



Testing the Standard Model in beta-decay: status and prospects

PSI 2016

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Outline

- **Exotic weak currents**
 - scalar / tensor contributions
 - β - ν correlation / beta asymmetry measurements
- **Nuclear / neutron beta decay** versus **LHC**
- **Weak magnetism**
- **Beta spectrum shape measurements**

1. Exotic weak currents (scalar, tensor)

a) β - ν correlation

$$a \frac{\vec{p}_e \cdot \vec{q}}{E_e E_\nu} \xrightarrow{\text{exp.}} \tilde{a} = \frac{a}{1 + b \frac{\gamma m_e}{E_e}} \quad \text{with } \gamma = \sqrt{1 - (\alpha Z)^2}$$

$$a_F \cong 1 - \frac{|C_S|^2 + |C'_S|^2}{|C_V|^2}$$
$$a_{GT} \cong -\frac{1}{3} \left[1 - \frac{|C_T|^2 + |C'_T|^2}{|C_A|^2} \right]$$

$$b_F \cong \text{Re} \frac{C_S + C'_S}{C_V}$$

Fierz term

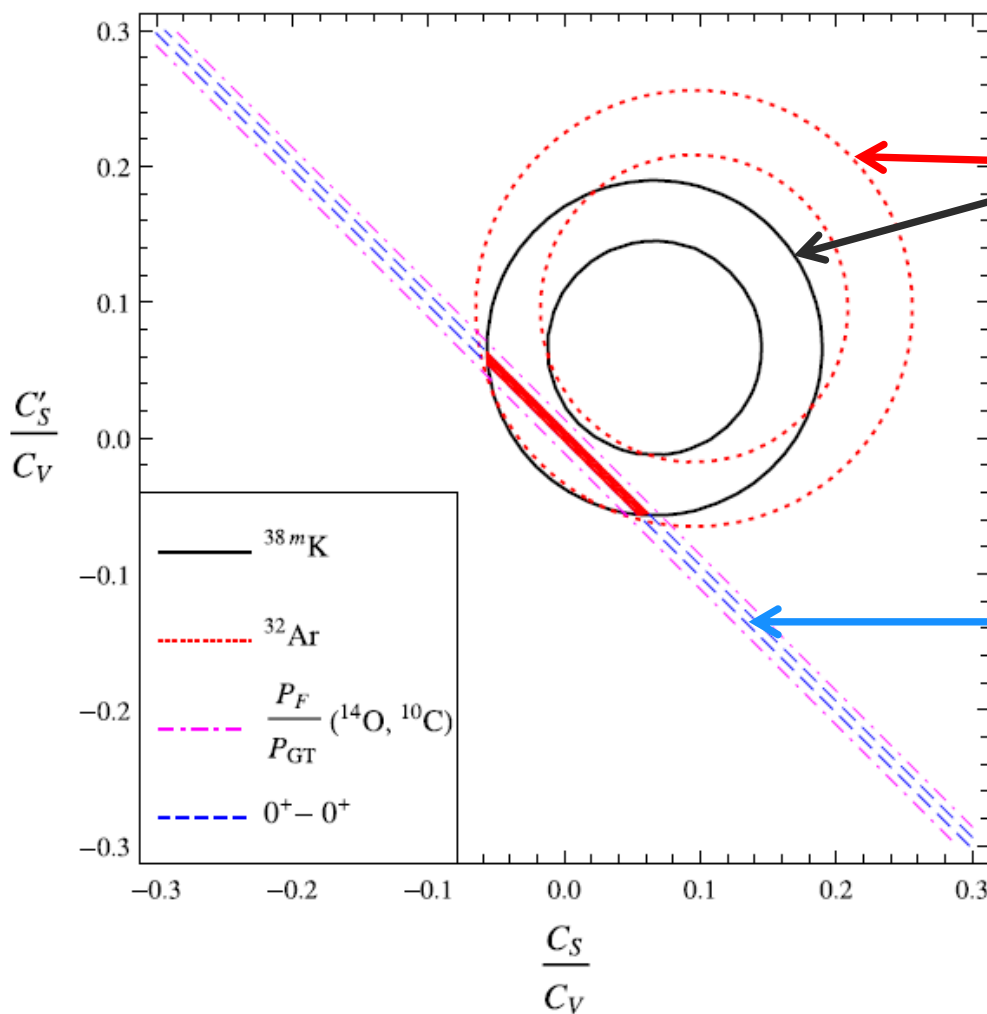
$$b_{GT} \cong \text{Re} \frac{C_T + C'_T}{C_A}$$

!!! for pure transitions weak interaction results are independent of nuclear matrix elements !!!

(assuming maximal P-violation and T-invariance for V and A interactions)

recoil corr. (induced form factors) $\approx 10^{-3}$; radiative corrections $\approx 10^{-4}$

Limits on scalar currents



$$a_F \cong 1 - \frac{|C_S|^2 + |C'_S|^2}{|C_V|^2}$$

^{32}Ar : Adelberger et al., PRL 83 (1999) 1299

^{38m}K : Gorelov, Behr et al., PRL 94 (2005) 142501

$$\mathcal{F}t^{0^+ \rightarrow 0^+} = \frac{K}{2G_F^2 V_{ud}^2 C_V^2 (1 + \Delta_R^V)} \frac{1}{(1 + b'_F)}$$

with

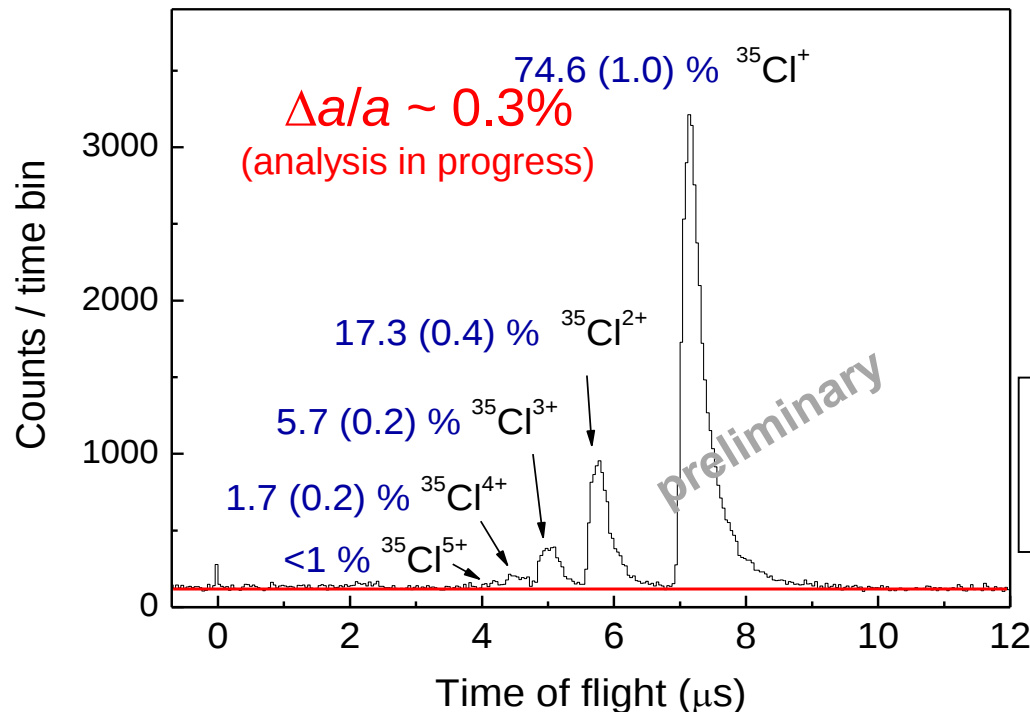
$$b'_F = \frac{\gamma m_e}{\langle E_e \rangle} \left(\frac{C_S + C'_S}{C_V} \right) \quad (\text{Fierz term})$$

Hardy & Towner, Phys. Rev. C 91 (2015) 025501

B. R. Holstein, J. Phys. G 41 (2014) 114001

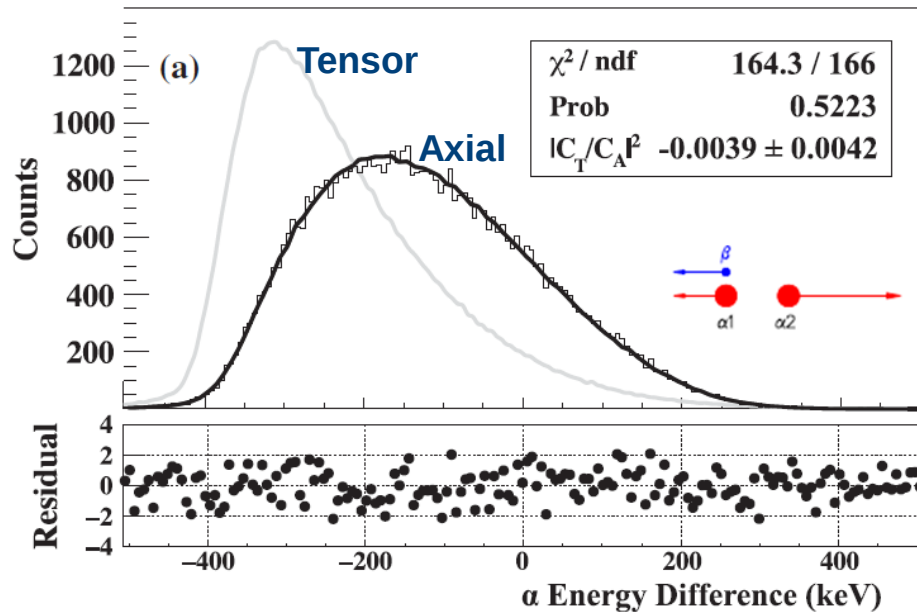
ongoing experiments in search for **scalar** weak currents:

- TRINAT (MOT): ^{38m}K repeat (prep.)
- LPCTrap @ GANIL (Paul): ^{19}Ne , ^{35}Ar (analysis)
- Jerusalem (MOT): ^{19}Ne (prep.)
- TamuTrap, Texas A&M (Penning): ^{32}Ar , ... ($T = 2$, βp) (prep.)
- WISARD @ ISOLDE (foil): ^{32}Ar , ... ($T = 2$, βp) (prep.)



