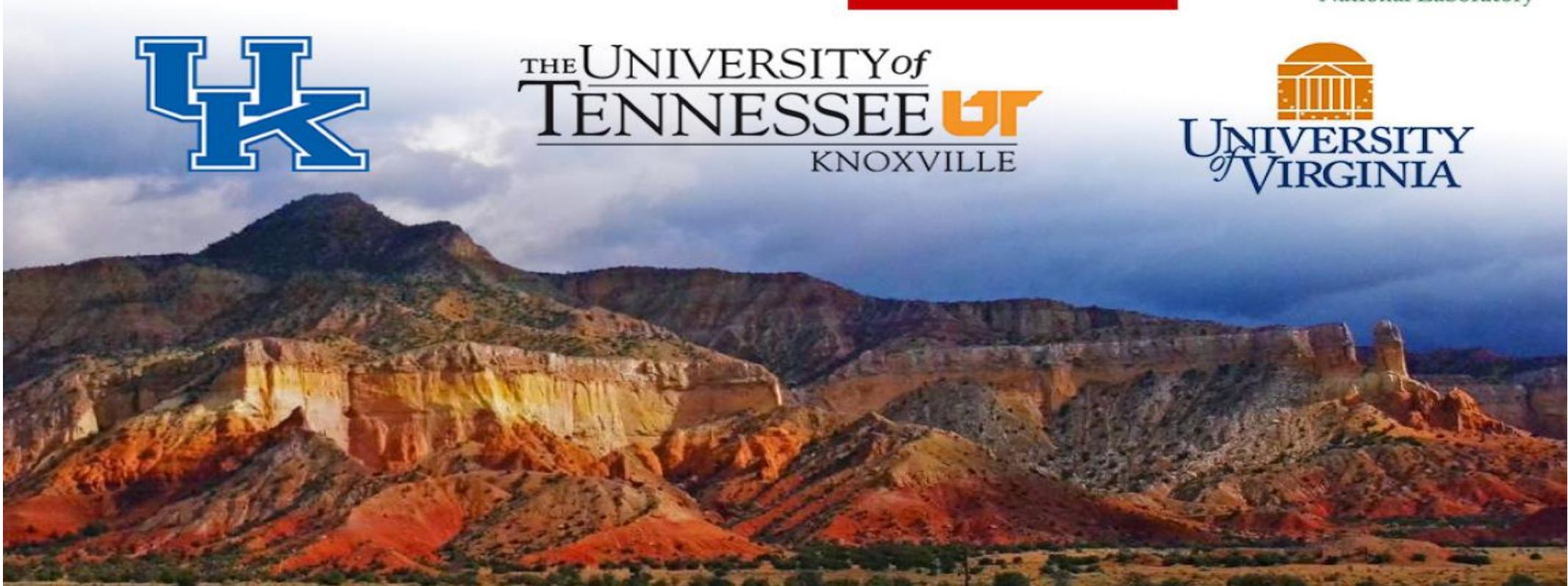
Slide courtesy of O. Naviliat-Cuncic

| Isotope                          | Method                     | Lab/Institution       |
|----------------------------------|----------------------------|-----------------------|
| ${}^6\text{He}$                  | thin foil; $4\pi$ detector | GANIL/LPC-Caen        |
| ${}^{114}\text{In}$              | MWDC+scintillators         | Krakow, Leuven        |
| ${}^{45}\text{Ca}$               | source in UCNA spectr.     | UT, ORNL, NCSU, KUL++ |
| ${}^6\text{He}$                  | CRES                       | UW, ANL++             |
| ${}^6\text{He}, {}^{20}\text{F}$ | Calorimetry                | NSCL/MSU, Wittenberg  |

# Next Steps

| Improvement  | Effect   |
|--|--|
| Extraction of 'b' via coincident spectra                     | Background reduction   |
| Simultaneous fit of $\eta$ , b, calibration & ERF parameters | Allows for bias study  |
| Utilize additional $\gamma$ source peaks in calibration      | More calibration points below $^{45}\text{Ca}$ endpoint energy |
| Realistic detector & electronic simulation                   | Analysis of MC at waveform level                               |

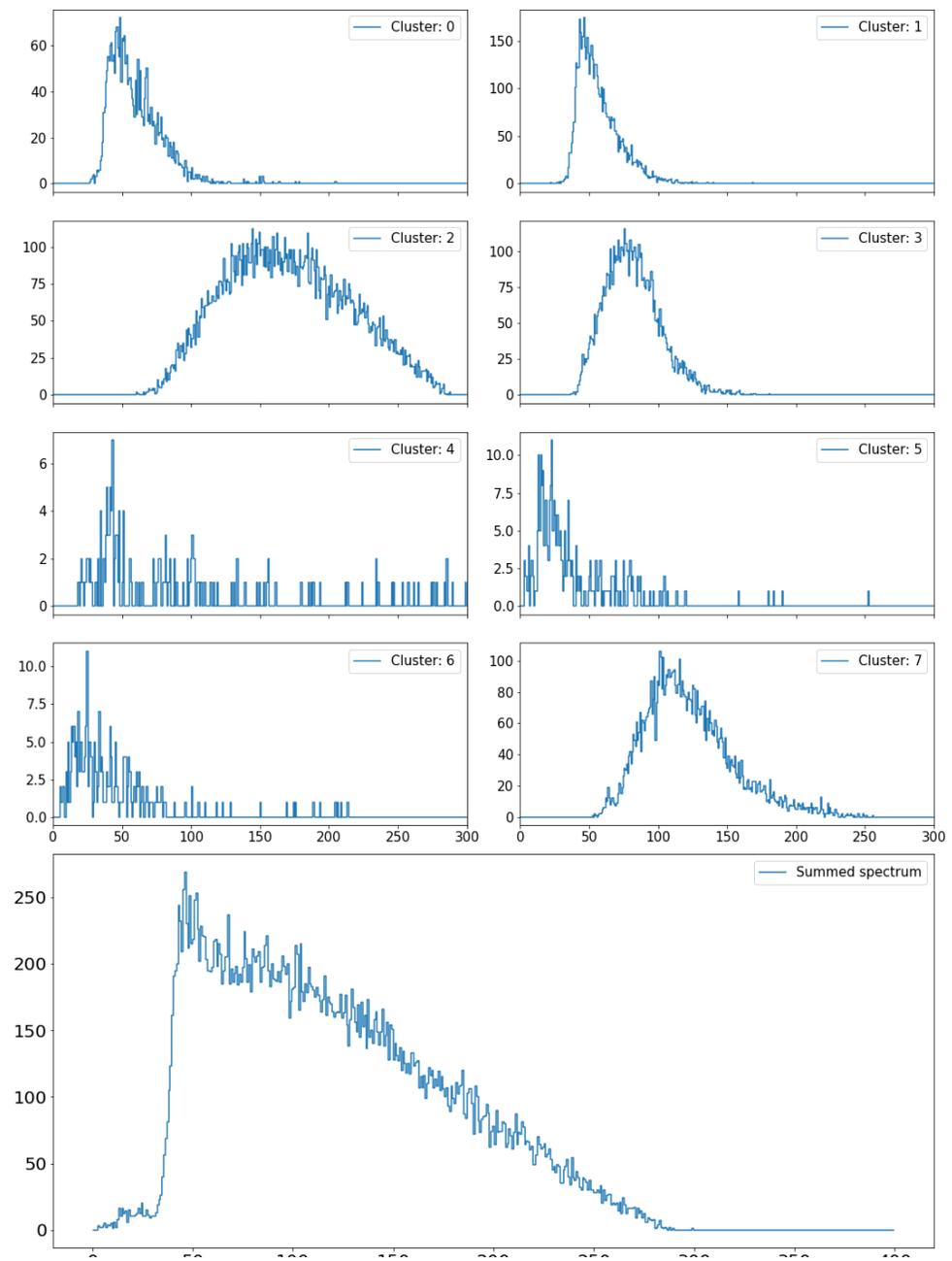
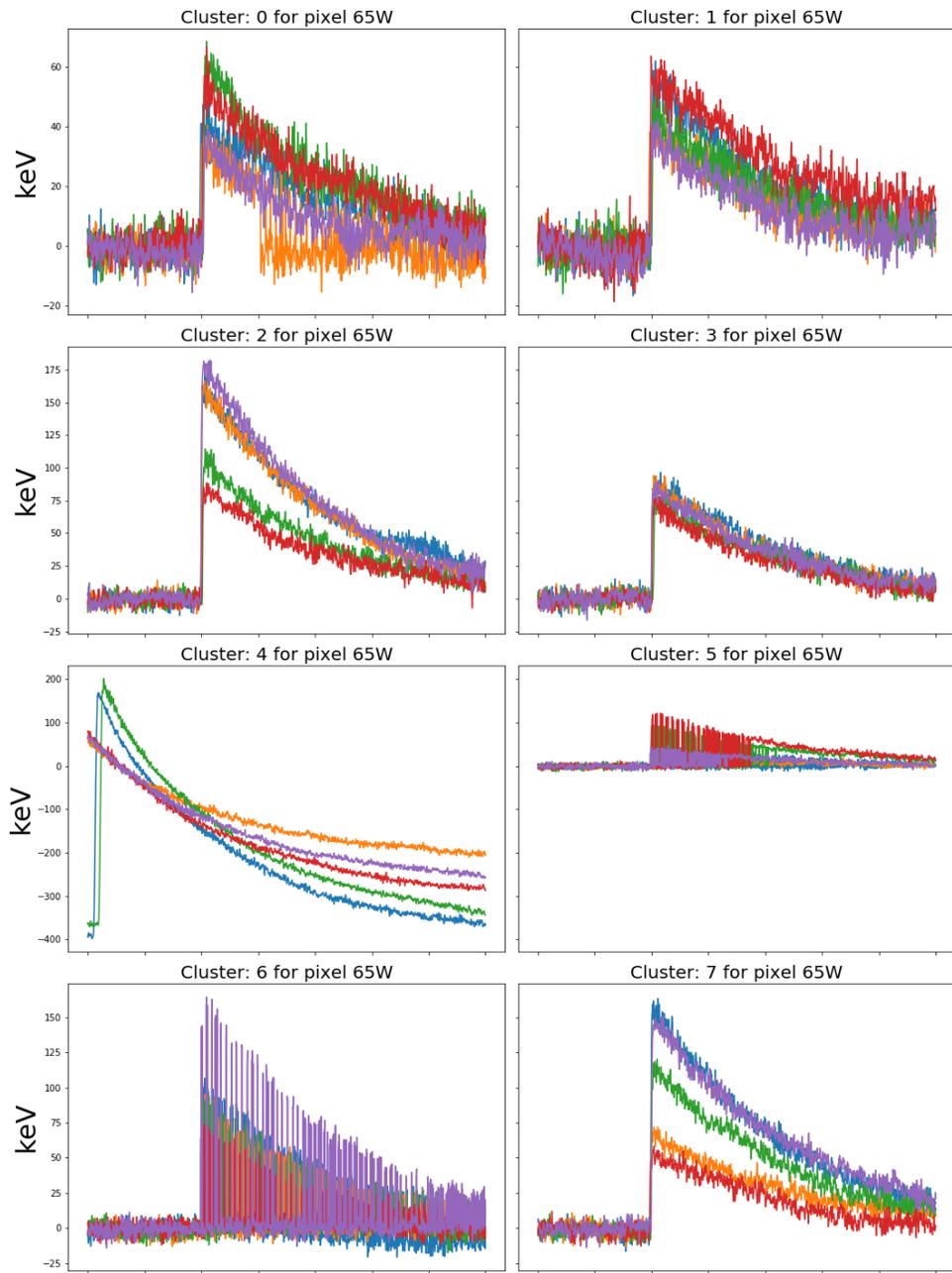
# Thank you for your time

