

# TOWARDS MORE PRECISE PREDICTIONS FOR TTH AND TTZ PRODUCTION AT THE LHC

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1. Motivations
2. Experimental Status
3. Higher Order Corrections
4. Preliminary Results on TTH and TTZ
5. Conclusions

# MOTIVATIONS: WHY TTH AND TTZ?

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- ▶ Top quark: Heaviest elementary particle known so far  
 $m_t \approx 173 \text{ GeV}$  (Gold Atom Mass  $\sim 197 \text{ u} \sim 183.21 \text{ GeV}$ ).  
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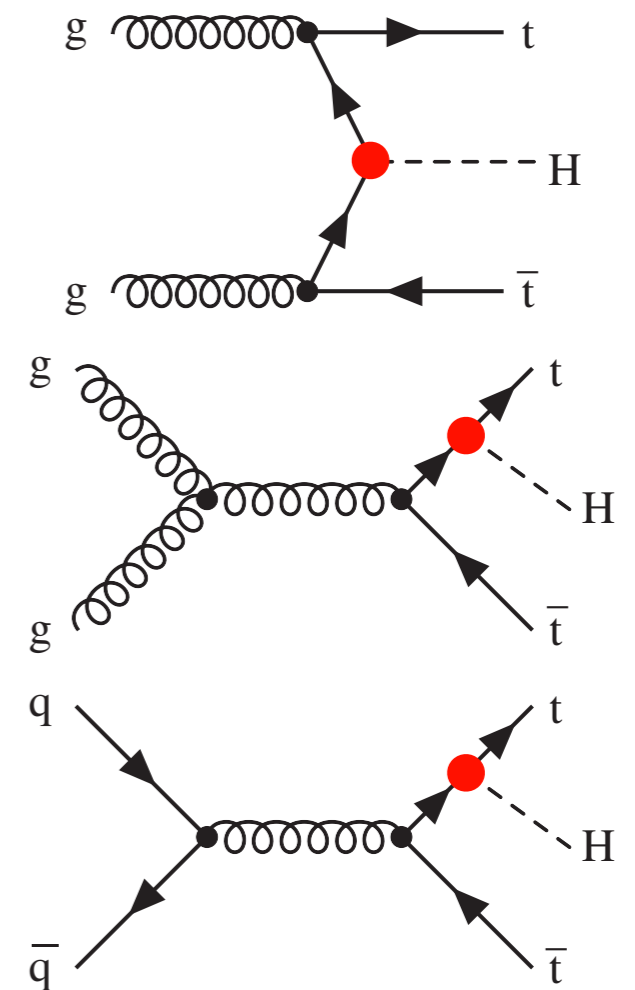
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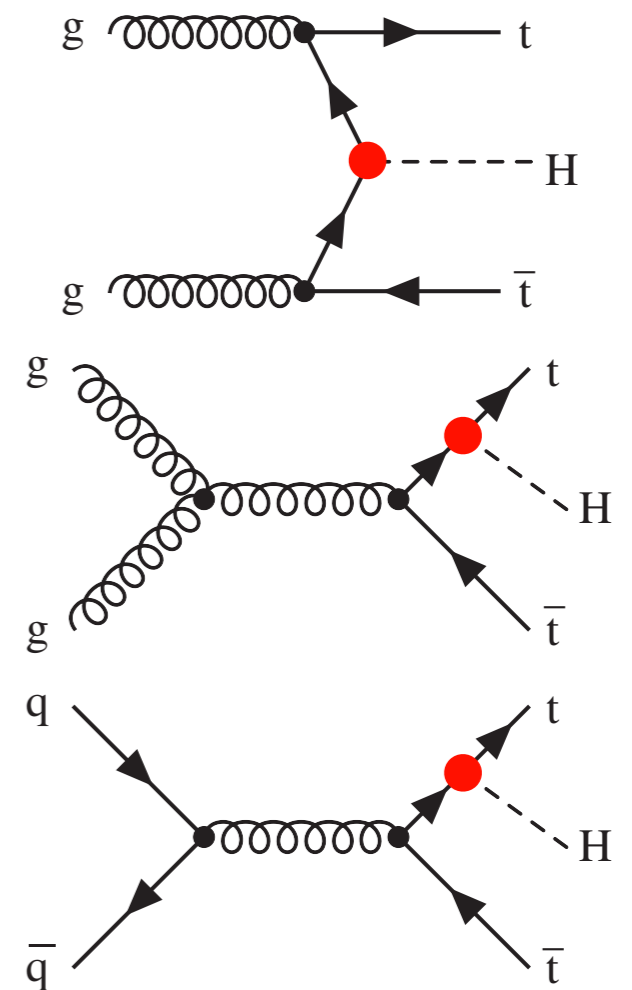
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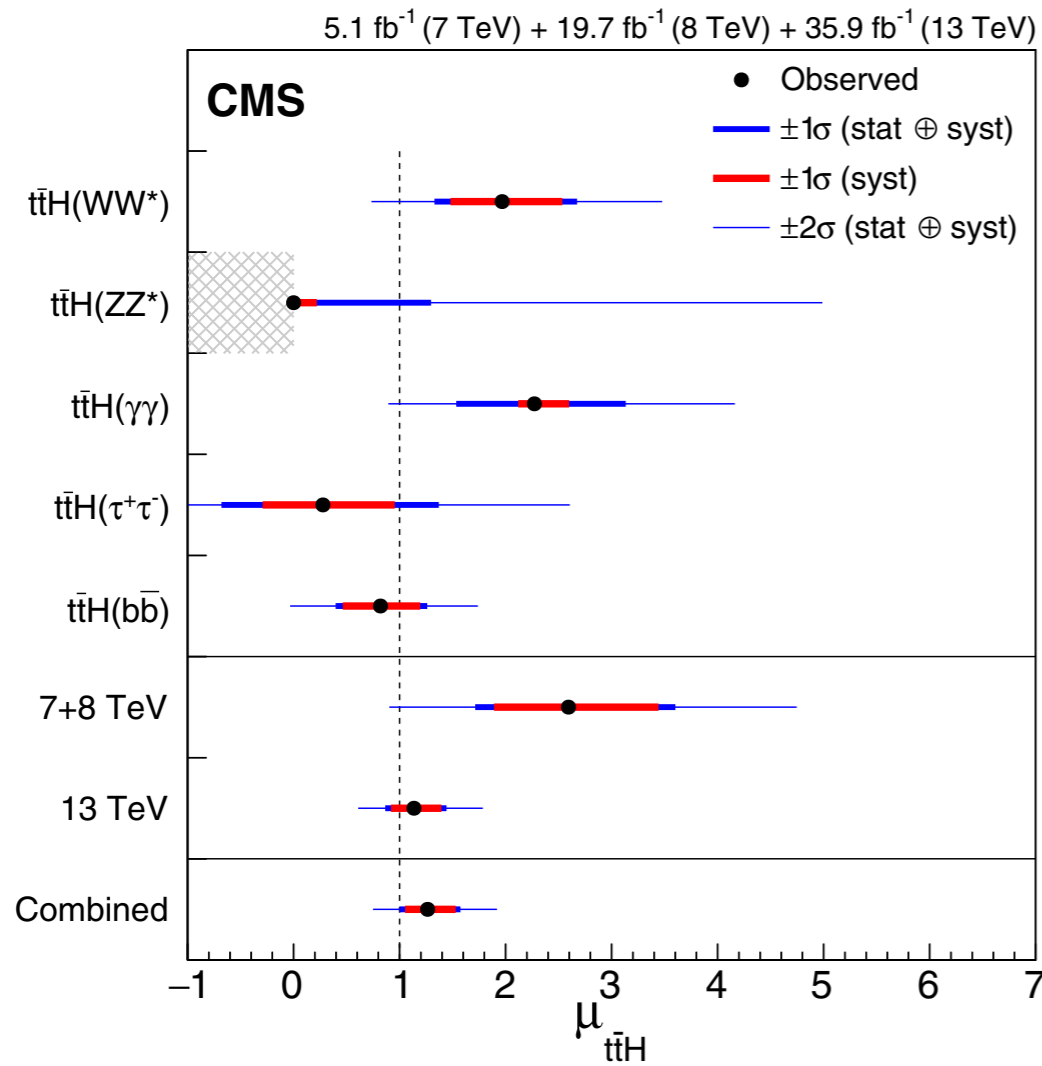
*Unambiguous interpretation of deviations*