^{35}Cl charge state distrib.
from the β decay of ^{35}Ar
(LPCTrap - GANIL)

Tensor currents - α - β - ν correlation with Paul-trapped ^8Li ions



α -particle breakup of $^8\text{Be}^*$

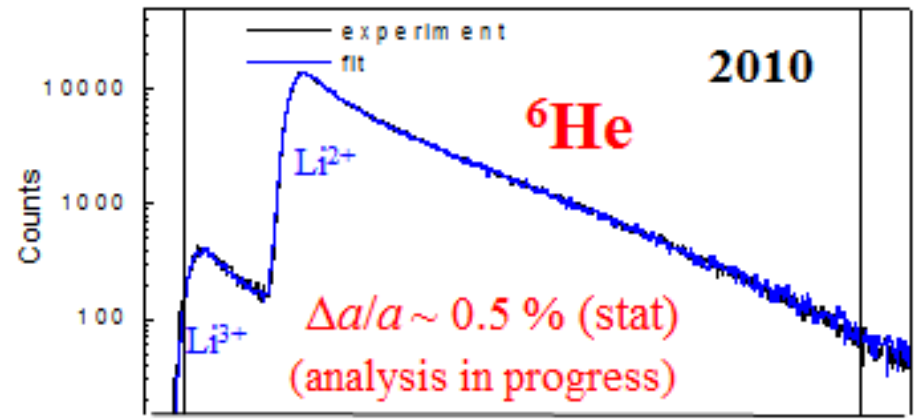
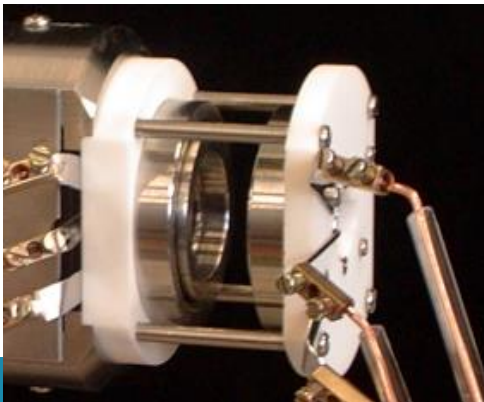
$$a_{\beta\nu} = -0.3342 (26)_{\text{stat}} (29)_{\text{sys}}$$

M.G. Sternberg, G.Savard et al., PRL 115 (2015) 182501

Tensor currents - LPCTrap @ GANIL - ^6He

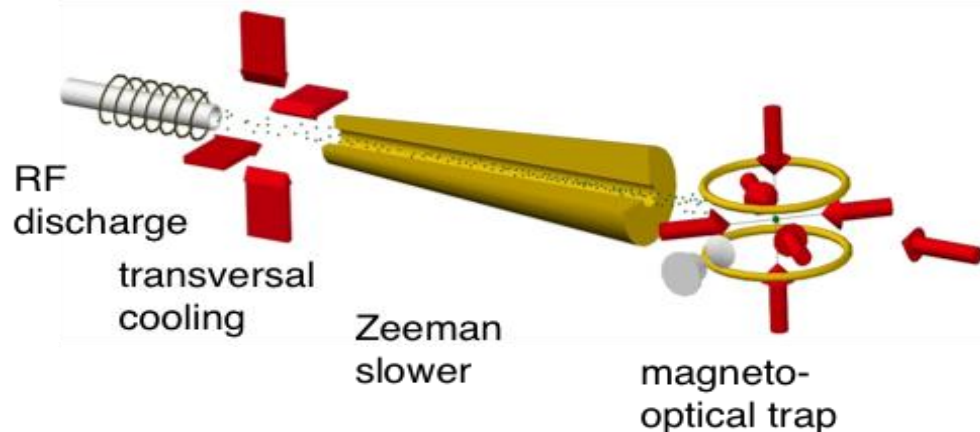
2006 (^6He): $a_{\beta\nu} = -0.3335(73)_{\text{stat}}(75)_{\text{syst}}$

X. Fléhard et al. J. Phys. G 38 (2011) 055101



Tensor currents - ${}^6\text{He}$ MOT Trap setup @ Univ. Washington, Seattle

P. Mueller, A. Garcia, et al.



0.1 % measurement - 2015

A. Knecht et al., NIM A 660 (2011) 43, Phys .Rev. C 86 (2012) 035506 & arXiv:1208.6433v2 [nucl-ex]

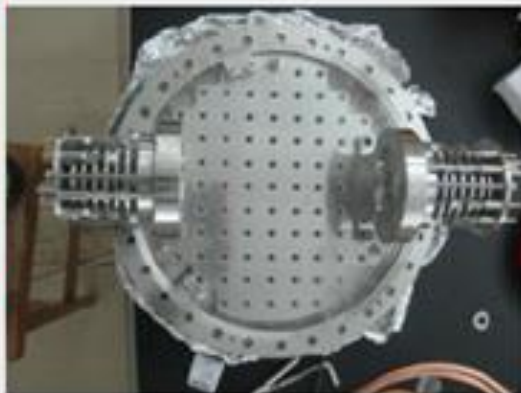
Tensor currents - ${}^6\text{He}$ EIB Trap (Weizmann Inst., Univ. Jerusalem, ...)

(M. Hass, G. Ron et al.)

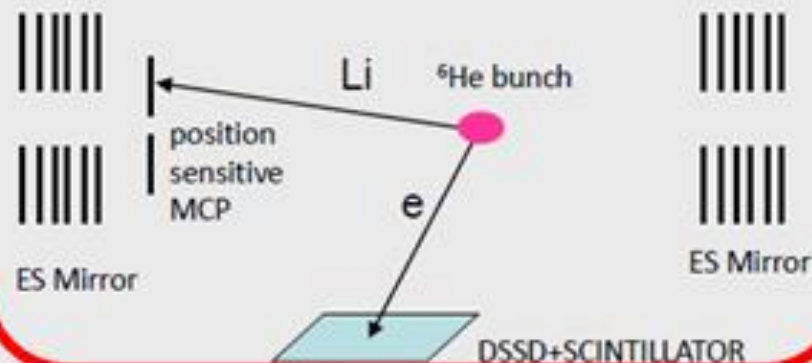
O. Aviv et al., J. Phys.: Conf. Ser. 337, 012020 (2012)



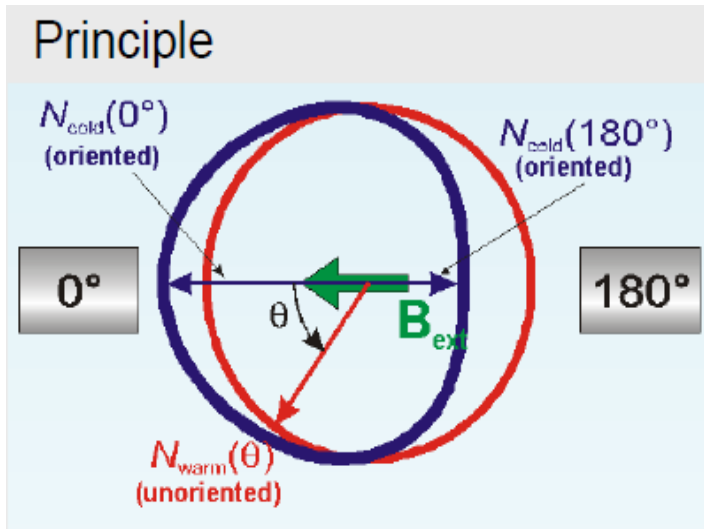
Electrostatic
Ion Beam
Trap



Principle: determine complete kinematics



b) β -asymmetry parameter in nuclear beta decay



$$W(\theta) = \frac{N(\theta)_{\text{pol}}}{N(\theta)_{\text{unpol}}} = 1 + \tilde{A} \quad P \quad \frac{v}{c} \quad Q \cos\theta$$

(P from independent meas.)

Geant4

$$\tilde{A} = \frac{A}{1 + b'_{GT}} \quad \text{with} \quad b'_{GT} = \frac{\gamma m_e}{\langle E_e \rangle} \left(\frac{C_T + C'_T}{C_A} \right)$$

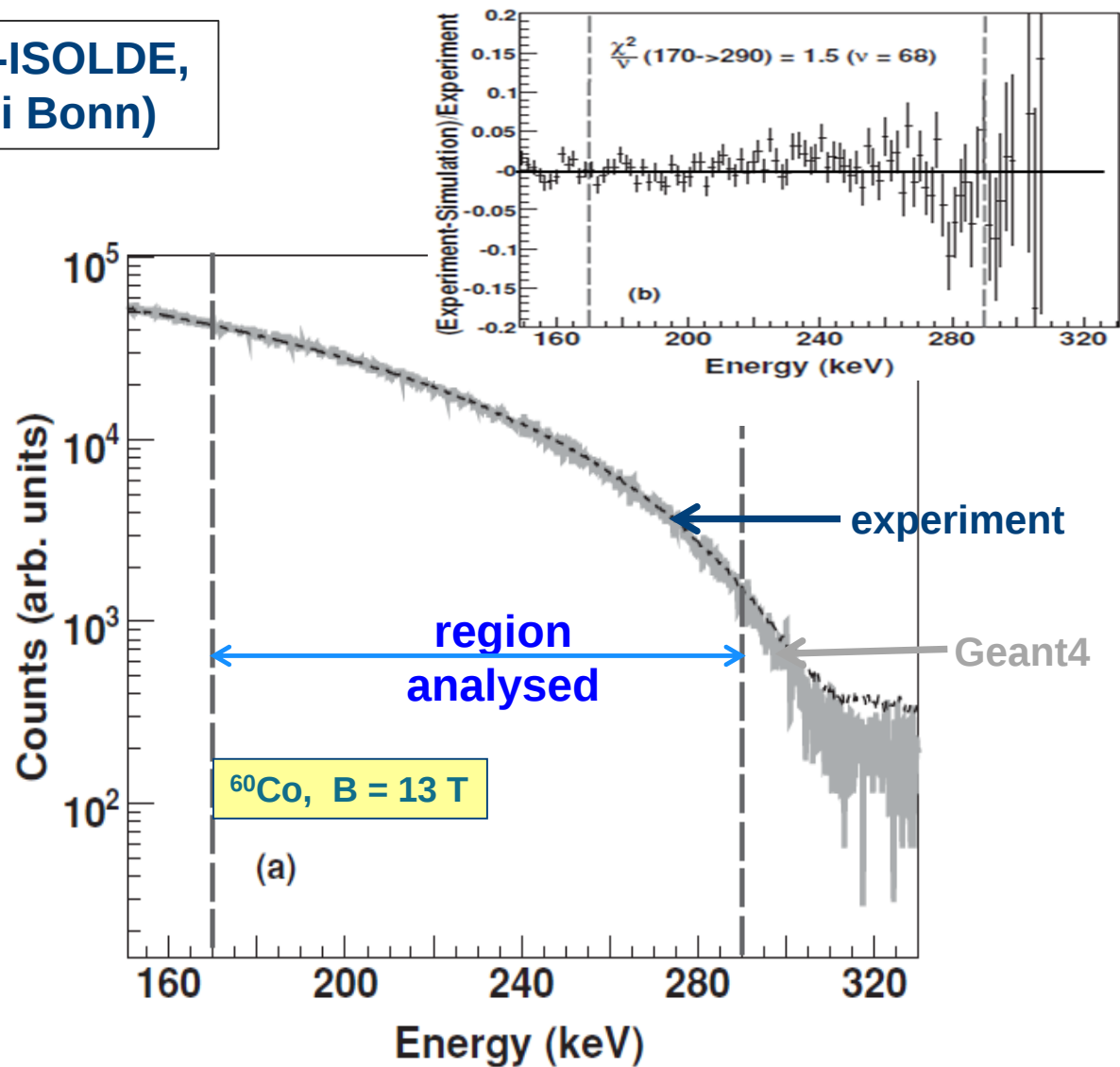
Analysis:

$$\frac{[W(\theta) - 1]_{\text{exp}}}{[W(\theta) - 1]_{\text{Geant}}} = \frac{\left[\tilde{A} \quad P \quad \frac{v}{c} \quad Q \cos\theta \right]_{\text{exp}}}{\left[\tilde{A}_{\text{SM}} \quad P \quad \frac{v}{c} \quad Q \cos\theta \right]_{\text{Geant}}} = \frac{\tilde{A}}{\tilde{A}_{\text{SM}}}$$