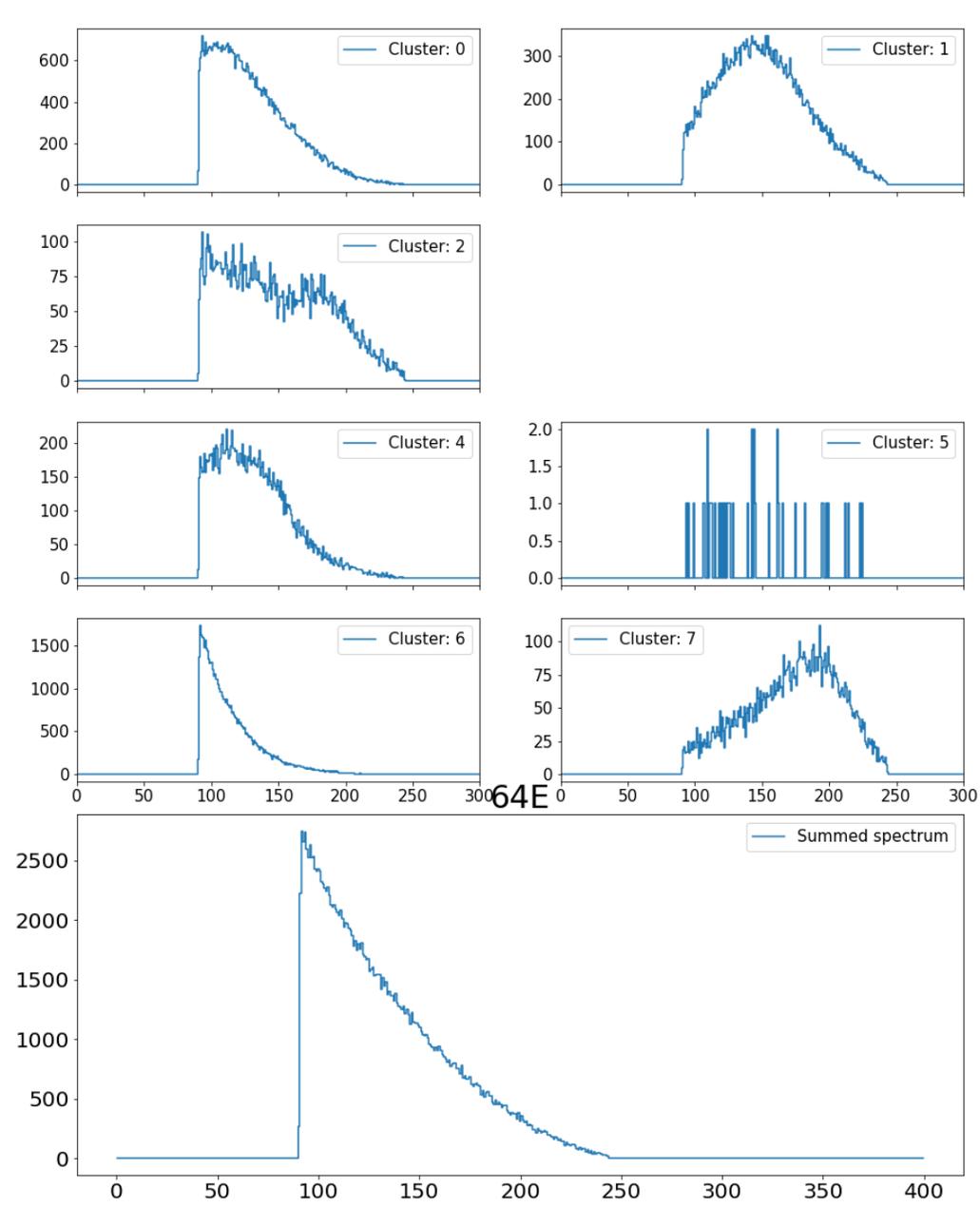
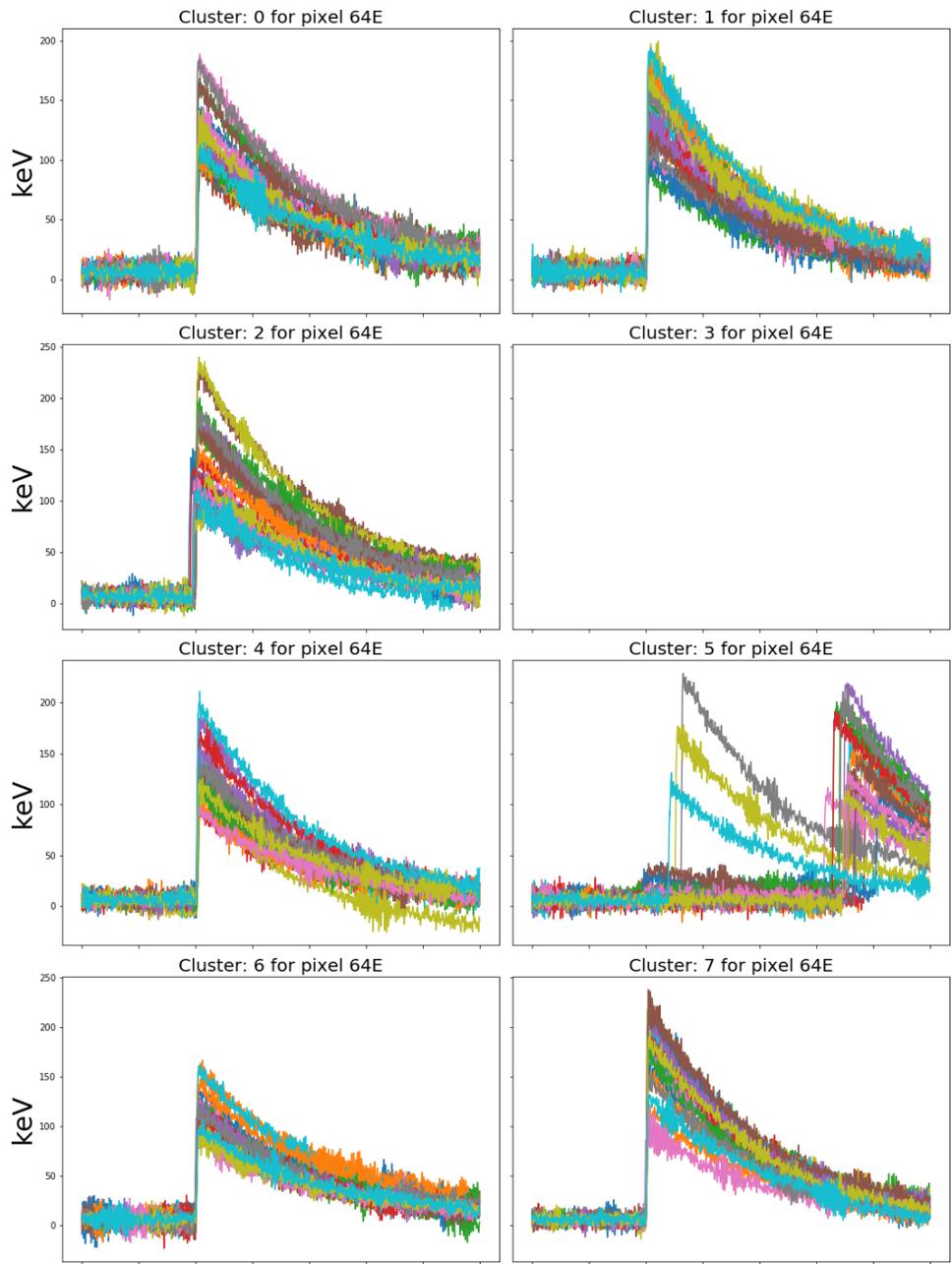


# Backup slides

# Kmeans Clustering Technique

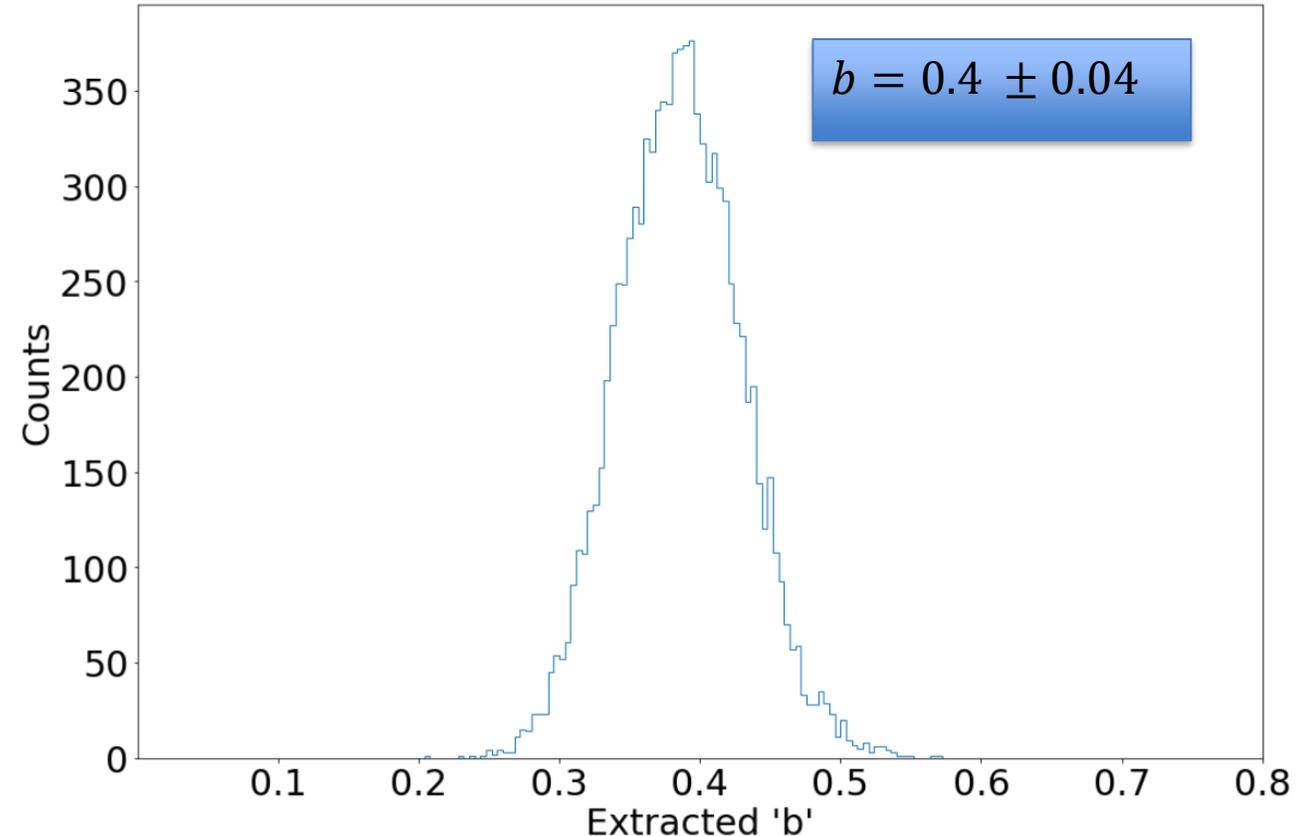
- Unsupervised learning (scikit-learn)
  - Data assumed to fall into one of  $X$  categories that are represented by some 'bin center'
  - ML algorithm determines bin centers by minimizing Euclidian distance of bin centers to data considered to be included in cluster
- Applied this technique to waveform data





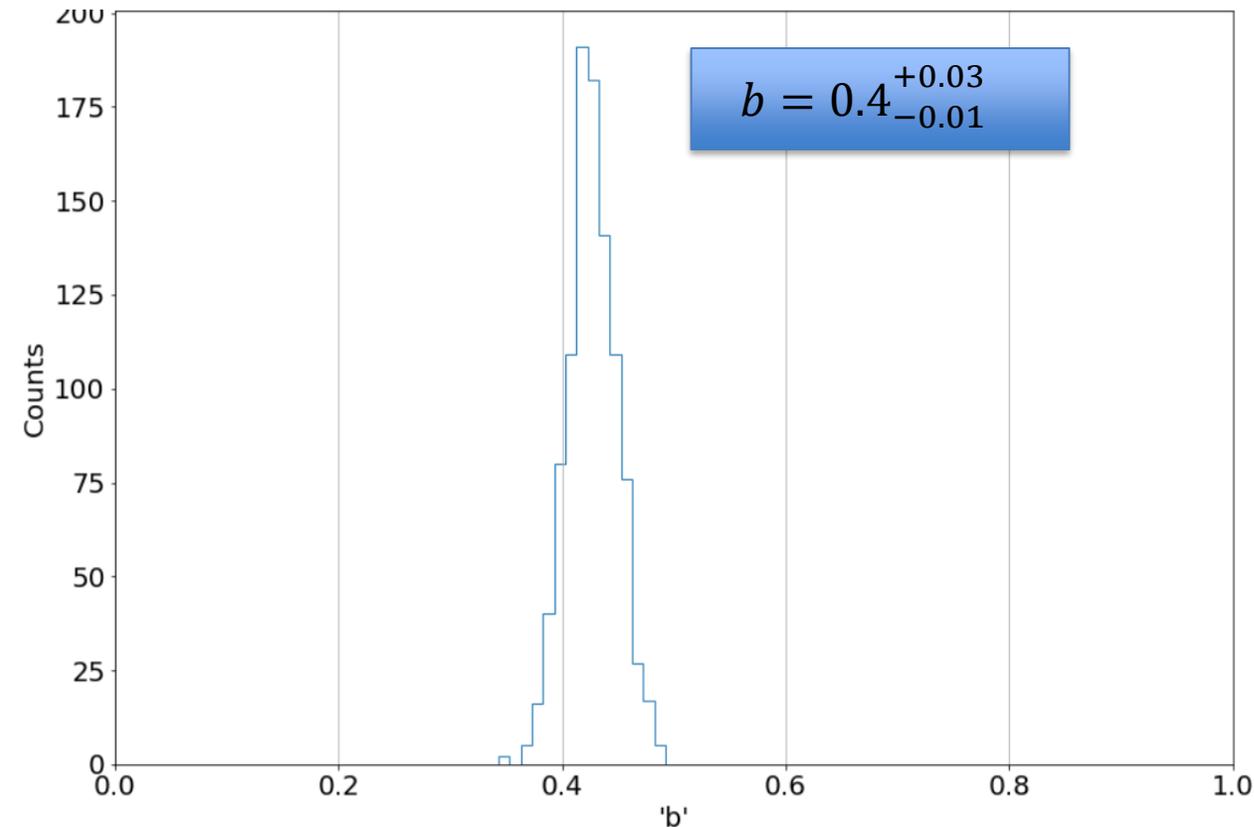
# MC Statistical Variation

- Bootstrapping technique
  - Number of counts in MC bins were resampled according to a poisson distribution centered at N counts.
  - Using resampled MC, a value of 'b' was extracted from observed data
  - Process repeated 10k times