- $ttZ$  is an important background in  $tth$  searches, in the decay channels  $H \rightarrow (b\bar{b}, WW^*, \tau\bar{\tau})$



# EXPERIMENTAL STATUS: TtH

PRL 120, 231801 (2018)

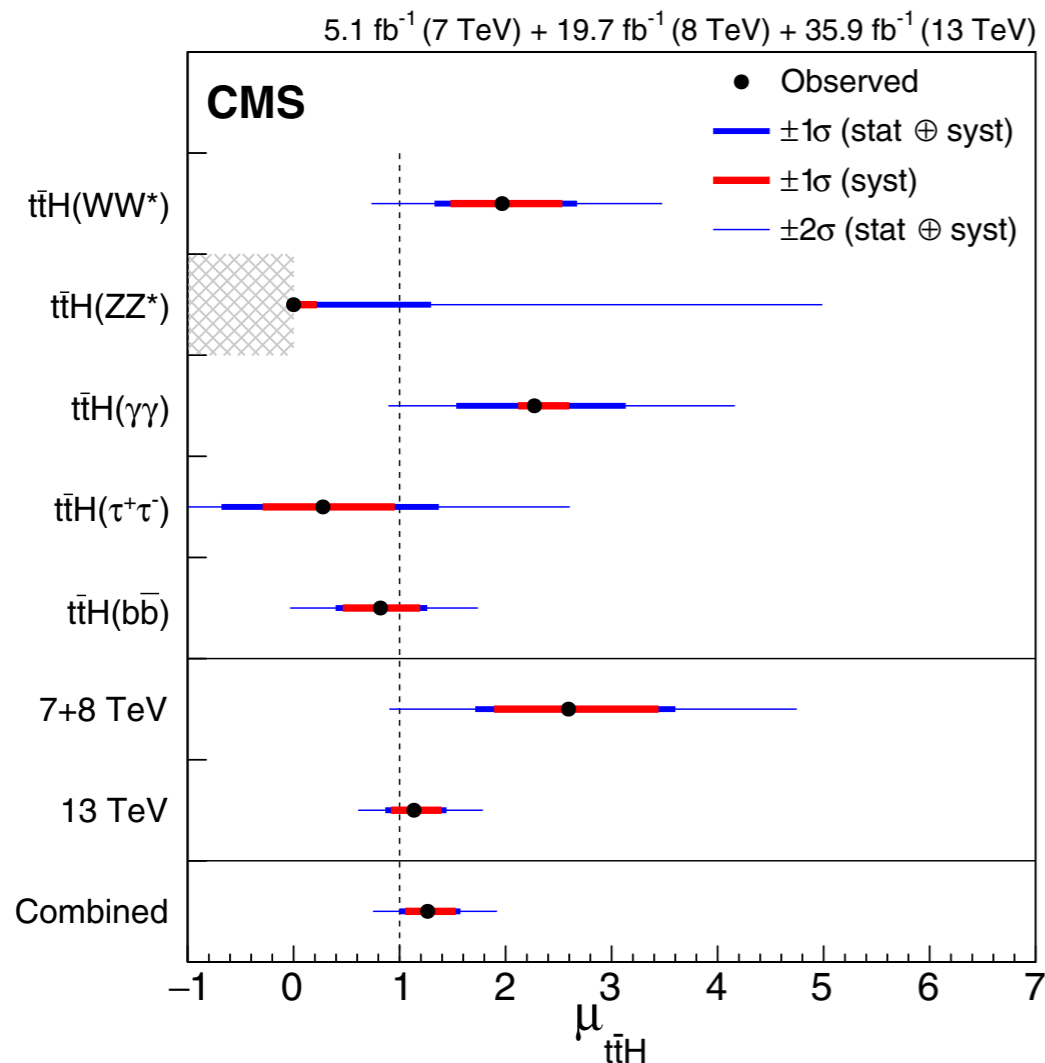


$$\mu_{t\bar{t}H} = 1.26^{+0.31}_{-0.26}$$

Parameter	Best fit	Statistical	Uncertainty		
			Experi- mental	Background theory	Signal theory
$\mu_{t\bar{t}H}^{WW^*}$	$1.97^{+0.71}_{-0.64}$	+0.42 -0.41	+0.46 -0.42	+0.21 -0.21	+0.25 -0.12
$\mu_{t\bar{t}H}^{ZZ^*}$	$0.00^{+1.30}_{-0.00}$	+1.28 -0.00	+0.20 -0.00	+0.04 -0.00	+0.09 -0.00
$\mu_{t\bar{t}H}^{\gamma\gamma}$	$2.27^{+0.86}_{-0.74}$	+0.80 -0.72	+0.15 -0.09	+0.02 -0.01	+0.29 -0.13
$\mu_{t\bar{t}H}^{\tau^+\tau^-}$	$0.28^{+1.09}_{-0.96}$	+0.86 -0.77	+0.64 -0.53	+0.10 -0.09	+0.20 -0.19
$\mu_{t\bar{t}H}^{b\bar{b}}$	$0.82^{+0.44}_{-0.42}$	+0.23 -0.23	+0.24 -0.23	+0.27 -0.27	+0.11 -0.03
$\mu_{t\bar{t}H}^{7+8 \text{ TeV}}$	$2.59^{+1.01}_{-0.88}$	+0.54 -0.53	+0.53 -0.49	+0.55 -0.49	+0.37 -0.13
$\mu_{t\bar{t}H}^{13 \text{ TeV}}$	$1.14^{+0.31}_{-0.27}$	+0.17 -0.16	+0.17 -0.17	+0.13 -0.12	+0.14 -0.06
$\mu_{t\bar{t}H}$	$1.26^{+0.31}_{-0.26}$	+0.16 -0.16	+0.17 -0.15	+0.14 -0.13	+0.15 -0.07