(KU Leuven, NICOLE-ISOLDE,
NPI Rez-Prague, Uni Bonn)



^3He - ^4He dilution refrigerator set-up



F. Wauters et al.,
Phys. Rev. C 82 (2010) 055502
Nucl. Instr. Meth. A 604 (2009) 563

$^{60}\text{CoCu}$, $B_{\text{ext}} = 13 \text{ T}$

$^{114}\text{InFe}$, $B_{\text{hf}} = 27 \text{ T}$

$^{67}\text{CuFe}$, $B_{\text{hf}} = 21 \text{ T}$

$$A_{\text{exp}}(^{60}\text{Co}) = -1.014(12)_{\text{stat}}(16)_{\text{syst}}$$

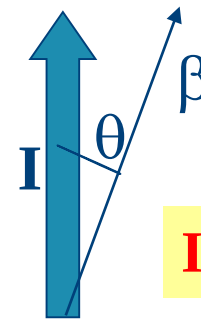
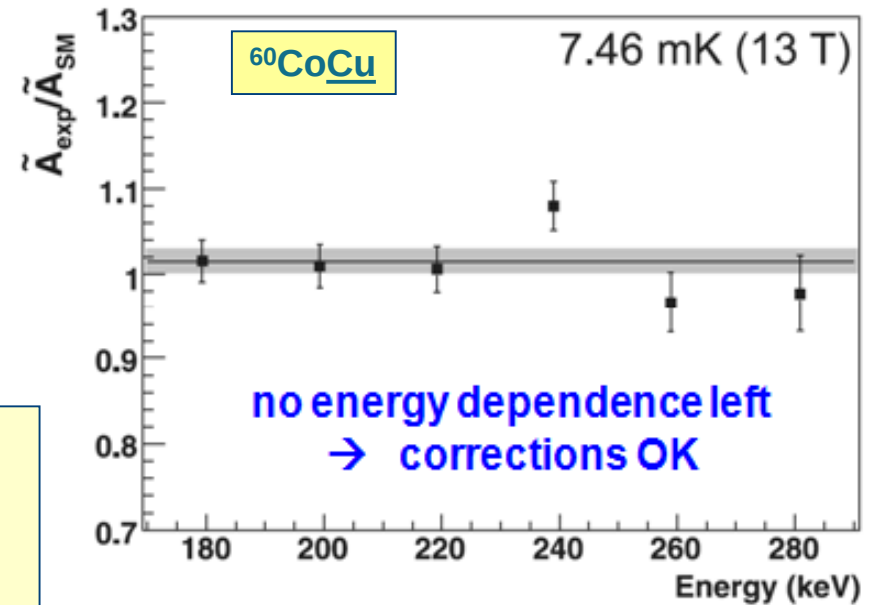
F. Wauters et al., Phys. Rev. C 82 (2010) 055502

$$A_{\text{exp}}(^{114}\text{In}) = -0.990(10)_{\text{stat}}(10)_{\text{syst}}$$

F. Wauters et al., Phys. Rev. C 80 (2009) 062501(R)

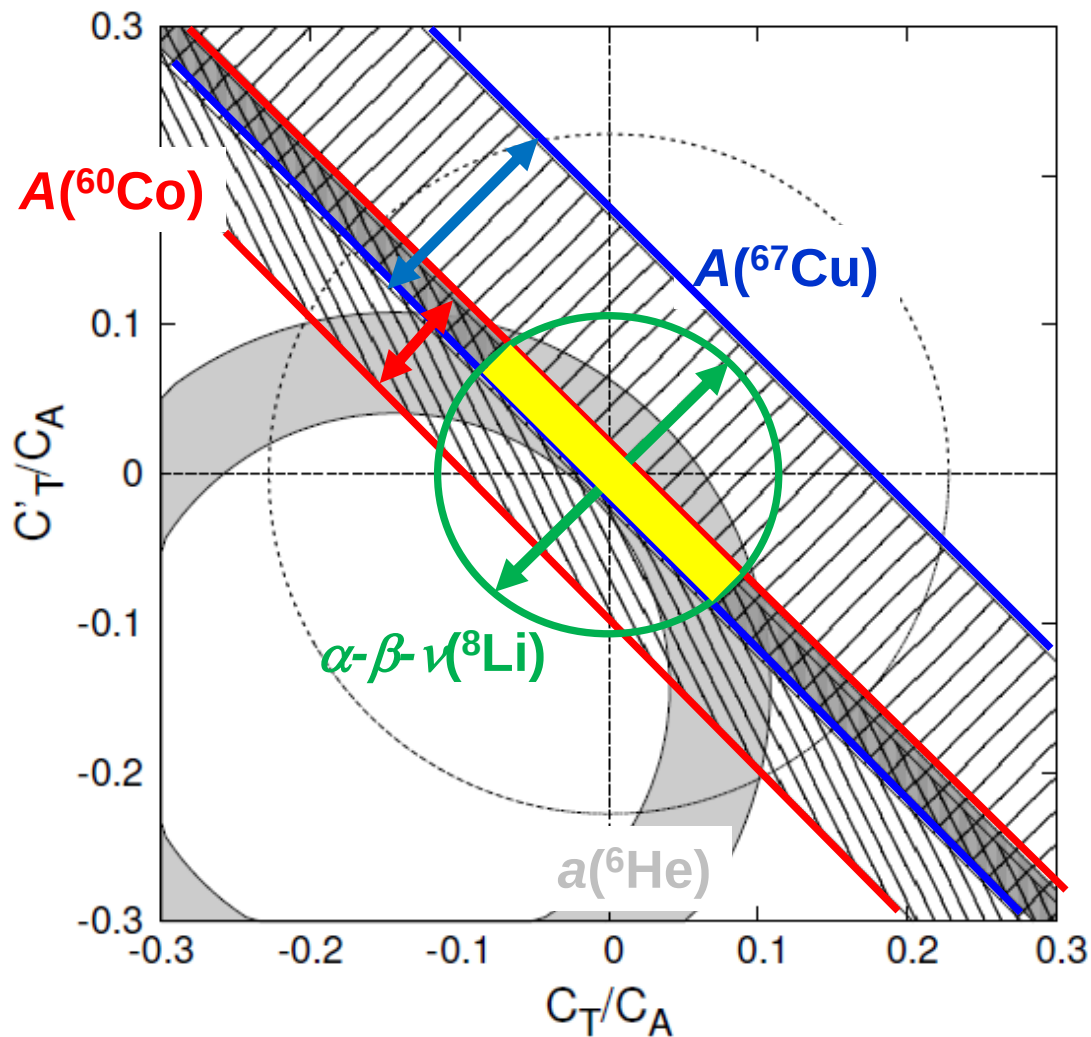
$$A_{\text{exp}}(^{67}\text{Cu}) = 0.587(8)_{\text{stat}}(12)_{\text{syst}}$$

G. Soti et al., Phys. Rev. C 90 (2014) 035502



IS431-experiment

Limits on tensor currents



$a(^6\text{He})$

C. Johnston et al.,
PR 132 (1963) 1149

$\alpha\text{-}\beta\text{-}\nu(^8\text{Li})$

M.G. Sternberg, G.Savard et al.,
PRL 115 (2015) 182501

$A(^{60}\text{Co})$

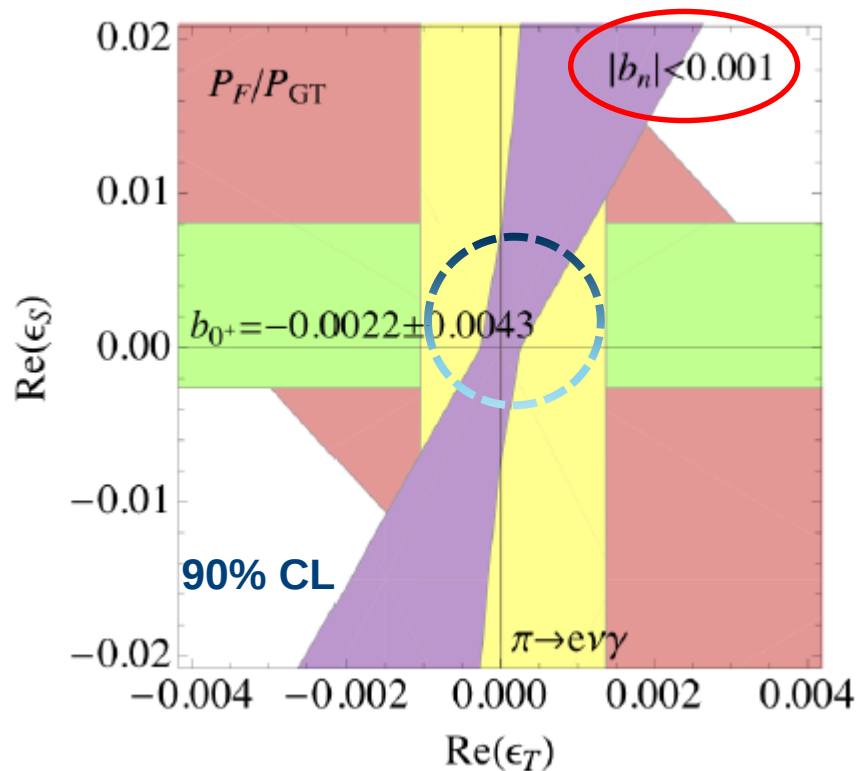
F. Wauters, N.S. et al.,
PR C 82 (2010) 055502

$A(^{67}\text{Cu})$

G. Soti, N.S. et al.,
PR C 90 (2014) 035502

Also: Poster F. Lenaers – ^{35}Ar
PhD Behling 2015 – ^{37}K

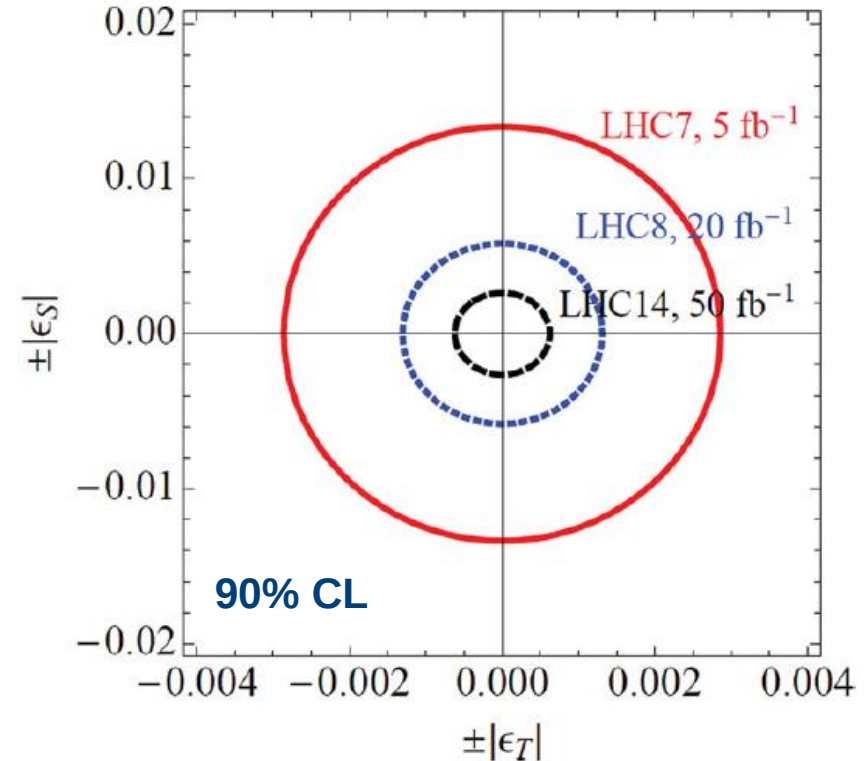
2. Measurements in nuclear/neutron β decay in the LHC era