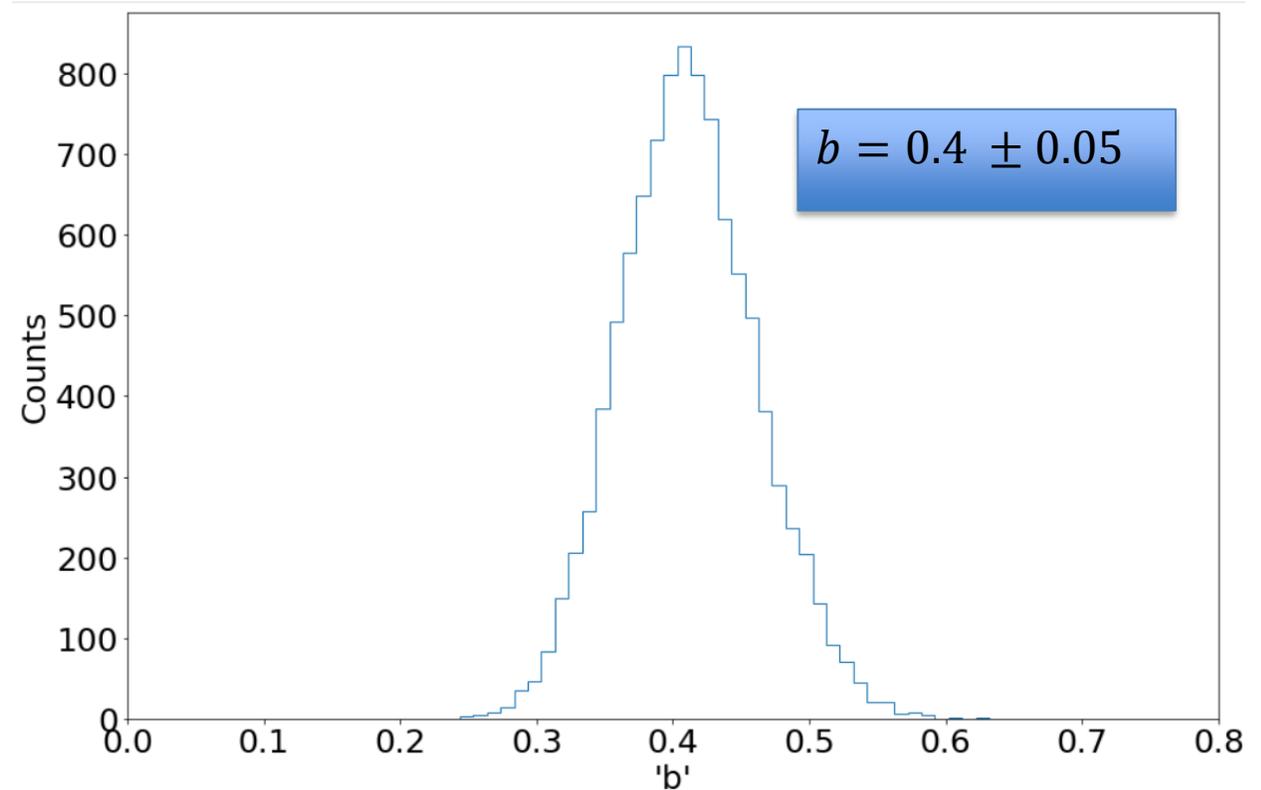
# Trapezoidal Energy Uncertainty

- Synthetic waveforms were generated
  - Noise was sampled from data power spectrum
  - Pulse shape: step function processed by (CR)-(RC)<sup>2</sup> shaper
    - Approximately equivalent to true electronics
  - 10K samples generated per amplitude.
  - Variance found to scale as 0.025\*E
  - (Study courtesy of David Perryman)
- Bootstrapping to estimate uncertainty
  - Observed energies were resampled according to a Gaussian distribution with  $\mu = E$  and  $\sigma = 0.025 \cdot E$
  - For each resampling, 'b' was extracted
  - Repeated 1E3 times



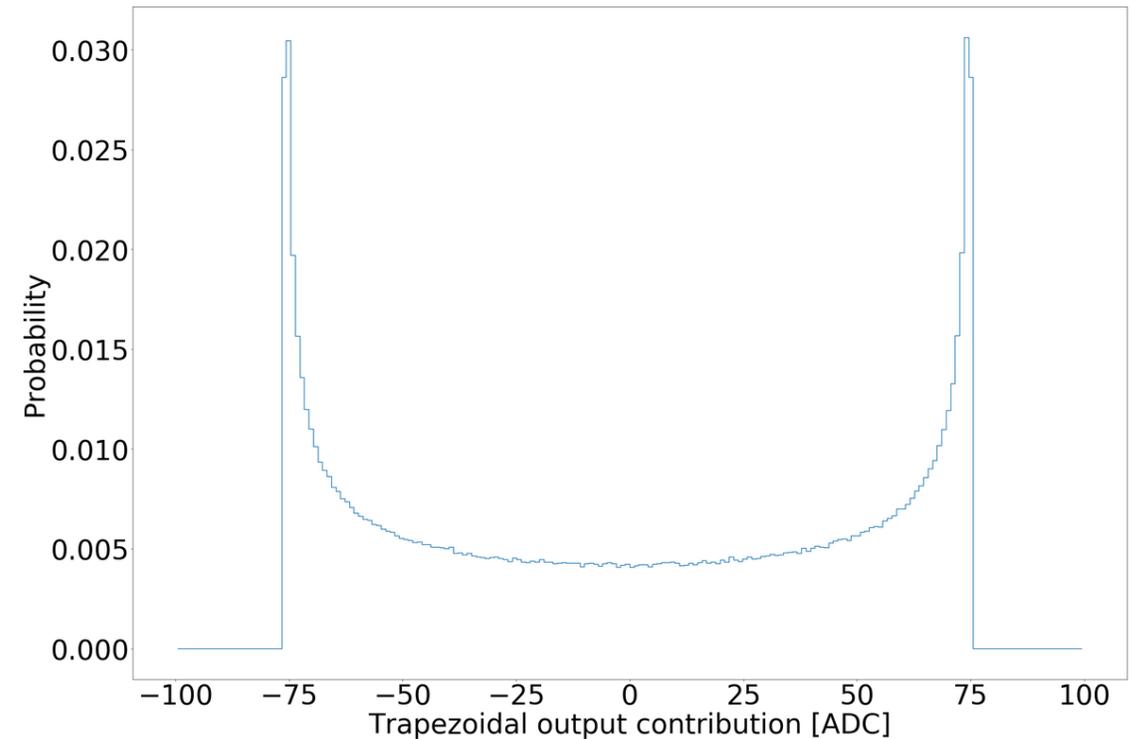
# ERF Systematic Uncertainty

- Bootstrapping technique
  - ERF is applied by randomly resampling the MC energies according to a gaussian distribution with  $\mu = E$  and  $\sigma = \sigma_{src.line}$  (width of source line)
  - $\therefore$  by simply repeating the procedures with different random seeds  $\rightarrow$  spread in 'b' due to ERF modelling
  - ERF generated with 1k different seeds for MC resampling
  - 'b' extracted for each set



# Baseline Oscillation Systematic Uncertainty

- Contribution of oscillating baseline to trapezoidal amplitude was calculated as a function of phase, frequency and amplitude.
- The baseline frequency was observed  $\sim 60$  kHz
- For  $10^6$  randomly sampled phases, and a fixed amplitude of 50 ADC (maximum allowed by cuts) recorded baseline contribution
- Used this distribution as a PDF
- MC  $b=0$  spectrum was used in place of data
- MC energies included randomly sampled energy contribution from above PDF
- A value of 'b' was fit for each random sampling
- Spread in 'b' was found to be comparable for both  $b=0$  and  $b=1$  spectra
- $\therefore$  Spread in observed data was taken as the maximum spread of the two spectra

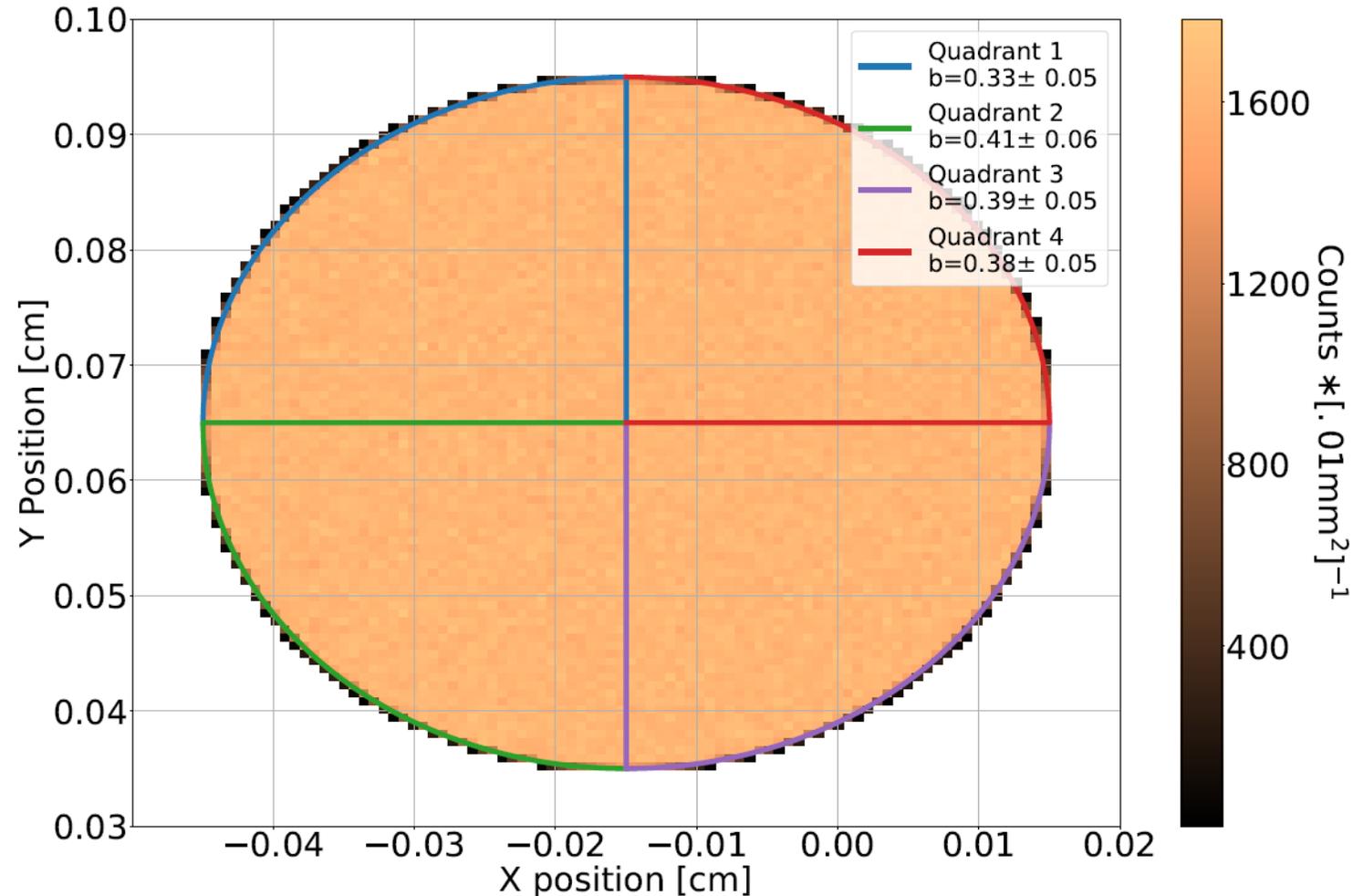


$$b = 0.4 \pm 0.06$$

# MC Source Position Uncertainty

- The events used in MC were separated into quarters
- The set of events for the relevant quarter was then used to extract 'b'
- The spread in 'b' was estimated as the spread in the values of 'b' extracted for each quarter