# EXPERIMENTAL STATUS: TTH

PRL 120, 231801 (2018)



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$\sim 13\%$   $\sim 12\%$   
22% combined

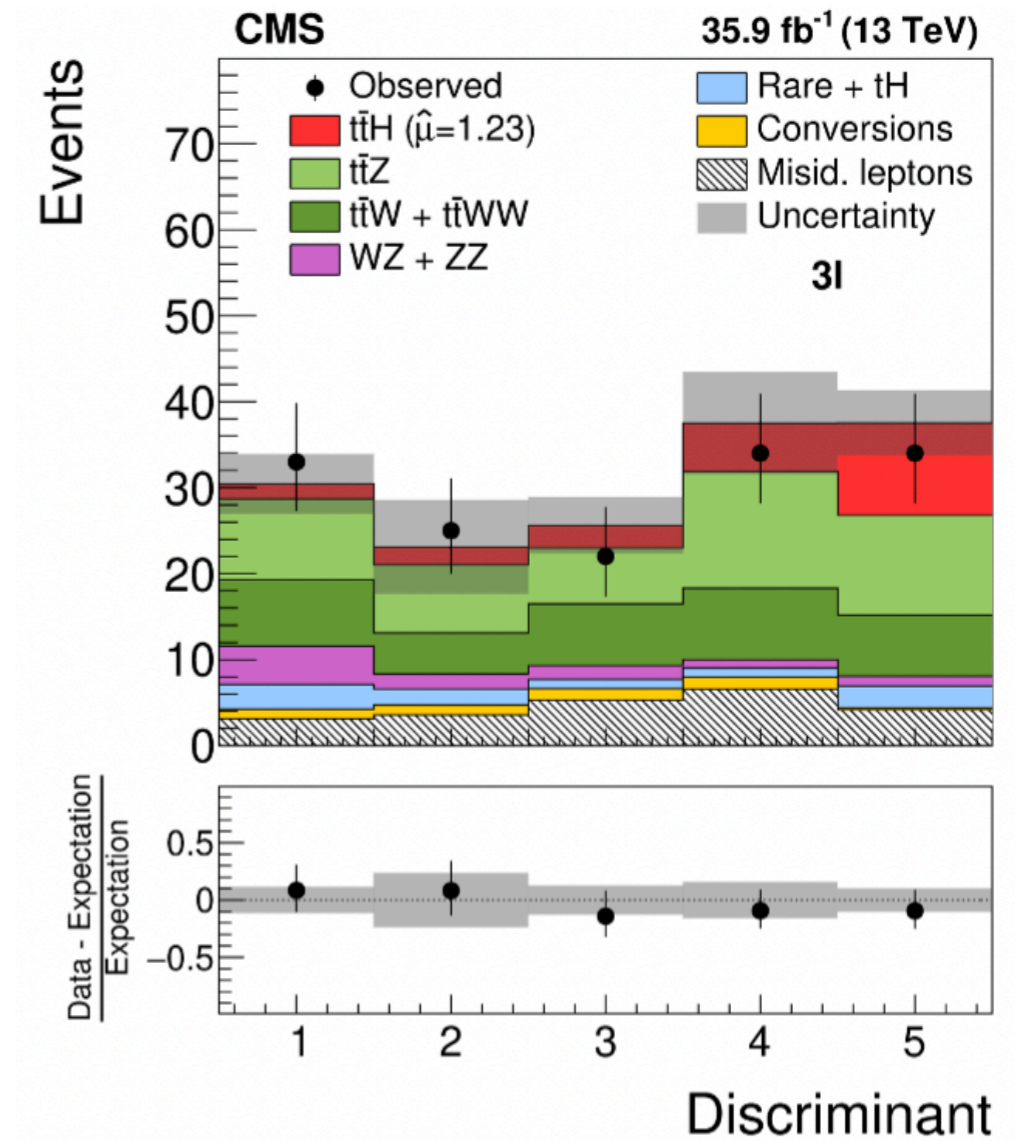
➔ Experimental uncertainty challenges the theory prediction.



# EXPERIMENTAL STATUS: TTZ

Important Background for tth!