nuclear and neutron decay, pion decay

O. Naviliat-Cuncic and M. Gonzalez-Alonso
 Annalen der Physik 525 (2013) 600.

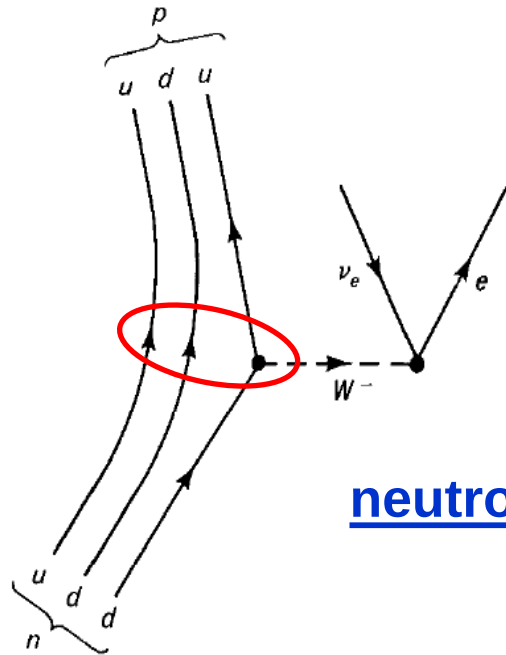
V. Cirigliano, et al.,
 J. High. Energ. Phys. 1302 (2013) 046



limits on scalar/tensor couplings
 obtained by CMS collaboration in
 $pp \rightarrow e + \text{MET} + X$ channel

S. Chatrchyan et al. (CMS Collab.)
 J. High. Energ. Phys. 08 (2012) 023

3. Good knowledge of **induced / recoil terms** required



quark involved in β decay is not free
but **bound in a nucleon**
→ extra terms induced by strong interaction

neutron / nuclear beta decay:

$$V_\mu(q^2) = \bar{p} [g_V(q^2) \gamma_\mu + \overset{\text{weak magnetism } b_{WM}}{g_M(q^2)} \sigma_{\mu\nu} \frac{q_\nu}{2M}] n$$

$$A_\mu(q^2) = \bar{p} [g_A(q^2) \gamma_\mu \gamma_5 + ig_P(q^2) \frac{q_\mu}{m_e} \gamma_5] n$$

→ affects values for **correlation coefficients** at level of **per mil to 1%**

weak magnetism term b_{WM} (CVC)

(N.S. et al., in prep.)

$T = 1/2 \quad J^\pi \rightarrow J^\pi$ mirror β transitions

$$b_{WM}(\beta^\mp) = A \sqrt{\frac{J}{J+1}} M_F^0 \mu^\mp$$

F.P. Calaprice and B.R. Holstein, NP A 273 (1976) 301

$$\mu^\mp = \mp(\mu_M - \mu_D)$$

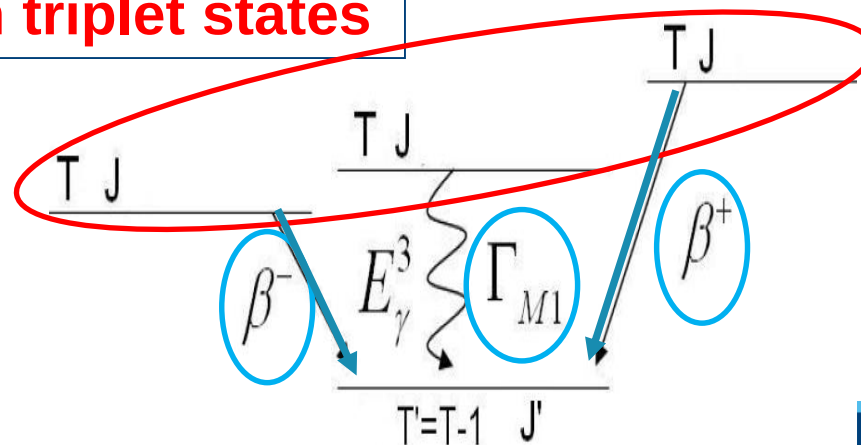
$$c = g_A M_{GT} \text{ from } \mathfrak{I}t\text{-value}$$

N. Severijns, I.S. Towner et al., PR C 78 (2008) 055501

GT β decays of isospin triplet states

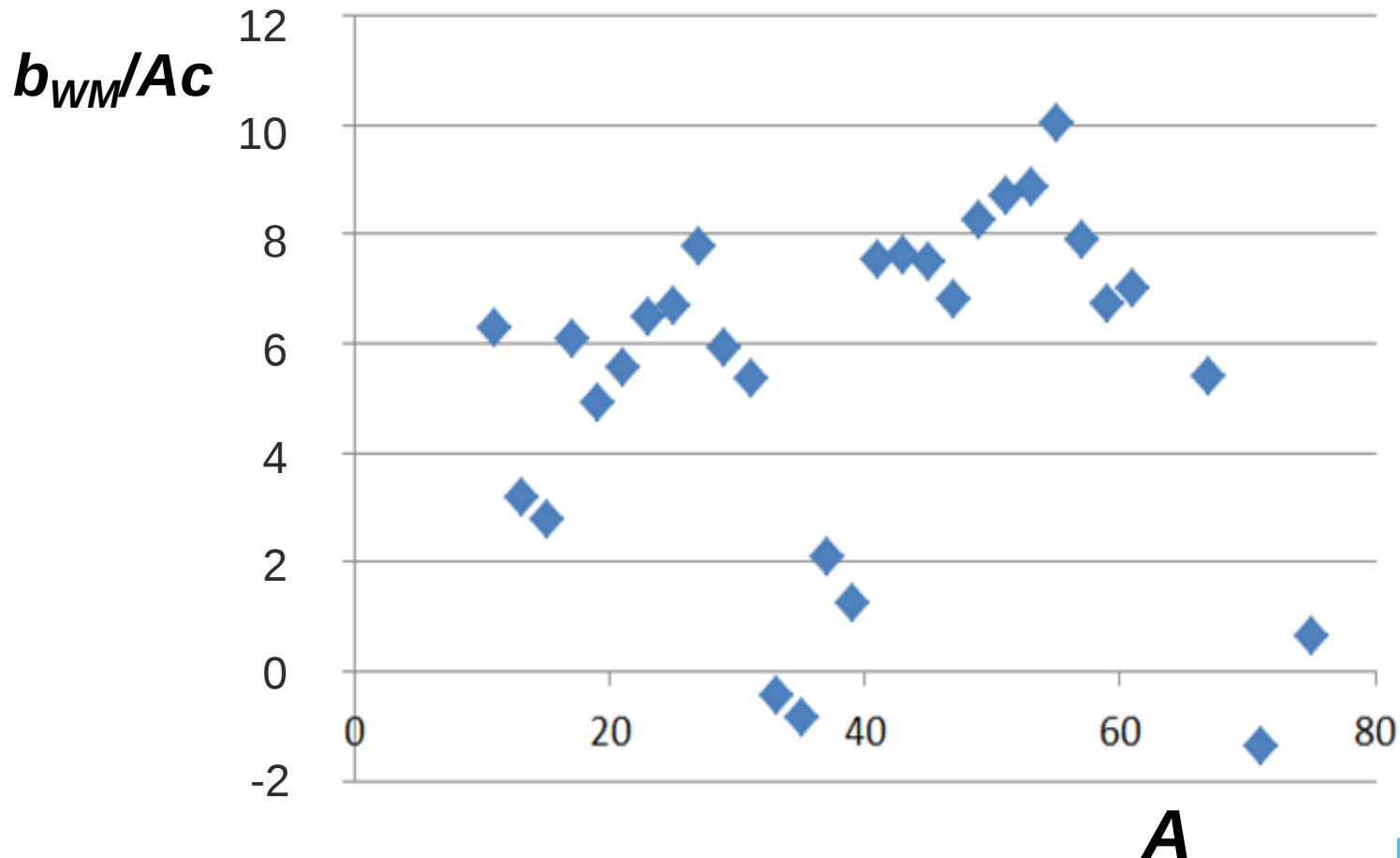
$$b_\gamma^2 = 6 \frac{\Gamma_{M1} M^2}{E_\gamma^3 \alpha}$$

$$c = g_A M_{GT} \text{ from } ft\text{-value}$$



weak magnetism term b_{WM} - experimental data

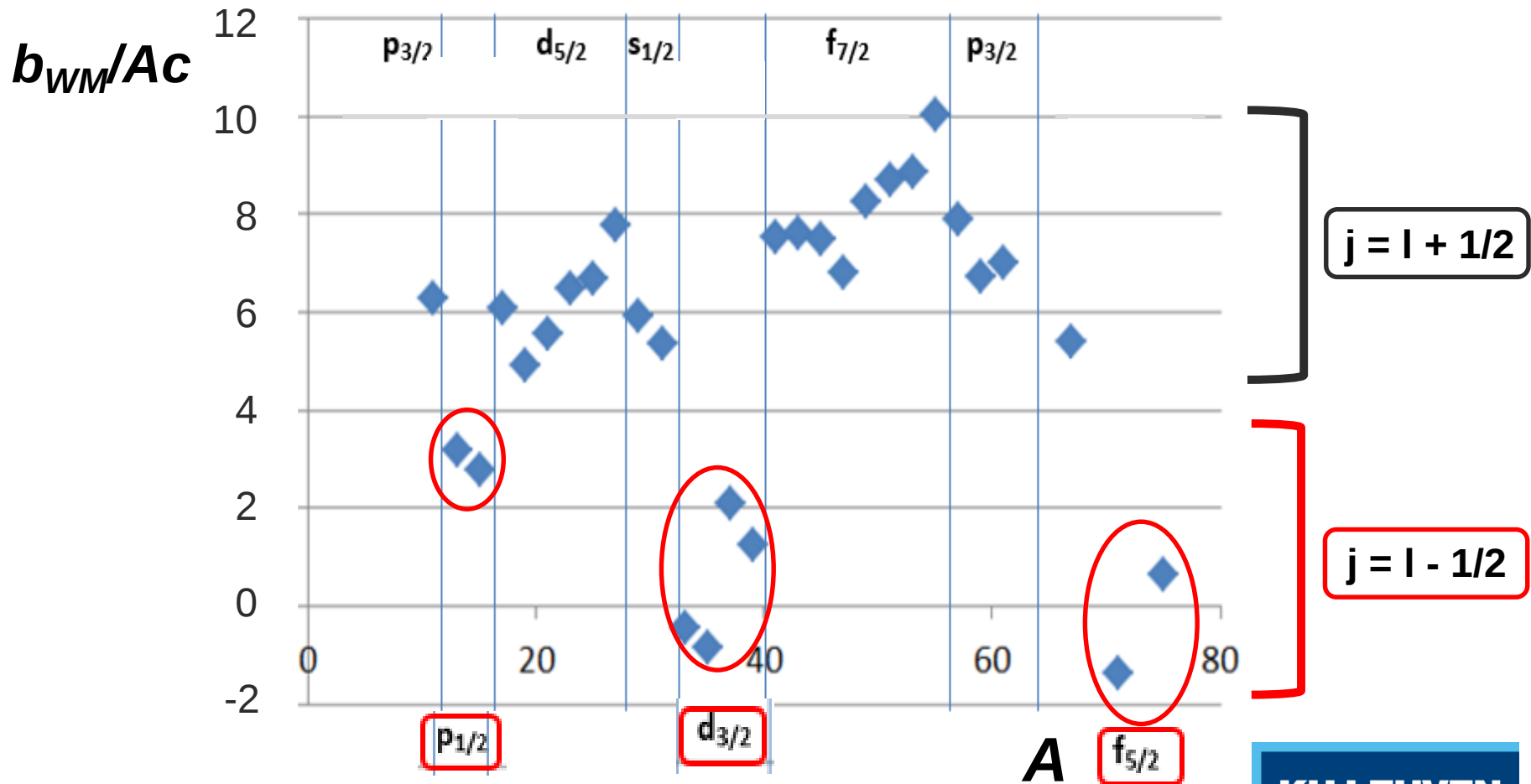
mirror β transitions: - updated Ft-values ($A < 75$; rel. prec. $< 0.2\%$ for $A < 41$)
- extracted weak magnetism form factor