$$b = 0.4^{+0.01}_{-0.07}$$

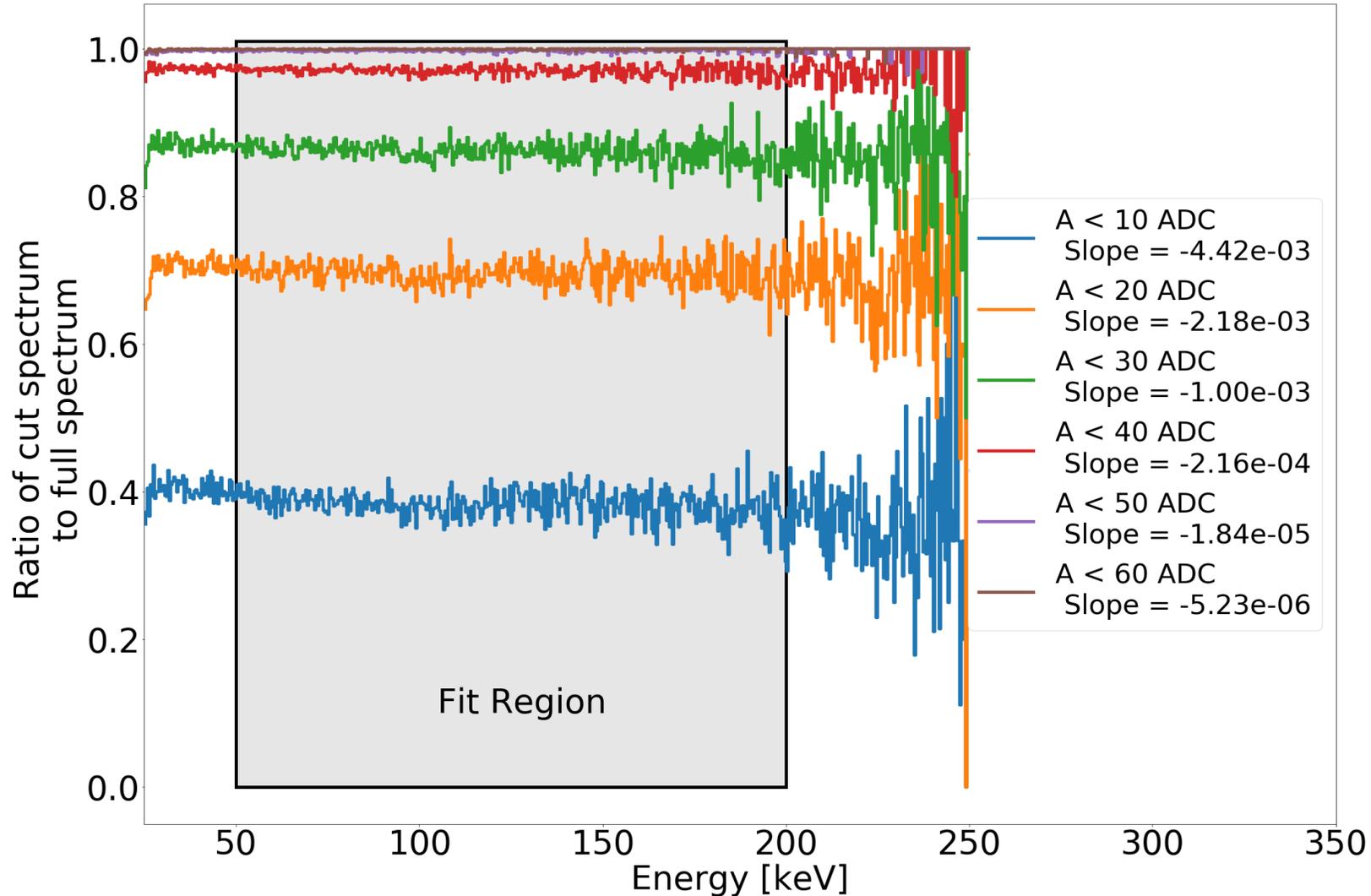


# Fit Range Variation

- The range was varied  $\pm 5$  bins at each end
- A value of 'b' was extracted for each range.
- The spread in the central values of 'b' was taken as the systematic uncertainty due to fit region.