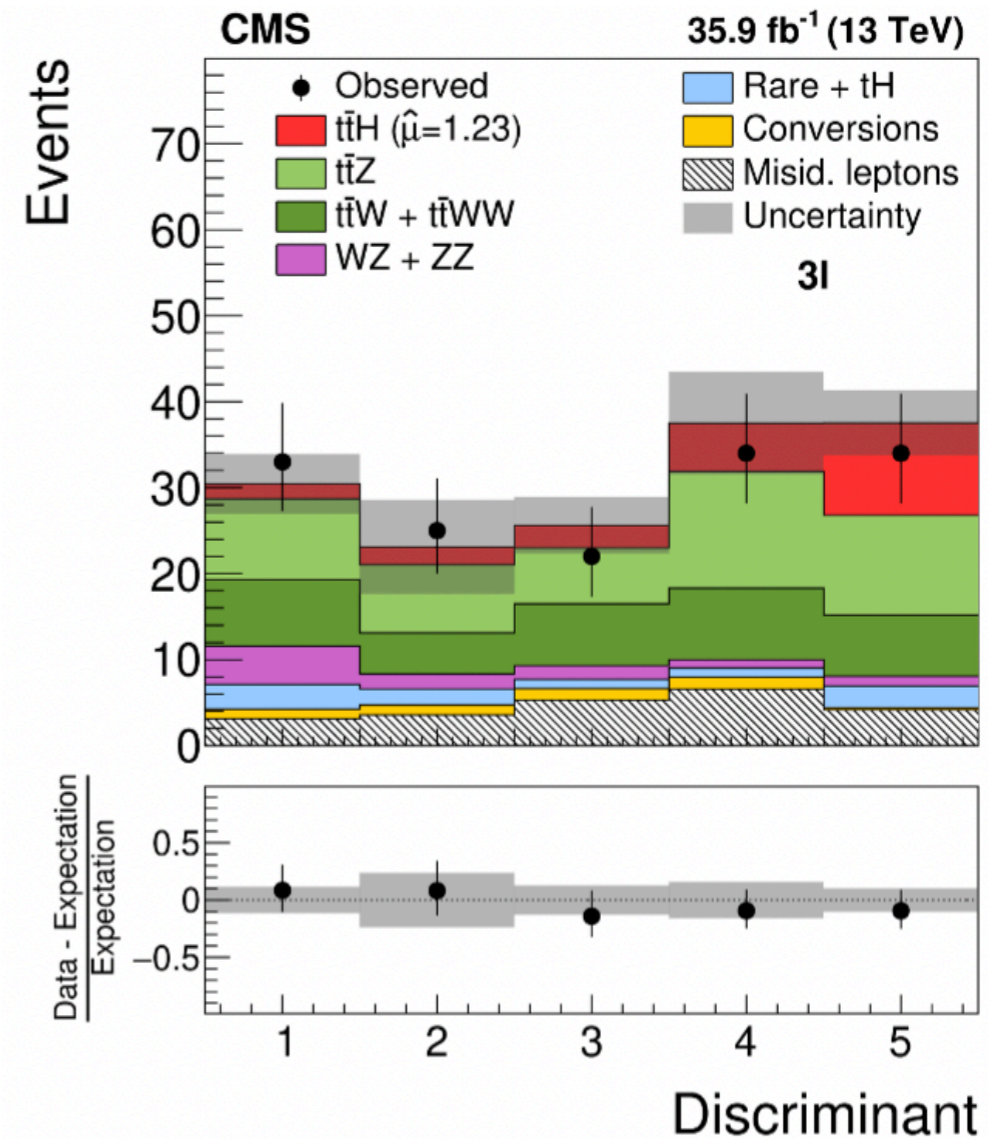
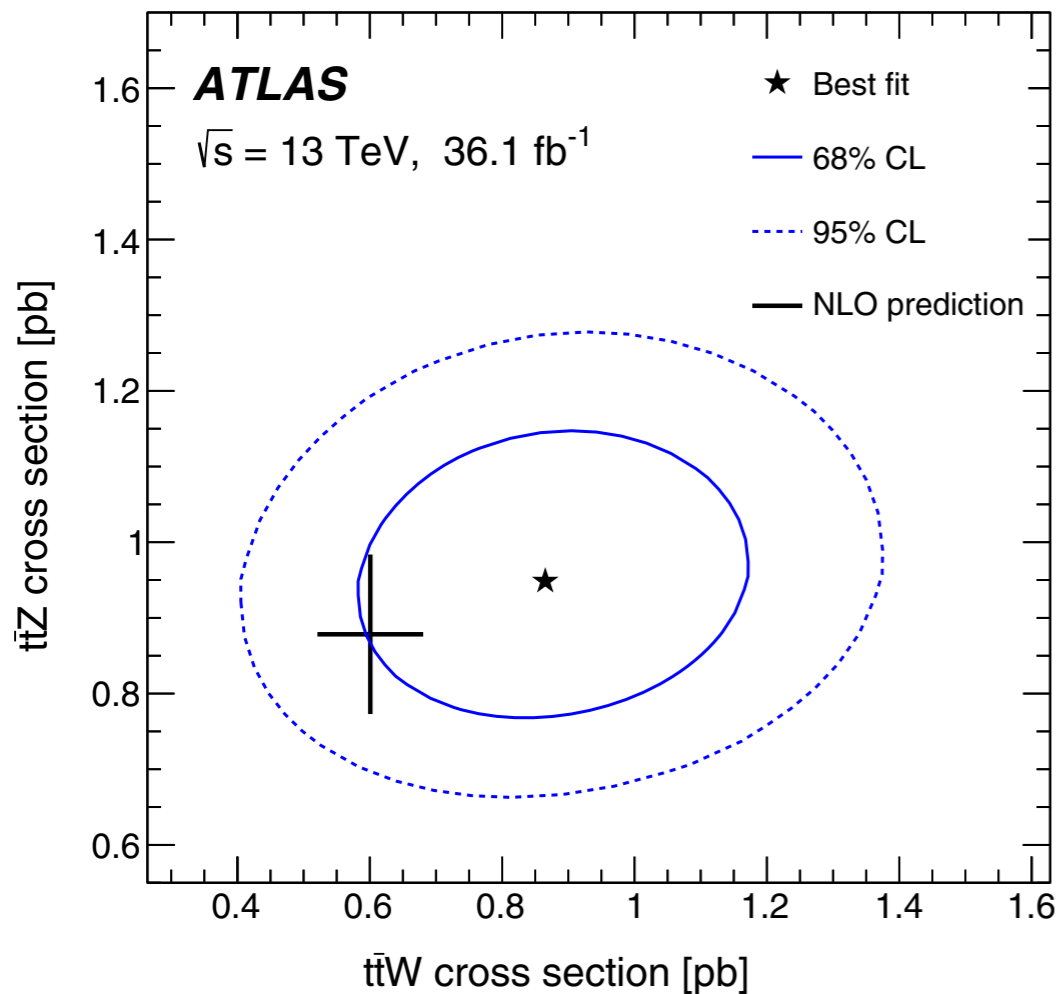
PRL 120(2018)231801



# EXPERIMENTAL STATUS: TTZ

Important Background for tth!

PRL 120(2018)231801



$\sigma_{t\bar{t}Z} = 0.95 \pm 0.08(\text{stat}) \pm 0.10(\text{syst}) \text{ pb}$	13%
$\sigma_{t\bar{t}W} = 0.87 \pm 0.13(\text{stat}) \pm 0.14(\text{syst}) \text{ pb}$	22%

PRD 99(2019)072009

Theory Prediction:

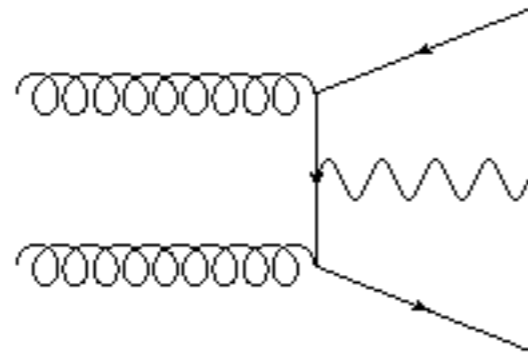
$\sigma_{t\bar{t}Z}^{NLO} = 0.88^{+0.09}_{-0.11} \text{ pb}$        $\sigma_{t\bar{t}W}^{NLO} = 0.6^{+0.08}_{-0.07} \text{ pb}$       13%

→ Need to go to higher theory precision: NNLO

# HIGHER ORDER CORRECTIONS

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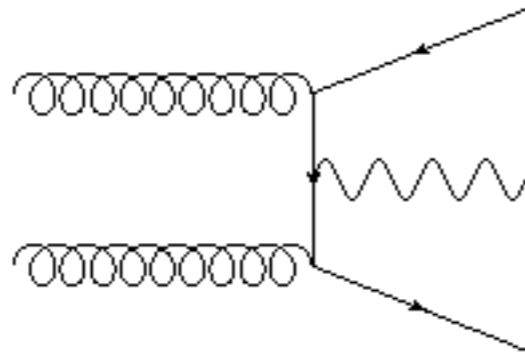
LO:



← Born

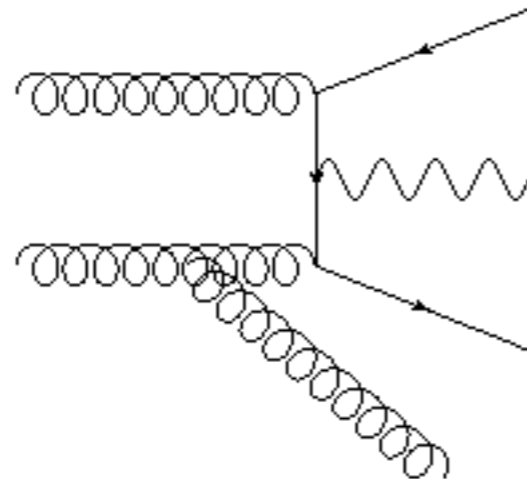
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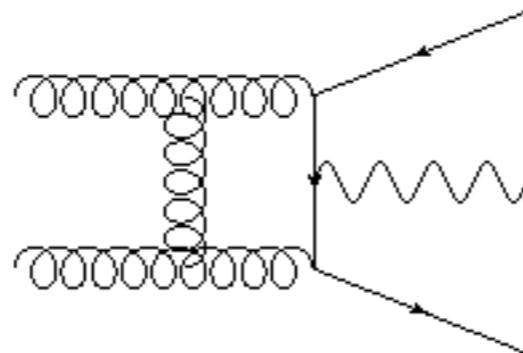