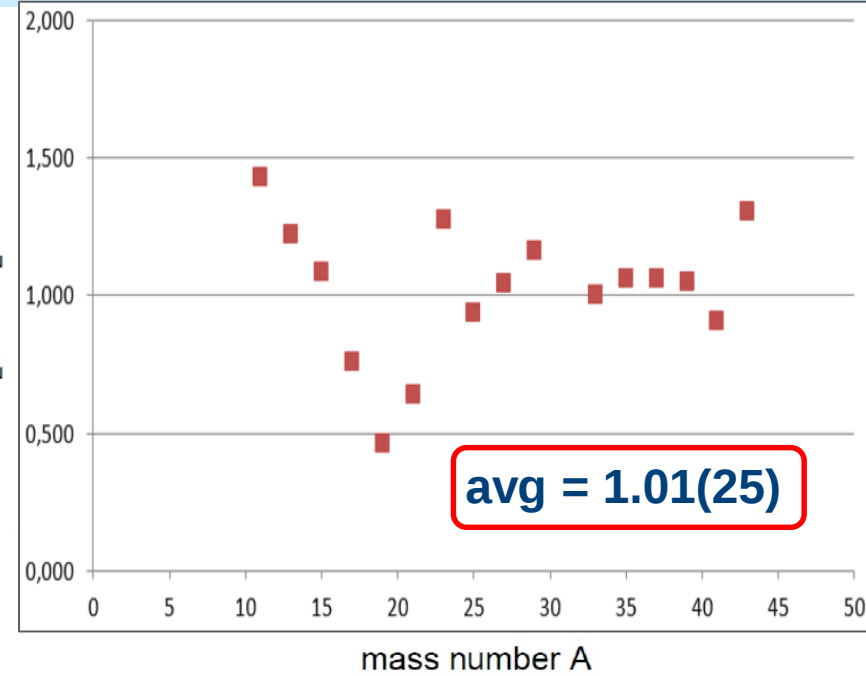
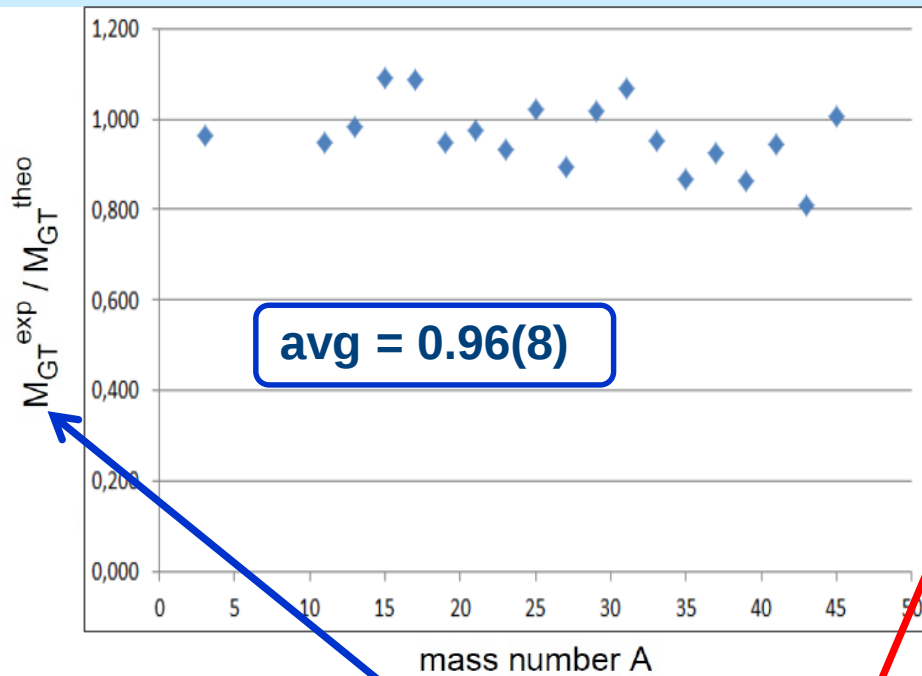
weak magnetism term b_{WM} - experimental data

mirror β transitions

$$b_{WM} \approx \mu_p - \mu_n$$



weak magnetism b_{WM} - mirror β transitions



$$c \cong g_A M_{GT}$$

$$\frac{b_{WM}}{Ac} \cong \left[\frac{g_M}{g_A} + \frac{g_V M_L}{g_A M_{GT}} \right]$$

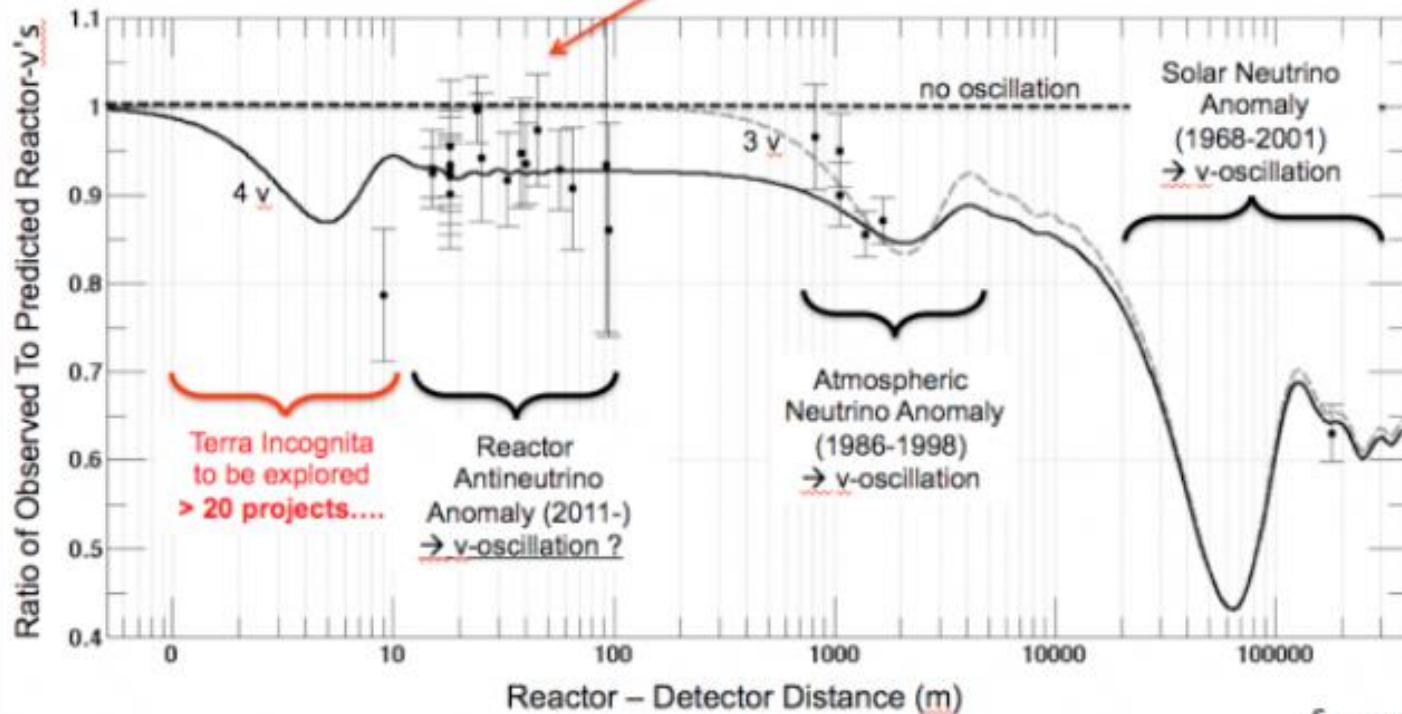
B. R. Holstein, RMP 46 (1974) 789
F.P. Calaprice et al., PR C 15 (1977) 2178

$(b/Ac)^{exp} / (b/Ac)^{theo}$	
mirror ($A = 3-45$)	0.97(11)
triplet ($A = 6-30$)	1.01(15)

N.S., I.S.Towner et al., to be published

also of interest to Reactor Neutrino Anomaly

■ Observed/predicted averaged event ratio: $R=0.927\pm0.023$ (3.0σ)



Mueller et al.,
Phys. Rev. C 83
(2011) 054615

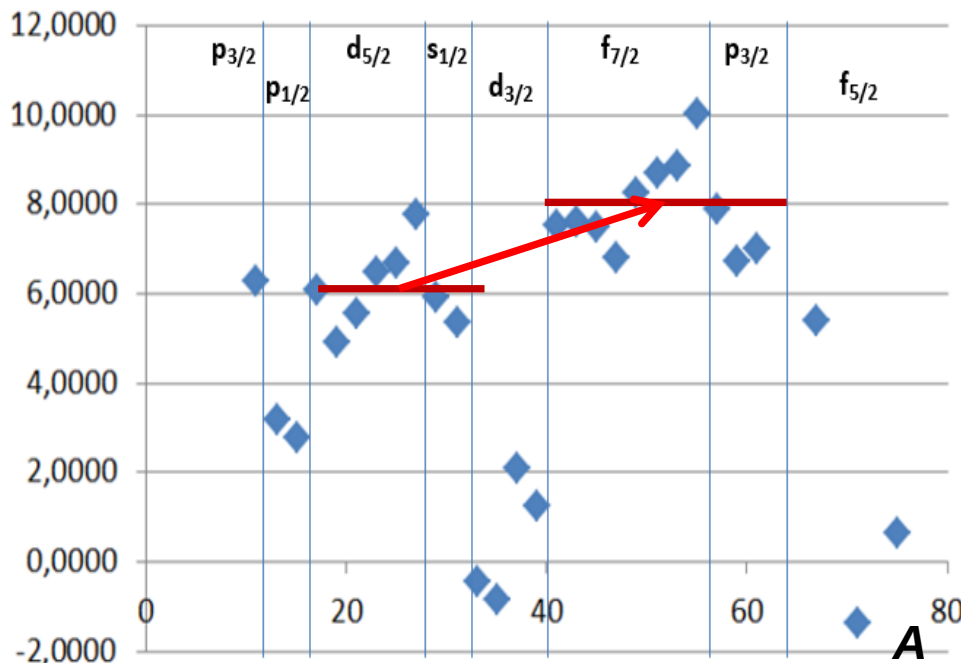
from Th. Lasserre

Too crude approximation for b_{WM} in fission fragment beta decays
may be (in part) responsible (see also A.C. Hayes et al., PRL 112 (2014) 202501)