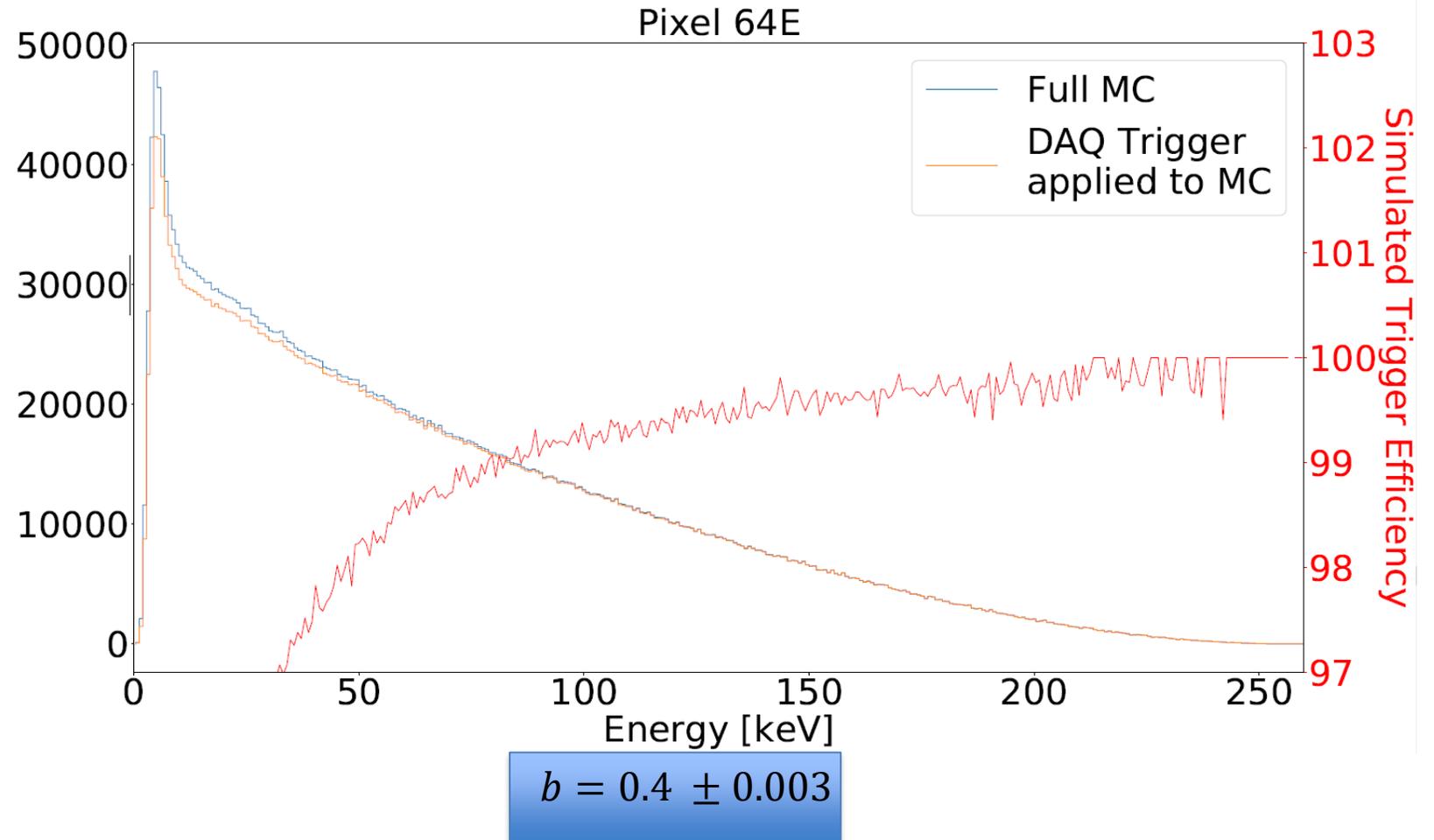
$$b = 0.4^{+0.03}_{-0.04}$$

# Baseline Oscillation Cut Uniformity

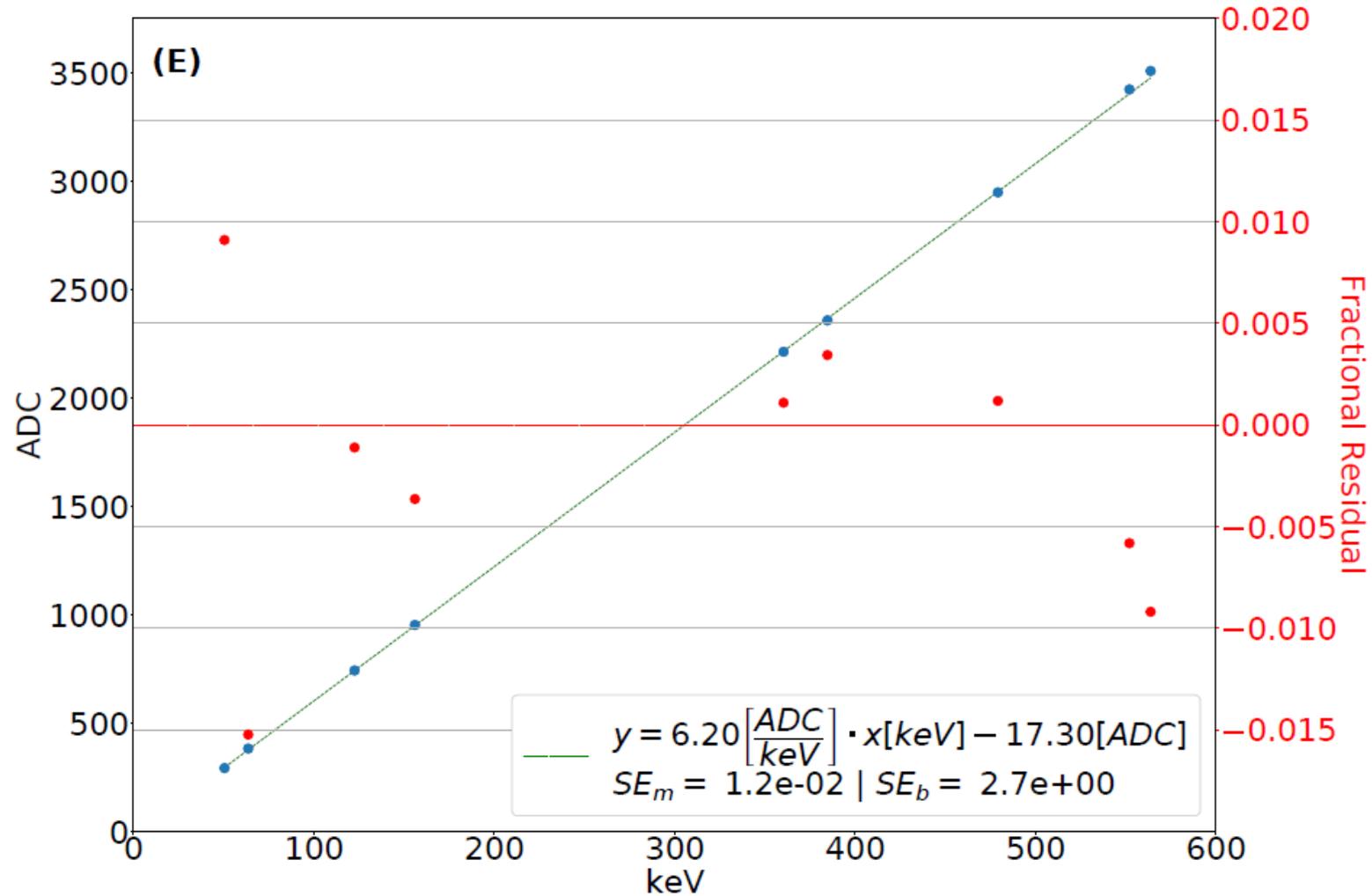


# Detector Efficiency

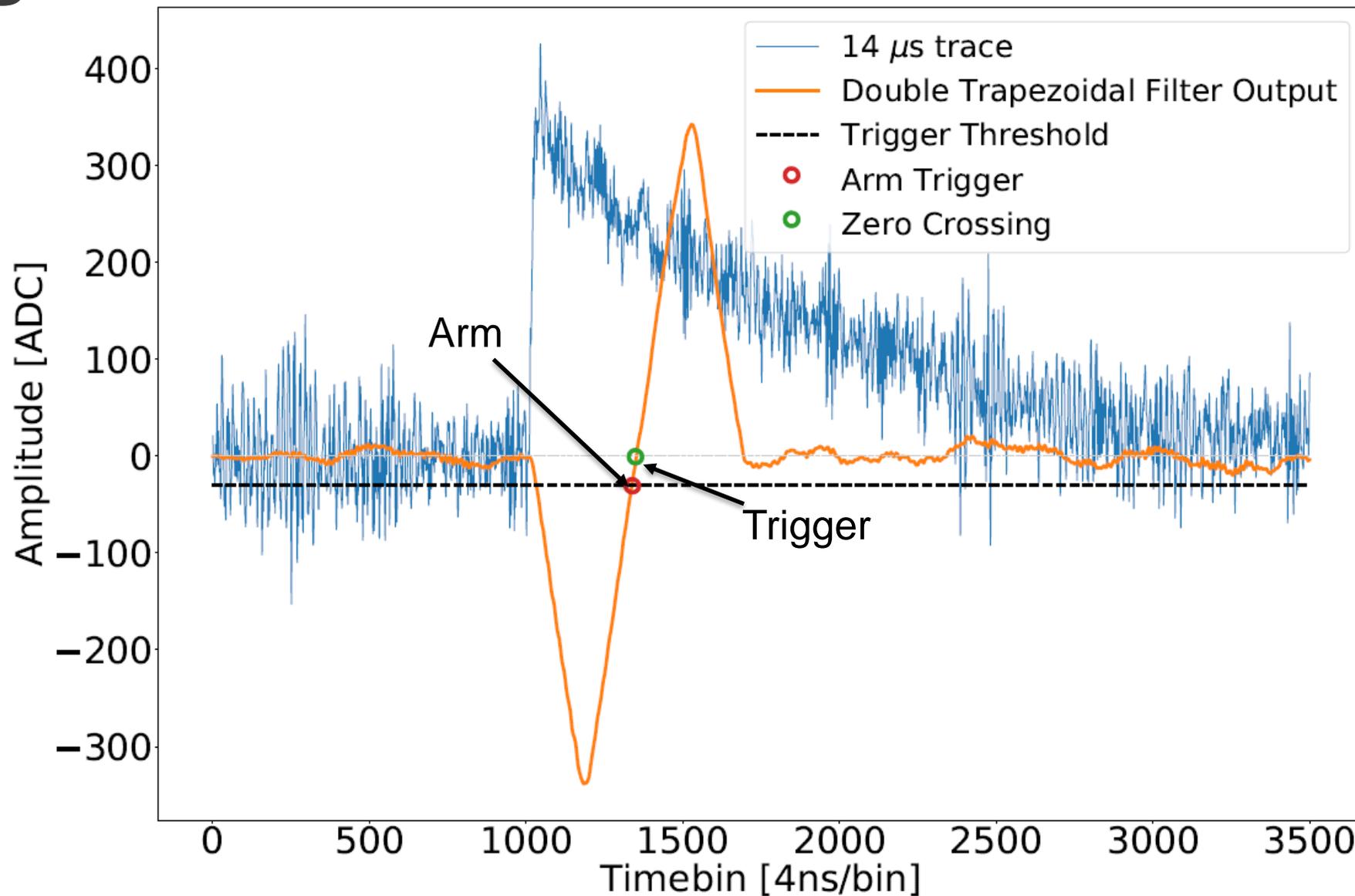
- The detector efficiency was estimated via simulation
  - DAQ trigger filter was applied to a set of MC  $b=0$  events.
  - The efficiency was estimated as  $1 - \frac{\text{number of events missed by the simulated DAQ}}{\text{total number of events}}$
- A value of 'b' was extracted from data with the efficiency correction and data without the efficiency correction.
- The uncertainty in 'b' was taken to be the spread in the two extractions