← Born

NLO:



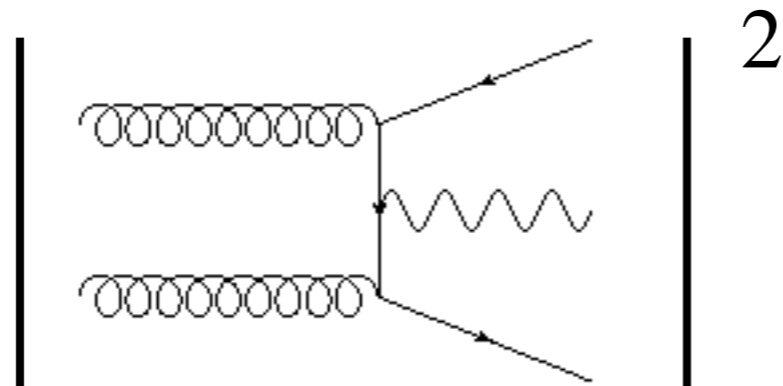
← Real emission radiation



← Loop

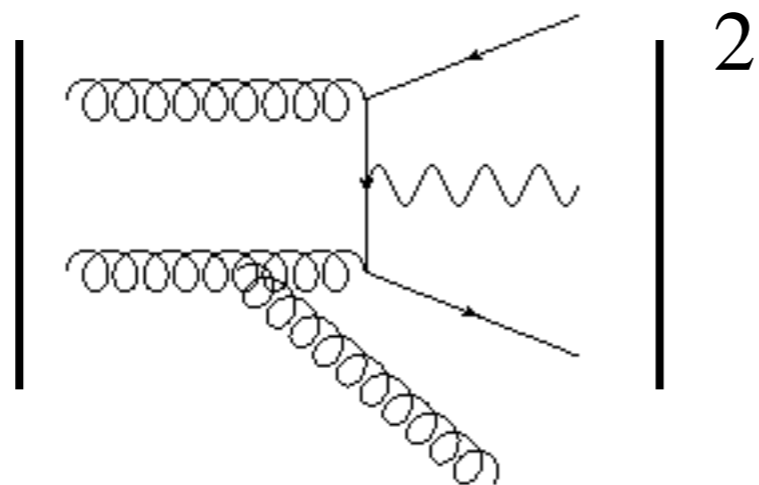
# HIGHER ORDER CORRECTIONS

LO:



← Born

NLO:



← + Real emission radiation

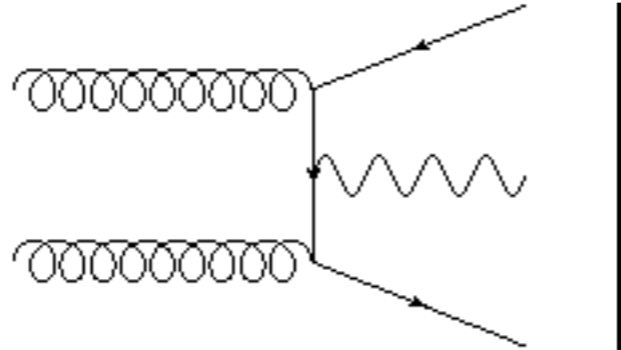
← Loop

$$2 \operatorname{Re} \left( \begin{array}{c} \text{Feynman diagram 1} \\ \text{Feynman diagram 2} \end{array} \right)$$

The equation shows the real part of the sum of two Feynman diagrams, each enclosed in large parentheses. The first diagram is a loop correction where a photon line forms a loop between the two vertices. The second diagram is a loop correction where a photon line forms a loop on the fermion line between the two vertices. The '2 Re' factor indicates that the real part of the sum of these diagrams is taken and multiplied by 2.

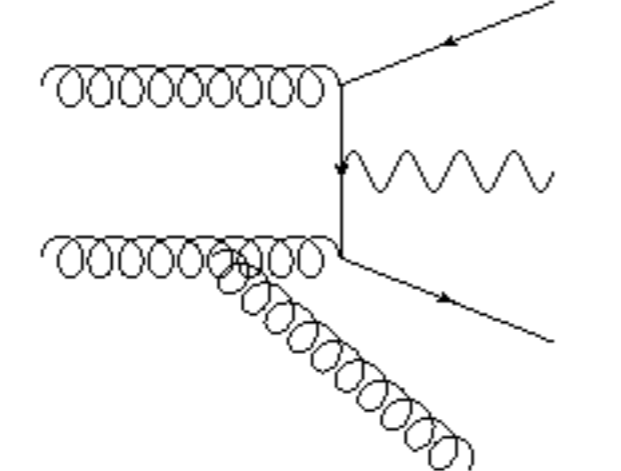
# HIGHER ORDER CORRECTIONS

LO:

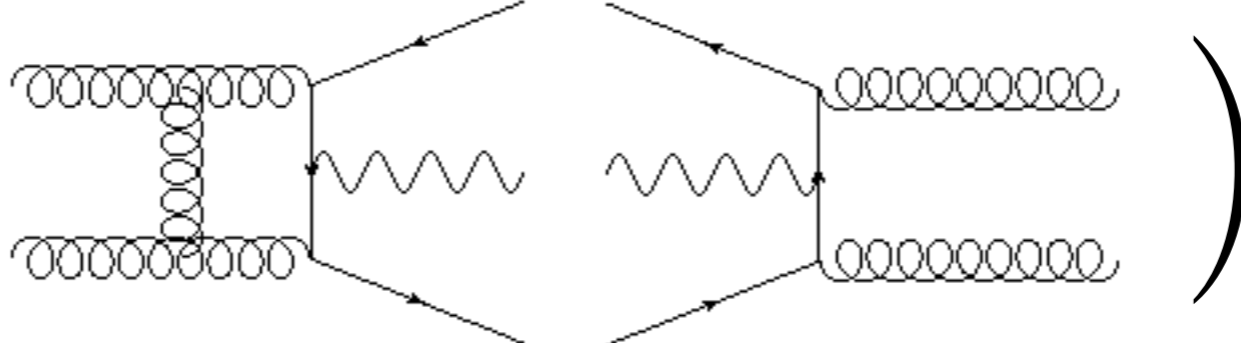
$$\int dPS_F \left| \text{Born} \right|^2$$


← Born

NLO:

$$\int dPS_{F+j} \left| \text{Real emission} \right|^2 + \text{Loop}$$


← Real emission radiation

$$\int dPS_F \ 2 \text{Re} \left( \text{Loop} \right)$$


← Loop

# COMPLICATIONS: SINGULARITIES

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1. UV singularities: Fixed through renormalization. (standard)

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After steps 1 and 2, Loop and Real emission radiation contributions are still separately singular, but the sum of them is finite for *well defined* observables (i.e. *Infrared Safe*).