Poster by L. Hayen

KU LEUVEN

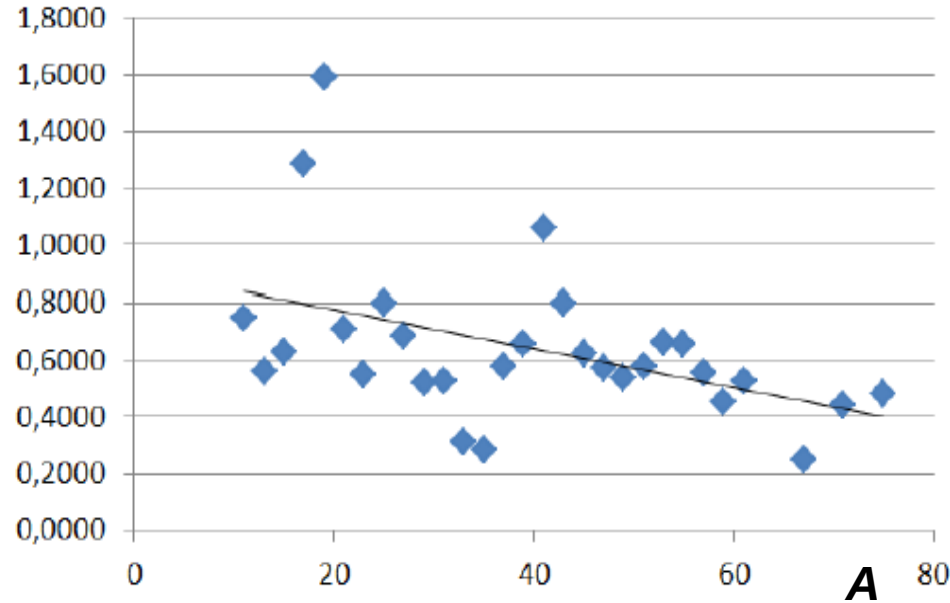
b_{WM}/Ac



$$j = l + 1/2$$

$$j = l - 1/2$$

$|c|$



Effect on spectral shape:

$$1 + \delta_{WM} E$$

$$\rightarrow \frac{dN}{dE} = \frac{4}{3M_n} \frac{b}{Ac}$$

Shift of $\frac{dN}{dE}$ by $0.5\% \text{ MeV}^{-1}$

$\rightarrow$ shift in ν -rate of $\approx -1\%$

New vistas and prospects in the LHC era

- new generation of (trap-based) correlation experiments
 - towards 0.1% precision level
- precise β -spectrum shape measurements:

$$d\Gamma \propto G_F F(Z, E) \left[1 + k \frac{1}{E_\beta} b_{\text{Fierz}} + k' E_\beta b_{\text{WM}} \right]$$

b_{Fierz} : scalar / tensor weak currents

b_{WM} : weak magnetism (Standard Model term)

- induced by strong interaction because decaying quark is not free but bound in a nucleon;
- is to be known better when reaching sub-percent precisions

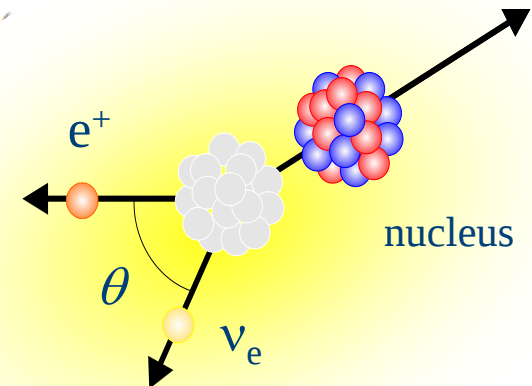
Note the different energy dependence of both effects !!

4. β spectrum shape measurements

Table VI Overview of the features present in the β spectrum shape (Eq. (4)), and the effects incorporated into the Beta Spectrum Generator Code. Here the magnitudes are listed as the maximal typical deviation for medium Z nuclei with a few MeV endpoint energy. Some of these corrections fall off very quickly (e.g. the exchange correction, X) but can be sizeable in a small energy region. Varying Z or W_0 can obviously allow for some migration within categories for several correction terms.

Item	Effect	Formula	Magnitude
1	Phase space factor	$pW(W_0 - W)^2$	Unity or larger
2	Traditional Fermi function	F_0 (Eq. (5))	
3	Finite size of the nucleus	L_0 (Eq. (17))	
4	Radiative corrections	R (Eq. (27))	
5	Shape factor	C (Eq. (125))	
6	Atomic exchange	X (Eq. (63))	
7	Atomic mismatch	r (Eq. (76))	
8	Atomic screening	S (Eq. (54)) ^a	To be evaluated in a case by case scenario.
9	Shake-up	See item 7 & Eq. (66) ^b	
10	Shake-off	See item 7 & Eq. (69) & $\chi_{\text{ex}}^{\text{cont}}$ ^c	
11	Distorted Coulomb potential due to recoil	Q (Eq. (26))	
12	Diffuse nuclear surface	U (Eq. (20))	
13	Recoiling nucleus	R_N (Eq. (22))	
14	Molecular screening	ΔS_{Mol} (Eq. (81))	
15	Molecular exchange	Case by case	
16	Bound state β decay	Γ_b/Γ_c (Eq. (77))	
17	Neutrino mass	Negligible	
18	Forbidden decays	Not incorporated	

**Analytical description + code,
accurate to few 10^{-4} level**
L. Hayen, N. Severijns et al., in prep.



Poster by L. Hayen

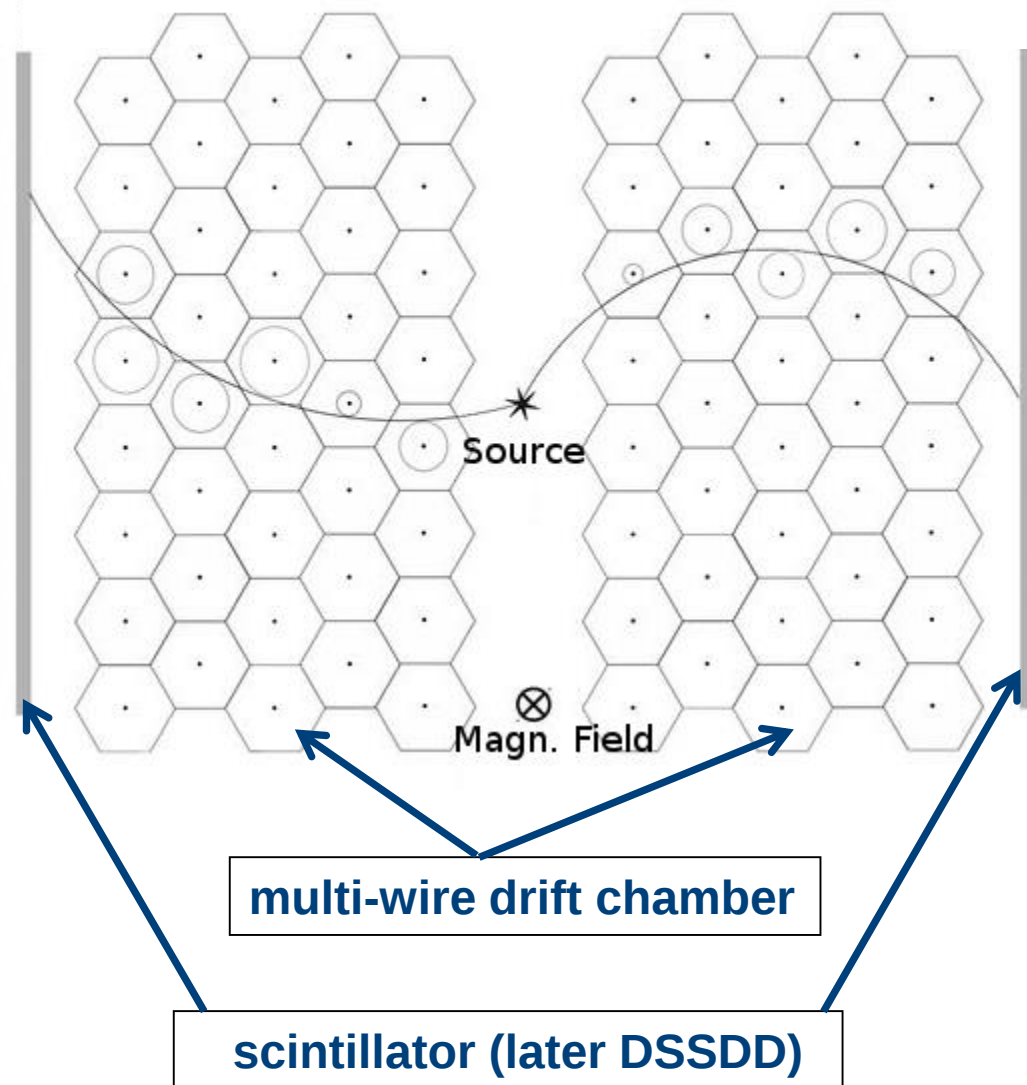
^a Here the Salvat potential of Eq. (57) is used with X (Eq. (55)) set to unity.

^b The effect of shake-up on screening was discussed in Sec. VI.C.1 with Eq. (66).