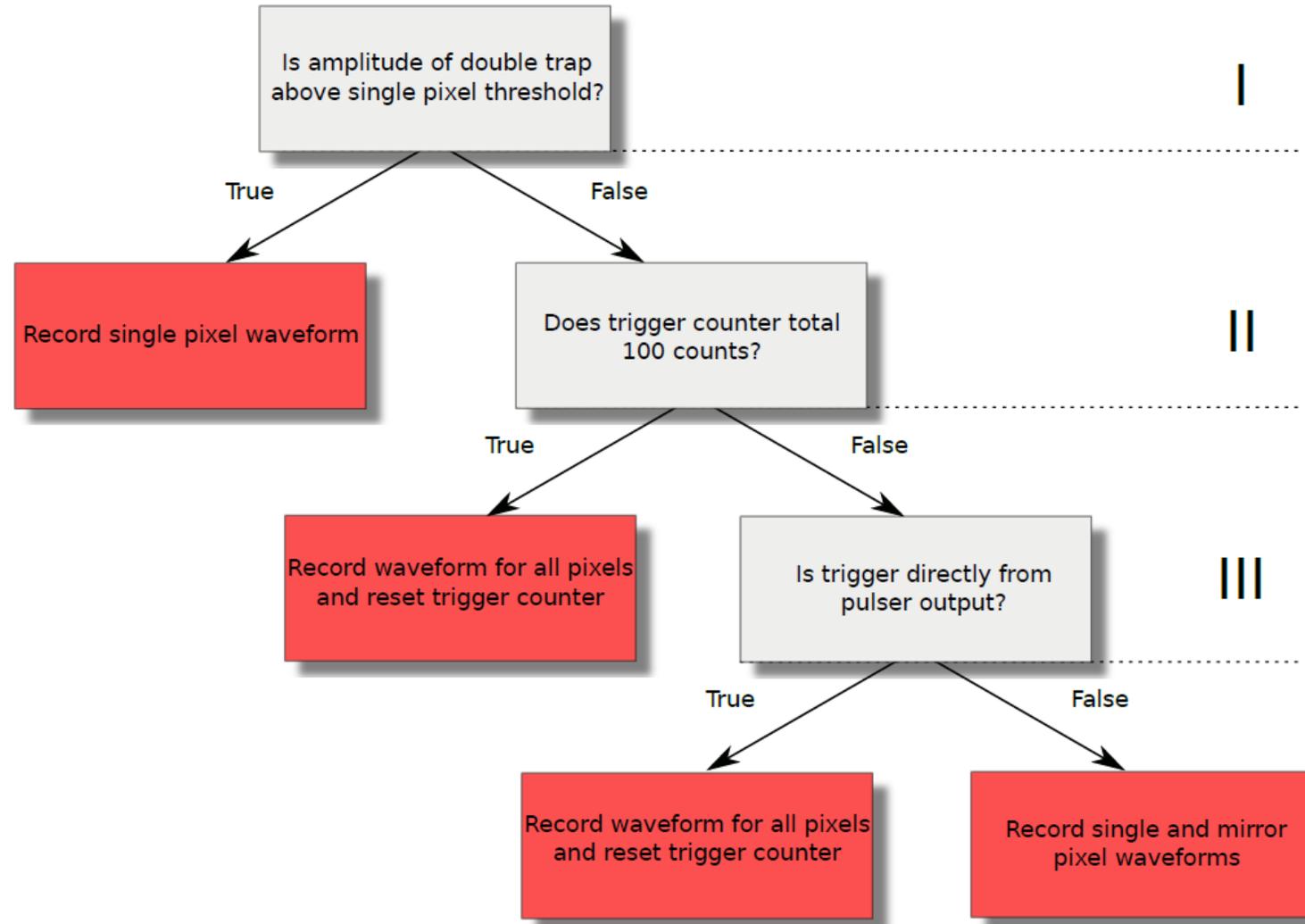
# Calibration & Linearity



# Trigger Scheme



# Trigger Scheme overview

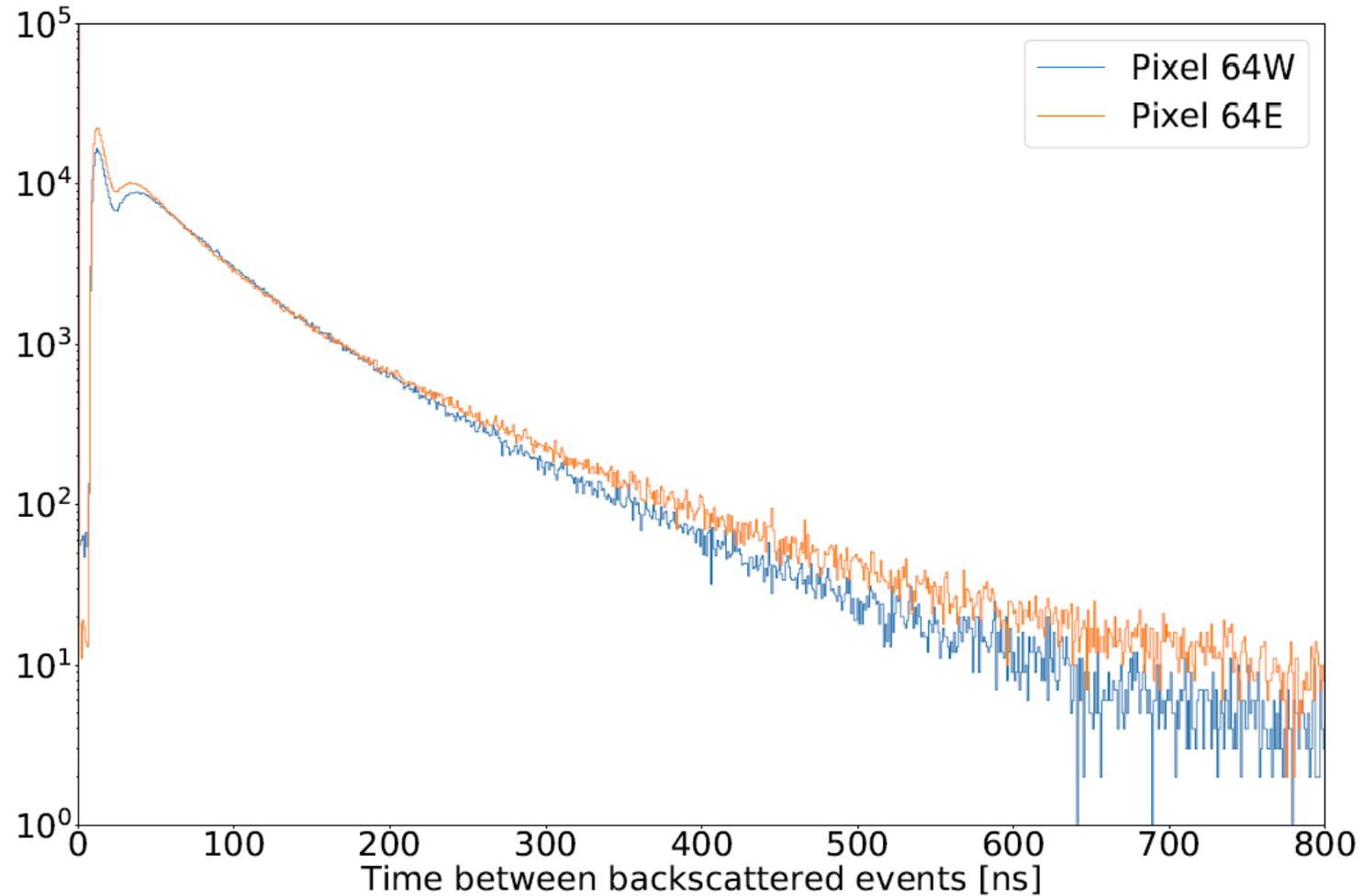


# Fit Range

- 150 keV – 220 keV
  - Detector efficiency  $\sim 99.9\%$  at 150 keV

$$- \frac{\sqrt{N}}{N} \sim 0.01$$

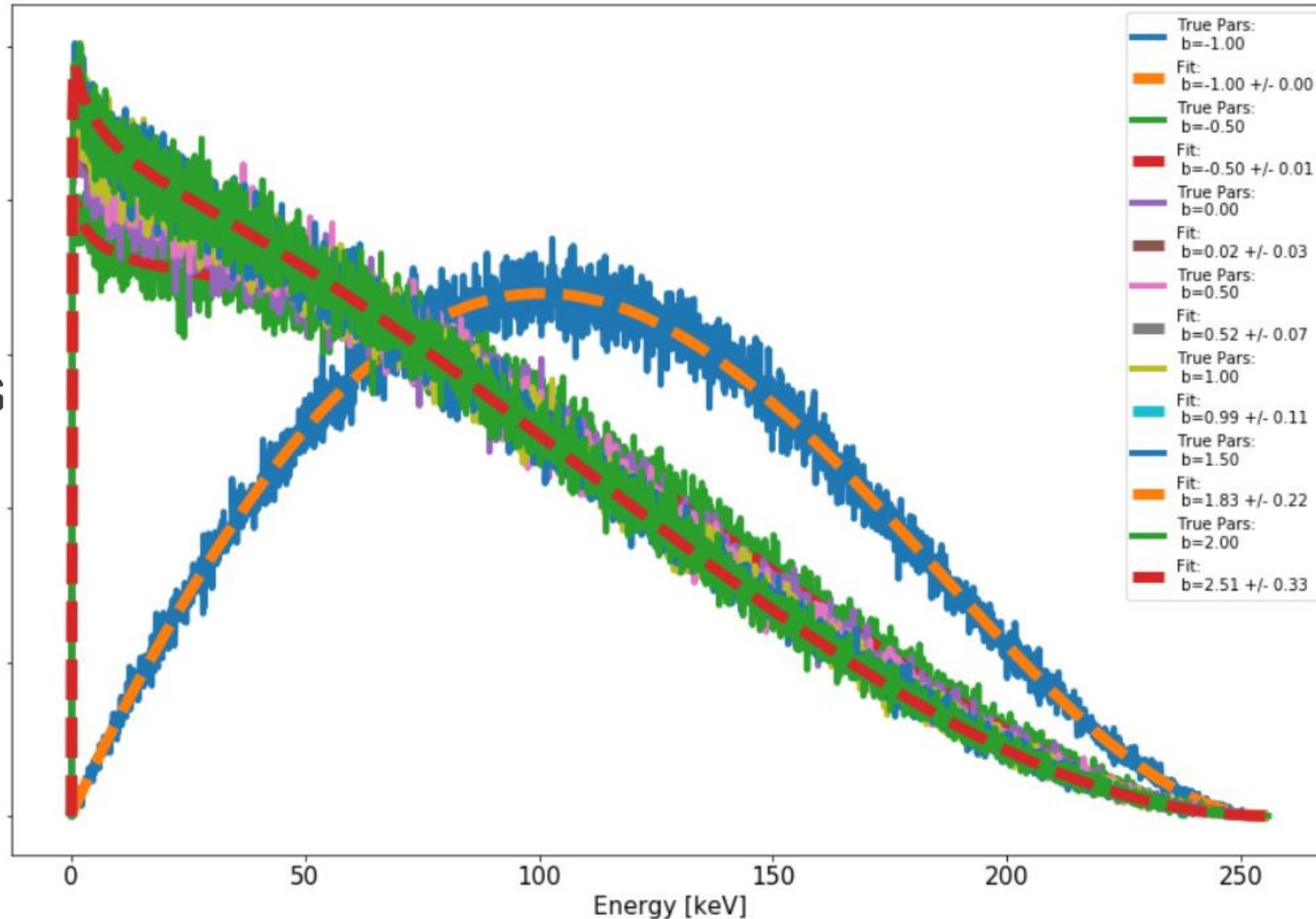
# Backscattered timing distribution



Simulation courtesy  
of B.Zeck

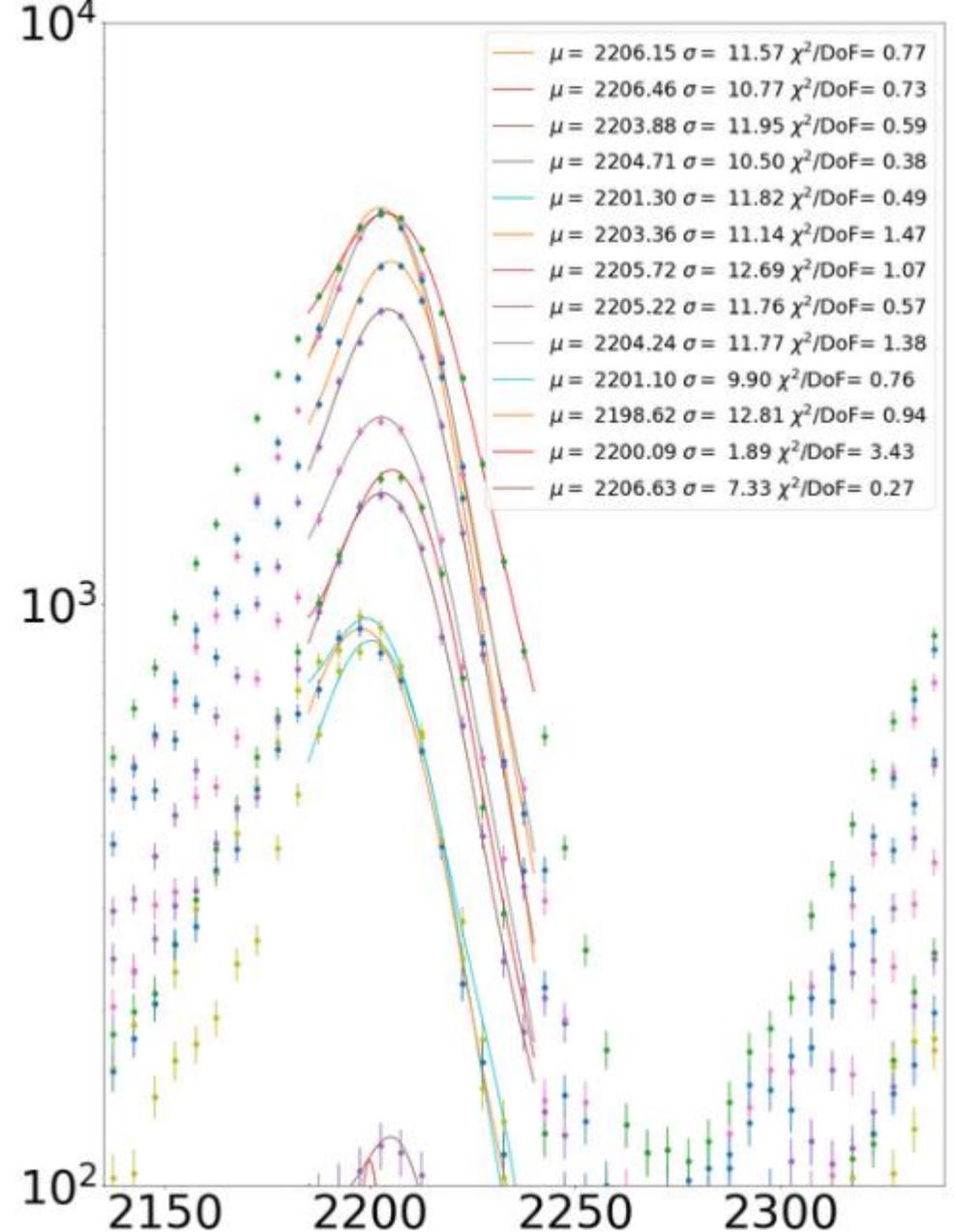
# b=0 & b=1 Spectra to Generate $^{45}\text{Ca}$ Spectrum with Arbitrary 'b'

- Calcium spectrum was generated for  $b \in [-1, 0.5, 0, 0.5, 1]$
- Each spectrum was finitely sampled
- Using  $w(0), w(1)$ , 'b' was extracted from each sampled spectrum (dotted lines)



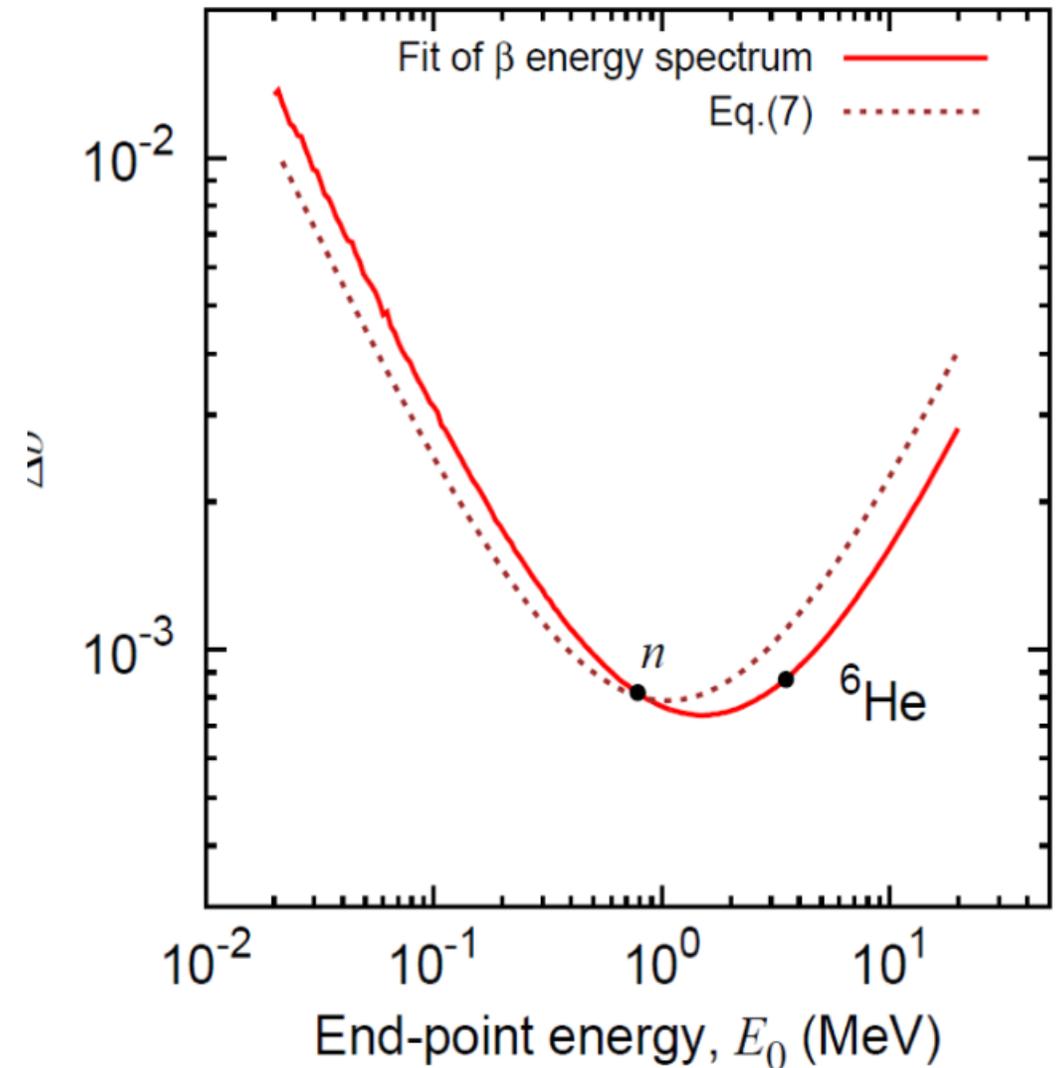
# Calibration Stability

- Shown on the right:
  - 363 keV source peak fit for all calibration runs throughout data collection
  - Peak stable to  $\pm 8$ ADC
  - Very stable gain & calibration