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1. UV singularities: Fixed through renormalization. (standard)
  2. Initial State Infrared Singularities: Absorbed in parton distribution functions, *PDF*'s. (standard)
- “*Technical complication*”:  
After steps 1 and 2, Loop and Real emission radiation contributions are still separately singular, but the sum of them is finite for *well defined* observables (i.e. *Infrared Safe*).
- ➔ Extra ingredient needed: A “*Recipe*” for combining contributions numerically.

# SUBTRACTION METHODS

---

$$\int_{F+j} \left| \text{Diagram 1} \right|^2 + \int_F 2 \operatorname{Re} \left( \text{Diagram 2} \right)$$

**Divergent**

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# SUBTRACTION METHODS

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$$\int_{F+j} \left[ \left| \text{Diagram 1} \right|^2 - CT \right] + \int_F \left[ 2 \operatorname{Re} \left( \text{Diagram 2} \right) + \int_j CT \right]$$

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Finite

Finite

# HIGHER ORDER CORRECTIONS

NNLO:

$$\int d\text{PS}_{F+jj} \left| \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right|^2 + \int d\text{PS}_{F+j} 2 \operatorname{Re} \left( \begin{array}{cc} \text{---} & \text{---} \\ \text{---} & \text{---} \end{array} \right) + \int d\text{PS}_F 2 \operatorname{Re} \left( \begin{array}{cc} \text{---} & \text{---} \\ \text{---} & \text{---} \end{array} \right) + \left| \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right|^2$$

The diagrammatic representation of the NNLO corrections is as follows:

- First term:** The squared magnitude of the tree-level amplitude,  $\int d\text{PS}_{F+jj} \left| \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right|^2$ , where the diagram shows a quark line splitting into two quarks and a gluon, with a gluon exchange between the two quarks.
- Second term:** The interference between the tree-level amplitude and the one-loop correction,  $\int d\text{PS}_{F+j} 2 \operatorname{Re} \left( \begin{array}{cc} \text{---} & \text{---} \\ \text{---} & \text{---} \end{array} \right)$ . The diagrams show the tree-level process and the one-loop process with a gluon loop on the quark line.
- Third term:** The interference between the tree-level amplitude and the two-loop correction,  $\int d\text{PS}_F 2 \operatorname{Re} \left( \begin{array}{cc} \text{---} & \text{---} \\ \text{---} & \text{---} \end{array} \right)$ . The diagrams show the tree-level process and the two-loop process with a gluon loop on the quark line and a gluon exchange between the quarks.
- Fourth term:** The squared magnitude of the two-loop correction,  $\left| \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} \right|^2$ , where the diagram shows a quark line with two gluon loops and a gluon exchange between the quarks.

# HIGHER ORDER CORRECTIONS

NNLO:

$$\int dPS_{F+jj} \left| \begin{array}{c} \text{[Diagram: Tree-level process with two jets]} \\ \hline \end{array} \right|^2 + \int dPS_{F+j} 2 \operatorname{Re} \left( \begin{array}{c} \text{[Diagram: Single real emission]} \\ \text{[Diagram: Loop correction]} \end{array} \right) + \int dPS_F 2 \operatorname{Re} \left( \begin{array}{c} \text{[Diagram: Two loops]} \end{array} \right) + \left| \begin{array}{c} \text{[Diagram: Single real emission]} \\ \hline \end{array} \right|^2$$

Double Real  
Single Real + Loop  
Two Loops

→ Infrared Singularities consequently more involved.

# STATUS OF HIGHER ORDER CORRECTIONS

---

## NLO:

- Tree-level Amplitudes: (Born, real emission radiation)  
Fully automatised.
- One-Loop Amplitudes: Fully automatised.
- Subtraction methods: Well established and fully automatised.
  - ➔ Fully automatic NLO computations.



# STATUS OF HIGHER ORDER CORRECTIONS

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## NNLO:

- Tree-level Amplitudes: (Born, real emission radiation)  
Fully automatised.
- One-Loop Amplitudes: Fully automatised.
- Two-Loops Amplitudes: Generically not known (case by case calculation).
- Subtraction methods: Different proposals (e.g. QT-subtraction).
  - ➔ NNLO results available only for certain processes.

# STATUS OF HIGHER ORDER CORRECTIONS

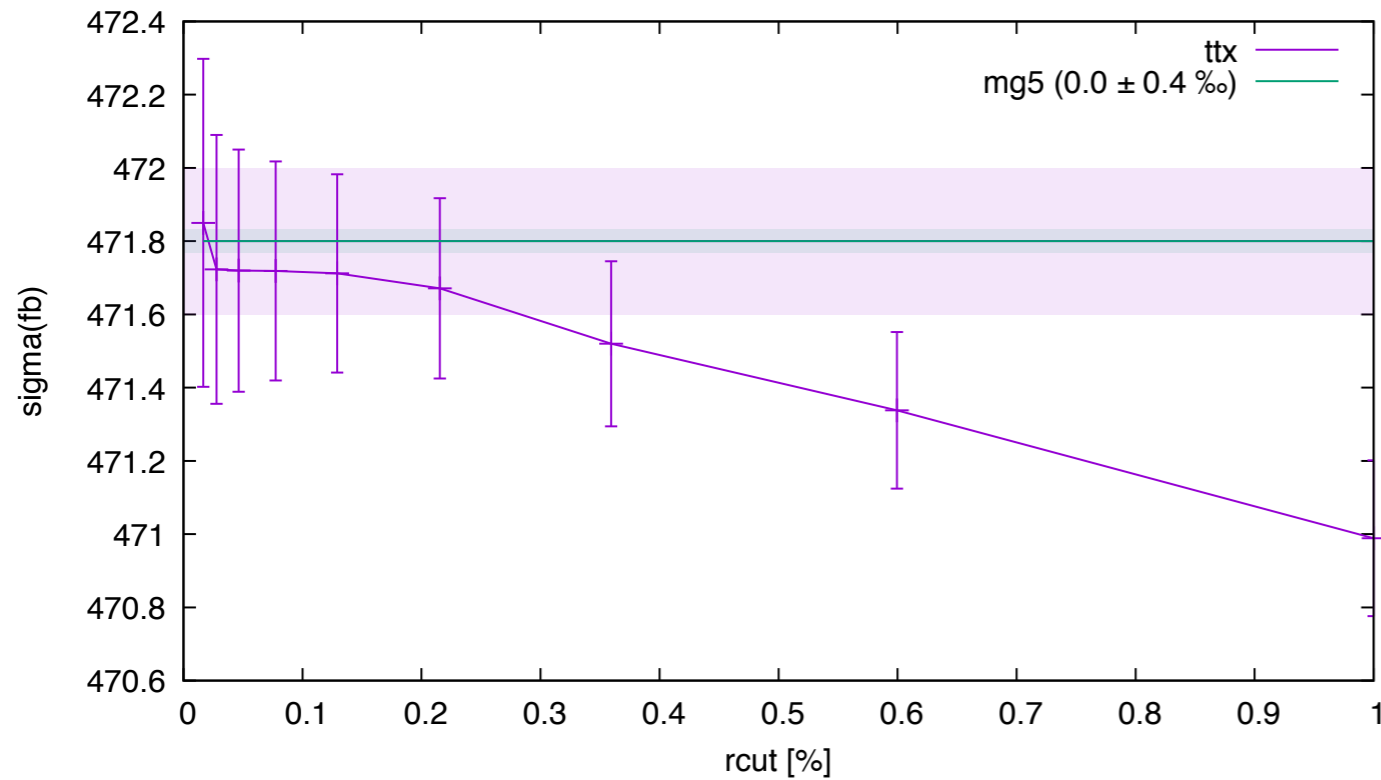
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## TTH and TTZ:

- Tree and One-loop amplitudes available (in our implementation thanks to *OpenLoops*).
- Two Loop amplitudes not known at the moment.
- Handling of infrared singularities:
  - ➔ Extension of the QT-subtraction method to  $tt$ +colorless currently under work: NLO validation completed and NNLO on the way.

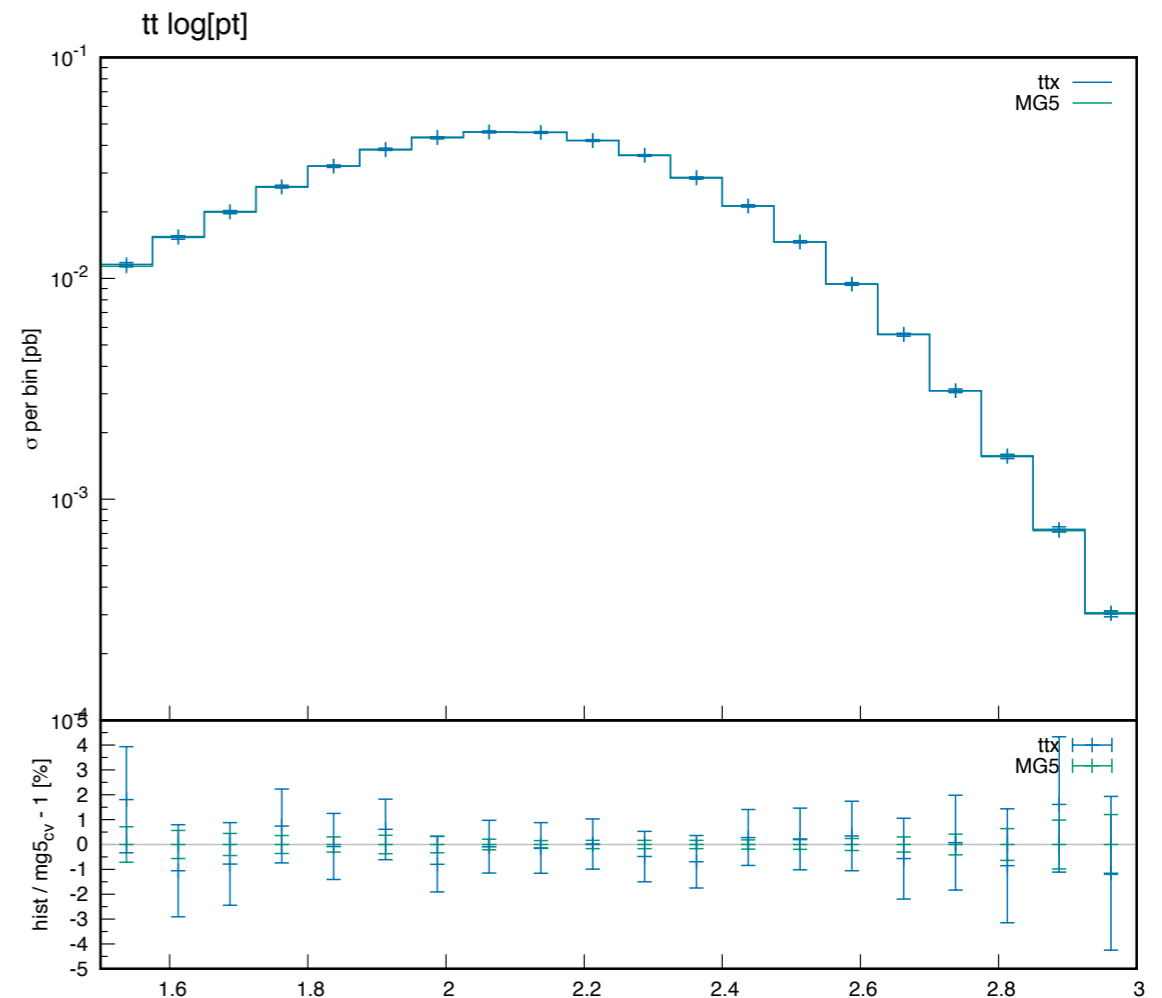
# PRELIMINARY RESULTS: TTH NLO

tth



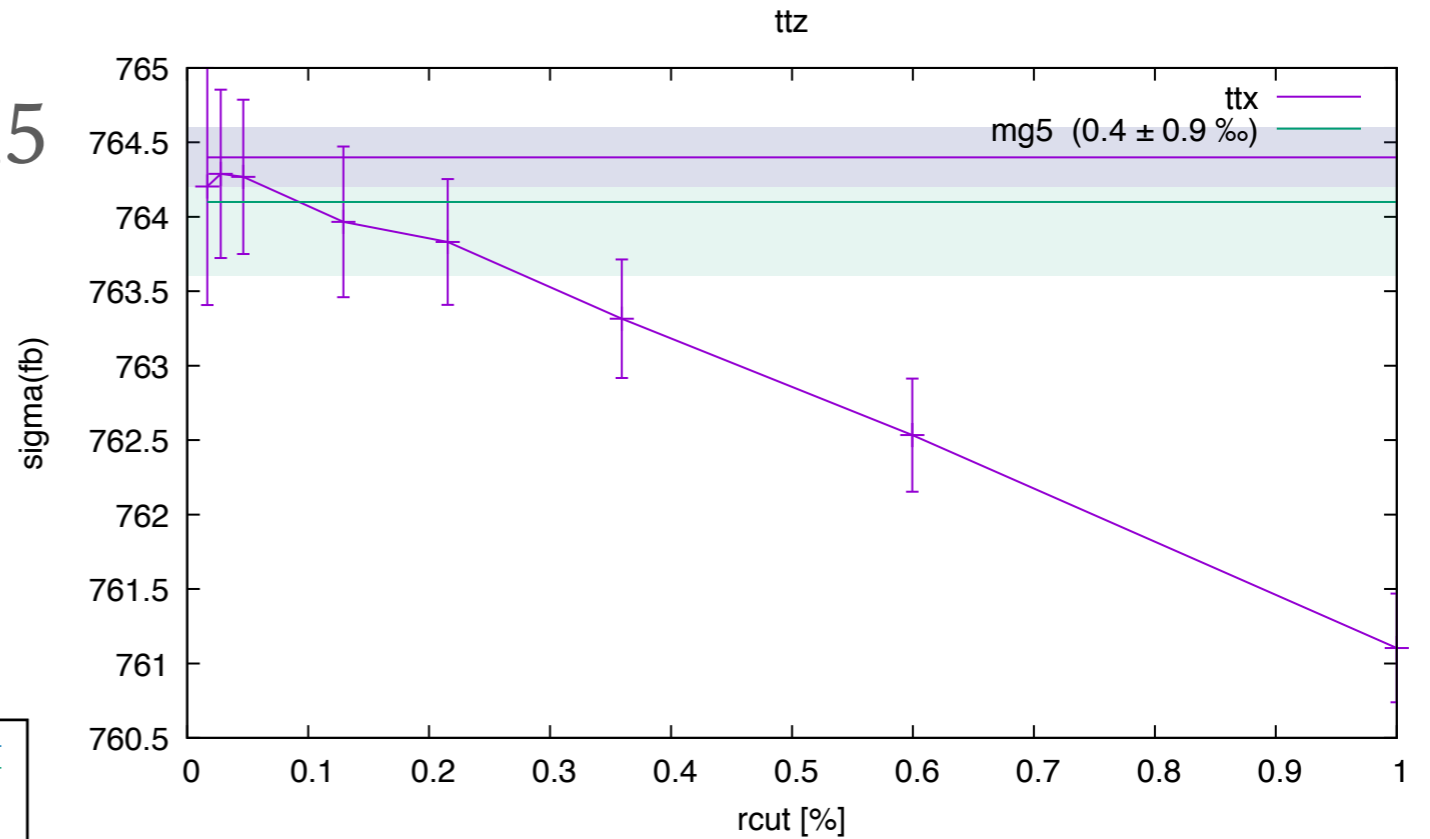
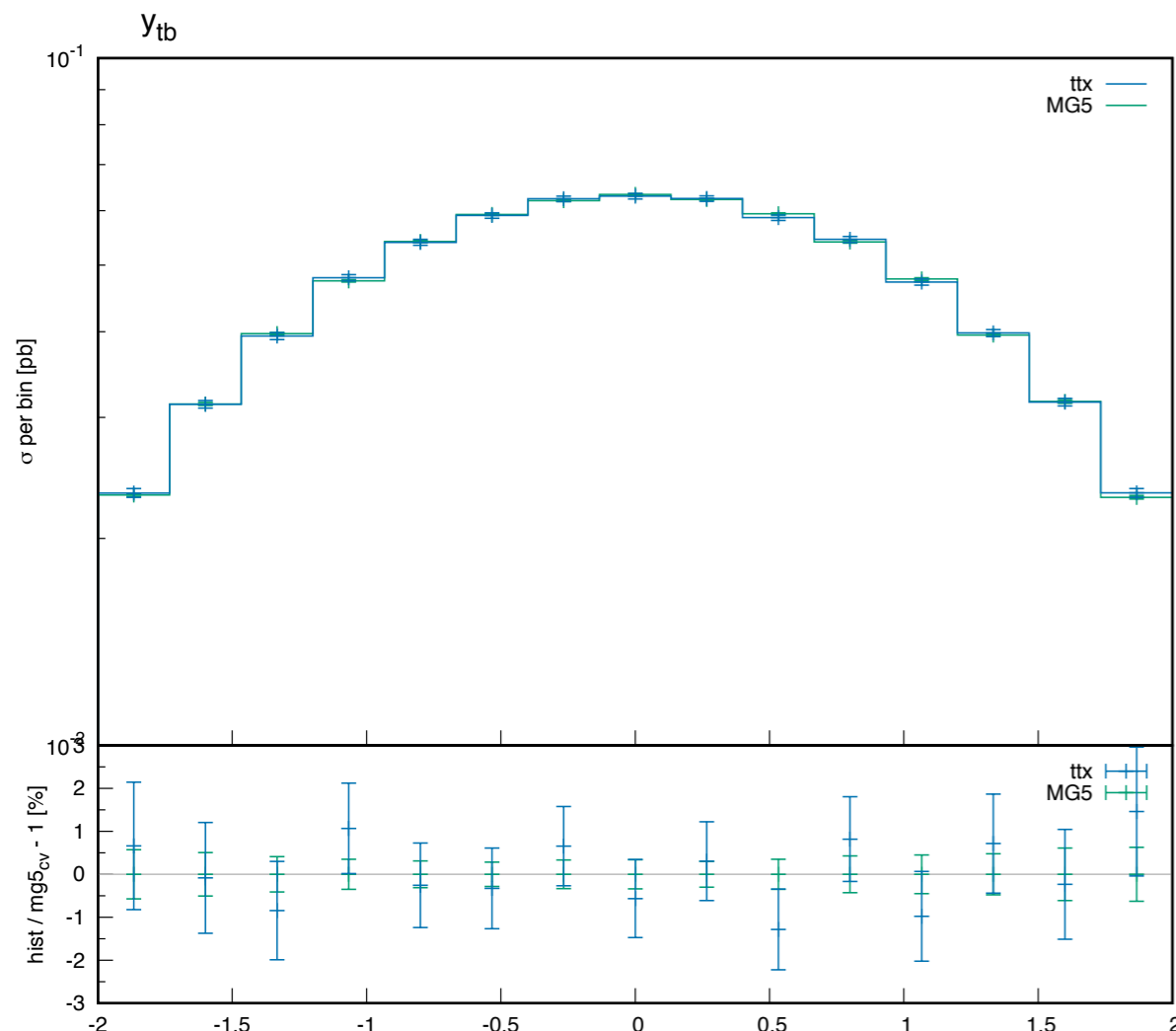
- Agreement with MadGaph5 within sub-permill numerical precision for the inclusive cross section.

- Fully agreement in differential distributions within percent-level numerical precision.



# PRELIMINARY RESULTS: TTZ NLO

- Agreement with MadGraph5 with a per-mill numerical precision for the inclusive cross section.



- Fully agreement in differential distributions within percent-level numerical precision (that could be lowered with more runtime of the MC).

# SO FAR...

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The NLO counter-term and soft function ( $\sim$  integrated counter-term) has been fully implemented for  $t\bar{t}$ +colorless within the QT-subtraction framework, finding perfect agreement with available software for  $t\bar{t}$ ,  $t\bar{t}h$  and  $t\bar{t}z$ .

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The NNLO counter-term has been implemented for  $t\bar{t}$ +colorless and checked in the  $t\bar{t}$  case. Work is being done to check that it works for  $t\bar{t}h$  and  $t\bar{t}z$ .

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Future work might involve the calculation of the NNLO soft function, and a full implementation in a Monte-Carlo framework to get phenomenological results.

The only missing ingredient would be the two-loop amplitudes which, thanks to recent advances in numerical techniques, we might obtain in not too far a future.





# QUESTIONS