^c Shake-off influences on screening and exchange corrections were discussed separately in Sec. VI.C.2. To be evaluated in a case by case scenario.



miniBETA spectrometer (Leuven / Krakow)

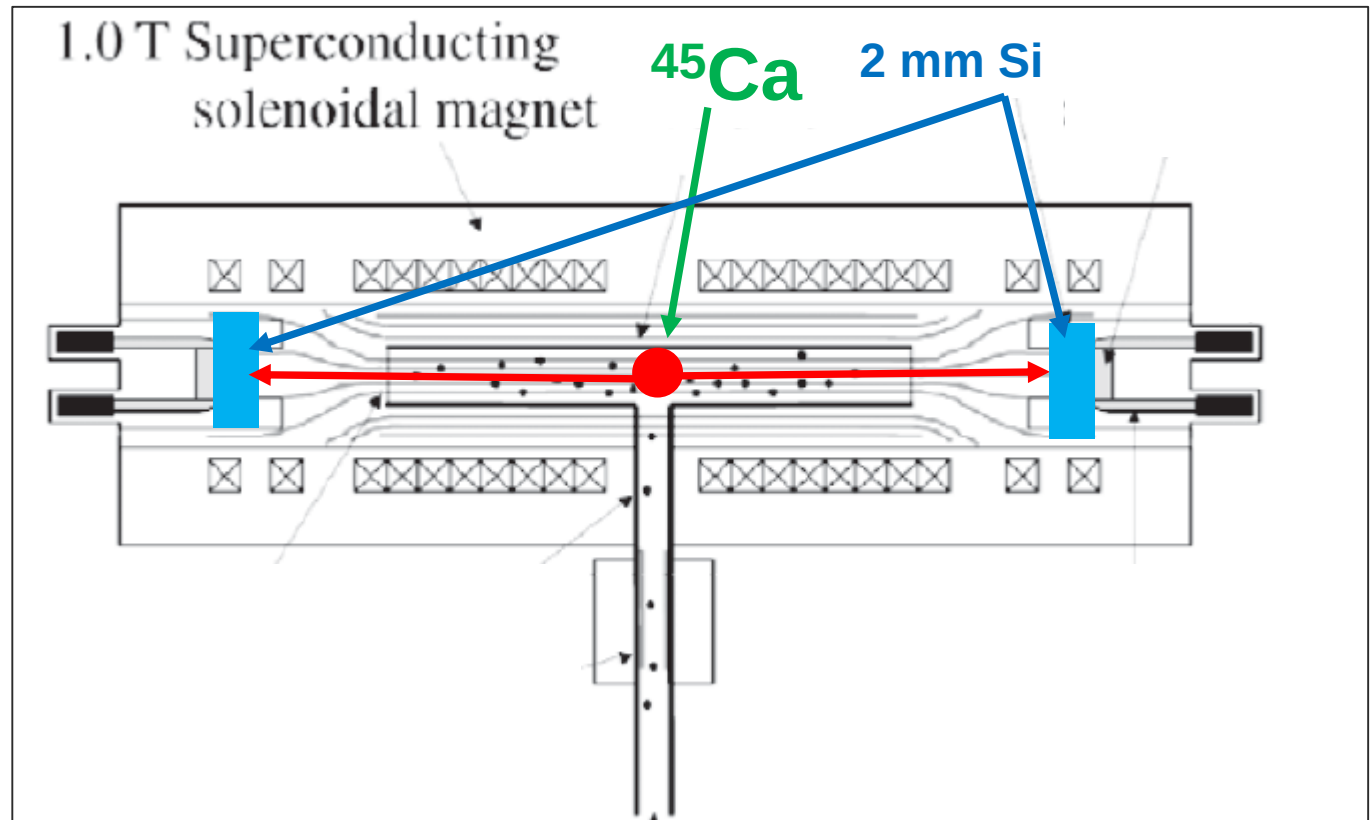


double-Si spectrometer (Leuven / LANL, A. Young)

two 2 mm segmented **Si** detectors in B- field, replacing UCNA MWPCs

- data in May 2016
- analysis ongoing

Talk of J. Wexler



Beta energy spectrum shape in ${}^6\text{He}$ decay - NSCL/MSU

(O. Naviliat-Cuncic et al.)

- **Long term goal**: Measure the **Fierz interference term** (b) in ${}^6\text{He}$ decay to search for weak tensor currents.
- **Current goal**: measure the **weak magnetism** (WM) form factor in ${}^6\text{He}$ decay for a tests of the strong form of CVC. The WM is the largest "hadronic SM background" in a measurement of b .

Poster of Xuejing Huyan

- **Principle**: use a **fragmented separated beam** to eliminate distortions in beta spectrum due to **back-scattering, out-scattering or dead-layers**.

single detector

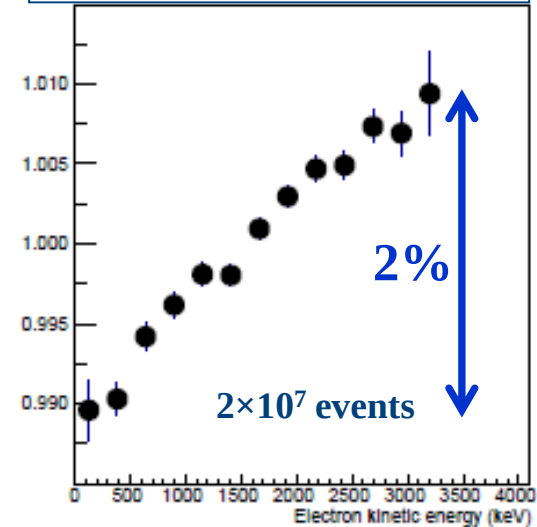
radioactive ${}^6\text{He}$ source

range of β particles

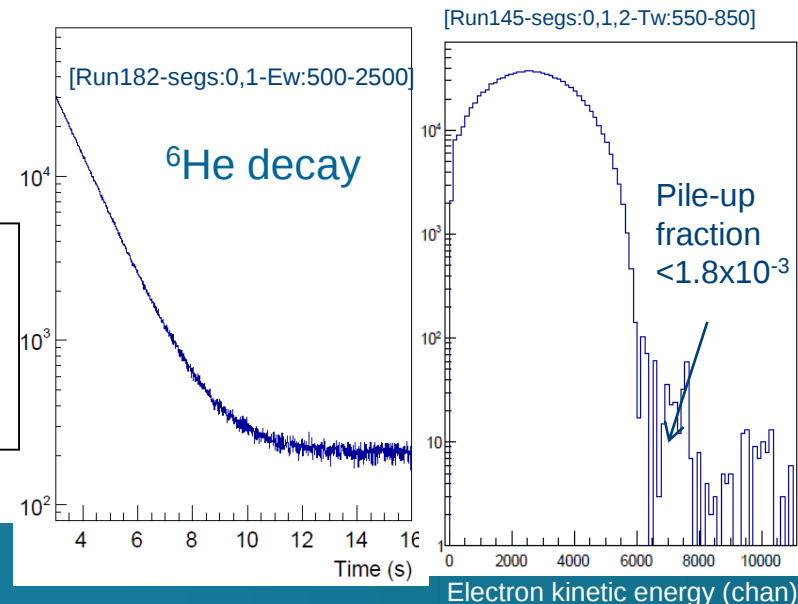
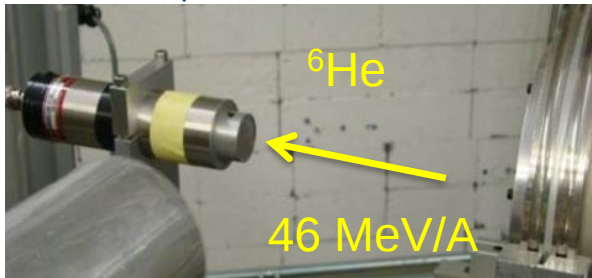
Collected statistics enables extracting the WM form factor at $\sim 5\%$ relative error

Effect of weak magnetism

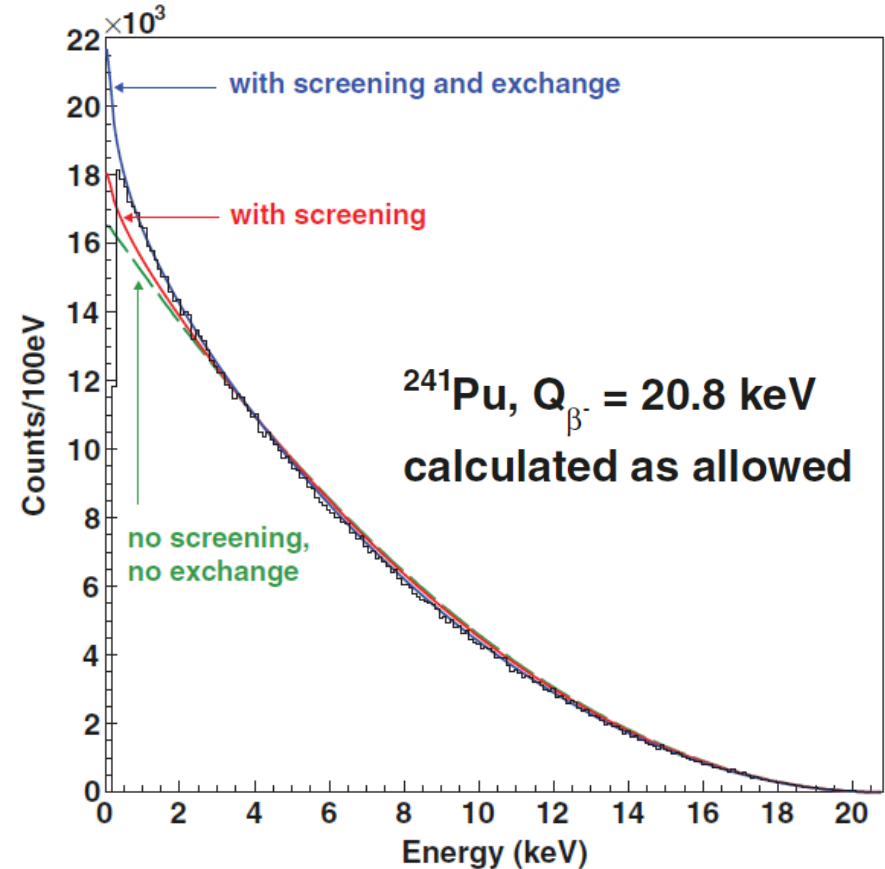
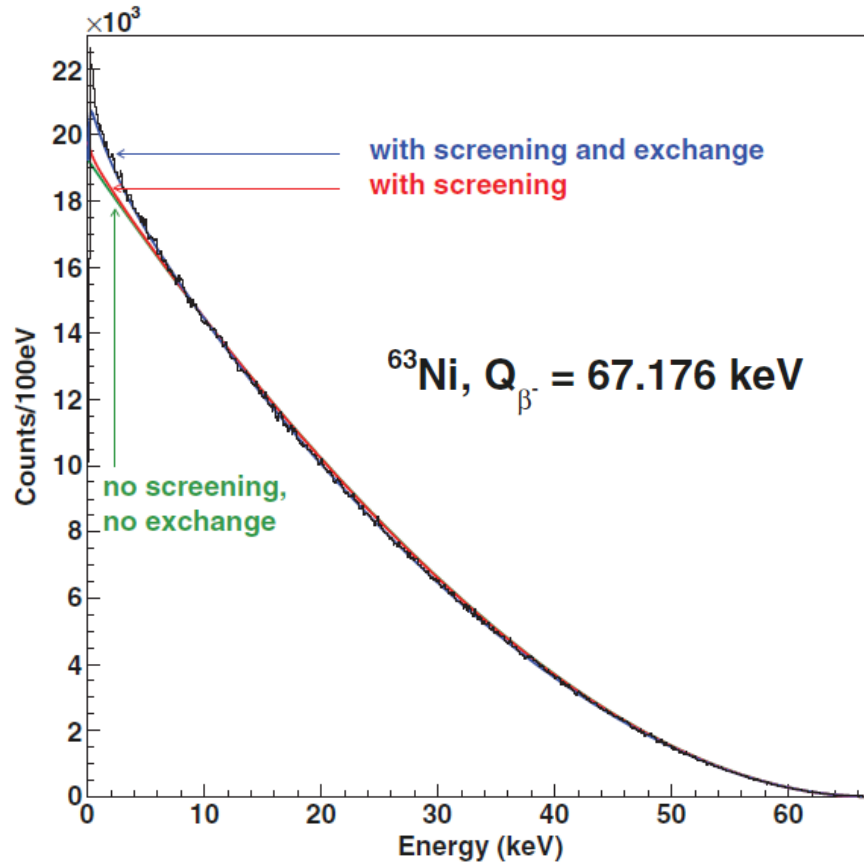
(Monte-Carlo simulation)