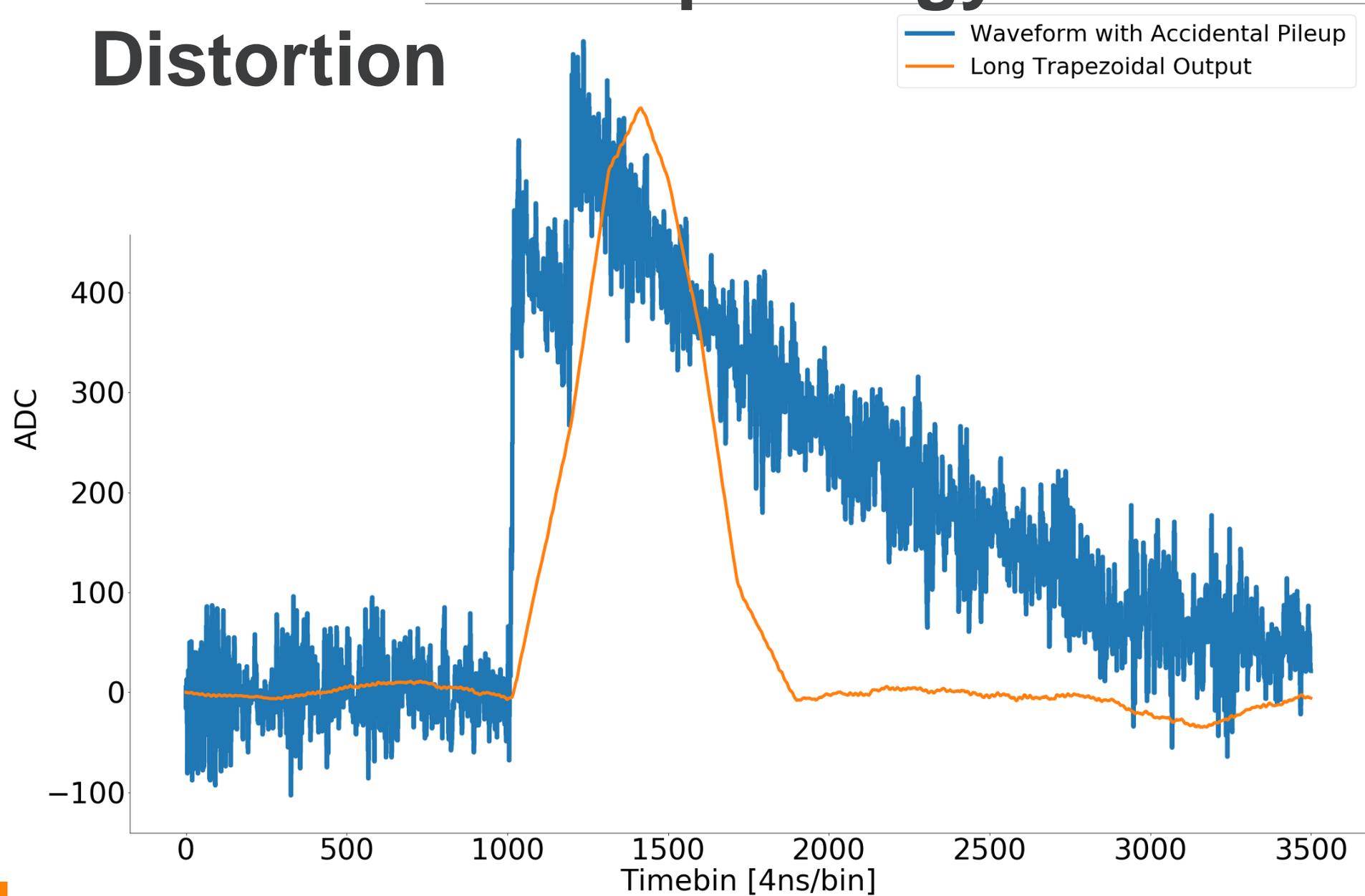


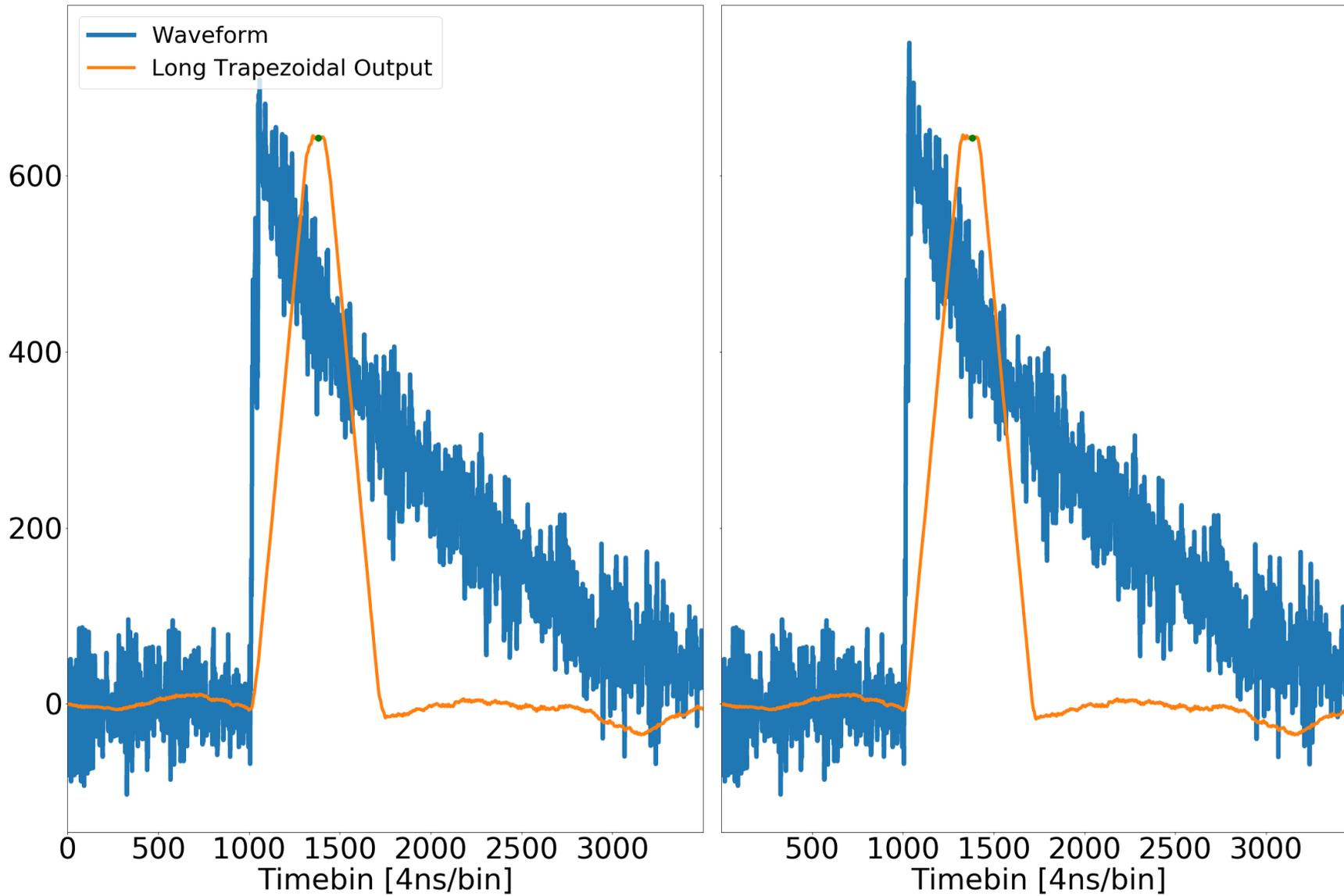
# Kinematic Sensitivity

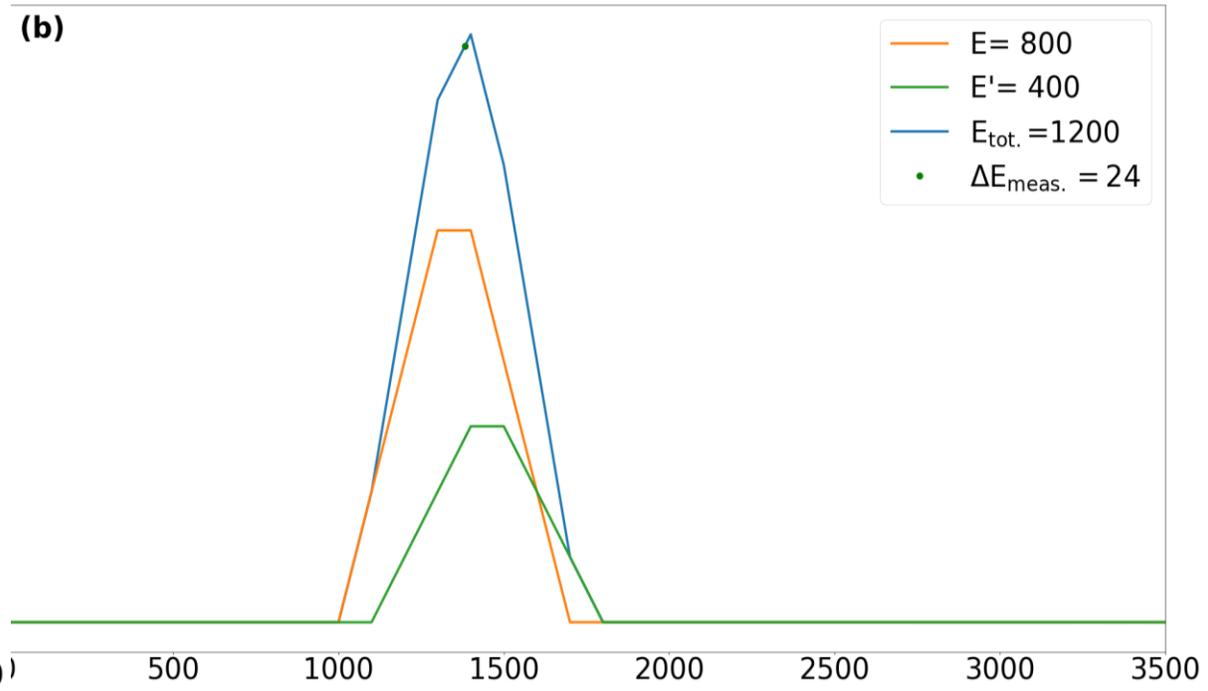
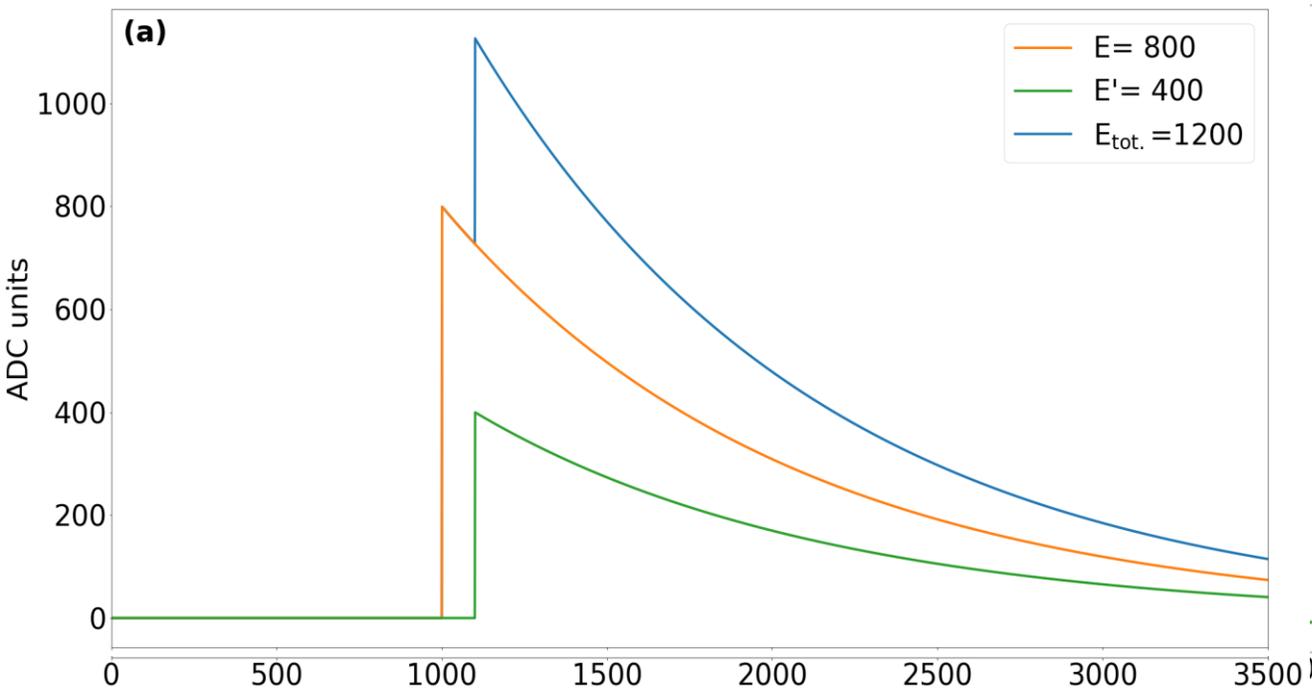
M. Gonzalez-Alonso and O. N.-C  
Phys. Rev. C **94** (2016) 035503