Experiment at NSCL



microcalorimeter measurements (CEA-Saclay)



X. Mougeot et al., PR A 86 (2012) 042506 and PR A 90 (2014) 012501

Conclusions and Outlook

1. β - ν correlation and β asymmetry measurements + Ft-values
→ improved limits on scalar and tensor type weak currents;
2. searches for new physics (bosons) at low energies are competitive
with direct searches at LHC for 10^{-3} precisions of b and beyond
many experiments ongoing or in preparation / planned
3. at sub-0.5% level of precision have to include effects induced by strong interaction
→ largest is weak magnetism
→ best observable: beta-spectrum shape

scalar / tensor currents & weak magnetism

distribution in

- electron and neutrino directions and in
- electron energy

from polarized nuclei :

$$d\Gamma \propto \underbrace{F(\pm Z, E_e)}_{\text{Fermi function}} \underbrace{\frac{p_e E_e (E_0 - E_e)^2 dE_e d\Omega_e d\Omega_\nu}{\text{phase space}}}_{\text{phase space}} \times \underbrace{\xi}_{\text{nuclear matrix elements}} d\Gamma_0$$

$$\times \left\{ 1 + \underbrace{a \frac{\vec{p}_e \cdot \vec{q}}{E_e E_\nu}}_{\beta\text{-v correlation}} + \underbrace{b \frac{\gamma m_e}{E_e}}_{\text{Fierz interference term (} b \equiv 0 \text{ in standard model)}} + \underbrace{A \frac{\vec{J} \cdot \vec{p}_e}{J E_e}}_{\beta\text{-asymmetry}} + \dots \right\}$$

Diagram illustrating the decay process and the resulting distribution:

The diagram shows a nucleus (represented by a cluster of red and blue spheres) decaying into an electron (e^+) and a neutrino (ν_e). The electron is emitted at an angle θ relative to the neutrino. The neutrino is represented by a yellow sphere. The electron is represented by an orange sphere. The angle θ is indicated between the electron and neutrino paths.

The β -asymmetry term is related to the nuclear spin $\vec{J}$ and the electron momentum $\vec{p}_e$:

$$A \frac{\vec{J} \cdot \vec{p}_e}{J E_e} = \cos \theta$$

The Fierz interference term is related to the parameter $\tilde{X}$:

$$\tilde{X} = \frac{X}{1 + b \frac{\gamma m_e}{E_e}} \quad \text{with} \quad \gamma = \sqrt{1 - (\alpha Z)^2}$$

the Standard Model and beyond:

- * $C_A = -1.27$ ($g_A/g_V = -1.2699(7)$ from n-decay)
- * $C_V' = C_V$ & $C_A' = C_A$ (maximal P-violation)
- * $C_S = C_S' = C_T = C_T' = C_P = C_P' \equiv 0$ (only V- and A-currents)

% level $\rightarrow \sim 300$ GeV
per mille level $\rightarrow \sim 2$ TeV

experimental upper limits: $|C_T^{(')}/C_A|$ and $|C_S^{(')}/C_V|$ at few % level
(neutron and nuclear β -decay)

N.S., O. Naviliat-Cuncic and M. Beck, Rev. Mod. Phys. 78 (2006) 991,
J. Nico, J. Phys. G 39 (2009) 104001,
D. Dubbers and M.G. Schmidt, Rev. Mod. Phys. 83 (2011) 1111,
V. Cirigliano et al., Prog. Part. Nucl. Phys. 71 (2013) 93,
F. Wauters et al., Phys. Rev. C 89 (2014) 025501,
B.R. Holstein, J. Phys. G 41 (2014) 114001.

- * **no time reversal violation**
(except for the CP-violation described by the phase in the CKM matrix)

Precision meas^{ts} in nuclear/neutron β decay in the LHC era

if particles that mediate new interactions are above threshold for LHC
→ Effective Field Theory allowing
direct comparison of low-energy and collider constraints

low-scale $O(1 \text{ GeV})$ effective Lagrangian for semi-leptonic transitions
(contributions from W-exchange diagrams and four-fermion operators)

link betw. EFT couplings ε_i and Lee-Yang nucleon-level effect. couplings C_i :

$$C_i = \frac{G_F(0)}{\sqrt{2}} V_{ud} \bar{C}_i \quad \text{with} \quad \bar{C}_S = g_S(\varepsilon_S + \tilde{\varepsilon}_S), \quad \bar{C}_T = 4g_T(\varepsilon_T + \tilde{\varepsilon}_T), \dots$$

$$\varepsilon_i, \tilde{\varepsilon}_i \approx \nu^2 / \Lambda_{BSM}^2 \quad \text{with} \quad \nu = (2\sqrt{2} G_F^{(0)})^{-1/2} \approx 170 \text{ GeV}$$
$$\text{if } \Lambda_{BSM} \sim 5 \text{ TeV} \rightarrow \varepsilon_i \sim 10^{-3}$$

T. Bhattacharya et al., Phys. Rev. D 85 (2012) 054512

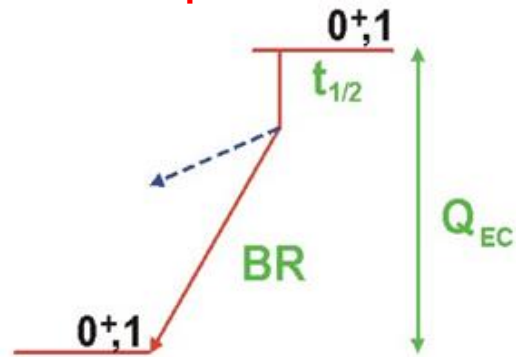
V. Cirigliano, et al., J. High. Energ. Phys. 1302 (2013) 046

O. Naviliat-Cuncic and M. Gonzalez-Alonso, Annalen der Physik 525 (2013) 600.

V. Cirigliano, et al., Progr. Part. Nucl. Phys. 71 (2013) 93

V_{ud} quark mixing matrix element & CKM unitarity

$$\underbrace{\mathcal{F}t^{0^+ \rightarrow 0^+}}_{\text{from experiment}} \equiv \underbrace{f_V t^{0^+ \rightarrow 0^+}}_{\text{nucleus dependent corrections}} \underbrace{(1 + \delta_{NS}^V - \delta_C^V) (1 + \delta_R')}_{\text{nucleus independent}} = \frac{K}{2G_F^2 V_{ud}^2 C_V^2 (1 + \Delta_R^V)}$$



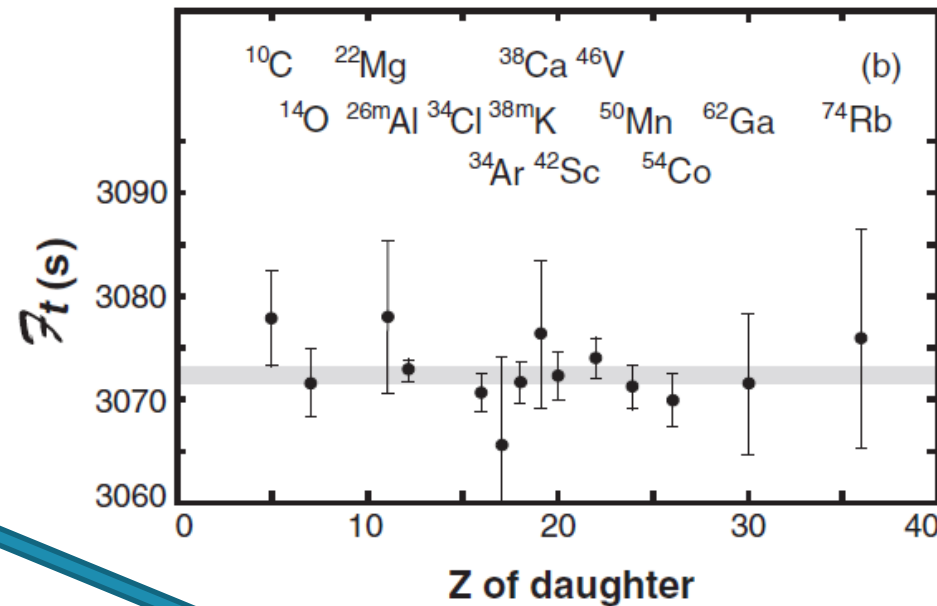
$$|V_{ud}| = 0.97417(21)$$

Hardy & Towner, PR C 91 (2015) 025501

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.99978(55)$$

$$|V_{us}| = 0.2253(8) \text{ (PDG14)}$$

Hardy & Towner, Phys. Rev. C 91 (2015) 025501



$$\mathcal{F}t^{0^+ \rightarrow 0^+} = 3072.27(72) \text{ s}$$

prospects - 1

1. pure Fermi transitions:
 - new data to improve Ft values
 - testing isospin corrections δ_C
 - nucleus-independent radiative correction Δ_R

2. neutron decay:
 - lifetime (t_{SPECT} , ...)
 - beta-asymmetry parameter A (PERKEO, UCNA)
 - $\beta\nu$ -correlation a (a_{SPECT} , Nab, AbBa, aCORN, ...)

3. $T = 1/2$ mirror β transitions:

$$Ft^{\text{mirror}} \left(1 + \frac{f_A}{f_V} \rho^2 \right) = 2Ft^{0^+ \rightarrow 0^+} = \frac{K}{G_F^2 V_{ud}^2 (1 + \Delta_R^V)}$$

N.S. , I.S. Towner et al.,
Phys. Rev. C 78 (2008) 055501

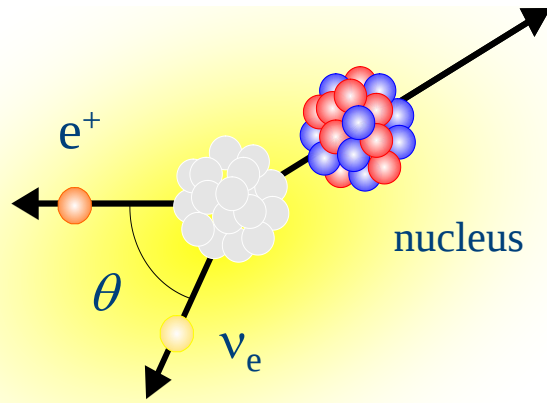
$$|V_{ud}| = 0.9719(17)$$

O. Naviliat-Cuncic & N.S., PRL 102 (2009) 142302

$$\rho = \frac{C_A M_{GT}}{C_V M_F}$$

6. β spectrum shape measurements

$$N(p)dp = K p^2 (W - W_0)^2 \cdot F(Z, p) \cdot L_0 \cdot C \cdot R_n \cdot RC \cdot S(E) dp$$



- phase space factor x constants
- $F(Z, p)$: Fermi function
- L_0 & C : finite size of nucleus
- R_n : finite mass of nucleus
- RC : radiative corrections
- $S(E)$: spectrum shape factor

$$\frac{dN}{dE} \approx 1 + \frac{4}{3M_n} \frac{b_{WM}}{Ac} E_e \Rightarrow \approx 0.8 \% \text{ MeV}^{-1}$$

(for a pure GT transition and neglecting terms $\propto 1/M^2$ and $\propto m_e^2/E$)

$$\rightarrow d\Gamma \propto G_F F(Z, E) \left[1 + k' \boxed{b_{WM} E_\beta} + k'' \boxed{\frac{b_{Fierz}}{E_\beta}} \right]$$