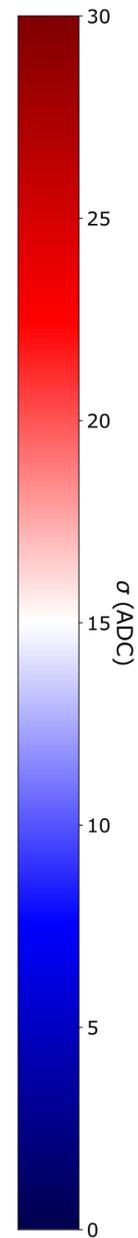
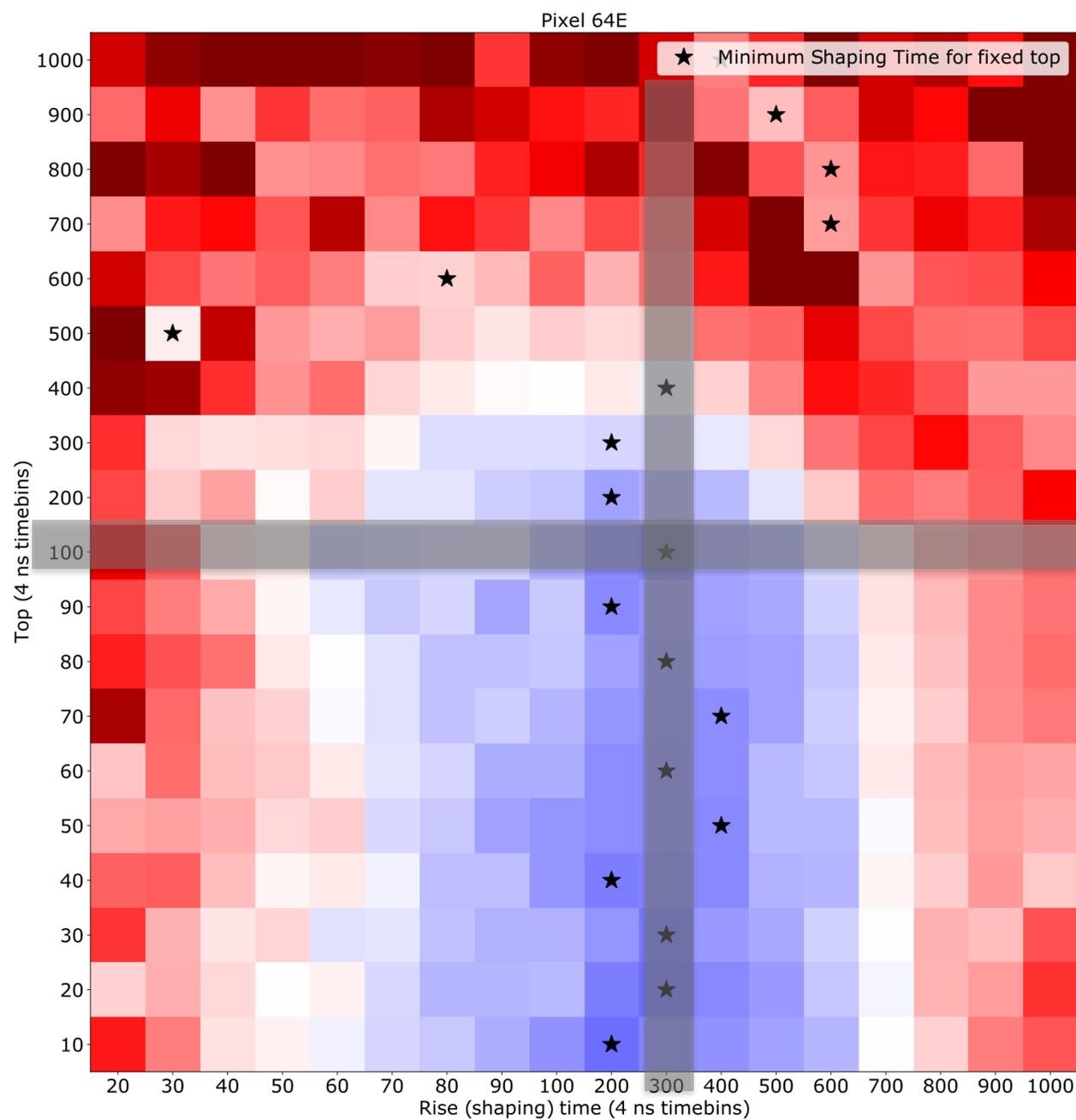


# Accidental Pileup Energy Distortion









Top = 400 ns (100 timebins)

- Accommodates risetime variation

→ Shaping time =  $1.2 \mu\text{s}$

- Minimum peak width

# Linear Least Squares Fit

- Suppose a WF ( $Y$ ) can be described by 'n' functions ( $f_j$ ) of  $t \in [t_0, t_1, \dots, t_m]$ . Let  $a_j$  be a scaling factor.

$$Y[i] = \sum_{j=0}^n a_j f_j(t_i)$$

$$F := \begin{bmatrix} f_0(t_0) & \cdots & f_m(t_0) \\ \vdots & \ddots & \vdots \\ f_0(t_n) & \cdots & f_m(t_n) \end{bmatrix} \quad a := \begin{bmatrix} a_0 \\ \vdots \\ a_m \end{bmatrix}$$

$$Y = F \cdot a$$

# Linear Least Squares Fit

$$Y = F \cdot a$$

$Y[i]$  represents the amplitude of the waveform of the  $i$ 'th bin

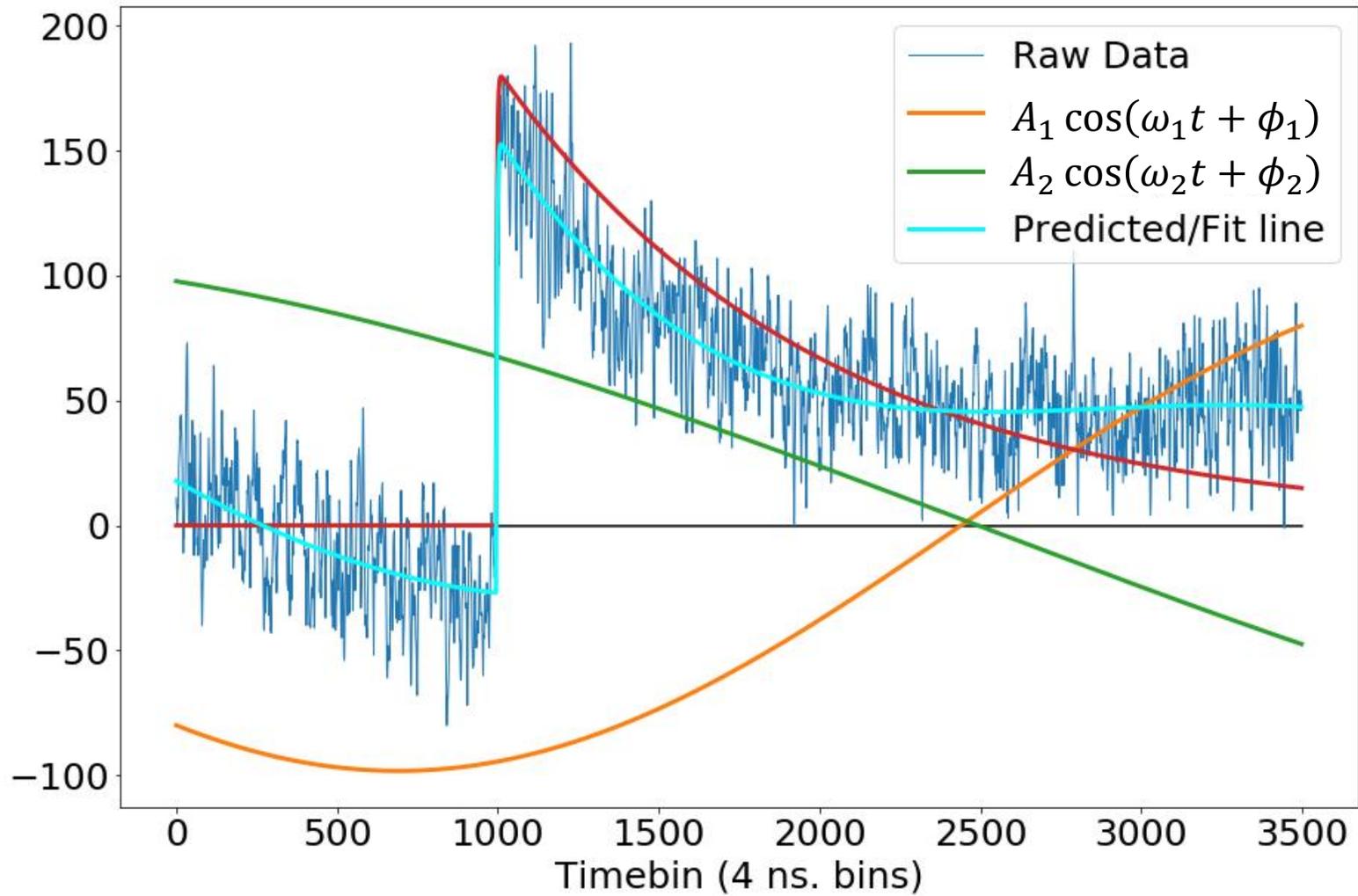
$$\rightarrow F^T \cdot Y = (F^T \cdot F) \cdot a$$

$$\rightarrow a = (F^T \cdot F)^{-1} \cdot F^T \cdot Y$$

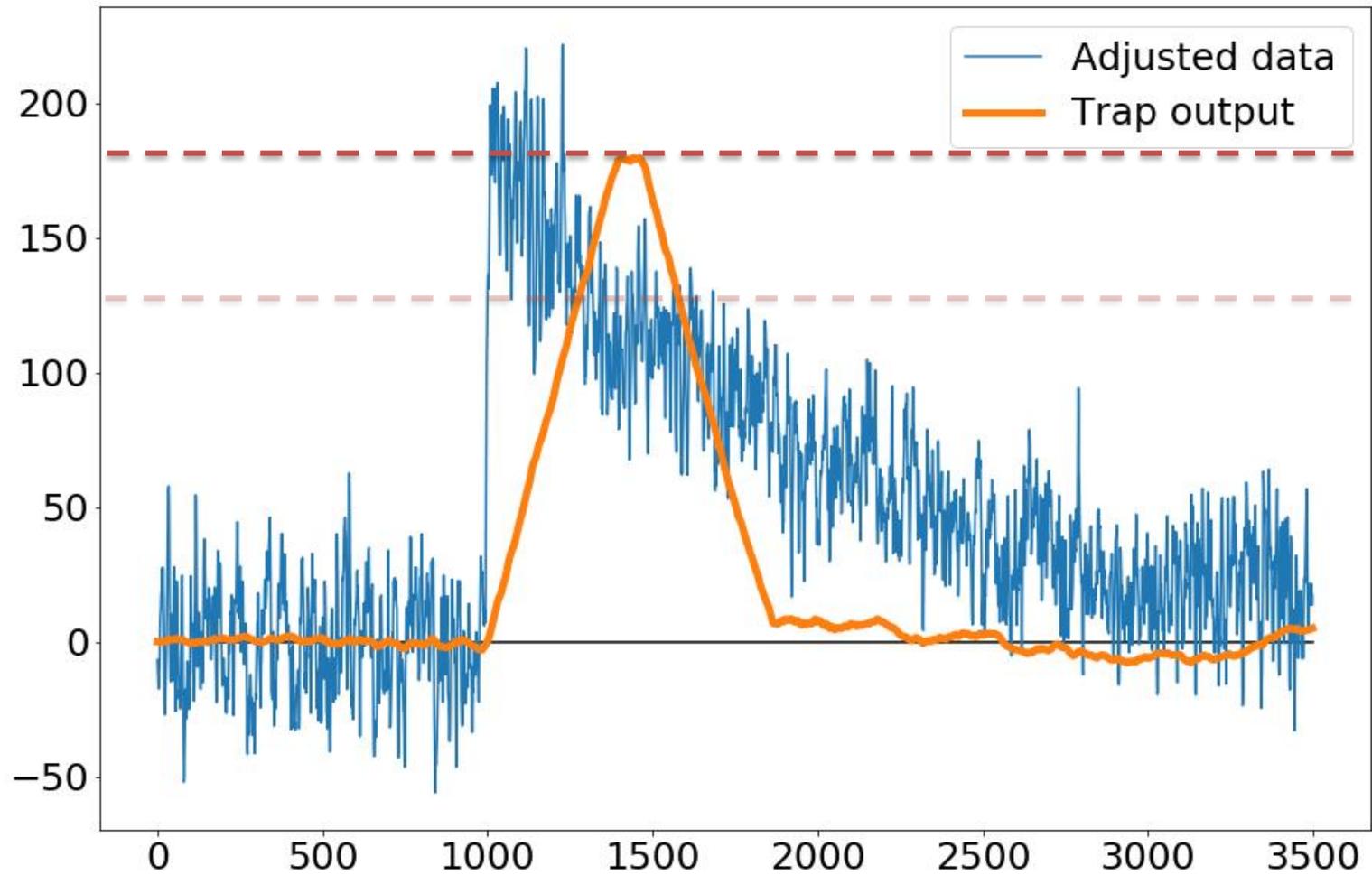
$$F = \left[ \begin{array}{c} \text{Green step function} \\ \text{Blue sine wave} \\ \text{Orange sine wave} \\ \dots \end{array} \right] \quad \text{N functions}$$

$$Y^T = \left[ \text{Blue noisy signal} \right] \quad \text{Suppose } Y = F \cdot a$$

$$\rightarrow a = (F^T \cdot F)^{-1} \cdot F^T \cdot Y$$



# Baseline oscillation removed



# Baseline oscillation removed

